

# 3-manifold

Created: 2025-12-09 Modified: 2025-12-09 20:58 | Tags: low-dimensional-topology, 3-manifolds Wesley Greysen

---

Key sources: [nLab:3-manifold](#), [dehn-surgery](#)

Orientable 3-manifolds can be built by Dehn surgery on framed links in  $S^3$ , so surgery data presents every example.

## Idea

Low-dimensional topology packages 3-manifolds via surgery: starting from  $S^3$ , perform Dehn surgery along framed links to obtain every orientable 3-manifold.

By [dehn-surgery](#), every [orientable-manifold](#) 3-manifold can be presented as a pair  $(K, r)$  where  $K$  is a [knot](#) in  $S^3$  and  $r = p/q \in \mathbb{Q} \cup \{\infty\}$  (called the **surgery coefficient**).

## See also:

- [4-manifold](#)
- [lens-space](#)

## REFERENCES

- [nLab:3-manifold](#), [dehn-surgery](#) | [nLab:3-manifold](#) |