

# PCA\_Iris\_Dataset

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## 1 PCA on Iris Data Set

Why this notebook To have hands-on exercise on PCA using Python

Reference None. Since IRIS Dataset is easily available, chosen that to try PCA

```
In [1]: import numpy as np
import matplotlib.pyplot as plt # for plotting
import seaborn as sns
import pandas as pd
from sklearn.preprocessing import StandardScaler # for column standardization
from scipy.linalg import eigh # for eigen value/vector calculation
```

### 1.1 Load Data Set

```
In [2]: df = pd.read_csv('../../datasets/iris-dataset/iris.csv')
df.head()
```

```
Out[2]:
```

	sepal_length	sepal_width	petal_length	petal_width	species
0	5.1	3.5	1.4	0.2	setosa
1	4.9	3.0	1.4	0.2	setosa
2	4.7	3.2	1.3	0.2	setosa
3	4.6	3.1	1.5	0.2	setosa
4	5.0	3.6	1.4	0.2	setosa

```
In [3]: df.describe()
```

```
Out[3]:
```

	sepal_length	sepal_width	petal_length	petal_width
count	150.000000	150.000000	150.000000	150.000000
mean	5.843333	3.054000	3.758667	1.198667
std	0.828066	0.433594	1.764420	0.763161
min	4.300000	2.000000	1.000000	0.100000
25%	5.100000	2.800000	1.600000	0.300000
50%	5.800000	3.000000	4.350000	1.300000
75%	6.400000	3.300000	5.100000	1.800000
max	7.900000	4.400000	6.900000	2.500000

```
In [4]: # move labels to a seperate data frame
df_labels = df['species']
df_data = df.drop('species',axis=1)
```

```
In [5]: df_labels.shape
```

```
Out[5]: (150,)
```

```
In [6]: df_labels.head()
```

```
Out[6]: 0    setosa
        1    setosa
        2    setosa
        3    setosa
        4    setosa
        Name: species, dtype: object
```

```
In [7]: df_data.shape
```

```
Out[7]: (150, 4)
```

```
In [8]: df_data.head()
```

```
Out[8]:   sepal_length  sepal_width  petal_length  petal_width
        0           5.1           3.5           1.4           0.2
        1           4.9           3.0           1.4           0.2
        2           4.7           3.2           1.3           0.2
        3           4.6           3.1           1.5           0.2
        4           5.0           3.6           1.4           0.2
```

## 1.2 Column Standardize the Data

```
In [9]: # Column Standardize the data
        standardized_data = StandardScaler().fit_transform(df_data)
```

```
In [10]: standardized_data.shape
```

```
Out[10]: (150, 4)
```

```
In [11]: standardized_data[1:4]
```

```
Out[11]: array([[ -1.14301691, -0.1249576 , -1.3412724 , -1.31297673],
                [-1.38535265,  0.33784833, -1.39813811, -1.31297673],
                [-1.50652052,  0.10644536, -1.2844067 , -1.31297673]])
```

## 1.3 Computing PCA manually

### 1.3.1 Compute Covariance Matrix

```
In [12]: # Compute covariance Matrix
        sample_data = standardized_data
        covar_matrix = np.matmul(sample_data.T, sample_data)
        covar_matrix.shape
```

```
Out[12]: (4, 4)
```

```
In [13]: covar_matrix
```

```
Out[13]: array([[150.          , -16.40538749, 130.7631236 , 122.69304501],
                [-16.40538749, 150.          , -63.07741446, -53.48161344],
                [130.7631236 , -63.07741446, 150.          , 144.41356456],
                [122.69304501, -53.48161344, 144.41356456, 150.          ]])
```

