

Linear Data Structures

- **Arrays**
 - **Access:** Time $O(1)$, Space $O(1)$
 - **Search:** Time $O(n)$, Space $O(1)$
 - **Insertion / Deletion (at end):** Time $O(1)$ (amortized for dynamic), Space $O(1)$
 - **Insertion / Deletion (at middle):** Time $O(n)$, Space $O(1)$
 - **Linked Lists (Singly, Doubly, Circular)**
 - **Access / Search:** Time $O(n)$, Space $O(1)$
 - **Insertion / Deletion (at beginning):** Time $O(1)$, Space $O(1)$
 - **Insertion / Deletion (at end):** Time $O(1)$ (with tail pointer), Space $O(1)$
 - **Stacks (Array/List implementation)**
 - **Push / Pop / Peek:** Time $O(1)$, Space $O(1)$
 - **Queues (Array/List implementation)**
 - **Enqueue / Dequeue:** Time $O(1)$, Space $O(1)$
 - **Hash Table / Hash Map / Hash Set**
 - **Insert / Delete / Search:** Average Time $O(1)$, Worst Time $O(n)$. Space $O(n)$ for storage.
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Trees

- Binary Tree Traversal (Inorder, Preorder, Postorder)
 - **Time:** $O(n)$, **Space:** $O(h)$ where h is the height of the tree ($O(n)$ in worst-case, $O(\log n)$ in best-case).
 - Binary Search Tree (BST)
 - **Search / Insert / Delete:** Average Time $O(\log n)$, Worst Time $O(n)$.
 - Balanced BSTs (AVL, Red-Black)
 - **Search / Insert / Delete:** Time $O(\log n)$, Space $O(\log n)$.
 - Heap (Min-Heap, Max-Heap)
 - **Insert / Delete:** Time $O(\log n)$
 - **Get Min/Max:** Time $O(1)$
 - **Build Heap:** Time $O(n)$
 - **Trie** (where M is the length of the key)
 - **Insert / Search / Delete:** Time $O(M)$, Space $O(N \cdot M)$ where N is the number of keys.
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Graphs

Let V be the number of vertices and E be the number of edges.

- **DFS / BFS:**

Time $O(V+E)$, Space $O(V)$.

- **Dijkstra's Algorithm:**

Time $O(E \log V)$ with a binary heap. Space $O(V)$.

- **Bellman-Ford Algorithm:**

Time $O(V \cdot E)$, Space $O(V)$.

- **Floyd-Warshall Algorithm:**

Time $O(V^3)$, Space $O(V^2)$.

- **Kruskal's Algorithm:**

Time $O(E \log E)$, Space $O(V+E)$.

- **Prim's Algorithm:**

Time $O(E \log V)$ with a binary heap. Space $O(V)$.

- **Topological Sort:**

Time $O(V+E)$, Space $O(V)$.

- **Strongly Connected Components (Tarjan's, Kosaraju's):**

Time $O(V+E)$, Space $O(V)$.

Sorting & Searching Algorithms

- **Linear Search:**

Time $O(n)$, Space $O(1)$.

- **Binary Search:**

Time $O(\log n)$, Space $O(1)$.

- **Merge Sort:**

Time $O(n \log n)$, Space $O(n)$.

- **Quick Sort:**

Average Time $O(n \log n)$, Worst Time $O(n^2)$. Space $O(\log n)$.

- **Heap Sort:**

Time $O(n \log n)$, Space $O(1)$.

- **Bubble / Selection / Insertion Sort:**

Time $O(n^2)$, Space $O(1)$.

- **Counting Sort:**

Time $O(n+k)$, Space $O(n+k)$ where k is the range of elements.

- **Radix Sort:**

Time $O(d \cdot (n+k))$, Space $O(n+k)$ where d is the number of digits.

String Algorithms

Let n be the length of the text and m be the length of the pattern.

- **Naive String Matching:** Time $O(n \cdot m)$, Space $O(1)$.
 - **Knuth-Morris-Pratt (KMP):** Time $O(n+m)$, Space $O(m)$.
 - **Rabin-Karp:** Average Time $O(n+m)$, Worst Time $O(n \cdot m)$. Space $O(1)$.
 - **Longest Common Subsequence (LCS):** Time $O(n \cdot m)$, Space $O(n \cdot m)$.
 - **Edit Distance:** Time $O(n \cdot m)$, Space $O(n \cdot m)$.
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Dynamic Programming & Recursion Examples

- **Fibonacci (Memoized/Tabulation):** Time $O(n)$, Space $O(n)$.
 - **0/1 Knapsack:** Time $O(N \cdot W)$, Space $O(W)$ where N is items and W is capacity.
 - **Longest Increasing Subsequence (LIS):** Time $O(n \log n)$, Space $O(n)$.
 - **Matrix Chain Multiplication:** Time $O(n^3)$, Space $O(n^2)$.
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Greedy Algorithms Examples

- **Activity Selection:** Time $O(n \log n)$ (if not sorted), Space $O(1)$.
 - **Fractional Knapsack:** Time $O(n \log n)$, Space $O(1)$.
 - **Huffman Coding:** Time $O(n \log n)$, Space $O(n)$.
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Divide & Conquer Examples

- **Closest Pair of Points:** Time $O(n \log n)$, Space $O(n)$.
 - **Strassen's Matrix Multiplication:** Time $O(n \log^2 7)$, Space $O(n^2)$.
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Advanced & Specialized

- **Union-Find / Disjoint Set Union (DSU):** Time $O(\alpha(n))$ (Amortized, nearly constant), Space $O(n)$.