

CS 2312: Lab 09

Shared Degree

Given a graph with $n \geq 2$ vertices, prove that there are at least two vertices with the same degree.

Two Terminals

Prove that if G is a DAG (has zero cycles) with at least two distinct sinks such that there is a path from every source to every sink, then G must have at least one node of outdegree ≥ 2 .

1-3 Trees

We say that a tree, T is a 1-3 tree if each of the vertices in the tree have either a degree of 3 or a degree of 1.

- Prove that if a 1-3 tree has l leaves, then it has $l - 2$ vertices of degree 3.
- Let T be a 1-3 tree with at least 4 leaves. Prove that in T there exists an internal vertex that is adjacent to exactly two leaves.