# Industry Concentration and Aggregate Price Dynamics

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#### Overview:

Inflation following COVID-19 reflects the confluence of several factors: swings in consumer demand, supply-chain bottlenecks, and expansionary fiscal and monetary policies. Corporate profits appear as one of the main factors behind the initial inflation surge and this paper develops general equilibrium framework that links competition within industries to aggregate price dynamics to explain this outcome. Building on recent empirical work, it accounts for differences in pricing power across firms, cross-price effects, and firm-specific shocks. Industry leaders are usually much larger than other firms and charge a higher markup. Evidence suggests their pricing behavior differs: they limit the pass-through of idiosyncratic cost shocks but are strategic and match price changes by rival firms. Meanwhile, trailing firms are generally much smaller and set prices monopolistically. On this basis, the framework yields several key results. First, due to strategic complementarity in pricing, the implied cost pass-through for industry leaders after an aggregate shock is around 25 percent higher than for an idiosyncratic shock, which aligns with evidence from Gödl-Hanisch and Menkhoff (2023). Second, due to differences in firms' demand schedules, aggregate shocks have an uneven impact, and the model explains differences in business cycle fluctuations across firms. Finally, if a negative productivity shock affects small firms more, industry leaders raise prices, resulting in 'excess' profits. In this case, the additional markup distortion significantly amplifies the inflationary impact of the shock.

## 1. Introduction

There has been a trend increase in industry concentration in the United States over the past few decades and markups appear higher as well (De Loecker, Eeckhout, and Unger, 2020). This paper is motivated by concerns rising pricing power contributed to the recent inflation bout following the COVID-19 pandemic. Profits explain around one-third of domestic price growth between mid-2020 and mid-2023, and the recent inflation episode has rekindled a long-standing debate on whether inflation is driven by expectations or pricing power (Cagan, 1979). Before the 1970s, many economists believed slack demand would lead prices to fall. The simultaneous rise of unemployment and prices (or 'stagflation') challenged this perception, and expectations were later viewed as the main driver of inflation. As a result, models for aggregate price dynamics tend to treat pricing power as peripheral. With the most recent episode, rapid profit-driven inflation may have 'de-anchored' expectations. Accordingly, this paper puts greater emphasis on market structure and develops a general equilibrium framework where only a few firms compete within industries. In this setting, higher concentration is associated with a lower aggregate price elasticity of demand and non-linearities from own- and cross-price effects. Changes in concentration and market structure affect the pass-through of cost shocks, leading to changes in the allocation of demand across firms. Cross-price effects can accelerate inflation, particularly when shocks affect a subset of firms, suggesting changes in relative costs and productivity are important. The resulting framework can help evaluate policies targeted at specific firms, such as progressive taxes or subsidized loans.

Macroeconomic models describing aggregate price dynamics typically assume monopolistic competition across identical firms. Starting with the observation that a few firms account for the majority of sales within most industries, a growing body of research indicates market position affects pricing behavior.<sup>2</sup> Leading firms absorb cost shocks and act strategically, matching price changes by rival firms. Meanwhile, smaller firms on the competitive fringe act monopolistically and adjust prices in line with their costs. A simple market structure with identical firms cannot fully account for these

<sup>&</sup>lt;sup>1</sup>The period between 2020Q2 and 2023Q2 in the NIPA tables (1.15) shows profits account for 38 percent of the price increase among domestic companies when looking at a unit of real gross value added. Labor compensation contributed to 30 percent of the increase, and non-labor costs contributed 32 percent. See section A.3 of the appendix for a more detailed discussion.

<sup>&</sup>lt;sup>2</sup>As will be discussed in section 2.2, more than 60 percent of market share is controlled by the top two firms on average when looking within narrowly defined markets for consumer goods. This result appears consistent across various studies. Furthermore, Gödl-Hanisch and Menkhoff (2023) finds most variation in the pass-through is within (rather than between) 4-digit industries.

dynamics. To evaluate the impact of economic shocks, this paper embeds a nested CES demand system featuring asymmetric firms into a New Keynesian framework with forward-looking agents. The demand system connects the pricing behavior of individual firms to their market position. The calibrated model makes a set of predictions in line with empirical evidence, both in aggregate and at the firm level. It also helps evaluate how competition shocks affect inflation and quantifies the associated economic losses.

Models for the aggregate economy frequently use quasi-kinked demand, e.g. Kimball (1995), to explain why firms limit the pass-through of cost shocks. In this case, the second derivative of the price elasticity of demand is negative with respect to the firm's own price, making large price increases costly compared to small ones. Instead, I consider a nested CES specification that adds strategic interaction between firms of different sizes. With strategic complementarity in pricing, firms match the price movements of their competitors, and the cross-price second derivative is positive. Given a realistic market structure with finite firms, both own- and cross-price effects are present, and these forces offset to varying degrees. Therefore, the nature of shocks matters, i.e., if they are uniform across firms, uneven, or idiosyncratic. The assumption that shocks are truly aggregate may not hold in practice. As highlighted in Gabaix (2011), idiosyncratic shocks to top firms explain a large share of total variation in output growth. Along with the demand schedule, the degree of nominal price rigidity may differ across firms.<sup>3</sup> The model presented here links the pass-through to three factors: the 'aggregate' nature of shocks; their expected persistence; and the strength of strategic complementarity between firms.

I specify quadratic price adjustment costs and firms smooth their price adjustments. As a consequence, price dispersion mostly reflects real rigidities, i.e. differences in the demand schedule across firms. The responses to different shocks are compared to studies looking at small and large firms over the business and financial cycles, most prominently Crouzet and Mehrotra (2020). Generally, the model aligns closely with observed outcomes. The analysis also draws on Baqaee, Farhi, and Sangani (2021), who argue shocks have first-order effects on efficiency and welfare when they act on existing market distortions. In other words, demand for goods from efficient and inefficient producers changes with their relative prices. This affects the allocative efficiency of the economy following shocks. If shocks are uneven, unaffected firms may exploit their market power and raise prices, leading to 'excess'

<sup>&</sup>lt;sup>3</sup>While omitted from the baseline, an extension allows for different price rigidities across firms.

profits and efficiency losses. As mentioned, profits explain much of the initial jump in inflation in 2020. The model makes a similar prediction for an impatience shock, but the level of concentration does not significantly influence this result. On the other hand, concentration is very relevant when shocks are uneven across firms.

There is a growing literature connecting oligopoly competition and aggregate price dynamics. Wang and Werning (2022) develop a general equilibrium model around an industry structure. This paper is similar but emphasizes heterogeneity in shocks, which leads to two distinct results: first, a nested CES system predicts large differences in the pass-through when comparing idiosyncratic and aggregate shocks; second, cross-price effects amplify shocks when they are uneven across firms. The setup is closest to Heise, Karahan, and Şahin (2022), which uses import competition to explain low inflation over the 2000s and 2010s. Heise et al. look at competition between domestic and foreign firms, whereas this paper compares large and small firms and incorporates general equilibrium effects between them. Some of the intuitions are also similar to Guimaraes and Sheedy (2011), which uses strategic interaction between retailers to explain sales. In isolation, retailers would reduce the number of sales following a monetary easing – yet with strategic substitutability, retailers maintain the number of sales relatively constant. The nested CES specification used here also implies that own- and cross-price effects frequently offset.

The analysis is organized as follows. Section 2 presents a set of stylized facts motivating the analysis, first regarding market structure and then for firm pricing behavior. The framework is presented in section 4 along with an overview of the solution method. The calibration and results are discussed in section 5. Results include changes in pass-through, price dynamics following shocks, the contribution of profits to inflation, and changes in allocative efficiency following shocks. Section 6 concludes with a discussion of the policy implications and future directions for research.

# 2. Changes in Industry and Product Market Structure

This section provides a set of stylized facts on market structure. Along with the distribution of market share, differences in markups across firms are of particular interest. Markups generate distortions from two different perspectives. On the supply side, they act as a 'tax' on the factors of production, which depresses output. On the demand side, markup dispersion reduces the allocative efficiency of

the economy. In an efficient economy, prices reflect the preferences of households along with the supply of different goods. If markups are uniform across goods, then the consumption basket is close to the optimal one. Markup dispersion is costly since households favor goods with low markups and not those with low production costs.

# 2.1. National Concentration and Superstar Firms

The literature has long established that sales within narrowly defined industries are dominated by a few firms (Simon and Bonini, 1958). In addition, the sales distribution is highly skewed (Buzzell, 1981).<sup>4</sup> More recent studies find large differences in productivity across firms within an industry (Cindy Cunningham et al., 2023). There is substantial evidence that markets in the United States have become more concentrated over recent decades and that productivity dispersion has grown. The increase in the national Herfindahl-Hirschman index (HHI), the principal measure of product market and industry concentration, is well documented and multiple studies link it to the expansion of 'superstar' firms (Autor, Dorn, et al., 2020; Grullon, Larkin, and Michaely, 2019).<sup>5</sup> There is some evidence for increased concentration in Europe as well, although the trend is less pronounced (Bajgar et al., 2023). Kwon, Y. Ma, and Zimmermann (2023) find that in the late 1970s, the top 0.1 percent of corporations accounted for less than 70 percent of total business assets in the United States. This share increased to almost 90 percent by the end of the 2010s. Similarly, the share of sales accruing to the top 0.1 percent increased 10-15 percentage points and now accounts for almost two-thirds of the total. To add an important nuance, concentration within industries appears to be the main driver of this trend, not the expansion of firms into new industries. Autor, Dorn, et al. (2020) find that top firms have expanded their primary business lines while participation across industries decreased.

<sup>&</sup>lt;sup>4</sup>Buzzell (1981) uses a market research database to infer firm size distribution, which closely adheres to a semi-logarithmic distribution. Each firm is around 1.7x the size of its next largest rival. The average market share of the top firm was around 33 percent, followed by 19 percent, 12 percent, and 7 percent for the second, third, and fourth largest competitors. More recent papers on this topic look at ancillary questions, including the relationship between the industry life-cycle and firm size (Dinlersoz and MacDonald, 2009), the role of product diversification in growth (Hutchinson, Konings, and Walsh, 2010), and the distribution of market share within retailers (Wilbur and Farris, 2014).

<sup>&</sup>lt;sup>5</sup>Superstar firms are those firms that dominate their markets in terms of sales and profits. The HHI is a common measure of concentration, calculated as the sum of the squared market shares of all firms in a given industry. If firms are identical and atomistic, this gives an HHI of 0. If one firm controls 100 percent of the market, this gives an HHI of 10,000.

## 2.2. Measuring Local Product Market Concentration

The geographic dimension is important, and there is an ongoing debate on whether concentration in local product markets increased or decreased. Two recent papers using product-level data from the Census Bureau find that local sales concentration rose in tandem with national measures, namely Autor, Patterson, and Van Reenen (2023) and Smith and Ocampo (2022). The underlying data in these studies remain fairly aggregated. Analyses of alternative, more granular commercial data sources in Rossi-Hansberg, Sarte, and Trachter (2018) and Benkard, Yurukoglu, and Zhang (2021) suggest that local product market concentration decreased. Both find the expansion of top firms across regional markets explains this decrease: in other words, large national firms are increasingly in competition with each other. Shimomura and Thisse (2012) analyze the consequences for consumer welfare.

Despite mixed evidence on the trends, local product market concentration in the United States is also higher than commonly appreciated. Benkard, Yurukoglu, and Zhang (2021) use a market research survey covering around 25,000 consumers per year between 1994 and 2019 and extract all questions relating to brands purchased, dividing them into goods that are closely substitutable. On this basis, 44 percent of product markets have an HHI above 2500 over the sample period. This is higher than most estimates circulating in the literature and meets the US Horizontal Merger Guidelines criterion for "highly concentrated." The same estimates indicate the top two firms in a market control 55-60 percent of sales on average. Other studies support this view. Looking at IRI retail scanner data, Mongey (2017) finds the median number of effective firms in a product category is around 3.7 and the revenue share of the top two firms is 66 percent. An analysis of Nielsen retail scanner data in Hottman, Redding, and Weinstein (2016) finds the top three or four firms account for the majority of market share within narrowly defined product groups. Furthermore, the leading firm usually has a much larger market share than others and charges a higher markup.<sup>7</sup> Affeldt, Duso, Gugler, et al. (2021) look at concentration in Europe through the lens of antitrust markets. Examining European Commission cases between 1995 and 2014, the study finds the average post-merger HHI for an antitrust market was around 2200 points with 4 firms competing on average.

<sup>&</sup>lt;sup>6</sup>These studies rely on retail data, which have several limitations. Many services, intermediate goods, and major durable purchases are absent. This extends to housing costs, healthcare, private education, and other significant outlays.

<sup>&</sup>lt;sup>7</sup>Hottman, Redding, and Weinstein (2016) find the leader's markup is 24 to 100 percent higher than the sector average, depending on the markup estimation.

# 2.3. The Distribution of Market Share in the European Union

The EU Merger Control Database compiled by Affeldt, Duso, and Szücs (2018) allows for an analysis of firm characteristics across well-defined market segments. The database covers the period between 1990 and 2014 and includes information on more than 5,000 cases reviewed by the European Commission as part of its antitrust enforcement.<sup>8</sup> The market share of the largest firm exceeds 30 percent in more than one-half of antitrust markets and exceeds 50 percent in almost one-quarter. The median share for the top firm is 40 percent. The appendix (section A.2) includes a full set of summary statistics.

The market leader is typically much larger than other firms. Figure 1 presents the main results. The left-hand panel shows how market share is distributed conditional on the number of firms within an industry. The top firm controls around 35 percent of the market in the typical industry (where n=4) and its lead remains fairly consistent as the number of firms increases (n>4). The right-hand panel gives the joint distribution of market share for the market leader and top trailing firm whenever both are reported. The top trailing firm tends to be significantly smaller than the market leader. Within an observation, the ratio of the market shares for the leading firm and top trailing firm gives a median value of 1.6x and the mean is around 1.9x. In addition, the top two firms control around 63 percent of the market on average and the median is similar at 61 percent. This may not generalize to the United States; still, the findings are consistent with Benkard, Yurukoglu, and Zhang (2021), Buzzell (1981), and Mongey (2017).

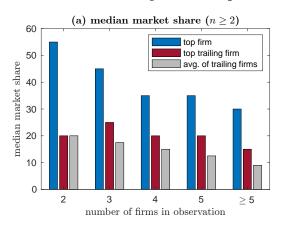
#### 2.4. Has Market Power Increased?

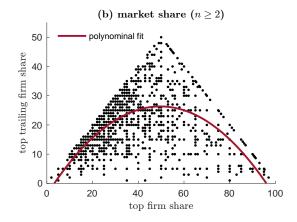
Since superstar firms tend to be highly efficient, the increase in market share is desirable as long as competition remains strong and there is no corresponding increase in market power. However, this may not be the case. Covarrubias, Gutiérrez, and Philippon (2019) find concentration in the United States was efficient in the 1990s, but was associated with rising market power in the 2000s.

<sup>&</sup>lt;sup>8</sup>Each case contains the name of the target firm and its potential acquirer, their market shares across different regions, and whether the merger was approved. Competing firms are identified for a large number of these markets along with the Commission's assessment of their market share. Nearly 31,000 markets are identified, over 23,000 of these observations contain information on the merging entities' market shares, and around 10,000 observations contain information on competing firms and their market shares.

 $<sup>^9</sup>$ The market share of the post-merger entity is used if the merger was approved. These calculations are limited to cases where both the leader and follower report market shares above 10 percent. The unconditional median is 1.7x.

Figure 1: European Commission Antitrust Markets





The left-hand panel separates observations in Affeldt, Duso, and Szücs (2018) by the number of firms reported. The median is taken across all corresponding observations. The first set of bars where n=2 makes clear there is usually some residual market share. Around 15 percent is unexplained in the median case, and a more complete set of tabulations is in the appendix (section A.2). The right-hand panel shows the joint distribution of market shares for the top and top trailing firms when both are reported. The top reported market share by observation is on the x-axis, and the next largest market share is on the y-axis. A second-order polynomial gives the conditional expectation. The prediction  $(y=-0.012x^2+1.213x-3.788)$  is very close to what local smoothing methods return.

Over this period, markups appear to grow disproportionately for firms already at the top of the markup distribution, and the market share of the same firms also expanded (Baqaee and Farhi, 2019; Barkai, 2020; De Loecker, Eeckhout, and Unger, 2020). Most of the aforementioned studies use a 'production function' approach to measure markups. As highlighted in Basu (2019), the resulting estimates are often implausibly large and some of the assumptions underlying the production function approach are problematic. Il

Despite some ambiguity on the basic facts, the literature has offered a variety of explanations for rising markups: First, network effects could be more prominent than in the past, particularly on digital platforms (OECD, 2022). Top managers may be increasingly adept at exploiting market power (Bao, De Loecker, and Eeckhout, 2022). The increase in markups may equally reflect a decline in labor bargaining power. Unionization rates in the United States are historically low. A large body of research shows concentration among employers is associated with lower wages (Azar, Marinescu, and Steinbaum, 2022; Mertens and Mottironi, 2023). Globalization may be adding pressure as well. Top firms have access to global supply chains and low-cost inputs abroad. They can achieve

<sup>&</sup>lt;sup>10</sup>The appendix provides an overview of the evolution of corporate profitability since the 1980s (see section A.l). There is some ambiguity about the overall trend, in large part because wages and profits are not cleanly separated. Using a comparable measure, profits increased by around 4 percentage points of GDP when comparing the 2010s with the 1980s.

ll Basu (2019) provides a useful overview. Issues include the neutrality of technological progress across factor inputs (Raval, 2023), the omission of some variable costs (Traina, 2018), and the presence of market power over labor and capital inputs (Mertens and Mottironi, 2023).

better economies of scale, diversify into international markets, and gain tax advantages from profit shifting. Amiti and Heise (2021) highlight the role of import penetration, which may lead smaller domestic firms to exit markets. Markups increase with firm age, which is rising in the United States (Peters, 2020; Hopenhayn, Neira, and Singhania, 2018). Related to this, a number of studies look at rising barriers to entry, regulatory capture, and rent-seeking. For example, Covarrubias, Gutiérrez, and Philippon (2019) attribute the decline in competition to the entrenchment of market leaders. Similarly, Zingales (2017) and Faccio and McConnell (2020) link regulatory capture and political connections to the lack of business dynamism in the United States.

The measurement issues should be taken seriously, and the rise in markups could stem from relatively benign causes or even prove illusory. The correlation between markups and firm size could simply reflect that fixed costs are higher for large firms and that significant investments are needed to arrive at the productivity frontier. While investment in physical capital has fallen over time, Crouzet and Eberly (2019) show investment in intangible capital has risen. In particular, superstar firms accumulated substantial digital capital, which explains much of their apparent productivity advantage (Tambe et al., 2020). Furthermore, markup estimates often exclude indirect 'overhead' costs, e.g., marketing and payments to management. Traina (2018) finds that markups have been relatively flat since the mid-1980s when these are included. Rising markups could also reflect changing household preferences. Rising purchasing power may shift the consumption basket towards high-markup goods (Döpper et al., 2022). The shift in consumption from manufacturing to services is important as well. Markups are generally higher in service sectors where owner-employees and pass-through income are prevalent (Cooper et al., 2015).

# 3. Firm Size and Pricing Behavior

Market position can influence pricing behavior in three different ways: differences in (i) the demand schedule, (ii) nominal price rigidities, and (iii) marginal costs following a shock. Much of the following discussion focuses on differences between small and large firms across these dimensions. This informs the modeling approach. While the literature tends to look at these elements separately, the model treats them as connected.

## 3.1. Market Position and the Price Elasticity of Demand

Early interest in the relationship between market position and price dynamics stemmed from antitrust cases. Markham (1951) discusses how rational market behavior could resemble collusion whenever price 'leaders' anticipate the prices of their rivals. While the industrial organization literature has much to offer, most models for aggregate price dynamics use a relatively simple market structure. General equilibrium requires a coherent relationship between individual prices, the demand schedule, and aggregate dynamics, which limits the toolkit available to macroeconomic researchers. The CES specification is popular because it meets these criteria while incorporating some realism in terms of pricing power.

A model capturing interactions between heterogeneous firms requires a more complicated functional form. Initially proposed in Dornbusch (1987), the nested CES form used here follows the specification of Atkeson and Burstein (2008), which combines a discrete CES aggregator, representing all firms within an industry, and a continuous CES aggregator across industries. This leads to strategic interaction between firms within an industry, but not across industries. Since consumers substitute between varieties (i.e., the products within the same industry) more easily than across goods, there is a positive association between market share and pricing power. The specification also builds on Shimomura and Thisse (2012), which captures the interaction between large and small firms using a nested CES form.<sup>12</sup>

Several papers empirically test if nested CES demand describes firm behavior accurately. The prediction is simple – large and small firms face different demand curves and set their prices accordingly. The evidence supports the nested CES view, at least when studies separate own- and cross-price effects. An analysis of French exporters by Berman, P. Martin, and Mayer (2012) finds large firms generally absorb a large part of exchange rate movements in their markups. Auer and Schoenle (2016) use BLS micro-price data to look at whether firms react to own-cost shocks or price changes by competitors. The results indicate the strength of strategic complementarity is hump-shaped in market share, while the pass-through of exchange rate shocks is U-shaped. Amiti, Itskhoki, and

<sup>&</sup>lt;sup>12</sup>As an alternative, Hottman, Redding, and Weinstein (2016) develops a specification where firms produce a number of closely substitutable varieties, which leads to the cannibalization of own sales from price changes.

<sup>&</sup>lt;sup>13</sup>Auer and Schoenle (2016) find the pass-through and slope of the best response price are respectively U- and hump-shaped. This reflects the transition from negligible market share to near monopoly and aligns with the nested CES prediction. The analysis in this paper focuses on oligopoly, i.e., the downward part of the 'U' and the upward part of the

Konings (2019) use Belgian manufacturing data and employ an instrumental variable design that controls for potential endogeneity between costs and final demand. The results suggest small firms fully pass through cost shocks while large firms have a much lower pass-through. Furthermore, large firms behave strategically while small firms do not. Again, these outcomes follow the nested CES prediction. Dedola, Kristoffersen, and Zullig (2021) and Bruine De Bruin et al. (2023) report similar results. The evidence supporting this specification appears robust, although some caution is due given potential reporting bias and the limited number of studies in circulation.

# 3.2. Price Adjustment Frictions

Price adjustment frictions can arise from a wide variety of sources. These include (i) explicit and implicit contracts, (ii) strategic interaction and price coordination failures, (iii) menu and information costs, (iv) managerial inattention and misalignment of incentives, (v) fear of alienating customers, and (vi) uncertainty around the duration of shocks. Firm size appears relevant in all these cases. For example, price increases by large firms might receive wider media attention. Alternatively, managers at small firms often balance multiple tasks, leading to greater managerial inattention. Studies looking at pricing behavior across firms usually find size is relevant. Still, a limited number are in circulation and they use a variety of data sources and methodologies, making it difficult to draw general conclusions. Other factors correlated with firm size, such as industry, could be latent as well.

Most studies find large firms adjust prices more frequently than small firms. An analysis of US producer prices by Goldberg and Hellerstein (2009) indicates large firms change prices two to three times more frequently than small firms.<sup>17</sup> Among goods-producing industries, the implied price duration of 4.3 months for large firms and 8.5 months for small firms. While large firms appear

<sup>&#</sup>x27;hump,' where firms limit their pass-through and become more strategic as market share increases. Monopoly levels of concentration are never considered.

<sup>&</sup>lt;sup>14</sup>Rival prices in Amiti, Itskhoki, and Konings (2019) are based on a price index of all firms in the same industry.

