

## Coordinated Planning and Control for Tethered Robot Pairs

Many important and rewarding science target locations on extra-planetary bodies lie in terrain that is rocky, uneven, or involves traversing steep inclines in order to access. Consider the search for ice in underground caves on Mars, or collecting soil samples and images from the bottom of a crater or ravine. These tasks, while very rewarding in terms of scientific value, are not easily achieved by humans nor the current generation of planetary rovers. This shortcoming of current exploratory technology has spurred considerable interest in the development of next generation rover designs featuring a tether that either connects the rover to a static point in the environment or, even more desirably, connects to another rover vehicle of equal capability. A tethered pair of robots not only benefits from the stability that a tether provides while rappelling down difficult terrains, but has added robustness benefits from having an additional robot at its disposal. For example, the base robot can reconfigure to provide maximal stability, it can descend down in order to help in case of immobility, and the pair can swap roles between (1) providing stability to the other and (2) traversing the terrain, allowing the tethered pair to safely traverse difficult terrain well beyond what a single anchored robot could achieve.

In this proposal we present an overview of the state-of-the-art in tethered robots designed with the goals mentioned above in mind and cover recent developments in motion planning for this difficult problem. We then propose two related research problems, viable solutions to which we believe would tremendously aid in the utility of tethered robot technology: a control strategy for re-configuring the tether between two rovers in order to deal with unforeseen challenges in the terrain, and a planning problem which uses this control strategy as a “submodule” while planning for coordinated descent/ascent of difficult terrain with a tether constraint. Solutions to these problems as we present them would be platform-independent, and could apply well beyond the scope of extra-planetary exploration. For example, it could be beneficial to attach a tether to Robonaut in case an emergency retraction is needed as it navigates the International Space Station. With the help and support of NASA’s STRF program, we propose to work on these problems for the duration of our studies.

### Tethered Rover Systems Background

Recent research into robot designs for the traversal of harsh and difficult terrains has featured several very different designs with different means of locomotion. Several of these

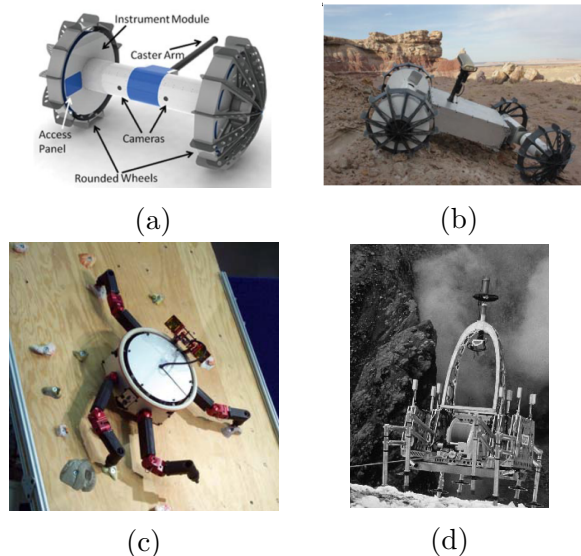


Figure 1: (a) The Axel II rover prototype (b) Two Axel II rovers in DuAxel configuration with support structure (c) Lemur IIb autonomous climbing robot (d) Dante II robot exploring a volcanic crater.

systems include an actuated winch or spooled tether used for communication and/or stability while locomoting. Notable examples include an eight-legged walking robot attached to a stationary base [Fig. 1d] and a pair of two-wheeled differential drive robots connected with a soft tether [Fig. 1b]. Even more novel recent robot designs could benefit from the presence of a tether attachment to an exploratory counterpart. We believe this list to include Lemur IIb, a four-legged climbing robot [Fig. 1c], which could potentially use an actuated tether to swing its counterpart onto protruding overhangs and then, in turn, rappel from the stabilized counterpart robot in order to reach the overhang safely.

