CS 61A Fall 2020

Interpreters

Discussion 11: November 11, 2020

1 Calculator

An interpreter is a program that understands other programs. Today, we will explore how to interpret a simple language that uses Scheme syntax called *Calculator*.

The Calculator language includes only the four basic arithmetic operations: +, -, *, and /. These operations can be nested and can take any numbers of arguments. A few examples of calculator expressions and their corresponding values are given on the right. Recall that the reader component of an interpreter parses input strings and represents them as data structures in the implementing language. In this case, we need to represent Calculator expressions as Python objects. To represent numbers, we can just use Python numbers. To represent the names of the arithmetic procedures, we can use Python strings (e.g. '+').

Call expressions are a bit more complicated. First, note that like Scheme call expressions, call expressions in Calculator look just like Scheme lists. For example, to construct the expression (+ 2 3) in Scheme, we would do the following:

```
scm> (cons '+ (cons 2 (cons 3 nil)))
(+ 2 3)
```

To represent Scheme lists in Python, we will use the Pair class. A Pair instance holds exactly two elements. Accordingly, the Pair constructor takes in two arguments, and to make a list we must nest calls to the constructor and pass in nil as the second element of the last pair. Note that in our implementation, nil is bound to a special user-defined object that represents an empty list, whereas nil in Scheme is actually an empty list.

```
>>> Pair('+', Pair(2, Pair(3, nil)))
Pair('+', Pair(2, Pair(3, nil)))
```

Each Pair instance has two instance attributes: first and rest, which are bound to the first and second elements of the pair respectively.

```
>>> p = Pair('+', Pair(2, Pair(3, nil)))
>>> p.first
'+'
>>> p.rest
Pair(2, Pair(3, nil))
>>> p.rest.first
2
```

```
calc> (+ 2 2)
4

calc> (- 5)
-5

calc> (* (+ 1 2) (+ 2 3))
15
```

Here's an implementation of what we described:

```
class Pair:
    """Represents the built-in pair data structure in Scheme."""
   def __init__(self, first, rest):
        self.first = first
        if not scheme_valid_cdrp(rest):
            raise SchemeError("cdr can only be a pair, nil, or a promise but was {}".format(rest))
        self.rest = rest
   def map(self, fn):
        """Maps fn to every element in a list, returning a new
       Pair.
       >>> Pair(1, Pair(2, Pair(3, nil))).map(lambda x: x * x)
       Pair(1, Pair(4, Pair(9, nil)))
        assert isinstance(self.rest, Pair) or self.rest is nil, \
            "rest element in pair must be another pair or nil"
        return Pair(fn(self.first), self.rest.map(fn))
   def __repr__(self):
        return 'Pair({}, {})'.format(self.first, self.rest)
class nil:
    """Represents the special empty pair nil in Scheme."""
   def map(self, fn):
        return nil
   def __getitem__(self, i):
        raise IndexError('Index out of range')
   def __repr__(self):
        return 'nil'
nil = nil() # this hides the nil class *forever*
```

Questions

1.1 Write out the Calculator expression with proper syntax that corresponds to the following Pair constructor calls. Also, draw out a box and pointer diagram corresponding to each input.

```
>>> Pair('+', Pair(1, Pair(2, Pair(3, Pair(4, nil)))))
```

```
>>> Pair('+', Pair(1, Pair(Pair('*', Pair(2, Pair(3, nil))), nil)))
```

- 1.2 Answer the following questions about a Pair instance representing the Calculator expression (+ (- 2 4) 6 8).
 - i. Write out the Python expression that returns a Pair representing the given expression, and draw a box and pointer diagram corresponding to it.
 - ii. What is the operator of the call expression? If the Pair you constructed in the previous part was bound to the name p, how would you retrieve the operator?
 - iii. What are the operands of the call expression? If the Pair you constructed in Part (i) was bound to the name p, how would you retrieve a list containing all of the operands? How would you retrieve only the first operand?

2 Evaluation

The evaluation component of an interpreter determines the type of an expression and executes corresponding evaluation rules.

Here are the evaluation rules for the three types of Calculator expressions:

- 1. **Numbers** are self-evaluating. For example, the numbers 3.14 and 165 just evaluate to themselves.
- 2. Names are looked up in the OPERATORS dictionary. Each name (e.g. '+') is bound to a corresponding function in Python that does the appropriate operation on a list of numbers (e.g. sum).
- 3. Call expressions are evaluated the same way you've been doing them all semester:
 - (1) **Evaluate** the operator, which evaluates to a function.
 - (2) **Evaluate** the operands from left to right.
 - (3) **Apply** the function to the value of the operands.

The function calc_eval takes in a Calculator expression represented in Python and implements each of these rules:

```
def calc_eval(exp):
    """Evaluates a Calculator expression represented as a Pair."""
    if isinstance(exp, Pair): # Call expressions
        fn = calc_eval(exp.first)
        args = list(exp.rest.map(calc_eval))
        return calc_apply(fn, args)
    elif exp in OPERATORS: # Names
        return OPERATORS[exp]
    else: # Numbers
        return exp
```

Note that calc_eval is recursive! In order to evaluate call expressions, we must call calc_eval on the operator and each of the operands.

The *apply* step in the Calculator language is straight-forward, since we only have primitive procedures. This step is more complex when it comes to applying Scheme procedures, which may include user-defined procedures.

Given the Python function that implements the appropriate Calculator operation and a Python list of numbers, the calc_apply function simply calls the function on the arguments, and regular Python evaluation rules take place.

```
def calc_apply(fn, args):
    """Applies a Calculator operation to a list of numbers."""
    return fn(args)
```

Questions

2.1 Suppose we want to add handling for comparison operators >, <, and = as well as and expressions to our Calculator interpreter. These should work the same way they do in Scheme.

```
calc> (and (= 1 1) 3)
3
calc> (and (+ 1 0) (< 1 0) (/ 1 0))
#f</pre>
```

- i. Are we able to handle expressions containing the comparison operators (such as <, >, or =) with the existing implementation of calc_eval? Why or why not?
- ii. Are we able to handle and expressions with the existing implementation of calc_eval? Why or why not?
- iii. Now, complete the implementation below to handle and expressions. You may assume the conditional operators (e.g. <, >, =, etc) have already been implemented for you.

```
def calc_eval(exp):
    if isinstance(exp, Pair):
        if ______: # and expressions
            return eval_and(exp.rest)
        else: # Call expressions
            return calc_apply(calc_eval(exp.first), list(exp.rest.map(calc_eval)))
    elif exp in OPERATORS: # Names
        return OPERATORS[exp]
    else: # Numbers
        return exp
```

def eval_and(operands):