<sup>&</sup>lt;sup>15</sup>The role of sales in price movements is well documented (Peter J Klenow and Malin, 2010; Kryvtsov and Vincent, 2021). On the other hand, Kehoe and Midrigan (2015) argue aggregate prices are sticky even if prices change frequently at the consumer level. Since prices usually return to the exact same level, the 'regular' price is fairly consistent over time. Still, the micro-evidence indicates retailers maintain substantial price flexibility. Casual observation, along with empirical evidence, suggests large firms are more adept at price discrimination through sales (Katz, 2019).

<sup>&</sup>lt;sup>16</sup>For example, when McDonald's increases 'dollar' menu prices, national media often report the price change.

<sup>&</sup>lt;sup>17</sup>Using product-level data across a number of retailers, Nakamura (2008) suggests most price variation arises at the retail level rather than manufacturer level. At the same time, the analysis of producer prices by Goldberg and Hellerstein suggests a high degree of flexibility, equal to that of consumer goods.

to change prices more often, the average price change is smaller. Amirault, Kwan, and Wilkinson (2006) obtain similar results for Canada, as do Stokman and Hoeberichts (2006) for the Netherlands. Other relevant studies include Álvarez and Hernando (2005), Coleman and Silverstone (2007), and Copaciu, Neagu, and Braun-Erdei (2010) and the findings are generally consistent. Still, is not entirely clear if large firms face lower nominal price rigidities. Small firms adjust their prices by greater margins, albeit less frequently. Gopinath and Itskhoki (2010) suggest most variation in price adjustment frequency takes place at highly disaggregated levels, i.e. individual industries. Uniform pricing policies may also drive the frequency of price adjustments (DellaVigna and Gentzkow, 2019).<sup>18</sup>

Price leadership and strategic interaction affect pricing as well. A comparison of experimental evidence on Stackelberg and Cournot competition in Hildenbrand (2010) suggests Stackelberg better fits observed outcomes under price competition, but not under quantity competition. Weber and Wasner (2023) argue price leaders only engage in price hikes if they expect their competitors to do the same. Coordination of price increases therefore requires a sector-wide cost shock. Of course, not all sectors have a clear price leader and other aspects of market structure play a role. For example, Levy et al. (1998) relate the high frequency of price changes among grocery stores to the intensity of competition, low margins on each good sold, and the price sensitivity of consumers. In sectors with high transaction volumes, the price serves as an active feedback mechanism and firms can accurately gauge consumer demand and rival prices. In sectors with few sellers and buyers, firms have less information on the price elasticity of demand, leading to coordination failures (Pennerstorfer et al., 2020).

# 3.3. Firm-Specific Marginal Costs and Aggregate Shocks

Since the publication of Gertler and Gilchrist (1994), studies looking at the financial cycle have paid close attention to firm size, which can serve as a proxy for the presence of financial constraints. The general view has been that small firms are more sensitive to monetary policy than large firms. Yet due to data limitations, both the basic facts on the financial accelerator and their interpretation remain subject to debate. For example, Ottonello and Winberry (2020) identify firms with low default

<sup>&</sup>lt;sup>18</sup>While the analysis here focuses on price dynamics within an industry, there is a long-standing literature looking at how differences in price adjustment speeds across industries affect the propagation of shocks. Basu (1995) shows a roundabout production structure amplifies initial price differences because they affect marginal costs. A subsequent paper by Nakamura and Steinsson (2010) constructs a menu cost model with different price adjustment frictions across sectors. This increases monetary non-neutrality compared to a model where price frictions are uniform.

risk as those most responsive to monetary shocks. Meanwhile, Pérez-Orive and Timmer (2023) find firms in financial distress respond most strongly to monetary tightening in terms of investment and employment. Financial strength does not appear to explain differences in firm performance over the business cycle at all in Crouzet and Mehrotra (2020).

Turning to the business cycle more generally, Crouzet and Mehrotra (2020) find large firms are less affected by economic fluctuations than small firms due to differences in export exposure. This is intuitive since large firms tend to be more diversified, both across different product categories and geographic markets. Similarly, Hong (2018) reports the markup for small firms fluctuates 45 percent more than for large firms over the business cycle. Wages appear particularly important in this context and large firms may exercise substantial power over labor markets (Azar, Marinescu, and Steinbaum, 2022). Mertens and Mottironi (2023) link growth in the markups of large firms to wage compression. Bargaining power among workers and employers likely varies over the business cycle, as highlighted in Lombardi, Riggi, and Viviano (2023). For example, large firms may cut working hours in a downturn as opposed to firing employees (Babecký et al., 2009). While the aforementioned studies cover the main outcomes of interest, the literature comparing small and large firms over the financial and business cycles is large. Miklian and Hoelscher (2022) provide a more comprehensive overview.

# 4. A New Keynesian Model with Asymmetric Competition

The framework here follows the general template used throughout the New Keynesian literature. It solves for aggregate price dynamics. It is forward-looking and assumes rational expectations. It incorporates the standard demand- and supply-side relationships: the investment-saving decision of households, the Phillips curve, and the Taylor rule. While the household side is standard, the firm side has three distinct elaborations: The first and most important is a nested CES demand system with asymmetric firms. The second is the addition of firm-specific marginal cost shocks. The third is firm-specific pricing frictions.<sup>20</sup> Nominal price rigidities relate to Rotemberg adjustment costs.

The modeling approach draws on the literature and emphasizes heterogeneity across several dimen-

<sup>&</sup>lt;sup>19</sup>Large firms usually offer a wage premium, even when controlling for skills (Gibson and Stillman, 2009). This might be one reason workers are more willing to accept cuts over downturns.

<sup>&</sup>lt;sup>20</sup>Differences in the expected persistence of shocks across firms can be implemented as well.

sions. The firm size and productivity distributions are highly skewed within industries. Industry leaders have a much larger market share and a higher degree of pricing power than trailing firms. The literature also suggests leading firms have some degree of monopsony power in factor markets and among suppliers. Franzoni, Giannetti, and Tubaldi (2023) provides evidence for rationing by suppliers during the Covid pandemic, which predominately affected small firms. Firm-specific cost shocks may reflect factors outside the model, such as bargaining power in labor negotiations or price increases by key suppliers. Various evidence suggests large firms set prices more frequently than small firms and the model allows for firm-specific price adjustment costs. Finally, several papers connect low inflation over the 2010s to stronger import competition (Auer and Fischer, 2010; Heise, Karahan, and Şahin, 2022). I include imports as part of the industry structure, but focus on the response to domestic shocks.

This section has four parts: The first part describes the basic setup of households and firms. It is followed by a discussion of nested CES demand and the contribution of own- and cross-price effects to pricing behavior. The next two parts (4.3 and 4.4) cover the solution for flexible and sticky prices respectively. Because the solution for identical firms tends to be straightforward, this is typically included as part of the exposition. The solution for asymmetric firms is relegated to the appendix since the derivations often require a recursive approach.

### 4.1. Households and Firms

Household utility is a function of consumption C and labor L

$$\max_{\{C_t, L_t, B_t\}} U_0 = \mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \left[ \log(C_t) - L_t \right]$$
(1)

subject to the budget constraint

$$P_t C_t + B_t \le W_t L_t + R_{t-1}^n B_{t-1} + P_t \Pi_t + T_t \tag{2}$$

where P is the aggregate price index, B bonds,  $R^n$  the nominal return on bonds, K capital, Q its price, W wages,  $\Pi$  profits, and T a lump sum transfer that accounts for price adjustment and capital rental costs. The optimality condition for labor implies

$$P_t C_t = W_t \tag{3}$$

The trade-off between consumption saving gives the normal Euler equation for bonds

$$1 = \mathbb{E}_t \left[ \beta \frac{P_t C_t}{P_{t+1} C_{t+1}} R_t^n \right] \tag{4}$$

Price adjustment costs are rebated to households, short-run capital is fixed, and trade is balanced. The resource constraint is therefore

$$Y_t = C_t + I_t \tag{5}$$

Monetary policy follows a Taylor rule

$$R_t^n = e^{m_t} R^n \left(\frac{P_t}{P_{t-1}}\right)^{\phi_{\pi}} \left(\frac{Y_t}{Y}\right)^{\phi_y} \tag{6}$$

where  $\phi_{\pi}$  and  $\phi_{y}$  determine the strength of the monetary policy response to deviations in inflation and output. The persistence of monetary policy shocks follows

$$m_t = \rho_m m_{t-1} + \varepsilon_t \quad \text{where} \quad \varepsilon_t \sim \mathcal{N}(0, \sigma_m)$$
 (7)

Firms within an industry each produce a variety of an intermediate good

$$y_{ijt} = e^{a_t} \bar{a}_{ij} \ell_{ijt}^{1-\alpha} \tag{8}$$

where  $\ell$  labor and  $\bar{a}$  is a firm-specific productivity level. The parameter  $\alpha$  represents the capital share in production. Capital is fixed and treated as numeraire. The persistence of aggregate productivity shocks follows

$$a_t = \rho_a a_{t-1} + \xi_t \quad \text{where} \quad \xi_t \sim \mathcal{N}(0, \sigma_a)$$
 (9)

The firm's budget constraint reflects labor and capital rental costs  $\delta$ 

$$\Pi_{ijt} = p_{ijt} y_{ijt} - w_t \ell_{ijt} - \delta \quad \text{where} \quad w_t = \frac{W_t}{P_t}$$
(10)

The relative price of the firm is denoted by p. The marginal cost C includes only wages and productivity

$$\mathcal{C}_{ijt} = \frac{1}{e^{a_t} \bar{a}_{ij}} \left( \frac{w_t}{1 - \alpha} \right)^{1 - \alpha} \tag{11}$$

Differences in marginal costs across firms relates to their long-run productivity level, which is time-invariant. Firm-specific productivity shocks are introduced in section 5.3.

## 4.2. Nested CES Demand

The production structure consists of a nested two-level CES aggregator consisting of industry- and firm-level output.<sup>21</sup> The specification follows Atkeson and Burstein (2008) and Shimomura and Thisse (2012), where the latter is a specific case of the former. The general case is discussed first.

#### 4.2.1. General Case

The nested CES specification of Atkeson and Burstein (2008) has the following structure. Final output bundles together a continuum of goods, each produced by an industry (indexed by j). In turn, industries bundle a finite number of varieties, each produced by an individual firm (indexed by s).

(i) 
$$Y_t = \left[ \int_0^1 y_{jt}^{\frac{\sigma-1}{\sigma}} dj \right]^{\frac{\sigma}{\sigma-1}}$$
 where for each industry (ii)  $y_{jt} = \left[ \sum_{i=1}^n y_{ijt}^{\frac{\varphi-1}{\varphi}} \right]^{\frac{\varphi}{\varphi-1}}$  (12)

where the number of firms  $n \ge 2$ . The elasticity of substitution across goods is given by  $\sigma$  and the elasticity of substitution across varieties is given by  $\varphi$ . The corresponding price indices are

(i) 
$$P_t = \left[ \int_0^1 P_{jt}^{1-\sigma} dj \right]^{\frac{1}{1-\sigma}}$$
 where for each industry (ii)  $P_{jt} = \left[ \sum_{i=1}^n P_{ijt}^{1-\varphi} \right]^{\frac{1}{1-\varphi}}$  (13)

<sup>&</sup>lt;sup>21</sup>There is an implicit assumption in this paper, general in macroeconomics, that an individual firm cannot change the aggregate price index. Hence the measure of industries is zero.

where  $P_t$  is the aggregate price index and  $P_{jt}$  gives the price index for each industry. The allocation of demand across goods and varieties takes the standard CES form

$$(i) \quad y_{jt} = \left(\frac{P_{jt}}{P_t}\right)^{-\sigma} Y_t \quad \text{and} \quad (ii) \quad y_{ijt} = \left(\frac{P_{ijt}}{P_{jt}}\right)^{-\varphi} y_{jt} = \left(\frac{P_{ijt}}{P_{jt}}\right)^{-\varphi} \left(\frac{P_{jt}}{P_t}\right)^{-\sigma} Y_t \quad (14)$$

Using relative prices, the demand schedule for each firm is written as

$$y_{ijt} = p_{ijt}^{-\varphi} \left[ \sum_{i=1}^{n} p_{ijt}^{1-\varphi} \right]^{\frac{\varphi-\sigma}{1-\varphi}} Y_t \tag{15}$$

The price elasticity of demand is therefore

$$\Psi_{ijt} \equiv \frac{\partial \log(y_{ijt})}{\partial \log(p_{ijt})} = (\varphi - \sigma)x_{ijt} - \varphi \quad \text{where} \quad x_{ijt} = \left(\frac{p_{ijt}}{p_{jt}}\right)^{1-\varphi} \equiv \frac{p_{ijt}y_{ijt}}{\sum_{i=1}^{n} p_{ijt}y_{ijt}}$$
(16)

$$= \frac{\varphi - \sigma}{n} - \varphi \quad \text{(if firms are identical)} \tag{17}$$

The price elasticity of demand is affected by a firm's market share x (as long as  $\varphi \neq \sigma$ ). Normally, the elasticity of substitution within an industry is greater than substitution across industries (i.e.  $\varphi > \sigma$ ). In other words, it is easier to substitute across relatively homogeneous varieties than different goods.<sup>22</sup>

#### 4.2.2. Nested CES Demand with Asymmetric Firms and Foreign Competition

Following Shimomura and Thisse (2012), I specify an asymmetric setup where a sector has a mix of large and small firms. Firms are divided by class  $s \in \{L, S\}$  into large (L) and small (S). Foreign imports (F) are also introduced. Domestic firms do not observe the pricing decision of foreign firms and treat it as exogenous. Within each size class, firms are identical. The industry-level price index becomes

$$p_{jt} = \left[ \underbrace{(p_{sjt}^{i})^{1-\varphi}}_{\text{own price}} + \underbrace{(n_{s}-1)(p_{sjt}^{-i})^{1-\varphi} + n_{-s}(p_{-sjt}^{-i})^{1-\varphi}}_{\text{rival prices}} + \underbrace{n_{F}(p_{Fjt})^{1-\varphi}}_{\text{imports}} \right]^{\frac{1}{1-\varphi}}$$
(18)

 $<sup>^{22}</sup>$ For example, a household may buy a different type of toothpaste if their preferred variety becomes too expensive. They could also use baking soda, but might resist this change since the goods are not perfect substitutes.

where i denotes the firm making the pricing decision and -i its domestic rivals. This specification adheres to the general nested CES case. Since all small and large firms are otherwise identical, they are summed together. This entails solving for cross-price effects. Generally, just one large firm (or 'market leader') is assumed so that  $n_L = 1$ . The leader faces multiple smaller rivals where  $n_S > 1$ . The large firm dominates the market and demand for its variety is less sensitive to the price. Since it is sensitive to changes in its market share, it reacts to price changes by rival firms, domestic and foreign, as part of its optimization problem.

#### 4.2.3. Linking the Price Elasticity of Demand to Firm Behavior

In economic models, key aspects of firm behavior – markups, the pass-through of marginal costs, and the best response price – relate to the slope and curvature of the price elasticity of demand. Among specifications allowing for a non-linear relationship between relative prices and relative demand, Kimball (1995) is probably the most common. In this case, the 'superelasticity,' or second-derivative of demand with respect to prices, results from the firm's own price and is generally negative. As a result, small price increases may lead to a disproportionate drop in demand, incentivizing firms to limit the pass-through of cost shocks. The presence of a finite number of firms also induces strategic behavior, which is not an inherent feature of Kimball demand. Firms adjust prices in response to price changes by other firms. The strength and direction of their response is described by the cross-price superelasticity of demand. Prices are strategic complements if the cross-price superelasticity is positive, meaning firms raise prices in response to a price hike by a rival firm. It is also possible they are substitutes. The cross-price effects are typically omitted when firms are identical, but they are important if asymmetries are present or shocks affect only a subset of firms.

#### 4.2.3.1. The Price Elasticity of Demand and Its Curvature

Ueda (2023) explains the relation between markups and the price elasticity of demand  $\Psi_t^i$  in a simple way. Borrowing from this exposition, take a one-period profit maximization problem where the

<sup>&</sup>lt;sup>23</sup>The total number of firms in an industry  $n = n_L + n_S + n_F$ .

budget constraint for firm i is

$$\Pi_t^i = \left( p_t^i - \mathcal{C}_t^i \right) y_t^i \tag{19}$$

Defining the markup  $\mu_t^i$  as price over marginal cost, the solution for the optimal price can be expressed in terms of the price elasticity of demand

$$p_t^i = \frac{\Psi_t^i}{\Psi_t^i + 1} \mathcal{C}_t^i \quad \Longleftrightarrow \quad \mu_t^i = \frac{\Psi_t^i}{\Psi_t^i + 1} \tag{20}$$

Next, defining the own-price superelasticity as

$$\Psi_t^{i,i} \equiv \frac{\partial \Psi_t^i}{\partial \log(p_t^i)} \tag{21}$$

When this term is negative, a typical assumption, it implies large price adjustments reduce demand by a greater extent than small adjustments. In the standard CES case  $\Psi_t^{i,i} = 0$ , i.e. the slope of the demand curve is a constant. Next, the co-movement of markups and prices determines the pass-through of marginal costs. This given by

$$\Psi_t^{\mu^i} \equiv \frac{\partial \log(\mu_t^i)}{\partial \log(p_t^i)} = \frac{\Psi_t^{i,i}}{\Psi_t^i(\Psi_t^i + 1)} \tag{22}$$

Following Amiti, Itskhoki, and Konings (2019), the cost pass-through  ${\cal P}_t^{\,i}$  is defined as

$$\mathcal{P}_t^i \equiv \frac{1}{1 + \Psi_t^{\mu^i}} \tag{23}$$

The cross-price superelasticity with respect to a competitor is given by

$$\Psi_t^{i,-i} \equiv \frac{\partial \Psi_t^i}{\partial \log(p_t^{-i})} \tag{24}$$

and the slope of the best response price  $\mathcal{B}_t^{\,i}$  is given by

$$\mathcal{B}_t^i \equiv \frac{\partial \log(p_t^i)}{\partial \log(p_t^{-i})} = \frac{\Psi_t^{i,-i}}{\Psi_t^i(\Psi_t^i + 1)} \tag{25}$$

Both the cost pass-through  $\mathcal P$  and the slope of the best response price  $\mathcal B$  serve as target values in the baseline calibration.

### 4.2.3.2. Asymmetric Nested CES Case

Given asymmetric firms, the industry-level price index follows (18) and the price elasticity of demand is given by

$$\Psi_{st}^{i} = (\varphi - \sigma) \left(\frac{p_{sjt}^{i}}{p_{jt}}\right)^{1 - \varphi} - \varphi \tag{26}$$

The firm's own-price superelasticity  $\Psi^{i,i}$  is then

$$\Psi_{st}^{i,i} = (\varphi - \sigma)(1 - \varphi) \frac{(n_s - 1)(p_{sjt}^i p_{sjt}^{-i})^{1 - \varphi} + n_{-s}(p_{sjt}^i p_{-sjt}^{-i})^{1 - \varphi} + n_F(p_{sjt}^i p_{Fjt})^{1 - \varphi}}{p_{it}^{2 - 2\varphi}}$$
(27)

and the cross-price superelasticity  $\Psi^{i,-i}$  is

$$\Psi_{st}^{i,-i} = -(\varphi - \sigma)(1 - \varphi) \frac{(n_s - 1)(p_{sjt}^i p_{sjt}^{-i})^{1-\varphi} + n_{-s}(p_{sjt}^i p_{-sjt}^{-i})^{1-\varphi} + n_F(p_{sjt}^i p_{Fjt})^{1-\varphi}}{p_{jt}^{2-2\varphi}}$$
(28)

The last expression for the cross-price elasticity can be divided into three components:

$$\dot{\Psi}_{st}^{i,-i} = -(\varphi - \sigma)(1 - \varphi) \frac{(n_s - 1)(p_{sjt}^i p_{sjt}^{-i})^{1 - \varphi}}{p_{it}^{2 - 2\varphi}} \quad \text{(elasticity to the price of same size firms)} \quad (29)$$

$$\ddot{\Psi}_{st}^{i,-i} = -(\varphi - \sigma)(1 - \varphi) \frac{n_{-s}(p_{sjt}^i p_{-sjt}^{-i})^{1-\varphi}}{p_{jt}^{2-2\varphi}}$$
 (elasticity to the price of other size firms) (30)

$$\ddot{\Psi}_{st}^{i,-i} = -(\varphi - \sigma)(1 - \varphi) \frac{n_F(p_{sjt}^i p_{Fjt})^{1-\varphi}}{p_{jt}^{2-2\varphi}}$$
 (elasticity to the price of foreign firms)

The first term  $\dot{\Psi}$  represents the cross-price superelasticity to other firms of the same size. These firms will choose the same price as the firm making the pricing decision and separating this term simplifies some of the subsequent analysis. The second term  $\ddot{\Psi}$  is the cross-price superelasticity to

firms that are a different size. The final term  $\ddot{\Psi}$  is the cross-price superlasticity to foreign prices. Own- and cross-price superlasticities perfectly offset with nested CES demand

$$\Psi_{st}^{i,i} = -\Psi_{st}^{i,-i}$$

If firms are identical and shocks are purely aggregate, the nested CES case collapses to the standard CES specification. Asymmetry in firm size and/or shocks is needed for a nested CES specification to meaningfully differ.<sup>24</sup> Still, this flexibility is useful since 'aggregate shocks' often reflect shocks to a subset of firms in reality, as highlighted in Gabaix (2011).

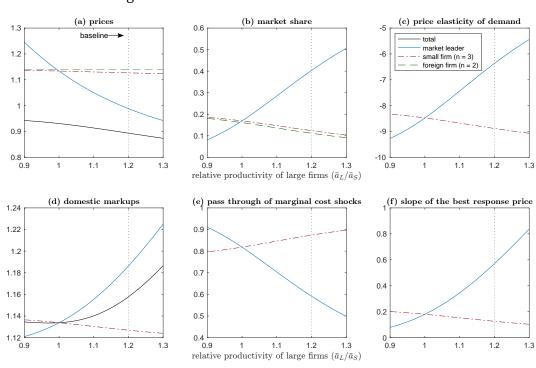


Figure 2: Market Structure Under Flexible Prices

The x-axis gives the relative productivity advantage of large firms over small firms, which is increasing from left to right. When large firms have an advantage, they set a lower relative price (panel a). In turn, this increases demand for their variety and their market share increases (panel b). As market share increases, demand becomes less sensitive to price changes, which allows large firms to increase their markup (panel d). Given the curvature of demand, large firms limit the pass-through of marginal cost shocks (panel e) and respond to competitors prices when their productivity advantage grows (panel f). Note: the 'total' in panel (a) reflects the industry price index.

Figure 2 shows the market structure resulting from nested CES demand when firms are asymmetric. There is one market leader ( $n_L = 1$ ) and multiple trailing firms ( $n_S = 3$ ). In equilibrium, the market share of firms is set by their relative efficiency ( $\bar{a}$ ). This lowers marginal costs and translates into

<sup>&</sup>lt;sup>24</sup>Quasi-kinked demand (Kimball, 1995) is an example of where the demand curve is adjusted by the firm's own-price superelasticity. Kimball demand can mimic strategic behavior if the curvature is adjusted appropriately, as suggested in Wang and Werning (2022). However, the correct adjustment is not always clear.

a price advantage. The x-axis displays the relative productivity of the large firm (i.e., the market leader). Moving from left to right, the market leader becomes more efficient and its production costs go down. It sets a lower price (panel a) and gains market share (panel b), which increases its markup (panel d). Because there are multiple trailing firms within each industry, they remain relatively small. The vertical dotted lines show the productivity gap in the baseline calibration and equilibrium outcomes. In this case, the market share of each small firm is around 12 percent. Therefore, they face highly elastic demand and cannot achieve a high markup. Furthermore, they do not respond to price adjustments by other firms and fully pass through cost shocks. The opposite is true of the market leader. In the baseline calibration, it passes through around 65 percent of cost increases to consumers, as opposed to 90 percent for small firms (panel e). Also, the leader matches around 50 percent of price increases by its rivals (panel f).