### 1.3.2 Compute Eigen Values and Eigen Vectors

```
In [14]: # calculate eigen values and eigen vectors
        eigen_values, eigen_vectors = eigh(covar_matrix)
```

```
In [15]: eigen_values.shape
```

```
Out[15]: (4,)
```

```
In [16]: eigen_vectors.shape
```

```
Out[16]: (4, 4)
```

```
In [17]: eigen_values
```

```
Out[17]: array([ 3.09115609, 22.10299175, 138.18313961, 436.62271256])
```

```
In [18]: eigen_vectors
```

```
Out[18]: array([[ 0.26199559,  0.72101681, -0.37231836,  0.52237162],
                [-0.12413481, -0.24203288, -0.92555649, -0.26335492],
                [-0.80115427, -0.14089226, -0.02109478,  0.58125401],
                [ 0.52354627, -0.6338014 , -0.06541577,  0.56561105]])
```

### 1.3.3 2-D Visualization

```
In [19]: # Since we are going to do 2-D visualization, take last two eigen vectors having max variance
        eigen_2d = eigen_vectors[:, [-1, -2]]
        eigen_2d = eigen_2d.T
        eigen_2d.shape
```

```
Out[19]: (2, 4)
```

```
In [20]: # project data points into hyper plane
        new_data_matrix = np.matmul(eigen_2d, standardized_data.T)
```

```
