

$$\int_0^{2\pi} \int_a^b \frac{y^2}{\pi(x^2+y^2)} r dr d\theta \quad x = r \cos \theta$$

$$\int_0^{2\pi} \int \frac{r^2 \sin^2 \theta}{\pi r^2} r dr d\theta$$

$$= \frac{(b^2 - a^2)}{\pi \cdot 2} \times \left\{ \frac{\theta}{2} - \frac{\sin(2\theta)}{4} \right\}_0^{2\pi}$$

$$= \frac{(b^2 - a^2)}{\pi \cdot 2} \times \{ \pi \} = \frac{1}{\pi \cdot 2} \pi (b^2 - a^2) = \boxed{\frac{b^2 - a^2}{2}}$$

$$\int_0^1 \int_0^{y^n} \sqrt{y^{n+1} + 1} dx dy$$

$$= \int_0^1 (\sqrt{y^{n+1} + 1}) y^n dy$$

$$= \int_1^2 \frac{\sqrt{t} dt}{n+1}$$

$$= \frac{1}{(n+1)} \frac{2(\sqrt{t})^{3/2}}{3} \Big|_1^2$$

$$y^{n+1} + 1 = t$$

$$(n+1)y^n dy = dt$$

$$\frac{2}{3(n+1)} [2\sqrt{2} - 1] \times \frac{3}{2} \times \frac{(n+1)^2}{[2\sqrt{2} - 1]} = \boxed{n+1}$$

$$\int_0^1 \int_0^{y^n} \sqrt{y^{n+1} + 1} dx dy$$

$$x^n = y$$

$$n =$$