The following sections show price dynamics remain highly tractable with the setup. In fact, ownand cross-price superelasticities serve as direct inputs when using undetermined coefficients, and the solution method can readily accommodate other demand functions. Section A.4.1 in the appendix includes some further discussion on solving for the price elasticity of demand.

## 4.3. Flexible Price Equilibrium

This section gives the solution method for the flexible price equilibrium when cross-price effects are present.<sup>26</sup> While numerical methods are preferred, an approach using log-linearization is included for illustration. The dynamic problem is more complicated but uses a similar first-order approximation. In the absence of price adjustment costs or nominal rigidities, firms optimize their profits as follows

$$\max_{p_{st}^i} \quad \Pi_{st}^i = \left( p_{st}^i - \boldsymbol{\mathcal{C}}_{st}^i \right) y_{st}^i \tag{32}$$

With identical firms, the solution for prices is straightforward. The solution for asymmetric firms incorporates the best reply into the firm's decision rule.

 $<sup>^{25}</sup>$ Note small firms are generally treated as less efficient than the market leader. The instance where they have an efficiency advantage is included for illustration only.

<sup>&</sup>lt;sup>26</sup>The flexible price equilibrium is also equivalent to the zero-inflation steady state in the dynamic problem. The log-linearized solution is only locally accurate but useful for illustrative purposes. See the appendix (section A.4.1) for further discussion.

#### 4.3.1. Identical Firms

When firms and industries are identical, demand follows (17) and the solution to the maximisation problem becomes

$$\frac{\partial \Pi_t}{\partial p_t} = 0 \quad \Longrightarrow \quad \left(1 - \frac{\mathcal{C}_t}{p_t}\right) \left(\frac{\varphi - \sigma}{n} - \varphi\right) = -1 \tag{33}$$

Solving for the price is simple in this case

$$p_t^* = \frac{(n-1)\varphi + \sigma}{(n-1)\varphi + \sigma - n} \mathcal{C}_t^* \tag{34}$$

Here, the price is a direct function of marginal costs. Also setting n=1 leads to the standard CES case (as does  $\varphi = \sigma$ ). It is relatively straightforward to determine how the number of firms in an industry affects the markup

$$\frac{\partial \mu_t^*}{\partial n} = \frac{\sigma - \varphi}{[(n-1)\varphi + \sigma - n]^2} < 0 \quad \text{given} \quad \varphi > \sigma \tag{35}$$

Accordingly, greater concentration is associated with rising markups.

#### 4.3.2. Asymmetric Firms

The solution to the firm's optimization problem under asymmetric oligopoly ( $n \ge 2$ ) proceeds as follows: Going back to the profit maximization problem faced by the firm<sup>27</sup>

$$\frac{\partial \Pi_{st}}{\partial p_{st}^{i}} = 0 \quad \Longrightarrow \quad \left(1 - \frac{\mathcal{C}_{st}}{p_{st}^{i}}\right) \underbrace{\left[\left(\varphi - \sigma\right) \left(\frac{p_{st}^{i}}{p_{jt}}\right)^{1 - \varphi} - \varphi\right]}_{\Psi_{st}^{i}} = -1 \tag{36}$$

Solving prices requires inverting the demand function

$$p_{st}^i = \frac{\Psi_{st}^i}{\Psi_{st}^i + 1} \mathcal{C}_{st} \tag{37}$$

The optimal price can be solved numerically or approximated using undetermined coefficients. Log-linearizing and taking a first-order Taylor expansion around the symmetric equilibrium price

<sup>&</sup>lt;sup>27</sup>Industries are identical and their index is dropped from the notation.

gives the following relationship

$$\tilde{p}_{st}^{i} = \underbrace{\frac{\Psi_{s}^{i}(\Psi_{s}^{i}+1)\mathcal{C}_{s}}{v_{s}}}_{1+\Omega_{s}^{i}} \tilde{\mathcal{C}}_{st} + \underbrace{\frac{\ddot{\Psi}^{i,-i}\mathcal{C}_{s}}{p_{s}^{-i}v_{s}}}_{\Omega_{s}^{*}} \tilde{p}_{-st}^{-i} + \underbrace{\frac{\ddot{\Psi}^{i,-i}\mathcal{C}_{s}}{p_{F}v_{s}}}_{\Omega_{s}^{F}} \tilde{p}_{Ft}$$
where  $v_{s} = p_{s}^{i}(\Psi_{s}^{i}+1)^{2} - (\Psi^{i,i} + \dot{\Psi}_{s}^{i,-i})\mathcal{C}_{s}/p_{s}^{i}$ 

Here, the term for similar-size rivals  $(\tilde{p}_{st}^{-i})$  is already incorporated on the left-hand side since  $\tilde{p}_{st}^i = \tilde{p}_{st}^{-i}$ . The resulting decision rule is a function of the firm's marginal costs and rival prices. It can be summarized as

$$\tilde{p}_{st}^i = (1 + \Omega_s^\prime) \, \tilde{\mathcal{C}}_{st} + \Omega_s^* \, \tilde{p}_{-st}^{-i} + \Omega_s^F \tilde{p}_{Ft} \tag{39}$$

Using the decision rule of rival firms allows the problem to be solved as a function of marginal costs and the foreign price alone

$$\tilde{p}_{st}^{i} = \frac{1 + \Omega_{s}'}{1 - \Omega_{s}^{*} \Omega_{-s}^{*}} \tilde{\mathcal{C}}_{st} + \frac{\Omega_{s}^{*} (1 + \Omega_{-s}')}{1 - \Omega_{s}^{*} \Omega_{-s}^{*}} \tilde{\mathcal{C}}_{-st} + \frac{\Omega_{s}^{F} + \Omega_{s}^{*} \Omega_{-s}^{F}}{1 - \Omega_{s}^{*} \Omega_{-s}^{*}} \tilde{p}_{Ft}$$
(40)

Markups and market share are determined using (16) and (37) respectively. While the method of undetermined coefficients is accurate around an initial point (e.g.  $p^*$ ), a numerical solution is needed for the steady state price when it materially deviates from the symmetric case.

# 4.4. Price Dynamics with Nominal Rigidities

Price adjustment frictions are specified using quadratic costs, as in Rotemberg (1982), which gives the same first-order solution as Calvo pricing in the standard three-equation New Keynesian model.<sup>28</sup> Solving the model with variable markups requires several steps: First, I outline the firm's problem and derive a first-order solution for its decision rule. Next, changes in firm-specific marginal costs are related to aggregate shocks. Finally, the response of the economy to inflation and the output gap are used to find the slope of the Phillips curve. This section focuses on the main steps, and the

<sup>&</sup>lt;sup>28</sup>When higher-order approximations are needed, there has been some debate about which specification better describes aggregate price dynamics. The evidence supporting Rotemberg pricing is generally favorable. Richter and Throckmorton (2016) finds a baseline New Keynesian model using Rotemberg pricing better fits observed price dynamics at the zero lower bound compared to an equivalent specification with Calvo pricing. Similarly, Oh (2020) finds Rotemberg pricing better fits the data when looking at uncertainty shocks.

appendix (section A.4) provides more detail.

#### 4.4.1. The Firm's Optimization Problem

The dynamic model introduces Rotemberg price adjustment costs, which are rebated to households

$$\frac{\Theta_s}{2} \left( \frac{P_{st}^i}{P_{st-1}^i} - 1 \right)^2 y_{jt} \quad \text{where} \quad \Theta_s = \gamma_s x_s \Theta$$
 (41)

The price adjustment costs  $\Theta$  are specified so they are proportional across firms. Accordingly,  $\Theta$  is multiplied by the steady state market share of each firm. This ensures the 'weight' firms put on their markup per unit sales is equal to the weight they put on the price adjustment cost. To examine how differences in nominal rigidities across firms affect outcomes, a shifter for the price adjustment cost  $\gamma_S$  is included as well. In the baseline,  $\gamma_S = \gamma_L = 1$ . With this in mind, the profit maximization problem becomes

$$\mathcal{L} = \mathbb{E}_{t} \sum_{k=0}^{\infty} \Lambda_{t+k} \left[ (p_{st+k} - \mathcal{C}_{st+k}) y_{st+k} - \frac{\Theta_{s}}{2} \left( \pi_{t+k} \frac{p_{st+k}}{p_{st+k-1}} - 1 \right)^{2} P_{jt+k} y_{jt+k} \right]$$
(42)

Aggregate inflation appears as an additional term. This is exogenous to the firm and represents a negative externality. Stochastic discounting follows from the household Euler condition

$$\Lambda_{t+k} = \beta^k \frac{P_t}{P_{t+k}} \frac{C_t}{C_{t+k}} \tag{43}$$

With identical industries, the FOC with respect to  $p_{st}^i$  yields

$$0 = p_{st}^{i} y_{st}^{i} + \left(p_{st}^{i} - \mathcal{C}_{st}^{i}\right) y_{st}^{i} \Psi_{st}^{i} - \Theta_{s} Y_{t} \left\{ \left(\pi_{t} \frac{p_{st}^{i}}{p_{st-1}^{i}} - 1\right) \pi_{t} \frac{p_{st}^{i}}{p_{st-1}^{i}} + \beta \mathbb{E}_{t} \left[ \left(\pi_{t+1} \frac{p_{st+1}^{i}}{p_{st}^{i}} - 1\right) \pi_{t+1} \frac{p_{st+1}^{i}}{p_{st}^{i}} \right] \right\}$$
(44)

The FOC is log-linearized and terms are collected using undetermined coefficients to find the decision rule for each firm

$$\tilde{p}_{st}^{i} = \Gamma_{s} \, \tilde{p}_{st-1}^{i} + \left(1 + \Gamma_{s}^{\prime}\right) \, \tilde{\mathcal{C}}_{st}^{i} + \, \Gamma_{s}^{*} \, \tilde{p}_{-st}^{-i} + \Gamma_{s}^{F} \, \tilde{p}_{Ft} + \widehat{\Gamma}_{s} \, \tilde{\pi}_{t} \tag{45}$$

In the expression above, the term for similar-size rivals is already incorporated on the left-hand side since  $\tilde{p}_{st}^{i} = \tilde{p}_{st}^{-i}$ . The decision rule is a function of past prices, marginal costs, rival prices, competition from imports, and inflation. The rival's decision rule gives the best reply

$$\tilde{p}_{st}^{i} = \underbrace{\frac{\Gamma_{s}}{1 - \Gamma_{s}^{*} \Gamma_{-s}^{*}}}_{Y_{s}} \tilde{p}_{st-1}^{i} + \underbrace{\frac{\Gamma_{s}^{*} \Gamma_{-s}}{1 - \Gamma_{s}^{*} \Gamma_{-s}^{*}}}_{Y_{s}^{*}} \tilde{p}_{-st-1}^{-i} + \underbrace{\frac{1 + \Gamma_{s}^{'}}{1 - \Gamma_{s}^{*} \Gamma_{-s}^{*}}}_{Y_{s}^{i}} \tilde{\mathcal{C}}_{st}^{i} + \underbrace{\frac{\Gamma_{s}^{*} (1 + \Gamma_{-s}^{'})}{1 - \Gamma_{s}^{*} \Gamma_{-s}^{*}}}_{Y_{-i}^{-i}} \tilde{\mathcal{C}}_{-st}^{-i} + \underbrace{\frac{\Gamma_{s}^{F} + \Gamma_{s}^{*} \Gamma_{F}^{F}}{1 - \Gamma_{s}^{*} \Gamma_{-s}^{*}}}_{Y_{s}^{F}} \tilde{p}_{Ft} + \underbrace{\frac{\Gamma_{s} + \Gamma_{s}^{*} \Gamma_{-s}^{F}}{1 - \Gamma_{s}^{*} \Gamma_{-s}^{*}}}_{Y_{s}^{T}} \tilde{n}_{t}$$

$$(46)$$

Terms are collected into the Y's for convenience where

$$Y_{s} = \frac{(\psi_{s} + \beta \Theta_{s} Y_{s}^{*}) Y_{-s}^{*} + \Theta_{s}}{\kappa_{s} - \beta \Theta_{s} Y_{s}}$$
 (own past price)

$$Y_s^* = \frac{(\psi_s + \beta \Theta_s Y_s^*) Y_{-s}}{\kappa_s - \beta \Theta_s Y_s}$$
 (rival past price)

$$Y_s^i = \frac{(\psi_s + \beta \Theta_s Y_s^*) Y_{-s}^{-i} - (p_s^i)^{-\varphi} p_j^{\varphi - \sigma} \Psi_s^i \mathcal{C}_s^i}{\kappa_s - \beta \Theta_s (Y_s + \rho)}$$
 (own marginal cost)

$$Y_s^{-i} = \frac{(\psi_s + \beta \Theta_s Y_s^*) Y_{-s}^i}{\kappa_s - \beta \Theta_s (Y_s + \rho)}$$
 (rival marginal cost) (50)

$$Y_s^F = \frac{(\psi_s + \beta \Theta_s Y_s^*) Y_{-s}^F + \omega_s}{\kappa_s - \beta \Theta_s (Y_s + \rho)}$$
 (import price) (51)

$$Y_s^{\pi} = \frac{(\psi_s + \beta \Theta_s Y_s^*) Y_{-s}^{\pi} - \Theta_s (1 - \rho \beta)}{\kappa_s - \beta \Theta_s (Y_s + \rho)}$$
 (inflation)

The convenience terms  $\kappa$ ,  $\psi$ , and  $\omega$  are defined as<sup>30</sup>

$$\kappa_s = \Theta_s + \beta \Theta_s - (p_s^i)^{1-\varphi} p_j^{\varphi-\sigma} \left[ \left( 1 - \frac{\mathcal{C}_s}{p_s^i} \right) \frac{\Psi_s^{i,i} + \dot{\Psi}_s^{i,-i}}{p_s^i} + \Psi_s^i \frac{\mathcal{C}_s}{p_s^i} \right]$$
(53)

$$\psi_{s} = (p_{s}^{i})^{1-\varphi} p_{j}^{\varphi-\sigma} \left(1 - \frac{C_{s}}{p_{s}^{i}}\right) \frac{\ddot{\Psi}_{s}^{i,-i}}{p_{-s}^{-i}}$$
(54)

$$\omega_s = (p_s^i)^{1-\varphi} p_j^{\varphi-\sigma} \left(1 - \frac{\mathcal{C}_s}{p_s^i}\right) \frac{\ddot{\Psi}_s^{i,-i}}{p_F} \tag{55}$$

In the solution for the Y's above, the term  $\rho$  refers generically to the persistence of the shock in question ( $\rho_a$  or  $\rho_m$ ). The steps behind the derivation are provided in the appendix (section A.4.2). The system consists of 12 unknowns and 12 equations, which are solved numerically. It is also

<sup>&</sup>lt;sup>29</sup>Log deviations are defined  $\tilde{x}_t = \log\left(\frac{x_t}{r}\right)$ . Time subscripts are dropped for steady state values.

<sup>&</sup>lt;sup>30</sup>Variables without a time subscript are at their steady state value.

necessary to relate exogenous shocks in the economy to changes in marginal costs for firms and inflation. Again, general equilibrium is solved using undetermined coefficients. For example, the aggregate response to the monetary policy shock m is summarized as

$$(i) \quad \tilde{\pi}_t = \Gamma^{\pi} m_t \qquad \qquad (ii) \quad \tilde{Y}_t = \Gamma^y m_t \qquad (56)$$

noting that marginal costs move in line with aggregate output. The solution for the undetermined coefficients  $\Gamma^{\pi}$  and  $\Gamma^{y}$  are covered in the following sections.

#### 4.4.2. The Relationship Between Marginal Costs and Aggregate Shocks

Wages and output share a simple relationship. The household labor/leisure trade-off determines the real wage

$$w_t = C_t \implies \widetilde{w}_t = \frac{1}{1-\alpha}\widetilde{Y}_t$$
 (57)

Here, I assume long-run capital is at its optimal level so that  $I = \delta K = \alpha Y$ . The log-linear marginal cost for each firm is

$$\widetilde{\boldsymbol{\mathcal{C}}}_{st} = (1 - \alpha)\widetilde{\boldsymbol{w}}_t - \boldsymbol{a}_t \iff \widetilde{\boldsymbol{\mathcal{C}}}_{st} = \widetilde{\boldsymbol{Y}}_t - \boldsymbol{a}_t \tag{58}$$

Accordingly, marginal costs are a function of aggregate output and the productivity shock. Firmspecific productivity shocks are discussed in the appendix (section A.6).

#### 4.4.3. Aggregate Shocks with Identical Firms

This section connects the main shocks (monetary policy and productivity) to changes in output and inflation. It covers the solution for identical firms. The solution for asymmetric firms requires a recursive approach that is covered in the appendix (section A.5). For the monetary policy shock, the Phillips curve is described by the ratio of  $\Gamma^{\pi}$  and  $\Gamma^{y}$  while the sacrifice ratio is the inverse.

## 4.4.3.1. Monetary Policy Shocks and the Phillips Curve

The monetary policy shock acts on demand through the household Euler equation. Log-linearizing and using the resource constraint (5)

$$\widetilde{Y}_{t} = \mathbb{E}_{t} \left[ \widetilde{Y}_{t+1} + \widetilde{P}_{t+1} \right] - \widetilde{P}_{t} - \widetilde{R}_{t}^{n}$$
(59)

In log-linear form, the Taylor rule is

$$\widetilde{R}_t^n = m_t + \phi_\pi \widetilde{\pi}_t + \phi_\nu \widetilde{Y}_t \tag{60}$$

Adding this to the household Euler equation for bonds gives

$$\widetilde{Y}_{t} = \mathbb{E}_{t} \left[ \widetilde{Y}_{t+1} + \widetilde{\pi}_{t+1} \right] - m_{t} - \phi_{\pi} \widetilde{\pi}_{t} - \phi_{y} \widetilde{Y}_{t}$$
(61)

Replacing  $\widetilde{Y}$  and  $\tilde{\pi}$  yields the aggregate demand relationship

$$\Gamma^{y} m_{t} = \rho_{m} (\Gamma^{y} + \Gamma^{\pi}) m_{t} - m_{t} - \phi_{\pi} \Gamma^{\pi} m_{t} - \phi_{y} \Gamma^{y} m_{t}$$

$$(62)$$

$$\Longrightarrow \Gamma^{\pi} = \frac{(1 + \phi_y - \rho_m)\Gamma^y + 1}{\rho_m - \phi_{\pi}} \tag{63}$$

With identical firms, there is no variation in relative prices and the log-linearized aggregate supply relationship is

$$\mathbf{Y}^{\pi}\tilde{\pi}_{t} = \mathbf{Y}^{i}\tilde{\boldsymbol{\mathcal{C}}}_{t}^{*} \tag{64}$$

where the solutions for  $Y^{\pi}$  and  $Y^{i}$  are

$$(i) \quad \mathbf{Y}^{\pi} = \frac{\Theta}{n} (1 - \rho_m \beta) \quad \text{and} \quad (ii) \quad \mathbf{Y}^i = n^{\frac{\varphi - \sigma}{1 - \varphi}} (p^*)^{1 - \sigma} \left( \varphi - \frac{\varphi - \sigma}{n} \right) \frac{\mathbf{C}^*}{p^*}$$
 (65)

Using (56), the monetary policy shock enters as

$$Y^{\pi}\Gamma^{\pi}m_{t} = Y^{i}\Gamma^{y}m_{t} \implies \Gamma^{\pi} = \frac{Y^{i}}{Y^{\pi}}\Gamma^{y}$$

$$(66)$$

This gives aggregate demand (63) and aggregate supply (66) where the  $\Gamma^{\pi}$  and  $\Gamma^{y}$  are the unknowns. Solving gives the reaction of output and inflation to a monetary policy shock and the ratio of  $\Gamma^{\pi}$  and  $\Gamma^{y}$  gives the slope of the Phillip curve

$$\frac{\Gamma^{\pi}}{\Gamma^{y}} = \frac{n^{\frac{1-\sigma}{1-\varphi}}(p^{*})^{-\sigma} \left(\varphi - (\varphi - \sigma)/n\right) \mathcal{C}^{*}}{\Theta(1-\rho_{m}\beta)}$$
(67)

To see how the parameters affect the slope, it is simple to take the limit cases. Setting n=1 gives

$$\frac{\Gamma^{\pi}}{\Gamma^{y}} = \frac{\sigma(p^{*})^{-\sigma} \mathcal{C}^{*}}{\Theta(1 - \rho_{m}\beta)} \quad \text{where} \quad p^{*} = \frac{\sigma}{\sigma - 1} \mathcal{C}^{*}$$
(68)

In the baseline calibration, the elasticity of substitution across goods  $\sigma=1$ . If just one firm monopolizes an industry, the markup becomes infinite and the slope of the Phillips curve goes to zero. In this case, monetary policy is completely non-neutral and only affects output. As the number of firms  $n \to \infty$ , then

$$\frac{\Gamma^{\pi}}{\Gamma^{y}} = \frac{\varphi(p^{*})^{-\sigma} \mathcal{C}^{*}}{\Theta(1 - \rho_{m}\beta)} \quad \text{where} \quad p^{*} = \frac{\varphi}{\varphi - 1} \mathcal{C}^{*}$$
(69)

With monopolistic competition, the slope of the Phillips curve implies some trade-off between inflation and output. Lower Rotemberg adjustment costs steepen the slope of the Phillips curve. When prices are fully flexible, i.e.  $\Theta = 0$ , the slope is vertical and monetary policy is completely neutral, only affecting prices. The same applies for the expected persistence of monetary policy shocks. As the persistence of monetary policy  $\rho_m$  increases, the slope of the Phillips curve steepens.

Although the solution for asymmetric firms is more complicated, it again relies on solving undetermined coefficients. The change in price for each firm is nested within the change industry price

index (where  $\tilde{\pi}_{it} = \tilde{\pi}_t$  given identical industries)

$$\tilde{\pi}_{t+1} = \mathbb{E}_{t} \left[ \frac{n_{s}(P_{s})^{1-\varphi}(\tilde{P}_{st+1} - \tilde{P}_{st}) + n_{-s}(P_{-s})^{1-\varphi}(\tilde{P}_{-st+1} - \tilde{P}_{-st}) + n_{F}(P_{F})^{1-\varphi}(\tilde{P}_{Ft+1} - \tilde{P}_{Ft})}{P_{j}^{1-\varphi}} \right]$$
(70)

Expected future inflation is a function of the monetary policy shock

$$\mathbb{E}_t \left[ \tilde{\pi}_{t+1} \right] = \rho_m \Gamma^{\pi} m_t \tag{71}$$

The monetary policy shock assumes no change in the relative price of foreign goods so that  $\tilde{p}_t^f = 0$  and  $\tilde{\pi}_t^f = \tilde{\pi}_t$ . Accordingly, the change in price for each firm in response to the monetary policy shock is

$$\mathbb{E}_t \left[ \widetilde{P}_{st+1} \right] - \widetilde{P}_{st} = \left[ \rho_m \, \Gamma^\pi + (\mathbf{Y}_s + \rho_m - 1) \Gamma_s^m + \mathbf{Y}_s^* \Gamma_{-s}^m \right] m_t \tag{72}$$

where

$$\Gamma_s^m = Y_s^\pi \Gamma^\pi + (Y_s^i + Y_s^{-i}) \Gamma^y \tag{73}$$

Aggregate demand (63) provides the second equation determining the system. Combining expressions, the only unknowns are  $\Gamma^{\pi}$  and  $\Gamma^{y}$  after some cancellation.