In [21]: 'Resultant matrix {0} x {1} = {2}'.format(eigen_2d.shape, standardized_data.T.shape, new_data_matrix.shape)
```

```
Out[21]: 'Resultant matrix (2, 4) x (4, 150) = (2, 150)'
```

```
In [22]: # Add label column
        new_data_matrix = np.vstack((new_data_matrix, df_labels))
```

```
In [23]: new_data_matrix.shape
```

Out[23]: (3, 150)

```
In [24]: # Transpose the matrix to have data points as rows
new_data_matrix = new_data_matrix.T
new_data_matrix.shape
```

Out[24]: (150, 3)

```
In [25]: new_data_matrix[:5]
```

```
Out[25]: array([[ -2.2645417283949003, -0.5057039027737857, 'setosa'],
                [ -2.08642550061616,  0.6554047293691359, 'setosa'],
                [ -2.3679504490625267,  0.31847731084724806, 'setosa'],
                [ -2.3041971611520102,  0.5753677125331943, 'setosa'],
                [ -2.3887774935056423, -0.6747673967025166, 'setosa']], dtype=object)
```

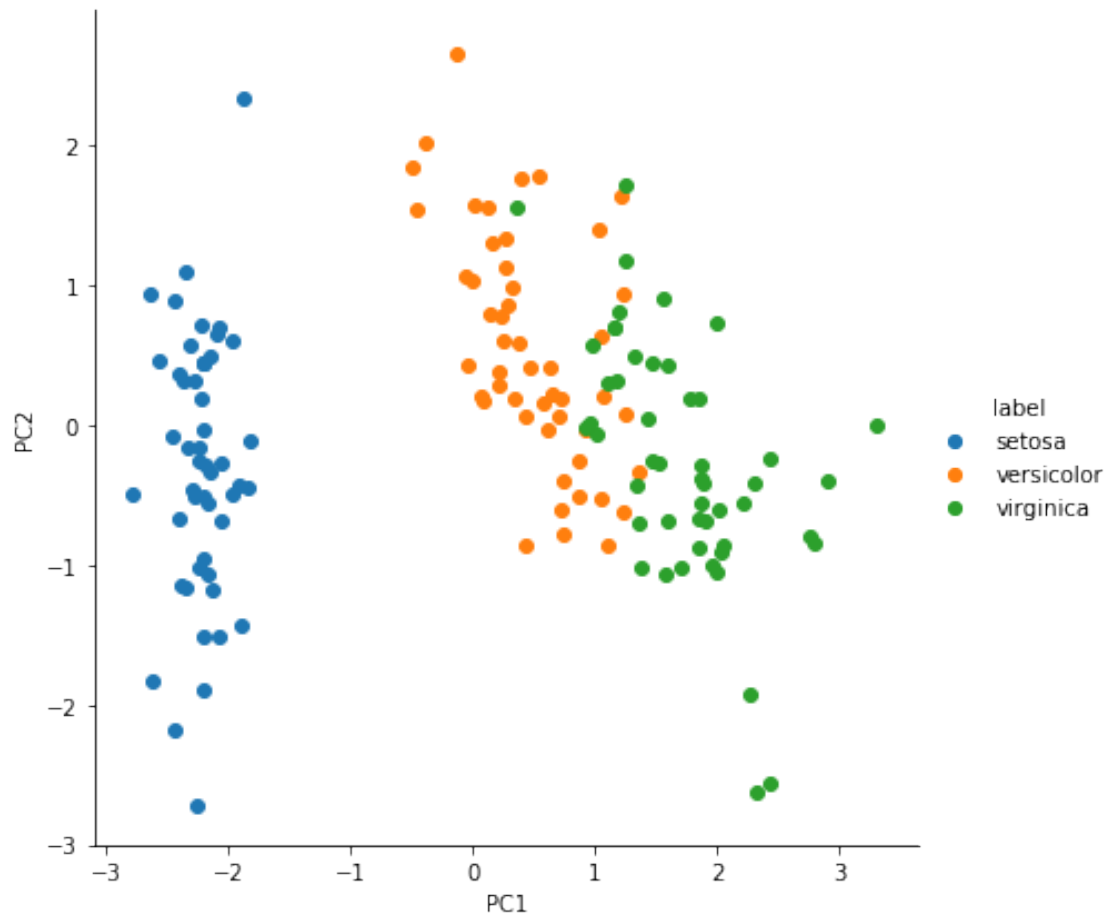
```
In [26]: # Create a data frame using new data matrix for plotting
new_data_df = pd.DataFrame(data=new_data_matrix, columns=['PC1', 'PC2', 'label'])
new_data_df.head()
```

```
Out[26]:
```

