

# Linear Data Structures

- Arrays
    - **Access:** Time O(1), Space O(1)
    - **Search:** Time O(n), Space O(1)
    - **Insertion / Deletion (at end):** Time O(1) (amortized for dynamic), Space O(1)
    - **Insertion / Deletion (at middle):** Time O(n), Space O(1)
  - Linked Lists (Singly, Doubly, Circular)
    - **Access / Search:** Time O(n), Space O(1)
    - **Insertion / Deletion (at beginning):** Time O(1), Space O(1)
    - **Insertion / Deletion (at end):** Time O(1) (with tail pointer), Space O(1)
  - Stacks (Array/List implementation)
    - **Push / Pop / Peek:** Time O(1), Space O(1)
  - Queues (Array/List implementation)
    - **Enqueue / Dequeue:** Time O(1), Space O(1)
  - Hash Table / Hash Map / Hash Set
    - **Insert / Delete / Search:** Average Time O(1), Worst Time O(n). Space O(n) for storage.
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# Trees

- Binary Tree Traversal (Inorder, Preorder, Postorder)
    - **Time:**  $O(n)$ , **Space:**  $O(h)$  where  $h$  is the height of the tree ( $O(n)$  in worst-case,  $O(\log n)$  in best-case).
  - Binary Search Tree (BST)
    - **Search / Insert / Delete:** Average Time  $O(\log n)$ , Worst Time  $O(n)$ .
  - Balanced BSTs (AVL, Red-Black)
    - **Search / Insert / Delete:** Time  $O(\log n)$ , Space  $O(\log n)$ .
  - Heap (Min-Heap, Max-Heap)
    - **Insert / Delete:** Time  $O(\log n)$
    - **Get Min/Max:** Time  $O(1)$
    - **Build Heap:** Time  $O(n)$
  - **Trie** (where  $M$  is the length of the key)
    - **Insert / Search / Delete:** Time  $O(M)$ , Space  $O(N \cdot M)$  where  $N$  is the number of keys.
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## Graphs

Let  $V$  be the number of vertices and  $E$  be the number of edges.

- **DFS / BFS:**

Time  $O(V+E)$ , Space  $O(V)$ .

- **Dijkstra's Algorithm:**

Time  $O(E \log V)$  with a binary heap. Space  $O(V)$ .

- **Bellman-Ford Algorithm:**

Time  $O(V \cdot E)$ , Space  $O(V)$ .

- **Floyd-Warshall Algorithm:**

Time  $O(V^3)$ , Space  $O(V^2)$ .

- **Kruskal's Algorithm:**

Time  $O(E \log E)$ , Space  $O(V+E)$ .

- **Prim's Algorithm:**

Time  $O(E \log V)$  with a binary heap. Space  $O(V)$ .

- **Topological Sort:**

Time  $O(V+E)$ , Space  $O(V)$ .

- **Strongly Connected Components (Tarjan's, Kosaraju's):**

Time  $O(V+E)$ , Space  $O(V)$ .

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# Sorting & Searching Algorithms

- **Linear Search:**

Time  $O(n)$ , Space  $O(1)$ .

- **Binary Search:**

Time  $O(\log n)$ , Space  $O(1)$ .

- **Merge Sort:**

Time  $O(n \log n)$ , Space  $O(n)$ .

- **Quick Sort:**

Average Time  $O(n \log n)$ , Worst Time  $O(n^2)$ . Space  $O(\log n)$ .

- **Heap Sort:**

Time  $O(n \log n)$ , Space  $O(1)$ .

- **Bubble / Selection / Insertion Sort:**

Time  $O(n^2)$ , Space  $O(1)$ .

- **Counting Sort:**

Time  $O(n+k)$ , Space  $O(n+k)$  where  $k$  is the range of elements.

- **Radix Sort:**

Time  $O(d \cdot (n+k))$ , Space  $O(n+k)$  where  $d$  is the number of digits.

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# String Algorithms

Let  $n$  be the length of the text and  $m$  be the length of the pattern.

- **Naive String Matching**: Time  $O(n \cdot m)$ , Space  $O(1)$ .
  - **Knuth-Morris-Pratt (KMP)**: Time  $O(n+m)$ , Space  $O(m)$ .
  - **Rabin-Karp**: Average Time  $O(n+m)$ , Worst Time  $O(n \cdot m)$ . Space  $O(1)$ .
  - **Longest Common Subsequence (LCS)**: Time  $O(n \cdot m)$ , Space  $O(n \cdot m)$ .
  - **Edit Distance**: Time  $O(n \cdot m)$ , Space  $O(n \cdot m)$ .
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## Dynamic Programming & Recursion Examples

- **Fibonacci (Memoized/Tabulation)**: Time  $O(n)$ , Space  $O(n)$ .
  - **0/1 Knapsack**: Time  $O(N \cdot W)$ , Space  $O(W)$  where  $N$  is items and  $W$  is capacity.
  - **Longest Increasing Subsequence (LIS)**: Time  $O(n \log n)$ , Space  $O(n)$ .
  - **Matrix Chain Multiplication**: Time  $O(n^3)$ , Space  $O(n^2)$ .
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## Greedy Algorithms Examples

- **Activity Selection**: Time  $O(n \log n)$  (if not sorted), Space  $O(1)$ .
  - **Fractional Knapsack**: Time  $O(n \log n)$ , Space  $O(1)$ .
  - **Huffman Coding**: Time  $O(n \log n)$ , Space  $O(n)$ .
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## Divide & Conquer Examples

- **Closest Pair of Points**: Time  $O(n \log n)$ , Space  $O(n)$ .
  - **Strassen's Matrix Multiplication**: Time  $O(n \log 27)$ , Space  $O(n^2)$ .
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## Advanced & Specialized

- **Union-Find / Disjoint Set Union (DSU):** Time  $O(\alpha(n))$  (Amortized, nearly constant), Space  $O(n)$ .