#### 4.4.3.2. Aggregate Productivity Shock

For productivity, the relation between the shock and aggregate output and inflation is given by

$$(i) \quad \widetilde{Y}_t = \Omega^y a_t \qquad \qquad (ii) \quad \widetilde{\pi}_t = \Omega^\pi a_t \qquad (74)$$

Compared to the monetary policy shock, the aggregate demand relationship changes somewhat. Combining the household Euler equation and the Taylor rule gives

$$\Omega^{\pi} = \frac{(1 + \phi_y - \rho_a)}{\rho_a - \phi_{\pi}} \Omega^y \tag{75}$$

With identical firms, aggregate supply is

$$\Omega^{\pi} = \frac{Y^i}{Y^{\pi}} (\Omega^y - 1) \tag{76}$$

Again there are two equations and two unknowns, which gives the solution for  $\Omega^{\pi}$  and  $\Omega^{y}$ . The appendix (section A.5.2) gives the solution for asymmetric firms.

# 5. Calibrated Model and Main Results

This section covers the main results in four parts. The first part presents the calibration and associated target values along with the resulting Phillips curve. The second part covers the pass-through and compares aggregate and idiosyncratic shocks. The third part describes the dynamic response to aggregate productivity and monetary policy shocks across firms along with the contribution of profits to inflation following an impatience shock. The final part covers firm-specific shocks. It looks at how these shocks affect the allocation of demand across firms and quantifies the associated efficiency costs.<sup>31</sup>

## 5.1. Model Calibration

Table 1 gives the baseline calibration, which matches industry characteristics. The model is solved at a quarterly frequency. The time discount factor and the capital share of income use standard values. The Taylor rule coefficients match the values originally proposed in Taylor (1993). The parameters describing the elasticity of substitution across varieties and goods follow Atkeson and Burstein (2008). The number of firms and their relative productivity are based on several target moments.

Target moments include the distribution of market share across large and small firms, the pass-through, and the best response price (see tables 2 and 3).<sup>32</sup> Additional outcomes of interest include

<sup>&</sup>lt;sup>31</sup>Differences in Rotemberg adjustment costs across large and small firms are covered in the appendix (section 5.2.3).

<sup>&</sup>lt;sup>32</sup>The pass-through is taken from table 2, column 4 of Amiti, Itskhoki, and Konings (2019) and the best-response price

Table 1: Baseline Parameter Values

Parameter	Value	Description
α	0.30	Capital returns to scale
β	0.99	Household time discount
$\sigma$	1	Elasticity of substitution across goods
$\varphi$	10	Elasticity of substitution across varieties
Θ	125	Rotemberg price adjustment costs
$\phi_\pi$	1.50	Monetary policy inflation reaction
$\phi_{y}$	0.125	Monetary policy output gap reaction
$n_L$	1	Number of large firms in an industry
$n_S$	3	Number of small firms in an industry
$n_F$	2	Number of foreign firms in an industry
ho	0.85	Persistence of shocks
$p_F$	1.14	Price of foreign imports (steady state)
$\bar{a}_L/\bar{a}_S$	1.2	Relative productivity of large firms
$\gamma_L/\gamma_S$	1	Relative price adjustment costs

the industry HHI, the aggregate markup, and price dispersion. Generally, steady state values align closely with the desired results, excepting some mismatch in the markup of large and small firms. The parameter for the price adjustment cost  $\Theta$  is equivalent to a 35 percent reset probability under Calvo pricing.<sup>33</sup> This appears consistent with the data. Large and small firms are assumed to have the same price adjustment costs in the baseline ( $\gamma_s = 1$ ).

Table 2: Industry-Level Targets

	Large firms		Small firms		_
Description	Target	Value	Target	Value	Source
Market share	0.40	0.40	0.15	0.13	Affeldt, Duso, and Szücs (2018)
Pass-through	0.50	0.58	0.80	0.87	Amiti, Itskhoki, and Konings (2019)
Slope of best response price	0.60	0.58	0.12	0.10	Ibid.
Markup ( $\mu-1$ )	0.24	0.19	0.16	0.13	Hottman, Redding, and Weinstein (2016

The allocation of market share in table 2 is based on the analysis of the EU Merger Control database

is from column 7. The markups correspond to the top decile and median firm in table 8 in Hottman, Redding, and Weinstein (2016). The markup estimates assume monopolistic competition and use product-level elasticities.

<sup>&</sup>lt;sup>33</sup>The corresponding parameter under Calvo pricing  $\theta$  is the probability a firm keeps the same price. The average price elasticity of demand in an industry is around 8.1 and setting  $\Theta=125$  matches a benchmark model using Calvo pricing where  $\theta\approx0.65$ , which implies the average duration is 8.6 months. Peter J. Klenow and Kryvtsov (2008) report the same average duration for the regular price.

by Affeldt, Duso, and Szücs (2018). The large firm target takes the average/median market share observed for large firms. The small firm target is based on the average market share of all trailing firms, but a lower value is acceptable since around 15 percent of market share is unreported. The slope of the best response price and the pass-through are from Amiti, Itskhoki, and Konings (2019). The model does not fully match the level of markups reported in Hottman, Redding, and Weinstein (2016), but the relative gap is the same. Moving to table 3, the HHI estimated by Benkard, Yurukoglu, and Zhang (2021) provides an alternative target for the distribution of market share. The study finds the median HHI in local product markets decreased from 2360 to 2045 between the years 1994 and 2019. The value generated by the model is at the upper end of this range. The aggregate markup is based on the long-term average of corporate accounting profits. The underlying tabulations are discussed in the appendix (section A.1). A meta-study by Tetlow (2022) finds the sacrifice ratio usually falls between 2 and 3, and this informs the Phillips curve target.

Table 3: Aggregate Targets

Description	Target (range)	Value	Source				
Targeted							
Median industry HHI (incl. foreign firms)	2045 - 2360	2340	Benkard et al. (2021)				
Aggregate markup ( $\mu-1$ )	0.13 - 0.16	0.16	See note.				
Import penetration in manufacturing	0.19 - 0.23	0.21	Hale et al. (2019)				
Slope of the Phillips curve	0.20 - 0.33	0.33	Tetlow (2022)				
Implied							
Price dispersion (std. dev. of log prices)	-	0.07	-				
Markup dispersion (std. dev. of log markups)	-	0.03	-				

Note: Section A.1 of the appendix covers the evolution of accounting profits. The relation between markups and aggregate profits is  $Y_t/(Y_t - \Pi_t) = \mu_t$ 

The model generates dispersion in prices and markups across the cross-section of firms. This is measured using the standard deviation of log prices and markups, weighted by market share. There are many estimates of price dispersion in the literature, but few apply directly to the model environment. Abbott (1989) appears to be the only example looking at producer prices. The study finds variation in prices is around 16 percent for the median industry when dividing the interquartile range for prices by the median. The model returns 15 percent by the same calculation. There are multiple studies looking at dispersion in consumer prices across retailers. Even for identical goods, the variation across retailers can be fairly large. Sheremirov (2020) finds the standard deviation is around 6.6 log points for homogeneous products in IRI retail scanner data. Kaplan and Menzio

(2015) finds the standard deviation of normalized prices for identical goods is 19 percent while this rises to 25 percent for closely substitutable goods.<sup>34</sup> Yet even when studies include near substitutes, it is unclear whether price dispersion arises from differences in producer prices or those set by retailers. As with markups, price dispersion is not targeted. The slope of the Phillips curve, another key outcome, is discussed in the following section.

### 5.1.1. Concentration and the Slope of the Phillips Curve

The Phillips curve describes the relationship between inflation and output. Wang and Werning (2022) look at how higher concentration affects the slope, and figure 3 presents a similar set of results. The left-hand panel gives the responsiveness of output to a monetary policy shock ( $\Gamma^y$ ). The center panel gives the responsiveness of inflation ( $\Gamma^{\pi}$ ). Their ratio gives the slope of the Phillips curve, which is presented in the right panel. Moving from left to right along the x-axis corresponds to an increase in concentration. This is evaluated in three ways: (i) identical firms where the number n changes; (ii) the baseline calibration where the productivity of the leader  $\bar{a}_L$  grows relative to the productivity of small firms; and (iii) the baseline calibration where the number of small firms  $n_S$  changes. Each change leads to a different allocation of market share, e.g. between the market leader and other firms or between domestic and foreign firms. The vertical dotted line shows the HHI implied by the baseline calibration.

 $\Gamma^{\pi}$  (inflation response)  $\Gamma^y$  (output response)  $/\Gamma^y$  (Phillips curve slope) -1.9 0.35 -0.55 -2.1 -0.6 0.3 -0.65 -2.3 0.25 # firms (identical) -0.7 -2.4 productivity/size # small firms 2000 2000 3000 4000 2500 3000 3500 4000 3500

Figure 3: Concentration and the Response to a Monetary Policy Shock (Baseline)

The x-axis displays the HHI and a move from left to right corresponds to an increase in concentration. The vertical dotted line gives the HHI corresponding to the baseline calibration. The left-hand panel shows the response of aggregate output to a monetary policy shock, while the center panel gives the response of inflation. The right-hand panel gives their ratio, i.e. the slope of the Phillips curve, which is decreasing as concentration rises. The four cases are (i) identical firms where n decreases, (ii) the baseline calibration where the productivity of the leader improves and its market share increases, and (iii) the baseline calibration where  $n_S$  decreases.

The results are close to those presented in Wang and Werning (2022). In their study, a naïve

<sup>&</sup>lt;sup>34</sup>Similarly, Böheim, Hackl, and Hölzl-Leitner (2021) find a coefficient of variation around 0.12 comparing online prices across retailers in Austria

oligopoly model closely matches a more sophisticated model with strategic complementarity and firm heterogeneity. The same could be said here. When looking at a range of plausible values for the HHI, different forms of concentration all lead to flattening of the slope of the Phillips curve, both the expansion of large firms and exit by small firms. However, exit by small firms has a large effect since the remaining small firms consolidate market share. This reduces the aggregate price elasticity of demand to a greater extent, at least when foreign firms are present.<sup>35</sup> While it is tempting to link higher concentration to the observed flattening of the Phillips Curve, even modest change requires a large increase in concentration in the context of the model.<sup>36</sup> In part, this is a consequence of the parameterization. Large and small firms face the same price adjustment costs in the baseline. Firm-specific adjustment costs are explored in section 5.2.3. The effect of concentration on the Phillips is ambiguous if nominal price adjustment costs fall as a consequence.

#### 5.1.2. The Pass-Through for Idiosyncratic and Aggregate (Domestic) Cost Shocks

While the solution for an aggregate shock remains the same as before, the response to an idiosyncratic shock requires some further explanation. Most elements are similar to section 4.4.1, but each firm's decision rule (46) needs two adjustments reflecting different own- and cross-price reactions. The convenience terms are modified so that

$$\kappa_s^* = \Theta_s + \beta \Theta_s - (p_s^i)^{1-\varphi} p_j^{\varphi-\sigma} \left[ \left( 1 - \frac{\mathcal{C}_s}{p_s^i} \right) \frac{\Psi_s^{i,i}}{p_s^i} + \Psi_s^i \frac{\mathcal{C}_s}{p_s^i} \right]$$
(77)

$$\psi_s^* = (p_s^i)^{1-\varphi} p_j^{\varphi-\sigma} \left(1 - \frac{C_s}{p_s^i}\right) \left(\frac{\dot{\Psi}_s^{i,-i}}{p_s^i} + \frac{\ddot{\Psi}_s^{i,-i}}{p_{-s}^i}\right) \tag{78}$$

The Y's are re-estimated accordingly. The log deviation in prices is given by

$$(i) \quad \tilde{p}_{st}^{i} = Y_{s} \, \tilde{p}_{st-1}^{i} + Y_{s}^{*} \, \tilde{p}_{-st-1}^{-i} + Y_{s}^{i} \, \widetilde{\boldsymbol{\mathcal{C}}}_{st}^{i} \quad \text{and} \quad (ii) \quad \tilde{p}_{-st}^{-i} = Y_{-s} \, \tilde{p}_{-st-1}^{-i} + Y_{-s}^{*} \, \tilde{p}_{st-1}^{i} + Y_{-s}^{-i} \, \widetilde{\boldsymbol{\mathcal{C}}}_{-st}^{i}$$

There is a degree of price smoothing, meaning the change in prices tends to be smaller than the change in costs – but also more durable. For this reason, the pass-through is measured over the

<sup>&</sup>lt;sup>35</sup>Strategic complementarity with foreign firms plays a role. The relationship between market share and the price elasticity of demand are presented in figure 16 in the appendix.

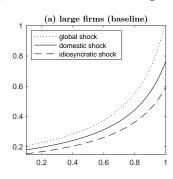
<sup>&</sup>lt;sup>36</sup>A decrease in the slope of the Phillips curve by 0.01 implies an increase in the HHI of more than 200 points. The change in HHI estimated by Benkard, Yurukoglu, and Zhang (2021) is around 300 points for the past 25 years.

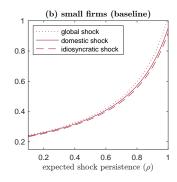
duration of the shock using

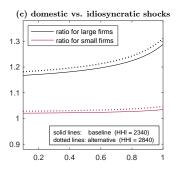
$$\mathcal{P} = rac{\sum_{t=1}^{t=t^*} \widetilde{p}_{st}^i}{\sum_{t=1}^{t=t^*} \widetilde{\mathcal{C}}_{st}^i}$$

where  $t^*$  is large enough to ensure both variables revert to their steady state.<sup>37</sup> The model is re-estimated over a range of values for the expected shock persistence.

Figure 4: The Pass-Through of Cost Shocks for Large and Small Firms (Full Time Horizon)







The x-axis displays the expected persistence of the shock. In the left and center panels, the y-axis gives the pass-through, which is measured over the entire duration of the shock. The solid lines give the response to an aggregate shock while the dashed lines describe the response when shocks are idiosyncratic. The 'global shock' includes a a reaction of foreign prices mirroring domestic inflation. The right-hand panel takes the ratio of aggregate and idiosyncratic shocks. The alternative scenario (dotted lines) in the right-hand panel modifies the baseline so that  $n_S = 2$  and  $p_F = 1.17$ . This increases the market share of the leading firm to 43 percent and significantly lowers the pass-through of idiosyncratic shocks.

The pass-through following a cost shock is presented in figure 4. Expectations play a role because firms weigh the future benefit of adjusting prices against the costs of doing so. When cost shocks are transient, firms prefer relatively small adjustments and absorb the associated costs (see the left-hand and center panels). When cost shocks are persistent, the pass-through increases. The pass-through is lower for large firms due to strategic complementarity with foreign firms. A permanent shock has near-complete pass-through for both small and large firms when global in scope, i.e. a shock affecting all domestic and foreign firms equally. The degree of pass-through by large firm drops when the shock only affects domestic firms or is idiosyncratic. For large firms, the difference is significant – the pass-through of a global shock is around 65 percent higher compared to an idiosyncratic shock and there is a 25 percent difference when comparing idiosyncratic and aggregate domestic shocks. This appears consistent with Gödl-Hanisch and Menkhoff (2023), which finds the differences in pass-through between idiosyncratic and aggregate shocks is around 30 percent.<sup>38</sup> This result is also supported by Dedola, Kristoffersen, and Zullig (2021) and Lafrogne-Joussier, J. Martin, and

 $<sup>^{37}</sup>$ Setting  $t^* = 1000$  ensures this margin is extremely small and indistinguishable from 0. In practice, the pass-through is only observed over a limited period and the appendix (section A.4.3) presents the same results for the first eight quarters of the shock.

 $<sup>^{38}</sup>$ The level of pass-through depends on the persistence of the shock. Bruine De Bruin et al. (2023) find the average pass-through following the COVID-19 shock was 60 percent.

Mejean (2023).<sup>39</sup> Along with the baseline, the right-hand panel in figure 4 includes an alternative scenario with higher concentration. As the HHI rises, both own- and cross-price effects become more prominent with larger jumps in the pass-through.

# 5.2. The Dynamic Response to Aggregate Shocks

This section looks at price dynamics following each of the shocks included in the model and draws comparisons with the empirical literature. Impulse responses are measured as the percent deviation from the steady state. The productivity shock is discussed first, followed by the monetary policy shock. With quadratic adjustment costs, dispersion arises solely from the cross-section of firms. This contrasts with most models incorporating Calvo price frictions, where dispersion arises from price staggering. Foreign prices are assumed to track domestic inflation.

#### 5.2.1. Productivity Shock

Figure 5 gives the dynamic response to a one percent productivity shock. As expected, it increases aggregate output and the real wage. While this raises the cost of labor and capital inputs for firms, the shock improves their efficiency and their costs drop. Because prices demonstrate significant inertia compared to costs due to Rotemberg pricing frictions, markups increase, particularly for large firms. This amplifies the steady state distortion and markup dispersion rises. The gap in relative prices relates to differences in pricing power and the pass-through. Large firms only pass through part of the cost saving to households and they cut their prices by less compared to small firms. Since the price level of large firms is below the level set by small firms in the steady state, the shock leads to price compression. Differences in relative prices also explain the reallocation of market share towards small firms.

The results align with two empirical studies. Sheremirov (2020) observes a positive co-movement between dispersion in regular prices and inflation.<sup>40</sup> For a 1 percentage point increase in inflation, dispersion in the log of regular prices increases 0.026 percent. The model implies a value of 0.028 percent. The results indicate small firms are more sensitive to the business cycle, which is consistent

<sup>&</sup>lt;sup>39</sup>In addition, Lafrogne-Joussier, J. Martin, and Mejean (2023) compares the pass-through for a shock to energy prices and a shock to the price of imported inputs. In the former case, the pass-through is near 100 percent whereas it is 30 percent for the latter. They also find the pass-through is higher for positive cost shocks than negative shocks.

<sup>&</sup>lt;sup>40</sup>Sheremirov (2020) also observes the Calvo model overstates the co-movement of price dispersion with inflation by a factor of 15 and a similar analysis is included in the appendix (section A.7).

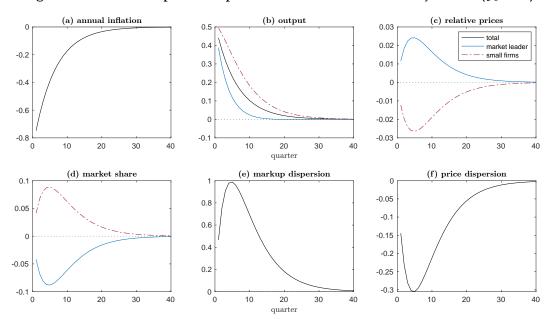


Figure 5: Baseline Impulse Response to a Positive Productivity Shock ( $\xi_0 = 1$ )

The initial shock increases aggregate productivity by one percent. The x-axis gives the number of quarters following the shock. The y-axis gives the deviation from the steady state. Inflation drops and output expands. While wages and capital rental costs increase, efficiency is also higher. The latter effect dominates and marginal costs drop. Small firms pass their savings to consumers and cut their relative prices more than large firms. This reduces price dispersion since small firms have a higher price in equilibrium. Large firms increase their markup by more than small firms. This increases markup dispersion.

with Crouzet and Mehrotra (2020). They find a differential in the response of sales to a change in GDP. The estimated elasticity of sales to GDP is 2.5 for the top 1 percent of firms (by size) and 3.1 for the bottom 99 percent. Looking at output, the model implies small firms are around 35 percent more sensitive to the business cycle than large firms, whereas the corresponding figure from Crouzet and Mehrotra is 24 percent.

#### 5.2.2. Monetary Policy Shock

Figure 6 presents the dynamic response to a one percentage point increase in the annualized interest rate. Aggregate inflation and output decline in response to the shock. When monetary policy tightens, marginal costs fall in line with output. Prices do not immediate adjust and markups are counter-cyclical. Due to differences in the price elasticity of demand, the effect of the shock on prices and output is not symmetric across firms and large firms are more sensitive. Large firms do not fully pass cost savings through to consumers, and they cut prices by less than small firms. Since small firms set a higher price in the steady state, this leads to price compression.<sup>41</sup> Demand for the variety

<sup>&</sup>lt;sup>41</sup>Price dispersion is measured using the weighted standard deviation of log prices in each time period, where the market share of each firm gives the weight. Log markups are similarly used to measure markup dispersion.

produced by the large firm drops since its relative price is higher, which leads to a decline in market share. Given monetary easing, the results are fully symmetric.

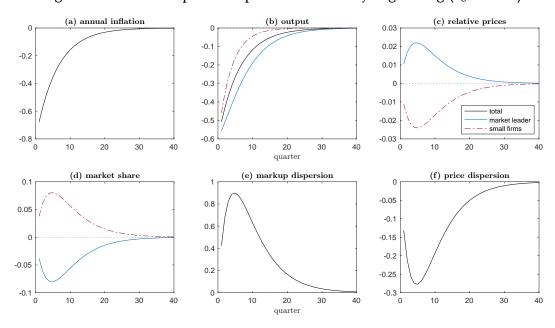


Figure 6: Baseline Impulse Response to Monetary Tightening ( $\varepsilon_0 = 0.25$ )

The monetary policy shock is equivalent to a one percentage point increase in the nominal interest rate. The x-axis gives the number of quarters following the shock. The y-axis gives the deviation from the steady state. Inflation drops by around 0.7 percent in the first period. The evolution of relative prices among small and large firms results from differences in pricing behavior. Marginal costs fall in line with output. Large firms do not fully pass through savings and set a higher relative price following the shock. As a consequence, they lose market share. Because large firms both charge a higher markup and increase it by more than small firms, this amplifies markup dispersion.

Price and markup dispersion move in opposite directions: both small and large firms increase their markup, but the increase for large firms is more pronounced. Large firms already charge a higher markup in equilibrium, so this amplifies the steady state distortion and markup dispersion rises. This outcome is consistent with Meier and Reinelt (2022) who find a contractionary monetary shock increases markup dispersion while easing lowers it. The implied change in the variance of log markups from a 1 percentage point increase in the interest rate is 0.001, matching what Meier and Reinelt report. The results are also consistent with Chiavari, Morazzoni, and Smirnov (2021) who find older/incumbent firms raise their markups in response to monetary tightening. However, other supporting empirical evidence is mixed. When looking at detailed firm-level microdata from the US Census Bureau's Quarterly Financial Report survey, Crouzet and Mehrotra (2020) do not find a statistically significant difference in the response across large and small firms to monetary policy.<sup>42</sup> Ferrando et al. (2021) look at the differential response of low- and high-markup firms to

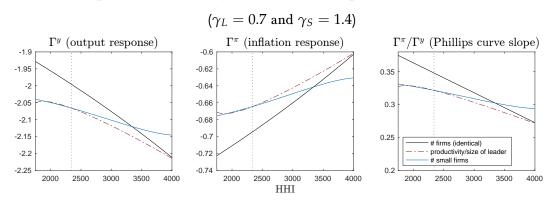
<sup>&</sup>lt;sup>42</sup>Crouzet and Mehrotra (2020) suggest economies of scope may play an important role in explaining why small firms are more sensitive to aggregate shocks. Large firms often operate in multiple industries and can compensate for

surprise monetary announcements. As borrowing costs rise in response to monetary tightening, high-markup firms maintain sales, evidence they limit the cost pass-through. This differs from the results presented here, but the study by Ferrando et al. focuses on the credit channel of monetary policy, which raises marginal costs. It is also possible differences in the price elasticity of demand across firms are confounded by other factors, such as financial constraints. As the following section shows, differences in price adjustment costs across firm are one such confounding factor.

#### 5.2.3. Differences in Nominal Price Adjustment Costs Across Firms

The results in Goldberg and Hellerstein (2009) indicate large firms have greater price flexibility than small firms, at least when measuring the time between price resets. Price adjustment costs in the model are set so that  $\gamma_L$  and  $\gamma_S$  are 0.7 and 1.4 respectively, meaning that large firms face much lower adjustment costs. As figure 7 shows, the slope of the Phillips curve becomes less sensitive to growing concentration compared with the baseline in figure 3. The interpretation is simple: although real rigidities become stronger as large firms expand, this is partially offset by lower nominal rigidities.

