MA111 Tutorial Sheet 5 – Final Answer Key

1. (i)
$$\oint_{\partial R} F_1 dx + F_2 dy = \frac{31}{60} = \iint_R \left(\frac{\partial F_2}{\partial x} - \frac{\partial F_1}{\partial y} \right) dx dy$$
.

$$\text{(ii)} \ \oint_{\partial R} F_1 \, dx + F_2 \, dy = 1 = \iint_R \left(\frac{\partial F_2}{\partial x} - \frac{\partial F_1}{\partial y} \right) \, dx dy.$$

- 2. (i) -4
 - (ii) 4
 - (iii) -4π
- 3. (i) $\frac{3\pi a^2}{2}$
 - (ii) a^2
- 4. (i) $\frac{(3\pi 8)a^2}{8}$ (ii) $3\pi a^2$

 - (iii) $\frac{3\pi 8}{4}$
- 5. 0
- 8. 0
- 9. (iii) 0
- 10. (i) -2π
 - (ii) 0

(iii)
$$\oint_C \frac{\partial (\ln r)}{\partial y} \, dx - \frac{\partial (\ln r)}{\partial x} \, dy = \begin{cases} -2\pi, & \text{if } (0,0) \text{ lies in the interior of } C \text{ in } \mathbb{R}^2; \\ 0, & \text{otherwise.} \end{cases}$$

- 11. (i) No
 - (ii) No