## The full Brillouin gain calculation



$$\left( v_p \partial_z + \partial_t + v_p \alpha_p / 2 \right) \widetilde{a}_p = -i \widetilde{g}_0 \widetilde{a}_s \widetilde{b}$$

$$\left( \pm v_s \partial_z + \partial_t + v_s \alpha_s / 2 \right) \widetilde{a}_s = -i \widetilde{g}_0^* \widetilde{b}^* \widetilde{a}_p$$

$$\left[ v_m \partial_z + \partial_t + \left( i \Delta_m + \gamma_m / 2 \right) \right] \widetilde{b} = -i \widetilde{g}_0^* \widetilde{a}_s^* \widetilde{a}_p ,$$

- 1. Tomes, M., Marquardt, F., Bahl, G. & Carmon, T. Phys. Rev. A 84, 063806 (2011).
- 2. Wolff, C., Steel, M. J., Eggleton, B. J. & Poulton, C. G. Phys. Rev. A 92, 13836 (2015).
- 3. Van Laer, R., Baets, R. & Van Thourhout, D. Phys. Rev. A 93, 1–15 (2016).
- 4. Sipe, J. E. & Steel, M. J. New J. Phys. 18, 1–39 (2016).
- 5. Kharel, P., Behunin, R. O., Renninger, W. H. & Rakich, P. T. Phys. Rev. A 93, 1–12 (2016).
- 6. Wolff, C., Smith, M., Stiller, B., & Poulton, C. (2021). JOSAB, 38 (4), 1243-1269.

## The full Brillouin gain calculation



$$\left( \frac{v_p \partial_z + \partial_t + v_p \alpha_p / 2}{v_p \partial_z + \partial_t + v_s \alpha_s / 2} \right) \widetilde{a}_p = -i \widetilde{g}_0 \widetilde{a}_s \widetilde{b}$$

$$\left( \pm \frac{v_s \partial_z + \partial_t + v_s \alpha_s / 2}{v_m \partial_z + \partial_t + (i \Delta_m + \gamma_m / 2)} \right) \widetilde{a}_s = -i \widetilde{g}_0^* \widetilde{a}_s^* \widetilde{a}_p$$

$$\left[ v_m \partial_z + \partial_t + (i \Delta_m + \gamma_m / 2) \right] \widetilde{b} = -i \widetilde{g}_0^* \widetilde{a}_s^* \widetilde{a}_p ,$$

**Propagation** 

**Detuning** 

Loss

- 1. Tomes, M., Marquardt, F., Bahl, G. & Carmon, T. Phys. Rev. A 84, 063806 (2011).
- 2. Wolff, C., Steel, M. J., Eggleton, B. J. & Poulton, C. G. Phys. Rev. A 92, 13836 (2015).
- 3. Van Laer, R., Baets, R. & Van Thourhout, D. Phys. Rev. A 93, 1–15 (2016).
- 4. Sipe, J. E. & Steel, M. J. New J. Phys. 18, 1–39 (2016).
- 5. Kharel, P., Behunin, R. O., Renninger, W. H. & Rakich, P. T. Phys. Rev. A 93, 1–12 (2016).
- 6. Wolff, C., Smith, M., Stiller, B., & Poulton, C. (2021). JOSAB, 38 (4), 1243-1269.