Figure 7: Firm-Specific Nominal Rigidities and the Response to a Monetary Policy Shock



The underlying exercise and its interpretation are the same as figure 3, except the nominal price adjustment costs of small and large firms are modified. Large firms are assumed to have a significantly lower price adjustment cost where  $\gamma_L=0.7$  and  $\gamma_S=1.4$ . The change in the slope of the Phillips curve from the expansion of large firms is ambiguous if their prices are more flexible.

A monetary policy shock is applied (as in figure 6) with a wedge in price adjustment costs and greater flexibility for large firms. As before, marginal costs drop in response to the shock and large firms pass-through a greater share of their savings. This results in a lower relative price, opposite to what happens in the baseline monetary shock. Similarly, the wedge in adjustment costs leads to lower markup dispersion and higher price dispersion in response to the shock. As mentioned in the previous section, the evidence on the effect of monetary policy on large and small firms is mixed.

industry-specific shocks whereas small firms are more exposed.

Differing nominal rigidities across firms could explain this inconsistency, although other channels may be important as well.

 $\gamma_L = 0.7$  and  $\gamma_S = 1.4$ output annual inflation relative prices 0.02 -0.1 market leade 0.01 small firms -0.2 -0.2 -0.3 -0.4-0.4 -0.6 -0.01 -0.5 -0.8 -0.02 30 40 30 market share (total) markup dispersion price dispersion 0.25 0.06 0.04 0.2 -0.2 0.02 0.15 -0.4 0.1 -0.02 -0.6 0.05 -0.04 -0.06 -0.8 20

Figure 8: Impulse Response to Monetary Tightening When Nominal Rigidities Differ ( $\varepsilon_0 = 0.25$ )

Here large firms have a lower price adjustment costs than small firms. The monetary policy shock is equivalent to a one percentage point increase in the nominal interest rate. The x-axis gives the quarter following the shock. The y-axis is scaled to give the deviation from the steady state.

# 5.3. The Dynamic Response to Firm-Specific Productivity Shocks

This section considers cost shocks that only affect small firms. These shocks are economy-wide and have general equilibrium effects. To give one example of such a shock, Franzoni, Giannetti, and Tubaldi (2023) provide evidence of rationing among suppliers during the COVID-19 shock. Suppliers favored larger customers, and small firms experienced longer backlogs. Their study suggests (i) supply backlogs were associated with rising industry CPI, (ii) trailing firms within an industry were more exposed to supply chain backlogs, and (iii) leading firms raised their markups following the shock. Changes in the tax wedge between small and large firms provides another instance where marginal costs may systematically differ. The model looks at how cross-price effects can amplify inflation and allows for some quantification of the resulting economic losses.

Strategic complementarity in pricing is one mechanism explaining why some firms may have earned 'excess' profits following the COVID shock. While the markup response to a productivity shock is typically pro-cyclical in the model, it is possible to generate a counter-cyclical response given a

negative productivity shock to small firms as long as the shock is persistent in expectation: Small firms pass the cost increase onto households, leaving their markup unchanged. Meanwhile, large firms raise prices as a strategic response, despite lower costs, resulting in a higher aggregate markup.

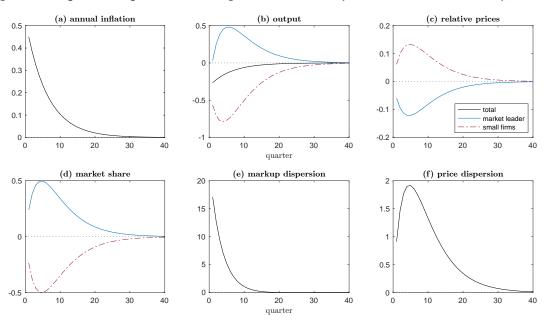


Figure 9: Impulse Response for a Negative Productivity Shock to Small Firms ( $\xi_0 = -1$ )

A negative 1 percent productivity shock is applied to small firms. This has general equilibrium effects, and there is an increase in inflation and a decline in output. Because the shock is firm-specific, there is a large impact on relative prices and market share. Large firms raise their markup, and markup dispersion significantly increases. Given a positive shock to small firms, the opposite would hold.

Figure 9 shows the impulse response following a productivity shock to small firms, using the baseline calibration. The shock is inflationary and reduces aggregate output, which lowers marginal costs for all firms. This allows large firms to set a lower relative price, and they gain market share. Still, large firms do not cut prices in line with costs and markup dispersion rises by 15 to 20 percent. Compared to a benchmark economy where all firms are monopolistic, inflation is only around 6-7 percent higher. In this case, nominal price rigidities largely dampen the cross-price response, but lower adjustment costs for large firms (i.e.  $\gamma_L/\gamma_S < 1$ ) can accelerate inflation. Likewise, markups increase following a highly persistent productivity shock to small firms. In the case where  $\rho_a = 0.98$ , small firms pass the entirety of the shock into prices and strategic complementarity leads to 20 percent higher inflation compared with a monopolistic benchmark. As the following section will discuss, there are also significant real effects from firm-specific shocks due to changes in markups, even if cross-price effects are relatively weak.

# 5.4. Measuring Allocative Efficiency

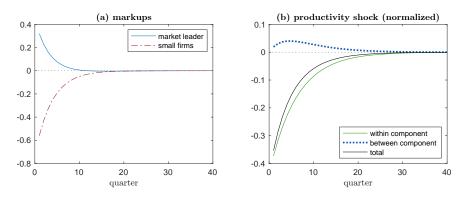
The reallocation of demand across firms affects the efficiency of the economy. Large and small firms have different productivity levels; hence, changes in demand across firms affect aggregate productivity. To measure this, the change in productivity A is divided into two components:

(i) 
$$A_t^w = y_S n_S \bar{a}_S e^{a_{St}} + y_L n_L \bar{a}_L e^{a_{Lt}}$$
 (ii)  $A_t^b = y_{St} n_S \bar{a}_S + y_{Lt} n_L \bar{a}_L$  (79)

where  $A^w$  gives the 'within' component, i.e. the change in productivity holding market share constant. The change from the reallocation of market share  $A^b$ , or the 'between' component, is more interesting since it reflects differences in pricing across firms.

Looking at the within component, the monetary tightening and productivity shocks from the previous sections both lead to efficiency losses. It is also evident that large firms lose market share in figures 5 and 6. Since they are the most efficient producers, this affects aggregate productivity – yet the effect is somewhat trivial when shocks are aggregate. The productivity shock results in a cumulative output gain of 2.9 percentage points. Reallocation to small firms lowers this by 0.1 percentage points, and the total cumulative output gain is 2.8 percent. For monetary policy tightening, the cumulative output loss amounts to 3.4 percentage points of potential, mostly from the within component. Again, around 0.1 percentage points is explained by reallocation across firms. While these losses are a second-order concern, shocks may affect firms unequally. In this case, the contribution of dynamic reallocation to productivity becomes more prominent.

Figure 10: Impulse Response Given a Negative Productivity Shock to Small Firms ( $\xi_0 = -1$ )



A one percent productivity shock is applied to small firms. Small firms cut their markup by less than large firms when facing a comparable shock. The relative price of small firms increases and demand shifts towards large firms. This reallocation partially offsets the static losses resulting from the shock.

Figure 10 gives the response of markups and aggregate productivity to a shock affecting small firms

alone. General equilibrium effects are present since the shock equally impacts small firms across industries. Reallocation to large firms partially offsets the loss from the shock. Following the shock, small firms are forced to raise their prices. Large firms raise their prices as a strategic response and also benefit from lower costs since output falls, leading to higher markups. The loss from the within component is 2.5 percentage points of potential output. The between component offsets this, adding 0.5 percentage points of potential output, meaning the net impact of the shock is around 2 percentage points of potential output. Still, this offsetting effect could be larger in a counterfactual sense. If strategic complementarity were absent, i.e., firms were purely monopolistic, the dynamic gain would be 40 percent larger: 0.8 percentage points.<sup>43</sup> The 0.3 percentage point difference reflects the 'cost' of market power in the model, making the shock almost 20 percent worse than a monopolistic benchmark. A more persistent productivity shock imposes a considerably higher cost. With  $\rho_a = 0.98$ , the efficiency losses under oligopoly are around 35 percent larger than a monopolistic alternative.

# 6. Discussion of Results

# 6.1. Policy Implications and Further Extensions

With higher inflation, there are indications the pass-through has recently increased (Amiti, Heise, et al., 2023).<sup>44</sup> This is consistent with the model's predictions and highlights the role of strategic complementarity in price setting. The nature of shocks appears highly relevant. For example, shocks to energy prices have a high pass-through (Lafrogne-Joussier, J. Martin, and Mejean, 2023). Since these shocks unambiguously affect all firms, pricing complementarities are strong.<sup>45</sup> With rising concentration, strategic complementarity becomes relevant when shocks only affect a subset of firms. This informs the debate on so-called 'greedflation' – the idea large corporates exploited inflation to exercise market power (Weber and Wasner, 2023; Franzoni, Giannetti, and Tubaldi, 2023).

 $<sup>^{43}</sup>$ To find the counterfactual, the number of firms is increased while targeting the same equilibrium allocation of market share between large and small firms. In practice, the alternative setting is  $n_L = 600$ ,  $n_S = 2900$ , and  $n_F = 2000$ . This eliminates both own-price effects and strategic complementarity since each firm's market share is negligible. Still, the same productivity wedge remains.

<sup>&</sup>lt;sup>44</sup>While rising concentration could explain the observed flattening of the Phillips curve over the 2000s, it was more likely a consequence of the inflation regime. With higher inflation, the Phillips curve has steepened (Hobijn et al., 2023). <sup>45</sup>An unexpected jump in the pass-through may have additional consequences. While the model here is completely forward-looking, inflation expectations likely have a backward-looking component. Jumps in the pass-through may deanchor such expectations.

As highlighted in the section on dynamic reallocation, strategic complementarity is a source of inefficiency when small firms are more exposed to cost or productivity shocks, which might have been the case following the COVID pandemic.<sup>46</sup> When these shocks are persistent, the model also shows higher markups accelerate inflation. This is much less the case with aggregate shocks where large firms absorb cost increases to some extent.

The baseline results also show that large firms disproportionately benefit from monetary easing (see figure 6). While large firms compress their profit margins more than small firms, they gain market share as a result. The results contribute to a literature arguing that low interest rates likely exacerbated the concentration trend. Of course, other channels likely played a role. One obvious example is M&A activity, which favors established firms (Blonigen and Pierce, 2016; Chatterjee and Eyigungor, 2023; Kroen et al., 2021). Low interest rates likely affect R&D as well, allowing market leaders to pull ahead. Liu, Mian, and Sufi (2019) argue that low rates widened the gap between firms at the innovation frontier and those behind, discouraging competition and market entry. The model here also suggests that small firms benefit from monetary tightening. There is some evidence against this, and the results may require further elaboration. A VAR analysis by Hamano and Zanetti (2022) indicates that monetary policy tightening both reduces firm entry and increases firm exit. Due to low rates of market entry, the short-term impact on productivity is negative: incumbent firms are insulated from competition and increase their markups. Such an extension would be useful, and Kharroubi and Smets (2024) develop a framework along these lines.

While monetary policy cannot target specific groups of firms, smaller firms may be more responsive to the credit channel, as in Ferrando et al. (2021). The interaction of market power and financial constraints appears an important area for future work. Macroprudential policies may have spillovers across different groups of firms, such as regulations on collateral quality. Furthermore, changes in fiscal policy, for example corporate taxation, can elicit a strong inflation response in the context of the model – not only through direct changes in marginal costs, but also through the competitive response of rival firms. There are several other areas for future research. The analysis here focuses on aggregate efficiency but not household welfare. With CES preferences, households gain utility

<sup>&</sup>lt;sup>46</sup>More generally, small firms appear more exposed to shocks because they exert less buyer power in factor markets.

<sup>47</sup>The authors further argue that this regime is not fully passive; rather, leading firms use innovation to realize a strategic advantage. Similarly, Colleen Cunningham, Ederer, and S. Ma (2021) documents the presence of 'killer' acquisitions where incumbents acquire rival firms solely to disrupt innovation within their industry.

from the presence of multiple varieties, and higher market entry would improve welfare, despite potential efficiency costs. Heterogeneity across industries – in terms of market structure, sensitivity to cost shocks, and price adjustment frictions – could also enrich the current set of results. Since the solution method is computationally efficient, solving a general equilibrium model with heterogeneous industries appears feasible. Finally, a literature considers the optimal price basket for the central bank inflation target. The results in this paper suggest the basket sould tilt more towards small firms. Their pricing behavior reflects underlying costs to a greater extent while large firms smooth cost shocks.

#### 6.2. Conclusion

This paper embeds an industry structure featuring strategic interaction between firms within a standard New Keynesian framework. The setup aligns with three key empirical findings: industry leaders usually control a significant share of the market; they charge higher markups; and their pricing behavior reflects some degree of strategic complementarity. There are several implications. First, rising concentration has a somewhat counterintuitive effect. Industry leaders focus on preserving market share and limit the pass-through of idiosyncratic cost shocks, leading to greater price stability. Fluctuations are largely absorbed by profits, with the downside that the markup 'tax' is relatively high. This leads to a second point. As the market share of leading firms increases, strategic complementarity strengthens. This leads to a strong increase in the cost pass-through following aggregate shocks, which may raise household inflation expectations. Third, the response of inflation to shocks depends on their aggregate nature and the strength of competition. This would explain why the pass-through for energy price shocks appears high in many estimates: an increase in energy prices unambiguously affects all firms, resulting in strong cross-price effects. Fourth, small firms may be more sensitive to cost shocks. In such a case, the model helps evaluate whether strategic complementarity is economically relevant. Under specific circumstances, e.g., a negative productivity shock affecting small firms more than large firms, strategic behavior may generate sizable efficiency losses, amplifying the adverse impact of the shock by 20 to 30 percent compared to a monopolistic benchmark. Cross-price effects also accelerate inflation, at least if shocks are persistent. Likewise, a negative productivity shock to small firms may raise the aggregate markup. Finally, price dynamics in the model match observed outcomes, which suggests that firm heterogeneity and differences in market power are relevant to price dynamics.

## References

- Abbott, Thomas A (1989). *Price Dispersion in U.S. Manufacturing*. Working Papers 89-7. Center for Economic Studies, U.S. Census Bureau.
- Adjemian, Stéphane, Houtan Bastani, Michel Juillard, Frédéric Karamé, Junior Maih, Ferhat Mihoubi, Willi Mutschler, George Perendia, Johannes Pfeifer, Marco Ratto, and Sébastien Villemot (2021). *Dynare: Reference Manual Version 4*. Dynare Working Papers 1. CEPREMAP.
- Affeldt, Pauline, Tomaso Duso, Klaus Gugler, and Joanna Piechucka (2021). Market Concentration in Europe: Evidence from Antitrust Markets. Discussion Papers of DIW Berlin 1930. DIW Berlin, German Institute for Economic Research.
- Affeldt, Pauline, Tomaso Duso, and Florian Szücs (2018). *EU Merger Control Database: 1990-2014*. Tech. rep. DIW Berlin, German Institute for Economic Research.
- Álvarez, Luis J. and Ignacio Hernando (2005). The price setting behaviour of Spanish firms: evidence from survey data.

  Working Papers 0537. Banco de España.
- Amirault, David, Carolyn Kwan, and Gordon Wilkinson (2006). Survey of Price-Setting Behaviour of Canadian Companies. Staff Working Papers 06-35. Bank of Canada.
- Amiti, Mary and Sebastian Heise (2021). *Has Market Power of U.S. Firms Increased?* Liberty Street Economics 20210621a. Federal Reserve Bank of New York.
- Amiti, Mary, Sebastian Heise, Fatih Karahan, and Ayşegül Şahin (2023). *Inflation Strikes Back: The Role of Import Competition and the Labor Market.* NBER Working Papers 31211. National Bureau of Economic Research, Inc.
- Amiti, Mary, Oleg Itskhoki, and Jozef Konings (2019). "International Shocks, Variable Markups, and Domestic Prices". In: *The Review of Economic Studies* 86(6), pp. 2356–2402. issn: 0034-6527. doi: 10.1093/restud/rdz005.
- Atkeson, Andrew and Ariel Burstein (2008). "Pricing-to-Market, Trade Costs, and International Relative Prices". In: *American Economic Review* 98(5), pp. 1998–2031. doi: 10.1257/aer.98.5.1998.
- Auer, Raphael and Andreas Fischer (2010). "The effect of low-wage import competition on U.S. inflationary pressure". In: *Journal of Monetary Economics* 57(4), pp. 491–503. issn: 0304-3932. doi: 10.1016/j.jmoneco.2010.02.007.
- Auer, Raphael and Raphael Schoenle (2016). "Market structure and exchange rate pass-through". In: *Journal of International Economics* 98, pp. 60-77. issn: 0022-1996. doi: 10.1016/j.jinteco.2015.10.003.
- Autor, David, David Dorn, Lawrence F Katz, Christina Patterson, and John Van Reenen (2020). "The Fall of the Labor Share and the Rise of Superstar Firms". In: *The Quarterly Journal of Economics* 135(2), pp. 645–709. issn: 0033-5533. doi: 10.1093/qje/qjaa004.
- Autor, David, Christina Patterson, and John Van Reenen (2023). Local and National Concentration Trends in Jobs and Sales: The Role of Structural Transformation. Working Paper 31130. National Bureau of Economic Research. doi: 10.3386/w31130.
- Azar, José, Ioana Marinescu, and Marshall Steinbaum (2022). "Labor Market Concentration". In: *Journal of Human Resources* 57(S), S167-S199. issn: 0022-166X. doi: 10.3368/jhr.monopsony.1218-9914R1.
- Babecký, Jan, Philip Du Caju, Theodora Kosma, Martina Lawless, Julian Messina, and Tairi Room (2009). *The margins of labour cost adjustment: survey evidence from European firms*. Working Paper Series 1106. European Central Bank.

- Bajgar, Matej, Giuseppe Berlingieri, Sara Calligaris, Chiara Criscuolo, and Jonathan Timmis (2023). "Industry Concentration in Europe and North America". In: *Industrial and Corporate Change*. issn: 0960-6491. doi: 10.1093/icc/dtac059.
- Bao, Renjie, Jan De Loecker, and Jan Eeckhout (2022). *Are Managers Paid for Market Power?* Working Paper 29918. National Bureau of Economic Research. doi: 10.3386/w29918.
- Baqaee, David and Emmanuel Farhi (2019). "Productivity and Misallocation in General Equilibrium". In: *The Quarterly Journal of Economics* 135(1), pp. 105-163. issn: 0033-5533. doi: 10.1093/qje/qjz030.
- Baqaee, David, Emmanuel Farhi, and Kunal Sangani (2021). *The Supply-Side Effects of Monetary Policy*. Working Paper 28345. National Bureau of Economic Research. doi: 10.3386/w28345.
- Barkai, Simcha (2020). "Declining Labor and Capital Shares". In: *The Journal of Finance* 75(5), pp. 2421-2463. doi: 10.1111/jofi.12909.
- Basu, Susanto (1995). "Intermediate Goods and Business Cycles: Implications for Productivity and Welfare". In: *The American Economic Review* 85(3), pp. 512–531. issn: 00028282.
- Basu, Susanto (2019). "Are Price-Cost Markups Rising in the United States? A Discussion of the Evidence". In: *Journal of Economic Perspectives* 33(3), pp. 3-22. doi: 10.1257/jep.33.3.3.
- Benkard, C. Lanier, Ali Yurukoglu, and Anthony Lee Zhang (2021). *Concentration in Product Markets*. Working Paper 28745. National Bureau of Economic Research. doi: 10.3386/w28745.
- Berman, Nicolas, Philippe Martin, and Thierry Mayer (2012). "HOW DO DIFFERENT EXPORTERS REACT TO EXCHANGE RATE CHANGES?" In: *The Quarterly Journal of Economics* 127(1), pp. 437–492. issn: 00335533, 15314650.
- Blonigen, Bruce A and Justin R Pierce (2016). Evidence for the Effects of Mergers on Market Power and Efficiency. Working Paper 22750. National Bureau of Economic Research. doi: 10.3386/w22750.
- Böheim, René, Franz Hackl, and Michael Hölzl-Leitner (2021). "The impact of price adjustment costs on price dispersion in e-commerce". In: *International Journal of Industrial Organization* 77, p. 102743. issn: 0167-7187. doi: 10.1016/j.ijindorg.2021.102743.
- Bruine De Bruin, Wändi, Keshav Dogra, Sebastian Heise, Edward S. Knotek, Brent Meyer, Robert W. Rich, Raphael Schoenle, Giorgio Topa, and Wilbert Van der Klaauw (2023). *Estimates of Cost-Price Passthrough from Business Survey Data*. FRB Atlanta Working Paper 2023-5. Federal Reserve Bank of Atlanta. doi: 10.29338/wp2023-05.
- Buzzell, Robert D. (1981). "Are There "Natural" Market Structures?" In: Journal of Marketing 45(1), pp. 42-51. issn: 00222429.
- Cagan, Phillip (1979). "The Reduction of Inflation by Slack Demand". In: *Persistent Inflation. Historical and Policy Essays*. Columbia University Press: New York Chichester, West Sussex, pp. 227-252. isbn: 9780231887939. doi: 10.7312/caga92282-010.
- Chatterjee, Satyajit and Burcu Eyigungor (2023). "The Firm Size-Leverage Relationship and Its Implications for Entry and Business Concentration". In: *Review of Economic Dynamics* 48, pp. 132–157. issn: 1094-2025. doi: 10.1016/j.red.2022.04.002.
- Chiavari, Andrea, Marta Morazzoni, and Danila Smirnov (2021). Heterogeneous markups cyclicality and monetary policy.

  Tech. rep. Technical Report, Pompeu Fabra University.