	PC1	PC2	label
0	-2.26454	-0.505704	setosa
1	-2.08643	0.655405	setosa
2	-2.36795	0.318477	setosa
3	-2.3042	0.575368	setosa
4	-2.38878	-0.674767	setosa

```
In [27]: sns.FacetGrid(data=new_data_df, hue='label', height=6).map(plt.scatter, 'PC1', 'PC2').add
```

```
Out[27]: <seaborn.axisgrid.FacetGrid at 0x7fc81357eef0>
```



## 1.4 PCA using SciKit-Learn

```
In [28]: # import required modules
         from sklearn import decomposition
```

```
In [29]: # init PCA
         pca = decomposition.PCA()
```

### 1.4.1 2-D Visualization

```
In [30]: # config required parameters
         pca.n_components = 2
         pca_data = pca.fit_transform(standardized_data)

         print('Size of PCA reduced data shape: ', pca_data.shape)
```

Size of PCA reduced data shape: (150, 2)

```
In [31]: # add labels to PCA new data matrix for plotting
pca_data = np.vstack((pca_data.T, df_labels)).T
print('New Projected Matrix shape : ', pca_data.shape)
```

New Projected Matrix shape : (150, 3)

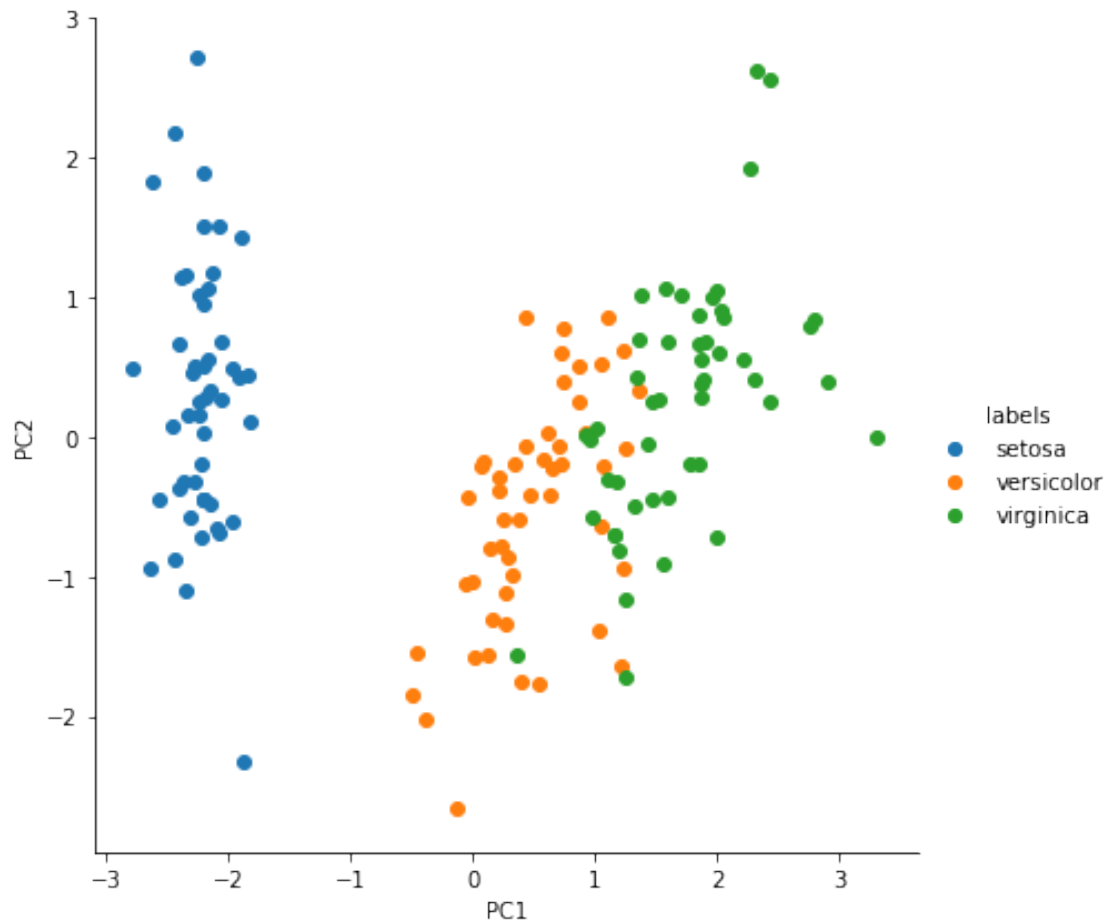
```
In [32]: # create dataframe out of PCA Data
new_data_df = pd.DataFrame(data=pca_data, columns=['PC1', 'PC2', 'labels'])
new_data_df.head()
```

```
Out[32]:
```

	PC1	PC2	labels
0	-2.26454	0.505704	setosa
1	-2.08643	-0.655405	setosa
2	-2.36795	-0.318477	setosa
3	-2.3042	-0.575368	setosa
4	-2.38878	0.674767	setosa

```
In [33]: # Plot the matrix
sns.FacetGrid(new_data_df, hue='labels', height=6).map(plt.scatter, 'PC1', 'PC2').add_
```

```
Out[33]: <seaborn.axisgrid.FacetGrid at 0x7fc8128e54a8>
```