- Coleman, Andrew and Brian Silverstone (2007). "Price changes by firms in New Zealand some evidence from the Quarterly Survey of Business Opinion". In: Reserve Bank of New Zealand Bulletin 70.
- Cooper, Michael, John McClelland, James Pearce, Richard Prisinzano, Joseph Sullivan, Danny Yagan, Owen Zidar, and Eric Zwick (2015). Business in the United States: Who Owns it and How Much Tax Do They Pay? Working Paper 21651. National Bureau of Economic Research. doi: 10.3386/w21651.
- Copaciu, Mihai, Florian Neagu, and Horia Braun-Erdei (2010). "Survey Evidence on Price-setting Patterns of Romanian Firms". In: *Managerial and Decision Economics* 31(2/3), pp. 235–247. issn: 01436570, 10991468.
- Covarrubias, Matias, Germán Gutiérrez, and Thomas Philippon (2019). From Good to Bad Concentration? U.S. Industries over the Past 30 Years. Working Paper 25983. National Bureau of Economic Research. doi: 10.3386/w25983.
- Crouzet, Nicolas and Janice C Eberly (2019). Understanding Weak Capital Investment: the Role of Market Concentration and Intangibles. Working Paper 25869. National Bureau of Economic Research. doi: 10.3386/w25869.
- Crouzet, Nicolas and Neil R. Mehrotra (2020). "Small and Large Firms over the Business Cycle". In: *American Economic Review* 110(11), pp. 3549–3601. doi: 10.1257/aer.20181499.
- Cunningham, Cindy, Lucia Foster, Cheryl Grim, John Haltiwanger, Sabrina Wulff Pabilonia, Jay Stewart, and Zoltan Wolf (2023). "Dispersion in Dispersion: Measuring Establishment-Level Differences in Productivity". In: *Review of Income and Wealth*. doi: 10.1111/roiw.12616.
- Cunningham, Colleen, Florian Ederer, and Song Ma (2021). "Killer Acquisitions". In: *Journal of Political Economy* 129(3), pp. 649–702. doi: 10.1086/712506.
- De Loecker, Jan, Jan Eeckhout, and Gabriel Unger (2020). "The Rise of Market Power and the Macroeconomic Implications". In: *The Quarterly Journal of Economics* 135(2), pp. 561-644. issn: 0033-5533. doi: 10.1093/qje/qjz041.
- Dedola, Luca, Mark Strøm Kristoffersen, and Gabriel Zullig (2021). "The extensive and intensive margin of price adjustment to cost shocks: Evidence from Danish multiproduct firms". In: Working Paper.
- Della Vigna, Stefano and Matthew Gentzkow (2019). "Uniform Pricing in U.S. Retail Chains". In: *The Quarterly Journal of Economics* 134(4), pp. 2011–2084. issn: 0033-5533. doi: 10.1093/qje/qjz019.
- Dinlersoz, Emin M. and Glenn MacDonald (2009). "The industry life-cycle of the size distribution of firms". In: *Review of Economic Dynamics* 12(4), pp. 648-667. issn: 1094-2025. doi: 10.1016/j.red.2009.01.001.
- Döpper, Hendrik, Alexander MacKay, Nathan Miller, and Joel Stiebale (2022). "Rising markups and the role of consumer preferences". In: *Harvard Business School Strategy Unit Working Paper* (22-025).
- Dornbusch, Rudiger (1987). "Exchange Rates and Prices". In: *The American Economic Review* 77(1), pp. 93–106. issn: 00028282.
- Faccio, Mara and John J McConnell (2020). Impediments to the Schumpeterian Process in the Replacement of Large Firms. Working Paper 27871. National Bureau of Economic Research. doi: 10.3386/w27871.
- Ferrando, Annalisa, Peter McAdam, Filippos Petroulakis, and Xavier Vives (2021). *Product market structure and monetary policy: evidence from the Euro Area.* Working Paper Series 2632. European Central Bank.
- Franzoni, Francesco A, Mariassunta Giannetti, and Roberto Tubaldi (2023). "Supply Chain Shortages, Large Firms' Market Power, and Inflation". In: Swiss Finance Institute Research Paper Series (23-105).

- Gabaix, Xavier (2011). "THE GRANULAR ORIGINS OF AGGREGATE FLUCTUATIONS". In: *Econometrica* 79(3), pp. 733–772. issn: 00129682, 14680262.
- Galí, Jordi (2015). Monetary Policy, Inflation, and the Business Cycle: An Introduction to the New Keynesian Framework and Its Applications Second edition. Economics Books 10495. Princeton University Press.
- Gertler, Mark and Simon Gilchrist (1994). "Monetary Policy, Business Cycles, and the Behavior of Small Manufacturing Firms". In: *The Quarterly Journal of Economics* 109(2), pp. 309-340. issn: 0033-5533. doi: 10.2307/2118465.
- Gibson, John and Steven Stillman (2009). "Why do big firms pay higher wages? Evidence from an international database". In: *The Review of Economics and Statistics* 91(1), pp. 213–218. issn: 00346535, 15309142.
- Gödl-Hanisch, Isabel and Manuel Menkhoff (2023). *Pass-Through of Cost-Push Shocks*. CESifo Working Paper Series 10520. CESifo
- Goldberg, Pinelopi K. and Rebecca Hellerstein (2009). *How rigid are producer prices?* Staff Reports 407. Federal Reserve Bank of New York.
- Gopinath, Gita and Oleg Itskhoki (2010). "FREQUENCY OF PRICE ADJUSTMENT AND PASS-THROUGH". In: *The Quarterly Journal of Economics* 125(2), pp. 675–727. issn: 00335533, 15314650.
- Grullon, Gustavo, Yelena Larkin, and Roni Michaely (2019). "Are US Industries Becoming More Concentrated?" In: *Review of Finance* 23(4), pp. 697–743. issn: 1572-3097. doi: 10.1093/rof/rfz007.
- Guimaraes, Bernardo and Kevin D. Sheedy (2011). "Sales and Monetary Policy". In: *American Economic Review* 101(2), pp. 844-76. doi: 10.1257/aer.101.2.844.
- Hale, Galina, Bart Hobijn, Fernanda Nechio, and Doris Wilson (2019). "How Much Do We Spend on Imports?" In: FRBSF Economic Letter.
- Hamano, Masashige and Francesco Zanetti (2022). "Monetary policy, firm heterogeneity, and product variety". In: European Economic Review 144, p. 104089. issn: 0014-2921. doi: 10.1016/j.euroecorev.2022.104089.
- Heise, Sebastian, Fatih Karahan, and Ayşegül Şahin (2022). "The Missing Inflation Puzzle: The Role of the Wage-Price Pass-Through". In: *Journal of Money, Credit and Banking* 54(Sl), pp. 7–51. doi: 10.1111/jmcb.12896.
- Hildenbrand, Andreas (2010). Cournot or Stackelberg competition? A survey on experimental evidence. MPRA Paper 24468. University Library of Munich, Germany.
- Hobijn, Bart, Russell Miles, James Royal, and Jing Zhang (2023). "The Recent Steepening of Phillips Curves". In: *Chicago Fed Letter* 0.
- Hong, Sungki (2018). "Price Markups for Small and Large Firms Over the Business Cycle". In: *Economic Synopses*(17), pp. 1–3. doi: 10.20955/es.2018.17.
- Hopenhayn, Hugo, Julian Neira, and Rish Singhania (2018). From Population Growth to Firm Demographics: Implications for Concentration, Entrepreneurship and the Labor Share. Working Paper 25382. National Bureau of Economic Research. doi: 10.3386/w25382.
- Hottman, Colin J., Stephen J. Redding, and David E. Weinstein (2016). "Quantifying the Sources of Firm Heterogeneity". In: *The Quarterly Journal of Economics* 131(3), pp. 1291–1364. issn: 0033-5533. doi: 10.1093/qje/qjw012.
- Hutchinson, John, Jozef Konings, and Patrick Paul Walsh (2010). "The Firm Size Distribution and Inter-Industry Diversification". In: *Review of Industrial Organization* 37(2), pp. 65–82. issn: 0889938X, 15737160.

- Kaplan, Greg and Guido Menzio (2015). "THE MORPHOLOGY OF PRICE DISPERSION". In: *International Economic Review* 56(4), pp. 1165-1206. doi: 10.1111/iere.12134.
- Katz, Michael L. (2019). "Multisided Platforms, Big Data, and a Little Antitrust Policy". In: *Review of Industrial Organization* 54(4), pp. 695-716. issn: 0889938X, 15737160.
- Kehoe, Patrick and Virgiliu Midrigan (2015). "Prices are sticky after all". In: *Journal of Monetary Economics* 75, pp. 35–53. issn: 0304-3932. doi: 10.1016/j.jmoneco.2014.12.004.
- Kharroubi, Enisse and Frank Smets (2024). *Monetary policy with profit-driven inflation*. BIS Working Papers 1167. Bank for International Settlements.
- Kimball, Miles S. (1995). "The Quantitative Analytics of the Basic Neomonetarist Model". In: *Journal of Money, Credit and Banking* 27(4), pp. 1241–1277.
- Klenow, Peter J and Benjamin A Malin (2010). *Microeconomic Evidence on Price-Setting*. Working Paper 15826. National Bureau of Economic Research. doi: 10.3386/w15826.
- Klenow, Peter J. and Oleksiy Kryvtsov (2008). "State-Dependent or Time-Dependent Pricing: Does it Matter for Recent U.S. Inflation?" In: *The Quarterly Journal of Economics* 123(3), pp. 863–904. issn: 0033-5533. doi: 10.1162/qjec. 2008.123.3.863.
- Kroen, Thomas, Ernest Liu, Atif R Mian, and Amir Sufi (2021). *Falling Rates and Rising Superstars*. Working Paper 29368. National Bureau of Economic Research. doi: 10.3386/w29368.
- Kryvtsov, Oleksiy and Nicolas Vincent (2021). "The Cyclicality of Sales and Aggregate Price Flexibility". In: *Review of Economic Studies* 88(1), pp. 334–377.
- Kwon, Spencer Yongwook, Yueran Ma, and Kaspar Zimmermann (2023). "100 Years of Rising Corporate Concentration". In: *SAFE Working Paper*(359). doi: 10.2139/ssrn.3936799.
- Lafrogne-Joussier, R., J. Martin, and I. Mejean (2023). *Cost Pass-Through and the Rise of Inflation*. INSEE Working Papers 2023-13. Institut National de la Statistique et des Etudes Economiques.
- Levy, Daniel, Shantanu Dutta, Mark Bergen, and Robert Venable (1998). "Price Adjustment at Multiproduct Retailers". In: *Managerial and Decision Economics* 19(2), pp. 81–120. issn: 01436570, 10991468.
- Liu, Ernest, Atif Mian, and Amir Sufi (2019). Low Interest Rates, Market Power, and Productivity Growth. Working Paper 25505. National Bureau of Economic Research. doi: 10.3386/w25505.
- Lombardi, Marco J, Marianna Riggi, and Eliana Viviano (2023). "Workers' Bargaining Power and the Phillips Curve: A Micro-Macro Analysis". In: *Journal of the European Economic Association*, jvad016. issn: 1542-4766. doi: 10.1093/jeea/jvad016.
- Markham, Jesse W. (1951). "The Nature and Significance of Price Leadership". In: *The American Economic Review* 41(5), pp. 891–905. issn: 00028282.
- Meier, Matthias and Timo Reinelt (2022). "Monetary Policy, Markup Dispersion, and Aggregate TFP". In: *The Review of Economics and Statistics*, pp. 1-45. issn: 0034-6535. doi: 10.1162/rest\_a\_01226.
- Mertens, Matthias and Bernardo Mottironi (2023). *Do larger firms have higher markups?* IWH-CompNet Discussion Papers 1/2023. Halle Institute for Economic Research.

- Miklian, Jason and Kristian Hoelscher (2022). "SMEs and exogenous shocks: A conceptual literature review and forward research agenda". In: *International Small Business Journal* 40(2), pp. 178-204. doi: 10.1177/02662426211050796.
- Mongey, Simon (2017). Market Structure and Monetary Non-neutrality. Staff Report 558. Federal Reserve Bank of Minneapolis. doi: 10.21034/sr.558.
- Nakamura, Emi (2008). *Pass-Through in Retail and Wholesale*. Working Paper 13965. National Bureau of Economic Research. doi: 10.3386/w13965.
- Nakamura, Emi and Jón Steinsson (2010). "Monetary Non-neutrality in a Multisector Menu Cost Model". In: *The Quarterly Journal of Economics* 125(3), pp. 961–1013. issn: 0033-5533. doi: 10.1162/qjec.2010.125.3.961.
- OECD (2022). The Evolving Concept of Market Power in the Digital Economy. Competition Policy Roundtable Background Note. OECD.
- Oh, Joonseok (2020). "The Propagartion of Uncertainty Shocks: Rotemberg Versus Calvo". In: *International Economic Review* 61(3), pp. 1097-1113. doi: 10.1111/iere.12450.
- Ottonello, Pablo and Thomas Winberry (2020). "Financial Heterogeneity and the Investment Channel of Monetary Policy". In: *Econometrica* 88(6), pp. 2473–2502. doi: 10.3982/ECTA15949.
- Palazzo, Berardino (2023). Corporate Profits in the aftermath of COVID-19. FEDS Notes 2023-09-08-5. Board of Governors of the Federal Reserve System (U.S.) doi: 10.17016/2380-7172.3364.
- Pennerstorfer, Dieter, Philipp Schmidt-Dengler, Nicolas Schutz, Christoph Weiss, and Biliana Yontcheva (2020). "IN-FORMATION AND PRICE DISPERSION: THEORY AND EVIDENCE". In: *International Economic Review* 61(2), pp. 871-899. doi: 10.1111/iere.12443.
- Pérez-Orive, Ander and Yannick Timmer (2023). Distressed Firms and the Large Effects of Monetary Policy Tightenings. FEDS Notes 2023-06-23-1. Board of Governors of the Federal Reserve System (U.S.) doi: 10.17016/2380-7172.3279.
- Peters, Michael (2020). "Heterogeneous Markups, Growth, and Endogenous Misallocation". In: *Econometrica* 88(5), pp. 2037–2073. doi: 10.3982/ECTA15565.
- Raval, Devesh (2023). "Testing the Production Approach to Markup Estimation". In: *The Review of Economic Studies*, rdad002. issn: 0034-6527. doi: 10.1093/restud/rdad002.
- Richter, Alexander W. and Nathaniel A. Throckmorton (2016). "Is Rotemberg pricing justified by macro data?" In: *Economics Letters* 149, pp. 44–48. issn: 0165-1765. doi: 10.1016/j.econlet.2016.10.011.
- Rossi-Hansberg, Esteban, Pierre-Daniel Sarte, and Nicholas Trachter (2018). *Diverging Trends in National and Local Concentration*. Working Paper 25066. National Bureau of Economic Research. doi: 10.3386/w25066.
- Rotemberg, Julio J. (1982). "Sticky Prices in the United States". In: Journal of Political Economy 90(6), pp. 1187–1211. issn: 00223808, 1537534X.
- Sheremirov, Viacheslav (2020). "Price dispersion and inflation: New facts and theoretical implications". In: *Journal of Monetary Economics* 114, pp. 59-70. issn: 0304-3932. doi: 10.1016/j.jmoneco.2019.03.007.
- Shimomura, Ken-Ichi and Jacques-François Thisse (2012). "Competition among the big and the small". In: *The RAND Journal of Economics* 43(2), pp. 329-347. doi: 10.1111/j.1756-2171.2012.00168.x.
- Simon, Herbert A. and Charles P. Bonini (1958). "The Size Distribution of Business Firms". In: *The American Economic Review* 48(4), pp. 607–617. issn: 00028282.

- Smith, Dominic A. and Sergio Ocampo (2022). *The Evolution of U.S. Retail Concentration*. Working Papers 22-07. Center for Economic Studies, U.S. Census Bureau.
- Stokman, Ad and Marco Hoeberichts (2006). *Price setting behaviour in the Netherlands: results of a survey.* Working Paper Series 607. European Central Bank.
- Tambe, Prasanna, Lorin Hitt, Daniel Rock, and Erik Brynjolfsson (2020). *Digital Capital and Superstar Firms*. Working Paper 28285. National Bureau of Economic Research. doi: 10.3386/w28285.
- Taylor, John B. (1993). "Discretion versus policy rules in practice". In: Carnegie-Rochester Conference Series on Public Policy 39, pp. 195–214. issn: 0167-2231. doi: 10.1016/0167-2231(93)90009-L.
- Tetlow, Robert J. (2022). How Large is the Output Cost of Disinflation? Finance and Economics Discussion Series 2022-079.

  Board of Governors of the Federal Reserve System (U.S.) doi: 10.17016/FEDS.2022.079.
- Traina, James (2018). Is Aggregate Market Power Increasing? Production Trends Using Financial Statements. Working Papers 272. The University of Chicago Booth School of Business, George J. Stigler Center for the Study of the Economy and the State.
- Ueda, Kozo (2023). "Duopolistic Competition and Monetary Policy". In: *Journal of Monetary Economics* 135, pp. 70-85. issn: 0304-3932. doi: 10.1016/j.jmoneco.2023.01.003.
- Wang, Olivier and Iván Werning (2022). "Dynamic Oligopoly and Price Stickiness". In: *American Economic Review* 112(8), pp. 2815–49. doi: 10.1257/aer.20201739.
- Weber, Isabella and Evan Wasner (2023). "Sellers' Inflation, Profits and Conflict: Why Can Large Firms Hike Prices in an Emergency?" In: *Review of Keynesian Economics* 11, pp. 183–213. doi: 10.4337/roke.2023.02.05.
- Wilbur, Kenneth C. and Paul W. Farris (2014). "Distribution and Market Share". In: *Journal of Retailing* 90(2). Empirical Generalizations in Retailing, pp. 154–167. issn: 0022-4359. doi: 10.1016/j.jretai.2013.08.003.
- Zingales, Luigi (2017). "Towards a Political Theory of the Firm". In: *Journal of Economic Perspectives* 31(3), pp. 113–30. doi: 10.1257/jep.31.3.113.

# A. Appendix

## A.1. The Evolution of Accounting Profits by Form of Incorporation

The headline profits of US corporations have risen over the past 40 years, but there are several caveats. The separation of wages and profits typical of C-corporations is less well-defined for other forms of incorporation. Most growth in registered businesses has been from partnerships and S-corporations. With both, profits are 'passed through' directly to owners, who report the income on their individual tax returns. This blurs the normal separation of wages and profits. For pass-through business owners, there is no large tax advantage to reporting either form of income, at least for upper tax brackets. In addition, many partnerships and S-corporations are set up as investment vehicles. Returns are reported as 'profits' and applicable taxes are paid accordingly. Therefore, headline profits should be adjusted for both officer compensation and portfolio income to ensure they are measured consistently over time.

Officer compensation (i.e., payments to owner-employees) is large relative to net income in the corporate sector. For S-corporations, officer compensation averaged 70 percent of net income from 1992 to 2016, while it was around 40 percent of net income for C-corporations. Notably, this ratio declined over time for both S- and C-corporations due in part to stricter enforcement of "reasonable pay" clauses. A decline in the effective tax rate on corporate profits probably motivated this shift as well. While payments to owner-employees for their labor cannot be easily distinguished from profits, it is possible to add officer compensation and profits together for a more consistent measure. This leads to a 50 percent upward revision in overall business profitability in the 1980s. Business activity was dominated by C-corporations during this period and officer compensation was relatively high. The same adjustment increases profitability by only 20 percent in the 2010s. As mentioned, a second source of bias comes from the inclusion of portfolio income in the net income of S-corporations and partnerships. Many are set up purely as investment vehicles, and the share of portfolio income in net income has grown over time. This leads to a potential double-counting problem for profits. To mitigate this, a second adjustment takes only business (or "ordinary") income earned by S-corporations and partnerships into account.

<sup>&</sup>lt;sup>48</sup>These tend to be smaller businesses, or at least closely held. The growth of pass-through entities is also consistent with growing service consumption since firms in the service sector tend to be smaller than in manufacturing.

 $<sup>^{49}</sup>$ Cooper et al. (2015) find that the effective tax rate on partnerships and S-corporations is lower than on C-corporations, which may explain their rapid growth.

For internal consistency, the results for table 4 are given in terms of net receipts rather than GDP. The growth in total net income (before adjustment) between 1981-89 and 2010-16 is equal to 7 percentage points of GDP – a significant increase. Including officer compensation lowers the change to 6 percentage points of GDP. Further excluding portfolio income reduces it to 4 percentage points of GDP. By this measure, accounting profits went from around 11 percent of GDP in the 1980s to 15 percent in the 2010s. A shift-share decomposition indicates the majority of the change is explained by S-corporations and partnerships. It takes the following form:

$$\Delta X_{it} = \sum_{i} (\Delta X_{ijt}) \omega_{it-1} + \sum_{i} (\Delta \omega_{it}) X_{it-1} + \sum_{i} (\Delta X_{it}) (\Delta \omega_{it})$$
within between dynamic reallocation

where X is total income over a time period, subdivided by type of entity i and weighted by their share of total receipts  $\omega_i$ . The first component – the 'within' category – holds weights constant. The change in profitability is positive for all types of incorporation by this measure. Next, the 'between' component describes the change in weights, which is negative for C-corporations and sole proprietorships. Finally, the 'dynamic' component gives the interaction of the two components. For example, S-corporations both grew and became more profitable over time.

While large public companies are somewhat more profitable than in the past, they explain a smaller share of total activity. They accounted for more than 80 percent of activity in the 1980s, and this share dropped to around 60 percent over the 2010s. S-corporations and partnerships both expanded and explain most of the overall increase in corporate profitability. Ownership of S-corporations is often highly concentrated, with 2-3 owners for the median firm. This may affect patterns of investment and how profits are distributed. Many studies looking at corporate profitability over time use the 1980s as their starting point. Studies looking at longer time periods suggest this period witnessed abnormally low returns and may not serve as an appropriate benchmark.

<sup>&</sup>lt;sup>50</sup>As a rule of thumb, net receipts are around 2.2x GDP. CBO data for households indicate a corresponding increase of 4.8 percentage points for business income (including dividends) over the same period. Gross net income for the pass-through sector is larger in the IRS data than what CBO reports (e.g. \$1.64 trillion compared to \$1.01 trillion in 2016). There are several explanations for the discrepancy. First, there is a well-known mismatch between personal tax records and business records. Second, some share of net income reported to the IRS may go towards net lending by firms. Finally, some share of profits may go to foreign nationals.

Table 4: Corporate Profitability by Form of Incorporation, Period Averages

#### (a) Share of Total Receipts

	1981-89	1990-99	2000-9	2010-16
C-corporation	0.833	0.742	0.665	0.625
S-corporation	0.068	0.149	0.175	0.192
Partnership	0.041	0.058	0.119	0.146
Sole proprietorship	0.058	0.051	0.041	0.038

#### (b) Net Income to Receipts

#### (c) Shift-Share Decomposition

	1981-89	1990-99	2000-9	2010-16	Δ Within	Between	Dynamic	Total
Total	0.035	0.051	0.056	0.069	0.026	0.000	0.008	0.034
C-corporation	0.027	0.036	0.035	0.046	0.016	-0.006	-0.004	0.006
S-corporation	0.021	0.042	0.056	0.064	0.003	0.003	0.005	0.011
Partnership <sup>a</sup>	0.059	0.114	0.119	0.134	0.003	0.006	0.008	0.017
Sole proprietorship	0.152	0.209	0.213	0.228	0.004	-0.003	-0.002	0.000

#### (d) Net Income and Officer Compensation to Receipts

#### (e) Shift-Share Decomposition

-	1981-89	1990-99	2000-9	2010-16	Δ Within	Between	Dynamic	Total
Total	0.053	0.068	0.072	0.082	0.020	-0.002	0.012	0.029
C-corporation	0.046	0.053	0.048	0.056	0.008	-0.010	-0.002	-0.004
S-corporation	0.039	0.078	0.094	0.101	0.004	0.005	0.008	0.017
Partnership <sup>a</sup>	0.059	0.114	0.119	0.134	0.003	0.006	0.008	0.017
Sole proprietorship	0.152	0.209	0.213	0.228	0.004	-0.003	-0.002	0.000

# (f) Net Ordinary Income and Officer Compensation to Receipts

#### (g) Shift-Share Decomposition

	1981-89	1990-99	2000-9	2010-16	$\Delta$ Within	Between	Dynamic	Total
Total	0.051	0.064	0.062	0.071	0.018	-0.005	0.008	0.020
C-corporation	0.046	0.053	0.048	0.056	0.008	-0.010	-0.002	-0.004
S-corporation	0.035	0.069	0.083	0.095	0.004	0.004	0.007	0.016
Partnership <sup>a</sup>	0.031	0.069	0.058	0.067	0.001	0.003	0.004	0.009
Sole proprietorship	0.152	0.209	0.213	0.228	0.004	-0.003	-0.002	0.000

*Notes:* The shift-share decomposition compares the periods 1981-9 and 2010-16. The needed series are not available for 1980. All tabulations are in terms of net receipts. Net receipts are roughly 2.2x GDP on average, although this varies over time.

#### A.2. Evidence from Antitrust Markets

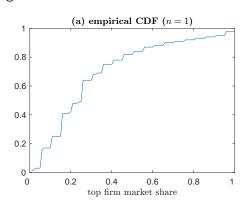
Figure 11 shows the CDF of market share reported in Affeldt, Duso, and Szücs (2018). The left-hand panel shows the CDF for observations where only the market share of the post-merger entity is reported. The right-hand panel shows the CDF of the top market share when observations include competing firms. Each line is based on the number of competitors. The results suggest there is a

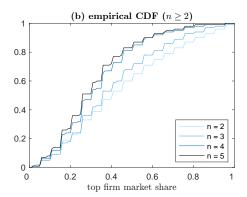
<sup>&</sup>lt;sup>a</sup>Partnerships exclude capital gains and real estate and rental income from net income for all years. *Source:* IRS Statistics of Income.

strong correlation between the number of firms reported and the market share of the leading firm.

This might be a feature of the data or a sign of upward bias when reporting is incomplete.

Figure 11: Cumulative Distribution of Top Market Shares Across Antitrust Markets

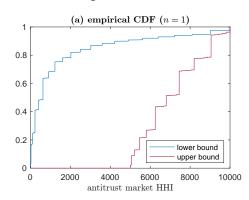


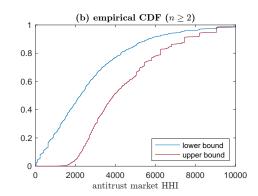


Source: Affeldt, Duso, and Szücs (2018)

Affeldt et al. calculate HHIs for each market.<sup>51</sup> The lower bound HHI assigns a value of zero to all unattributed market share. Otherwise, it is calculated in the normal way. The upper bound for the post-merger HHI adds the square of all residual market share. In other words, the residual market share is treated as one missing competitor. The corresponding CDFs are given in figure 12.

Figure 12: Distribution of HHIs Across Antitrust Markets





Source: Affeldt, Duso, and Szücs (2018)

In the left-hand panel of figure 12, market share is only reported for the post-merger entity and most is treated as a residual. The resulting gap between the lower and upper bound is large. The lower bound estimate in the right-hand panel is more interesting. It suggests the HHI is above 2000 in the median antitrust market, at least when multiple firms are reported.<sup>52</sup> This threshold is

<sup>&</sup>lt;sup>51</sup>The calculation uses the post-merger market share if applicable and the market shares of competing firms.

<sup>&</sup>lt;sup>52</sup>While it is likely more detailed information was collected on markets that are concentrated, the majority of cases (51 percent) include information on competitors. For cases where information on competitors is omitted, the post-merger entity is only marginally smaller than cases including such information: 30 versus 34 percent.

significant since the EU guidelines on horizontal mergers flag potential competition concerns for higher levels of concentration. Furthermore, almost one-quarter of markets are assessed to have an HHI of 3000 or higher. As with Benkard, Yurukoglu, and Zhang (2021), this suggests the prevailing level of concentration in most markets is higher than commonly appreciated.

Table 5: Descriptive Statistics for Antitrust Markets by Number of Firms ( $n \ge 2$ )

		Top Firm Market Share					
# Firms	Count	Mean	Median	Std. Dev.			
2	1940	52.8	55.0	22.3			
3	2523	46.0	45.0	18.8			
4	2766	38.2	35.0	16.4			
5	1411	36.1	35.0	15.7			
> 5	1288	33.5	30.0	14.9			
Total	9928	42.1	40.0	19.3			

		Avg. Share of Trailing Firms					
# Firms	Count	Mean	Median	Std. Dev.			
2	1940	22.1	20.0	12.4			
3	2523	17.5	17.5	7.0			
4	2766	13.8	15.0	4.7			
5	1411	11.8	12.5	3.7			
> 5	1288	9.0	9.0	3.0			
Total	9928	15.5	15.0	8.3			

		Share of Leader vs. Follower					
# Firms	Count	Mean	Median	Std. Dev.			
2	1441	2.17	1.75	1.24			
3	2172	1.97	1.57	1.11			
4	2400	1.78	1.50	0.88			
5	1228	1.80	1.50	0.89			
> 5	1075	1.73	1.50	0.81			
Total	8316	1.90	1.59	1.02			

		Unexplained Market Share					
# Firms	Count	Mean	Median	Std. Dev.			
2	1940	25.4	20.0	24.9			
3	2523	19.8	15.0	20.2			
4	2766	21.1	19.0	19.6			
5	1411	17.7	15.0	18.2			
> 5	1288	16.2	10.0	17.2			
Total	9928	20.5	15.0	20.6			

Source: Affeldt, Duso, and Szücs (2018).

Table 5 provides a set of descriptive statistics from Affeldt, Duso, and Szücs (2018), tabulated by the number of firms within an observation (including the post-merger entity). Outcomes of interest

include the top firm's market share, the average market share of trailing firms, the ratio of market shares for the leader and top trailing firm, and the market share not attributed to any firm. The ratio of the leader and top follower is restricted to observations where both have a market share greater than 10 percent.

# A.3. Past and Present Inflation Episodes in the United States

As commentators have pointed out, the jump in inflation following COVID shares some similarities with the inflation of the 1950s.<sup>53</sup> During the Second World War, the United States severely rationed consumer goods. With the outbreak of the Korean War, fears that rationing would be reintroduced led US consumers to bring consumption forward. The resulting demand shock generated rapid price growth. When it became evident that the scale of economic mobilization for the Korean War would be limited, inflation expectations dropped, and inflation quickly normalized. With the COVID pandemic, consumer spending quickly reoriented from services to goods. At least in good-producing sectors, limited supply and high demand allowed firms to raise prices – perhaps a classic case of too much money chasing too few goods. Unlike the Korean War episode, demand remained elevated following the COVID shock. While real household disposable income dropped strongly in 2022, households continued to draw on savings. Domestic price growth normalized by the end of the second quarter of 2023, although underlying inflation may continue as wages catch up to prices.

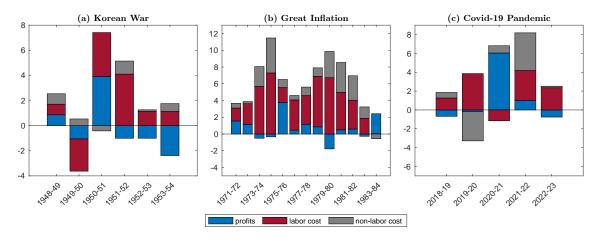


Figure 13: Contribution to Price Growth Among Domestic Companies (Annual Percent Change)

The three episodes represent the largest inflation spikes in the United States since 1950. The bars give the contribution of each component to overall price growth among domestic non-financial companies (based on NIPA table 1.15). Annual growth is measured from the end of the second quarter of each year.

 $<sup>^{53}</sup> https://www.cfr.org/article/what-korean-war-era-reveals-about-feds-inflation-dilemma$ 

Palazzo (2023) shows that government interventions and debt refinancing by firms affected the reporting of profits. He proposes holding net taxes and net interest (both components of non-labor costs) constant. Using the adjustments proposed by Palazzo, profits explain around 25 percent of price growth between 2019 and 2023Q3. This remains 2x their normal contribution to price growth. Without this adjustment, profits account for 40 percent of price growth. Arguably, the unadjusted data better reflect the true contribution of profits to price growth: First, taxes and subsidies have reverted to their normal level. Second, net interest expenses show a declining trend before the COVID-19 pandemic and later realizations consistent with the trend.

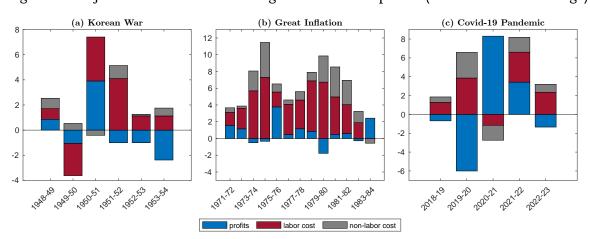


Figure 14: Adjusted Price Growth Among Domestic Companies (Annual Percent Change)

The COVID-19 inflation episode is adjusted following Palazzo (2023). Non-labor costs attributed to tax and subsidies are linearly interpolated between 2019Q4 and 2022Q1 while net interest expenses are held constant at their 2019Q4 levels. In this case, profits account for around 25 percent of price growth between 2019 and 2023Q3 while non-labor costs make up 22 percent. The initial surge in inflation between 2020-21 is still explained by profits.

#### A.4. Nested CES Demand

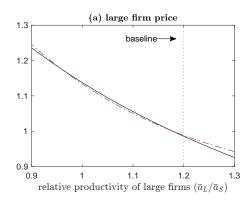
#### A.4.1. Solving the Flexible Price Equilibrium

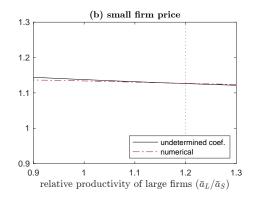
The method of undetermined coefficients is solved around the point where all firms are identical. As figure 15 makes clear, it is locally accurate around  $p^*$ . Since small firms set prices monopolistically, the curvature is minimal and the method of undetermined coefficients works well. This is less the case for large firms since their pricing behavior is non-linear.<sup>54</sup>

Table 6 gives the pricing rules when firms are identical. The  $\Omega$ 's are the same as in (40). The Y's

<sup>&</sup>lt;sup>54</sup>While a higher-order Taylor approximation would be more accurate, is not straightforward to implement when incorporating the best reply of rival firms. One option is that firms may solve for their own price using a second-order approximation while using a first-order approximation for rival prices.

Figure 15: Comparison of Solution Methods in the Flexible Price Equilibrium





collect the coefficients for the firm's own marginal cost (Y<sup>i</sup>) and the marginal cost of its rival (Y<sup>-i</sup>).

Table 6: Estimated Decision Rules at  $p^*$ 

	$\Omega'$	$\Omega^*$	Y <sup>i</sup>	$Y^{-i}$
Large firms	-0.224	0.183	0.786	0.163
Small firms	-0.116	0.069	0.895	0.055

The difference between large and small firms in terms of pricing behavior is already apparent. Large firms put most weight on their own marginal costs, but also consider the marginal costs of their rivals to some degree. Meanwhile, small firms do not consider the costs of rival firms.

#### A.4.2. Solving the Dynamic Problem

With Rotemberg adjustment costs, the profit maximization problem becomes

$$\mathbb{E}_{t} \sum_{k=0}^{\infty} \Lambda_{t+k} \left[ \left( p_{sjt+k} - \mathcal{C}_{sjt+k} \right) y_{sjt+k} - \frac{\Theta_{s}}{2} \left( \pi_{t+k} \frac{p_{sjt+k}}{p_{sjt+k-1}} - 1 \right)^{2} P_{t+k} Y_{t+k} \right]$$
(80)

The FOC with respect to  $p_{sjt}$  gives

$$0 = p_{sjt}y_{sjt} \left[ 1 + \Psi_{st}^{i} \left( 1 - \frac{C_{sjt}}{p_{sjt}} \right) \right] - \Theta_{s} \left( \pi_{t} \frac{p_{sjt}}{p_{sjt-1}} - 1 \right) \pi_{t} \frac{p_{sjt}}{p_{sjt-1}} Y_{t} \dots + \beta \Theta_{s} \mathbb{E}_{t} \left[ \frac{C_{t}}{C_{t+1}} \left( \pi_{t+1} \frac{p_{sjt+1}}{p_{sjt}} - 1 \right) \pi_{t+1} \frac{p_{sjt+1}}{p_{sjt}} Y_{t+1} \right]$$
(81)

The solutions for identical and asymmetric firms follow. In both cases, any unnecessary index is dropped from the notation.

#### A.4.2.1. Identical Firms

Using (14) and noting that

$$p_{jt} = n^{\frac{1}{1-\varphi}} p_{sjt} \tag{82}$$

where the solution for  $p_{sjt}$  is given by (34). The FOC of the pricing equation (42) becomes

$$0 = p_{st}^{1-\varphi} p_{jt}^{\varphi-\sigma} Y_t \left[ 1 + \left( \frac{\varphi - \sigma}{n} - \varphi \right) \left( 1 - \frac{\mathcal{C}_{st}}{p_{st}} \right) \right] - \frac{\Theta}{n} \left( \pi_t \frac{p_{st}}{p_{st-1}} - 1 \right) \pi_t \frac{p_{st}}{p_{st-1}} Y_t \dots$$

$$+ \beta \Theta_s \mathbb{E}_t \left[ \frac{C_t}{C_{t+1}} \left( \pi_{t+1} \frac{p_{st+1}}{p_{st}} - 1 \right) \pi_{t+1} \frac{p_{st+1}}{p_{st}} Y_{t+1} \right]$$

$$= n^{\frac{\varphi-\sigma}{1-\varphi}} p_s^{1-\sigma} \left[ 1 + \left( \frac{\varphi-\sigma}{n} - \varphi \right) \left( 1 - \frac{\mathcal{C}_{st}}{p_{st}} \right) \right] - \frac{\Theta}{n} \left( \pi_t - 1 \right) \pi_t + \frac{\beta \Theta}{n} \mathbb{E}_t \left[ \Lambda_{t+1} \left( \pi_{t+1} - 1 \right) \pi_{t+1} \right]$$

given  $C_t = Y_t$ . Log-linearizing the pricing equation

$$0 = n^{\frac{\varphi - \sigma}{1 - \varphi}} p_s^{1 - \sigma} \left( \varphi - \frac{\varphi - \sigma}{n} \right) \frac{\mathcal{C}_s}{p_s} \widetilde{\mathcal{C}}_{st} - \frac{\Theta}{n} \widetilde{\pi}_t + \frac{\beta \Theta}{n} \widetilde{\pi}_{t+1} \quad \text{where} \quad p_s = \frac{(n-1)\varphi + \sigma}{(n-1)\varphi + \sigma - n} \mathcal{C}_s$$

Monopolistic competition is a special case of nested CES demand where n = 1. The elasticity of inflation to the monetary shock is

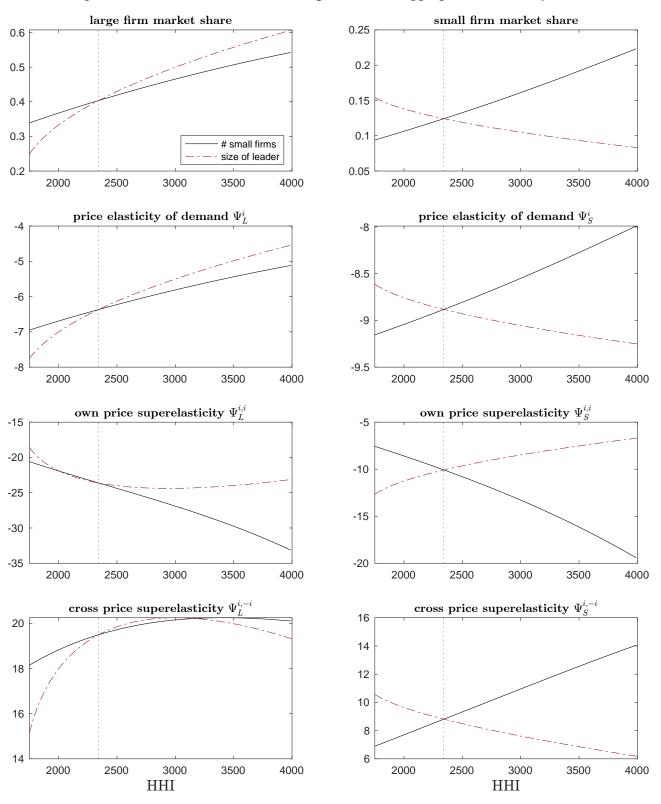
$$\Gamma^{y} = \frac{\Theta(1 - \rho_{m}\beta)/n}{n^{\frac{\varphi - \sigma}{1 - \varphi}} p_{s}^{1 - \sigma} \left(\varphi - (\varphi - \sigma)/n\right) \mathcal{C}_{s}/p_{s}} \Gamma^{\pi}$$
(84)

where (63) gives the second equation. The elasticity of inflation to the productivity shock is similarly

$$\Omega^{y} = \frac{\Theta(1 - \rho_{m}\beta)/n}{n^{\frac{\varphi - \sigma}{1 - \varphi}} p_{s}^{1 - \sigma} \left(\varphi - (\varphi - \sigma)/n\right) C_{s}/p_{s}} \Omega^{\pi} + 1$$
(85)

where (75) gives the second equation needed to solve the system.

Figure 16: Concentration and the Response to an Aggregate Productivity Shock



The x-axis displays the HHI and a move from left to right corresponds to an increase in concentration. The left column shows outcomes for large firms and the right column gives the equivalent for small firms. The top row gives market share. The black solid line shows the effect of exit by small firms. The dashed red line shows the effect of an increasing productivity gap. In both cases the market share of large firms increases. For small firms, exit and growing productivity wedge have opposite effects. With a growing productivity wedge, the market share of small firms decreases. With exit, the remaining small firms consolidate greater market share. The remaining panels give the impact on the overall price elasticity of demand and the ownand cross-price superelasticities.

#### A.4.2.2. Asymmetric Firms

The FOC with respect to  $p_{st}^i$  gives

$$0 = p_{st}^{i} y_{st}^{i} \left[ 1 + \left( (\varphi - \sigma) \left( \frac{p_{st}^{i}}{p_{jt}} \right)^{1 - \varphi} - \varphi \right) \left( 1 - \frac{\mathcal{C}_{st}^{i}}{p_{st}^{i}} \right) \right] \dots \\ - \Theta_{s} \left( \pi_{t} \frac{p_{st}^{i}}{p_{st-1}^{i}} - 1 \right) \pi_{t} \frac{p_{st}^{i}}{p_{st-1}^{i}} Y_{t} + \beta \Theta_{s} \mathbb{E}_{t} \left[ \frac{C_{t}}{C_{t+1}} \left( \pi_{t+1} \frac{p_{st+1}^{i}}{p_{st}^{i}} - 1 \right) \pi_{t+1} \frac{p_{st+1}^{i}}{p_{st}^{i}} Y_{t+1} \right]$$
(86)

Using (14) and dividing through by  $Y_t$  this becomes

$$0 = (p_{st}^{i})^{1-\varphi} p_{jt}^{\varphi-\sigma} \left[ 1 + \Psi_{st}^{i} \left( 1 - \frac{\mathcal{C}_{st}^{i}}{p_{st}^{i}} \right) \right] - \Theta_{s} \left( \pi_{t} \frac{p_{st}^{i}}{p_{st-1}^{i}} - 1 \right) \pi_{t} \frac{p_{st}^{i}}{p_{st-1}^{i}} \dots + \beta \Theta_{s} \mathbb{E}_{t} \left[ \left( \pi_{t+1} \frac{p_{st+1}^{i}}{p_{st}^{i}} - 1 \right) \pi_{t+1} \frac{p_{st+1}^{i}}{p_{st}^{i}} \right]$$
(87)

Log-linearizing and taking a first-order Taylor expansion, noting that  $ilde{p}_{st}^{\,i} = ilde{p}_{st}^{-i}$ 

$$0 = (1 - \varphi)(p_{s}^{i})^{-\varphi}p_{j}^{\varphi - \sigma} \left[ 1 + \Psi_{s}^{i} \left( 1 - \frac{C_{s}^{i}}{p_{s}^{i}} \right) \right] \tilde{p}_{s}^{i} \dots$$

$$+ (\varphi - \sigma)(p_{s}^{i})^{1 - \varphi}p_{j}^{2\varphi - \sigma - 1} \left[ 1 + \Psi_{s}^{i} \left( 1 - \frac{C_{s}^{i}}{p_{s}^{i}} \right) \right] \left[ n_{s}(p_{s}^{i})^{-\varphi} \tilde{p}_{st}^{i} + n_{-s}(p_{-s}^{-i})^{-\varphi} \tilde{p}_{-st}^{-i} + p_{F}^{-\varphi} \tilde{p}_{Ft} \right] \dots$$

$$+ (p_{s}^{i})^{1 - \varphi}p_{j}^{\varphi - \sigma} \left[ \left( 1 - \frac{C_{j}^{i}}{p_{s}^{i}} \right) \left[ \frac{\Psi_{s}^{i,i} + \dot{\Psi}_{s}^{i,-i}}{p_{s}^{i}} \tilde{p}_{st}^{i} + \frac{\ddot{\Psi}_{s}^{i,-i}}{p_{-s}^{-i}} \tilde{p}_{-st}^{-i} + \frac{\ddot{\Psi}_{st}^{i,-i}}{p_{Ft}} \tilde{p}_{Ft} \right] - \Psi_{s}^{i} \frac{C_{j}^{i}}{p_{s}^{i}} (\tilde{C}_{st}^{i} - \tilde{p}_{st}^{i}) \right] \dots$$

$$- \Theta_{s}(\tilde{\pi}_{t}^{i} + \tilde{p}_{st}^{i} - \tilde{p}_{st-1}^{i}) + \beta \Theta_{s} \mathbb{E}_{t} \left[ \tilde{\pi}_{t+1}^{i} + \tilde{p}_{st+1}^{i} - \tilde{p}_{st}^{i} \right]$$

$$(88)$$

In the steady state

$$\Psi_s^i = -\left(1 - \frac{\mathcal{C}_s^i}{p_s^i}\right)^{-1} \implies 1 + \Psi_s^i \left(1 - \frac{\mathcal{C}_s^i}{p_s^i}\right) = 0 \tag{89}$$

so the first two terms of (88) can be ignored

$$0 = (p_{s}^{i})^{1-\varphi} p_{j}^{\varphi-\sigma} \left[ \left( 1 - \frac{\mathcal{C}_{j}^{i}}{p_{s}^{i}} \right) \left[ \frac{\Psi_{s}^{i,i} + \dot{\Psi}_{s}^{i,-i}}{p_{s}^{i}} \tilde{p}_{st}^{i} + \frac{\ddot{\Psi}_{s}^{i,-i}}{p_{-s}^{-i}} \tilde{p}_{-st}^{-i} + \frac{\ddot{\Psi}_{st}^{i,-i}}{p_{Ft}} \tilde{p}_{Ft} \right] - \Psi_{s}^{i} \frac{\mathcal{C}_{j}^{i}}{p_{s}^{i}} (\tilde{\mathcal{C}}_{st}^{i} - \tilde{p}_{st}^{i}) \right] \dots \\ - \Theta_{s} (\tilde{\pi}_{t}^{i} + \tilde{p}_{st}^{i} - \tilde{p}_{st-1}^{i}) + \beta \Theta_{s} \mathbb{E}_{t} \left[ \tilde{\pi}_{t+1}^{i} + \tilde{p}_{st+1}^{i} - \tilde{p}_{st}^{i} \right]$$

$$(90)$$

Expression 90 shows the role of the superelastiticies in a clear way. Given a log-linear approximation around the steady state, they adjust the slope of the price elasticity of demand. They also perfectly offset if firms are identical. The decision rule is characterized as

$$\tilde{p}_{st}^{i} = Y_{s} \, \tilde{p}_{st-1}^{i} + Y_{s}^{*} \, \tilde{p}_{-st-1}^{-i} + Y_{s}^{i} \, \tilde{\mathcal{C}}_{st}^{i} + Y_{s}^{-i} \, \tilde{\mathcal{C}}_{-st}^{-i} + Y_{s}^{F} \, \tilde{p}_{Ft} + Y_{s}^{\pi} \, \tilde{\pi}_{t}$$

$$(91)$$

Rival firms follow

$$\tilde{p}_{-st}^{-i} = Y_{-s} \, \tilde{p}_{-st-1}^{-i} + Y_{-s}^* \, \tilde{p}_{st-1}^{\,i} + Y_{-s}^{\,i} \, \tilde{\mathcal{C}}_{-st}^{\,-i} + Y_{-s}^{\,i} \, \tilde{\mathcal{C}}_{-st}^{\,i} + Y_{-s}^{\,F} \tilde{p}_{Ft} + Y_{-s}^{\pi} \tilde{\pi}_t \tag{92}$$