### 1.4.2 CDF of Data Variances

```
In [34]: pca.n_components = 4
pca_data = pca.fit_transform(standardized_data)

percentage_var_explained = pca.explained_variance_ / np.sum(pca.explained_variance_)
print('Percentage of data explained: ',percentage_var_explained)

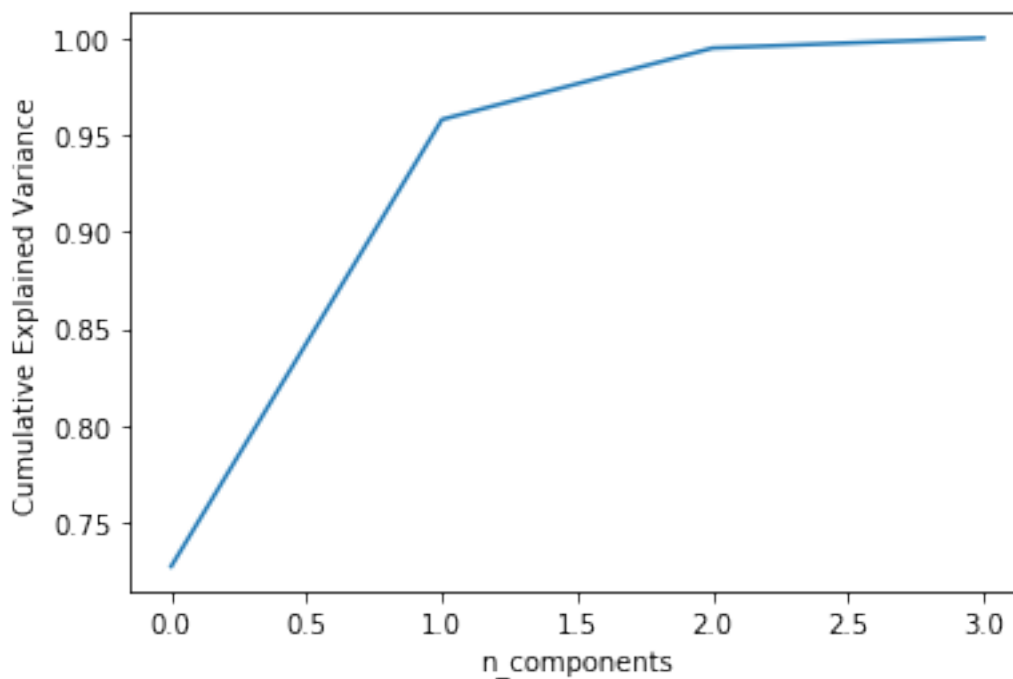
cum_var_explained = np.cumsum(ppercentage_var_explained)

print('Cumulative Sum of Vairances explained : ', cum_var_explained)
```

```
Percentage of data explained: [0.72770452 0.23030523 0.03683832 0.00515193]
Cumulative Sum of Vairances explained : [0.72770452 0.95800975 0.99484807 1.          ]
```

```
In [35]: plt.figure(1, figsize=(6,4))
plt.plot(cum_var_explained)
plt.xlabel('n_components')
plt.ylabel('Cumulative Explained Variance')

Out[35]: Text(0, 0.5, 'Cumulative Explained Variance')
```



### 1.4.3 Pair Plot of all components

```
In [36]: print(pca_data.T.shape, df_labels.shape)
pca_data = np.vstack((pca_data.T, df_labels))
pca_data = pca_data.T
print(pca_data.shape)
```

```
(4, 150) (150,)
(150, 5)
```

```
In [37]: new_data_df = pd.DataFrame(data=pca_data, columns=['PC1', 'PC2', 'PC3', 'PC4', 'labels'])
new_data_df.head()
```

```
Out[37]:
```

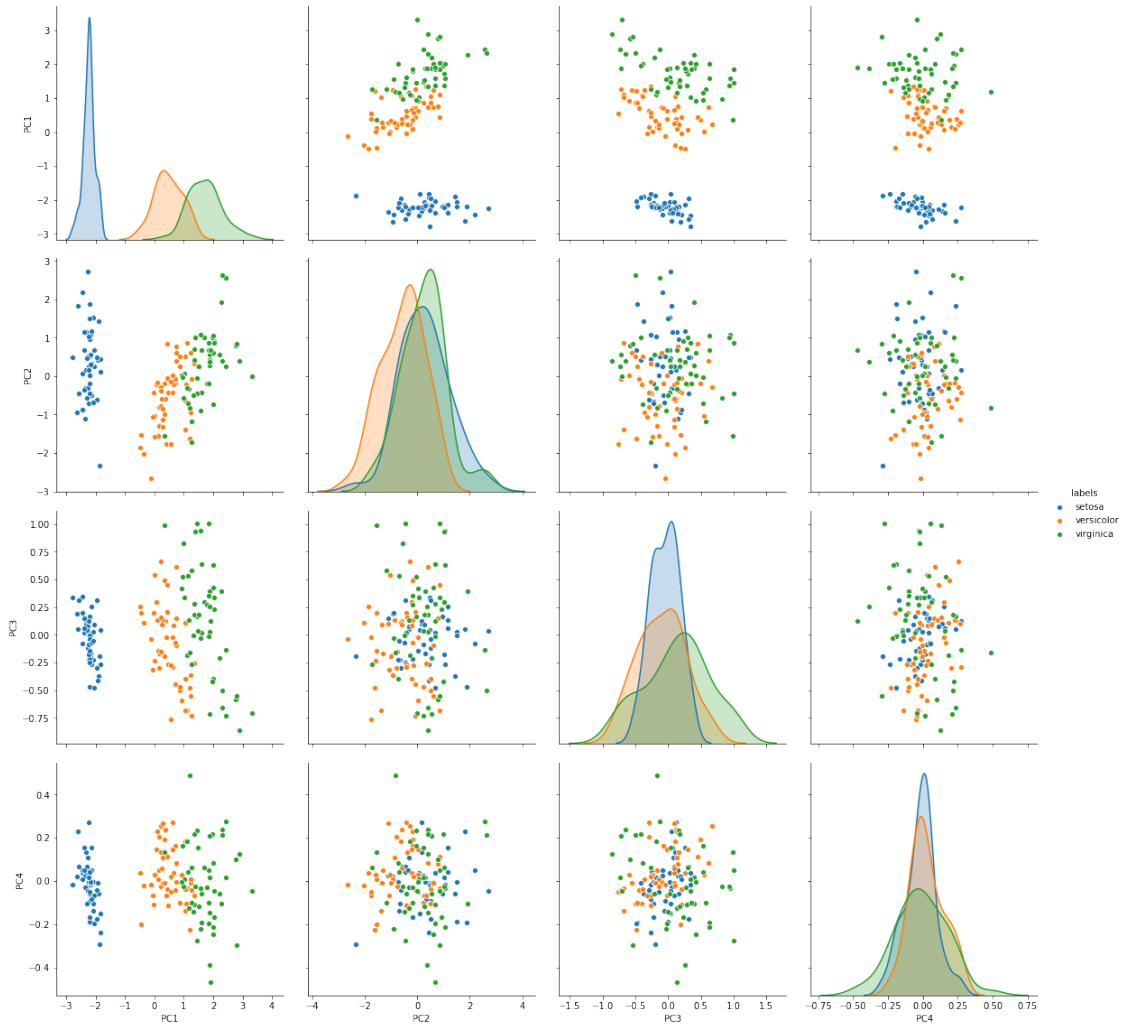
	PC1	PC2	PC3	PC4	labels
0	-2.26454	0.505704	-0.121943	-0.0230733	setosa
1	-2.08643	-0.655405	-0.227251	-0.103208	setosa
2	-2.36795	-0.318477	0.0514796	-0.0278252	setosa
3	-2.3042	-0.575368	0.0988604	0.0663115	setosa
4	-2.38878	0.674767	0.0214278	0.0373973	setosa

```
In [38]: sns.pairplot(new_data_df, hue='labels', vars=['PC1', 'PC2', 'PC3', 'PC4'], height=4)
```

```
/home/mlstudy/anaconda3/envs/mlstudy_1/lib/python3.6/site-packages/scipy/stats/stats.py:1713:
    return np.add.reduce(sorted[indexer] * weights, axis=axis) / sumval
```

```
Out[38]: <seaborn.axisgrid.PairGrid at 0x7fc7ef767cc0>
```





```
In [39]: #plt.scatter(pca_data[:,0], pca_data[:,1],c=df_labels)
df_labels.unique()
```

```
Out[39]: array(['setosa', 'versicolor', 'virginica'], dtype=object)
```

```
In [40]: # create map of labels to int for plotting
targets = df_labels.unique()
targets
```

```
Out[40]: array(['setosa', 'versicolor', 'virginica'], dtype=object)
```