Given some shock, expected prices in the next period are

$$\mathbb{E}_{t} \left[ \tilde{p}_{st+1}^{i} \right] = Y_{s} \, \tilde{p}_{st}^{i} + Y_{s}^{*} (Y_{-s} \, \tilde{p}_{-st-1}^{-i} + Y_{-s}^{*} \, \tilde{p}_{st-1}^{i} + Y_{-s}^{i} \, \tilde{\mathcal{C}}_{-st}^{-i} + Y_{-s}^{-i} \, \tilde{\mathcal{C}}_{st}^{i} + Y_{-s}^{F} \tilde{p}_{Ft} + Y_{-s}^{\pi} \tilde{\pi}_{t}) \dots$$

$$+ \rho \left[ Y_{s}^{i} \, \tilde{\mathcal{C}}_{st}^{i} + Y_{s}^{-i} \, \tilde{\mathcal{C}}_{-st}^{-i} + Y_{s}^{F} \, \tilde{p}_{Ft} + Y_{s}^{\pi} \, \tilde{\pi}_{t} \right]$$

$$(93)$$

where  $\rho$  is the persistence of the shock. This suggests

$$Y_s = \frac{(\psi_s + \beta \Theta_s Y_s^*) Y_{-s}^* + \Theta_s}{\kappa_s - \beta \Theta_s Y_s}$$
(94)

$$Y_s^* = \frac{(\psi_s + \beta \Theta_s Y_s^*) Y_{-s}}{\kappa_s - \beta \Theta_s Y_s}$$
(95)

$$Y_s^i = \frac{(\psi_s + \beta \Theta_s Y_s^*) Y_{-s}^{-i} - (p_s^i)^{-\varphi} p_j^{\varphi - \sigma} \Psi_s^i \mathcal{C}_s^i}{\kappa_s - \beta \Theta_s (Y_s + \rho)}$$

$$(96)$$

$$Y_s^{-i} = \frac{(\psi_s + \beta \Theta_s Y_s^*) Y_{-s}^i}{\kappa_s - \beta \Theta_s (Y_s + \rho)}$$

$$(97)$$

$$Y_s^F = \frac{(\psi_s + \beta \Theta_s Y_s^*) Y_{-s}^F + \omega_s}{\kappa_s - \beta \Theta_s (Y_s + \rho)}$$
(98)

$$Y_s^{\pi} = \frac{(\psi_s + \beta \Theta_s Y_s^*) Y_{-s}^{\pi} - \Theta_s (1 - \rho \beta)}{\kappa_s - \beta \Theta_s (Y_s + \rho)}$$

$$(99)$$

where

$$\kappa_s = \Theta_s + \beta \Theta_s - (p_s^i)^{1-\varphi} p_j^{\varphi-\sigma} \left[ \left( 1 - \frac{\mathcal{C}_s}{p_s^i} \right) \frac{\Psi^{i,i} + \dot{\Psi}_s^{i,-i}}{p_s^i} + \Psi^i \frac{\mathcal{C}_s}{p_s^i} \right]$$
(100)

$$\psi_s = (p_s^i)^{1-\varphi} p_j^{\varphi-\sigma} \left(1 - \frac{\mathcal{C}_s}{p_s^i}\right) \frac{\ddot{\Psi}_s^{i,-i}}{p_{-s}^{-i}} \tag{101}$$

$$\omega_s = (p_s^i)^{1-\varphi} p_j^{\varphi-\sigma} \left(1 - \frac{\mathcal{C}_s}{p_s^i}\right) \frac{\ddot{\Psi}_s^{i,-i}}{p_F} \tag{102}$$

Once relative prices are known, the change in the market share of each firm is given by

$$\tilde{x}_{st}^{i} = \frac{\Psi_{s}^{i,i} + \dot{\Psi}_{s}^{i,-i}}{(\varphi - \sigma)p_{s}^{i}} \tilde{p}_{st}^{i} + \frac{\ddot{\Psi}_{s}^{i,-i}}{(\varphi - \sigma)p_{-s}^{-i}} \tilde{p}_{-st}^{-i} + \frac{\ddot{\Psi}_{s}^{i,-i}}{(\varphi - \sigma)p_{F}} \tilde{p}_{Ft}$$
(103)

Output for each firm is equal to

$$\tilde{y}_{st}^i = \tilde{x}_{st}^i + \tilde{Y}_t + \tilde{P}_t - \tilde{p}_{st}^i \tag{104}$$

Table 7: Estimated Decision Rules (Baseline Calibration)

	Y	Y*	Yi	$Y^{-i}$	$\mathbf{Y}^F$	Υπ
Large firms	0.768	0.020	0.104	0.013	0.020	-0.287
Small firms	0.773	0.005	0.157	0.002	0.005	-0.278

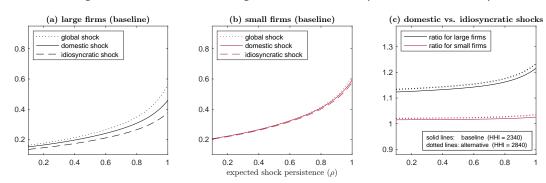
#### A.4.3. The Pass-Through of Cost Shocks

The pass-through is measured over the first eight periods of the shock

$$\mathcal{P} = rac{\sum_{t=1}^{t=8} \widetilde{p}_{st}^i}{\sum_{t=1}^{t=8} \widetilde{\mathcal{C}}_{st}^i}$$

Compared to the estimates presented in figure 4, this change in the time horizon significantly lowers the observed pass-through. The difference between the aggregate and idiosyncratic regimes remains similar as shown in the right-hand panel of figure 17.

Figure 17: The Pass-Through of Cost Shocks (Two Year Horizon)



The x-axis displays the expected persistence of the shock and the y-axis gives the pass-through, measured over the entire duration of the shock. The solid lines in the left-hand and center panels give the response to an aggregate shock while the dashed lines describe the response when shocks are idiosyncratic. The right-hand panel takes the ratio of aggregate and idiosyncratic shocks. The alternative scenario (dotted lines) in the right-hand panel modifies the baseline so that  $\bar{a}_L=0.89$ . This increases the market share of the leading firm to 43 percent and significantly lowers the pass-through of idiosyncratic shocks.

## A.5. Aggregate Shocks with Asymmetric Firms

#### A.5.1. Monetary Policy Shock

As before, the elasticity of output and inflation to the monetary policy shock is

$$\widetilde{Y}_t = \Gamma^y m_t \tag{105}$$

$$\tilde{\pi}_t = \Gamma^{\pi} m_t \tag{106}$$

The decision rule for each firm can be written

$$\widetilde{P}_{st} - \widetilde{P}_t = Y_s^{\pi} \Gamma^{\pi} m_t + Y_s \left( \widetilde{P}_{st-1} - \widetilde{P}_{t-1} \right) + Y_s^* \left( \widetilde{P}_{-st-1} - \widetilde{P}_{t-1} \right) + \left( Y_s^i + Y_s^{-i} \right) \Gamma^y m_t \tag{107}$$

The log-linearized price index is

$$\widetilde{P}_{t} = \frac{n_{s}(P_{s})^{1-\varphi}\widetilde{P}_{st} + n_{-s}(P_{-s})^{1-\varphi}\widetilde{P}_{-st} + n_{F}(P_{F})^{1-\varphi}\widetilde{P}_{Ft}}{p^{1-\varphi}}$$
(108)

Assuming that foreign prices move with the overall price index (i.e.  $\widetilde{P}_{Ft}=\widetilde{P}_t$  or  $\widetilde{p}_{Ft}=0$ )

$$\widetilde{P}_{t} = \chi^{F} \frac{n_{s}(P_{s})^{1-\varphi} \widetilde{P}_{st} + n_{-s}(P_{-s})^{1-\varphi} \widetilde{P}_{-st}}{P^{1-\varphi}} \quad \text{where} \quad \chi^{F} = \frac{P^{1-\varphi}}{n_{s}(P_{s})^{1-\varphi} + n_{-s}(P_{-s})^{1-\varphi}}$$
(109)

while (63) gives the relation between  $\Gamma^y$  and  $\Gamma^{\pi}$ . The price index is a restriction. If all small firms set their relative price above it, then the relative price of all large firms must set their price below.

Recalling  $\Gamma^{\pi}$  solves

$$\Gamma^{\pi} = \frac{\widetilde{P}_t - \widetilde{P}_{t-1}}{m_t} \tag{110}$$

the decision rule can be restated as

$$\widetilde{P}_{st} - \widetilde{P}_t - Y_s(\widetilde{P}_{st-1} - \widetilde{P}_{t-1}) - Y_s^*(\widetilde{P}_{-st-1} - \widetilde{P}_{t-1}) = \left[ Y_s^{\pi} \Gamma^{\pi} + (Y_s^i + Y_s^{-i}) \Gamma^y \right] m_t$$
(111)

In the first period of the monetary policy shock, this reduces to

$$\frac{\widetilde{P}_{st} - \widetilde{P}_t}{m_t} = \Gamma_s^m \quad \text{where} \quad \Gamma_s^m = Y_s^\pi \Gamma^\pi + (Y_s^i + Y_s^{-i})\Gamma^y$$
(112)

Recognizing the recursive nature of the problem

$$\mathbb{E}_t \left[ \frac{\widetilde{P}_{st+1} - \widetilde{P}_{t+1}}{m_t} \right] = Y_s \Gamma_s^m + \rho_m \Gamma_s^m + Y_s^* \Gamma_{-s}^m$$
(113)

This implies

$$\mathbb{E}_t \left[ \frac{\widetilde{P}_{st+1} - \widetilde{P}_{st}}{m_t} \right] = \mathbb{E}_t \left[ \frac{\widetilde{P}_{t+1} - \widetilde{P}_t}{m_t} \right] + (Y_s + \rho_m - 1) \Gamma_s^m + Y_i^* \Gamma_{-s}^m$$
(114)

Using (110)

$$\mathbb{E}_t \left[ \widetilde{P}_{st+1} \right] - \widetilde{P}_{st} = \left[ \rho_m \Gamma^{\pi} + (Y_s + \rho_m - 1) \Gamma_s^m + Y_s^* \Gamma_{-s}^m \right] m_t \tag{115}$$

Accordingly, the following identity and (63) jointly determine  $\Gamma^{\pi}$  and  $\Gamma^{y}$  along with (110) and (115) and the definition of  $\Gamma_{i}^{m}$ 

$$\mathbb{E}_{t}\left[\widetilde{P}_{t+1}\right] - \widetilde{P}_{t} = \chi^{F} \mathbb{E}_{t} \left[ \frac{n_{s}(P_{s})^{1-\varphi}(\widetilde{P}_{st+1} - \widetilde{P}_{st}) + n_{-s}(P_{-s})^{1-\varphi}(\widetilde{P}_{-st+1} - \widetilde{P}_{-st})}{P^{1-\varphi}} \right]$$
(116)

### A.5.2. Aggregate Productivity Shock

The decision rule for each firm can be written in terms of the price level

$$\widetilde{P}_{st} - \widetilde{P}_t = Y_s^{\pi} \Omega^{\pi} a_t + Y_s \left( \widetilde{P}_{st-1} - \widetilde{P}_{t-1} \right) + Y_s^* \left( \widetilde{P}_{-st-1} - \widetilde{P}_{t-1} \right) + \left( Y_s^i + Y_s^{-i} \right) \left( \Omega^y - 1 \right) a_t \tag{117}$$

where

$$\Omega^{\pi} = \frac{\widetilde{P}_t - \widetilde{P}_{t-1}}{a_t} \tag{118}$$

The decision rule can be restated as

$$\widetilde{P}_{st} - \widetilde{P}_t - Y_i(\widetilde{P}_{st-1} - \widetilde{P}_{t-1}) - Y_s^*(\widetilde{P}_{-st-1} - \widetilde{P}_{t-1}) = \left[ Y_s^{\pi} \Omega^{\pi} + (Y_s^i + Y_s^{-i})(\Omega^y - 1) \right] a_t$$
 (119)

In the first period of the monetary policy shock, this reduces to

$$\frac{\widetilde{P}_{st} - \widetilde{P}_t}{a_t} = \Omega_s^a \quad \text{where} \quad \Omega_s^a = Y_s^{\pi} \Omega^{\pi} + (Y_s^i + Y_s^{-i})(\Omega^y - 1)$$
(120)

Solving recursively

$$\mathbb{E}_t \left[ \frac{\widetilde{P}_{st+1} - \widetilde{P}_{t+1}}{a_t} \right] = (Y_s + \rho_a) \Omega_s^a + Y_s^* \Omega_{-s}^a$$
(121)

This implies

$$\mathbb{E}_t \left[ \frac{\widetilde{P}_{st+1} - \widetilde{P}_{st}}{a_t} \right] = \mathbb{E}_t \left[ \frac{\widetilde{P}_{t+1} - \widetilde{P}_t}{a_t} \right] + (Y_s + \rho_a - 1)\Omega_s^a + Y_s^* \Omega_{-s}^a$$
(122)

Using (118)

$$\mathbb{E}_t \left[ \widetilde{P}_{st+1} \right] - \widetilde{P}_{st} = \left[ \rho_a \, \Omega^{\pi} + (Y_s + \rho_a - 1) \Omega_s^a + Y_s^* \Omega_{-s}^a \right] a_t \tag{123}$$

Finally,  $\Omega^{\pi}$  solves the following identity (using expressions 75, 118, and 123 and the definitions of  $\Omega_s^a$  above)

$$\mathbb{E}_{t}\left[\widetilde{P}_{t+1}\right] - \widetilde{P}_{t} = \chi^{F} \mathbb{E}_{t} \left[ \frac{n_{s}(P_{s})^{1-\varphi}(\widetilde{P}_{st+1} - \widetilde{P}_{st}) + n_{-s}(P_{-s})^{1-\varphi}(\widetilde{P}_{-st+1} - \widetilde{P}_{-st})}{P^{1-\varphi}} \right]$$
(124)

# A.6. Firm-Specific Shocks

#### A.6.1. Productivity of Small Firms

First, take that productivity shocks are different across firms

$$\mathcal{C}_{st} = \frac{1}{e^{a_{st}}\bar{a}_s} \left(\frac{w_t}{1-\alpha}\right)^{1-\alpha} \tag{125}$$

For simplicity, shocks to large firms are set to zero ( $a_{Lt} = 0$ ). Meanwhile, shocks to small firms follow

$$a_{St} = \rho_a a_{St-1} + \xi_t \tag{126}$$

Accordingly, the prices of small firms are given by

$$\widetilde{P}_{St} - \widetilde{P}_{t} = Y_{L}^{\pi} \Omega^{\pi} a_{St} + Y_{S} (\widetilde{P}_{St-1} - \widetilde{P}_{t-1}) + Y_{S}^{*} (\widetilde{P}_{Lt-1} - \widetilde{P}_{t-1}) + Y_{s}^{i} (\Omega^{y} a_{St} - a_{St}) + Y_{s}^{-i} \Omega^{y} a_{St}$$
(127)

while for large firms

$$\widetilde{P}_{Lt} - \widetilde{P}_{t} = Y_{S}^{\pi} \Omega^{\pi} a_{Lt} + Y_{L} (\widetilde{P}_{Lt-1} - \widetilde{P}_{t-1}) + Y_{L}^{*} (\widetilde{P}_{St-1} - \widetilde{P}_{t-1}) + Y_{L}^{i} \Omega^{y} a_{St} + Y_{L}^{-i} (\Omega^{y} a_{St} - a_{St})$$
(128)

As before, each expression can be rearranged so that

$$\widetilde{P}_{St} - \widetilde{P}_{t} - Y_{S}(\widetilde{P}_{St-1} - \widetilde{P}_{t-1}) - Y_{S}^{*}(\widetilde{P}_{Lt-1} - \widetilde{P}_{t-1}) = \left[ Y_{S}^{\pi} \Omega^{\pi} + Y_{s}^{i}(\Omega^{y} - 1) + Y_{s}^{-i} \Omega^{y} \right] a_{St}$$
 (129)

$$\widetilde{P}_{Lt} - \widetilde{P}_t - Y_L(\widetilde{P}_{Lt-1} - \widetilde{P}_{t-1}) - Y_L^*(\widetilde{P}_{St-1} - \widetilde{P}_{t-1}) = \left[Y_L^{\pi}\Omega^{\pi} + Y_L^{i}\Omega^{y} + Y_L^{-i}(\Omega^{y} - 1)\right]a_{St} \quad (130)$$

Meaning in the first period, the shock is given by

$$\widetilde{P}_{St} - \widetilde{P}_t = \Omega_S^a a_{St}$$
 where  $\Omega_S^a = Y_S^{\pi} \Omega^{\pi} + Y_S^i (\Omega^y - 1) + Y_S^{-i} \Omega^y$  (131)

$$\widetilde{P}_{Lt} - \widetilde{P}_t = \Omega_S^a a_{St}$$
 where  $\Omega_L^a = Y_L^{\pi} \Omega^{\pi} + Y_L^i \Omega^y + Y_L^{-i} (\Omega^y - 1)$  (132)

Solving recursively

$$\mathbb{E}_t \left[ \frac{\widetilde{P}_{st+1} - \widetilde{P}_{t+1}}{a_{St}} \right] = (Y_s + \rho_a) \Omega_s^a + Y_s^* \Omega_{-s}^a$$
(133)

This implies

$$\mathbb{E}_t \left[ \frac{\widetilde{P}_{st+1} - \widetilde{P}_{st}}{a_{St}} \right] = \mathbb{E}_t \left[ \frac{\widetilde{P}_{t+1} - \widetilde{P}_t}{a_{St}} \right] + (Y_s + \rho_a - 1)\Omega_s^a + Y_s^* \Omega_{-s}^a$$
(134)

Using (118)

$$\mathbb{E}_t \left[ \widetilde{P}_{st+1} \right] - \widetilde{P}_{st} = \left[ \rho_a \, \Omega^{\,\pi} + (\mathsf{Y}_s + \rho_a - 1) \Omega_s^a + \mathsf{Y}_s^* \Omega_{-s}^a \right] a_{St} \tag{135}$$

Finally,  $\Omega^{\pi}$  solves the following identity (using expressions 118 and 135 and the definitions of  $\Omega_i^a$  above)

$$\mathbb{E}_{t}\left[\widetilde{P}_{t+1}\right] - \widetilde{P}_{t} = \chi^{F} \mathbb{E}_{t}\left[\frac{n_{s}(P_{s})^{1-\varphi}(\widetilde{P}_{st+1} - \widetilde{P}_{st}) + n_{-s}(P_{-s})^{1-\varphi}(\widetilde{P}_{-st+1} - \widetilde{P}_{-st})}{P^{1-\varphi}}\right]$$
(136)

The solution for a shock to large firms is similar.

# A.7. The Standard NK Model with Price Staggering

How do the results for markup and price dispersion presented earlier compare to the standard New Keynesian model with price staggering? The standard model is implemented using Dynare, modifying the replication package for Galí (2015) chapter 3.<sup>55</sup> The calibration matches the main outcomes from the baseline model. The settings in table 8 give the same equilibrium markup (0.14)

 $<sup>^{55}</sup>$ Refer to Gali (2015) for details on how Calvo pricing is implemented. Dynare is a software program designed to solve dynamic stochastic general equilibrium models (Adjemian et al., 2021).

and slope for the Phillips curve (0.36). All other parameter settings are identical to table 1.

Table 8: Alternative Parameter Values

Parameter	Value	Description
$\sigma \\ \theta$	8.1 0.65	Elasticity of substitution across goods Probability firm keeps the same price

The standard deviation of log prices can be determined as follows. In each period of the shock, some fraction  $1-\theta$  of firms can reset their price. This means in period t a share  $\theta^t$  of firms will never reset their price. For all prices  $P_t^* = \{\widetilde{P}_0, \widetilde{P}_1^*, \widetilde{P}_2^*, ..., \widetilde{P}_t^*\}$ , their respective weights are given by  $\omega_t = \{\omega_0, \omega_1, \omega_2, ..., \omega_t\}$  where

$$\omega_0 = \theta^t \quad \text{and} \quad \omega_k = (1 - \theta)\theta^{t-k} \quad \text{for} \quad 0 < k \le t$$
 (137)

Since the aggregate price index moves in each period, relative prices are given by

$$\boldsymbol{p}_t^* = \boldsymbol{P}_t^* - \widetilde{P}_t \tag{138}$$

where  $\widetilde{P}_t$  is the aggregate price index. The set of corresponding markups is similarly

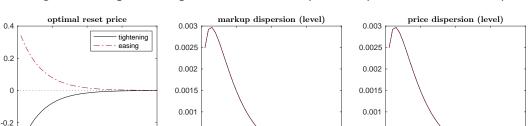
$$\boldsymbol{\mu}_t^* = \boldsymbol{P}_t^* - \widetilde{\boldsymbol{C}}_t \tag{139}$$

To solve for the optimal reset price  $P^*$  in each period, the relation between inflation and prices is given by

$$\widetilde{P}_t = \theta \widetilde{P}_{t-1} + (1-\theta)\widetilde{P}_t^* \implies \widetilde{\pi}_t = \frac{1-\theta}{\theta}(\widetilde{P}_t^* - \widetilde{P}_t) \text{ since } \widetilde{\pi}_t = \widetilde{P}_t - \widetilde{P}_{t-1}$$
 (140)

This is sufficient to both derive the reset price and calculate the weighted standard deviation of log prices and markups. Both the monetary and productivity shocks are implemented

The results for the monetary shock are presented in figure 18. Because there is no price or markup dispersion in the steady state, both are presented in levels (using log markups and log prices). Output and inflation are identical to the baseline results in figure 6. The initial effect of the shock on markup



0.0005

Figure 18: Impulse Response to a Monetary Shock (Standard NK Model)

The figure shows the response of prices and markups in a model with Calvo pricing. The left-hand panel shows the price firms choose when they get the opportunity to reset. The center and right-hand panels show the impact on price and markup dispersion, taking the weighted standard deviation. For a 1 percent increase/decrease in the nominal interest rate, there is an increase in the dispersion of log markups and log prices since they are identical in the steady state.

quarter

0.0005

-0.4

and price dispersion grows since only a fraction  $1-\theta$  of firms can reset their price. The change in dispersion over time relates to two factors: (i) the size of the price reset and (ii) movement in the aggregate price index. Take for example monetary tightening. A resetting firm will choose a price below the aggregate price index. This increases dispersion. Now take that the firm does not reset its price again. First, the aggregate price index will gradually converge to the reset price, reducing price dispersion. After this point, it will continue to move below the reset price, increasing dispersion.

Unlike the baseline model, both monetary tightening and easing increase markup and price dispersion (see figure 18). There is no price dispersion in equilibrium, so this is expected. Still, results in Sheremirov (2020) suggest dispersion in regular prices and inflation are positively correlated, meaning a deflationary shock should generate price compression. This is not the case. In addition, Calvo pricing may imply an excessive level of price dispersion. In Sheremirov (2020), a 1 percentage point increase in annual inflation raises the standard deviation of log prices by 0.050 whereas the standard NK model returns almost 4x this estimate. Table 9 presents the corresponding estimates.

<sup>&</sup>lt;sup>56</sup>The coefficient (0.050) omits industry as a control. It falls to 0.026 when controlling for industry. Still, the 'correct' level of price dispersion is up for debate. Ideally, this would be measured using closely substitutable varieties. The comparison in Sheremirov (2020) captures dispersion across retailers.

Table 9: OLS Regression of Price Dispersion on Inflation Following a Productivity Shock

	NK Model	Baseline
Price dispersion	(1)	(2)
T (1	0.010***	0.020***
Inflation	0.219***	0.039***
<b>O</b>	(0.019)	(0.004)
Constant	0.033***	-0.002***
	(0.001)	(0.002)
R-squared	0.763	0.691

Standard errors in parentheses
\*\*\* p<0.01, \*\* p<0.05, \* p<0.1