The Dante II robot design consisted of eight legs for locomotion and an actuated winch used for rappelling down steep and difficult terrain from a static anchor point. Both actuation mechanisms were attached to a base frame with a sensor arch protruding from the top of the structure [1]. A variety of sensing equipment, including a pan/tilt camera and a laser range finder, were attached to the arch in order to retrieve and transmit data from remote locations. In 1994 the system was deployed into Mount Spurr, an active volcanic site, in order to record data for further scientific analysis. The robot's control during this time was a combination of supervised autonomous motions and remote teleoperation [2]. During the mission the robot suffered from a failure where the robot incurred a lateral force at its contact point with the tether, fell over, and was not able to correct itself. Apart from this occurrence, however, the 5-day mission was regarded as a success in showing the capabilities of robotic systems to act as "surrogate scientists"; exploring where humans would not otherwise be able.

More recently, NASA's Jet Propulsion Laboratory has been working on a two-wheeled differential drive tethered robot, appropriately named "Axel". The Axel II robot design features collapsible, paddled wheels, making the system more appropriate for longer and more remote missions as this design is more robust to issues such as high-centering and failures such as that encountered by Dante II [3]. The tether mechanism is connected to the axle between the two wheels and is actively spooled as the wheels move relative to the body of the robot. Two variants of the system are presented: one in which Axel is attached to a stationary anchor point, and a second where two Axel robots are tethered together and deployed via a central support beam ("DuAxel") [4].

The open question in either design variation is how to plan autonomous descent and corresponding ascent paths for the deploying tethered Axel robot in uneven, rocky, extra-planetary terrains. A solution framework is

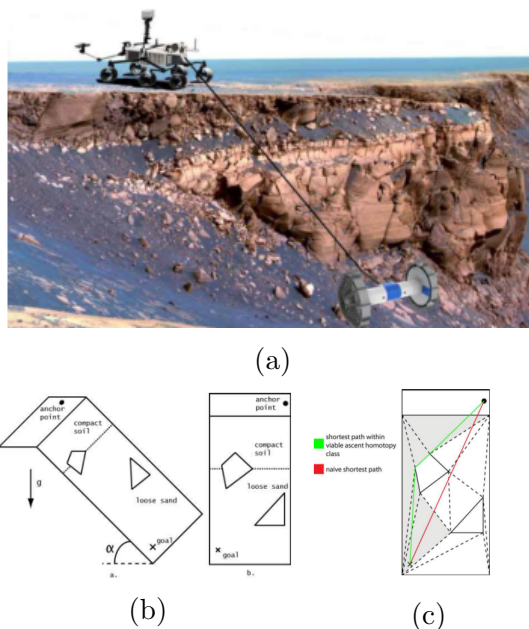


Figure 2: (a) Conceptualized descent terrain for Axel II mission (b) example projection of terrain to 2D plane (c) example solution: viable controllable regions for ascent (shaded), naive shortest path (red), shortest path within viable homotopy class (green).

presented which projects this complex problem to a two-dimensional plane and, building on foundational work addressing the tether constraint problem from a computational geometry perspective [5, 6], extends this approach to produce “controllable” paths by deriving equations of motion arising from the constraints of the Axel robot [7]. The planning problem the authors address in this work is of planning a single mission, consisting of a descent and corresponding ascent, while being stabilized by tether attachment to a static anchor point. The resulting algorithm first plans the more difficult ascent path and then uses the solution to limit its search for viable descent paths lying in the same homotopy class.

While this solution represents substantial progress well-grounded in foundational work, the assumptions and simplifications made leave much to be desired in terms of robust autonomous exploration. Projecting these types of difficult three-dimensional terrain environments in two-dimensions and representing obstacles as simple polygons [Fig. 2b] is not a realistic strategy for complex extra-planetary terrains. This strategy makes the additional assumptions of prior perfect knowledge of the environment, frictionless interaction of the tether with the ground plane, and quasi-static motion of the robot. Most relevant to the work proposed in the next section is that it remains an open question as to how best to plan autonomous motions for the DuAxel configuration where two dynamic robots take turns belaying each other.

### Proposed Research

*The main goal of this research is to address the problem of planning for tethered pairs of exploratory robots in their full three-dimensional workspace, i.e., without projecting the problem to a lower dimension. Our solution provides a control strategy for addressing unforeseen obstacles and failures, and uses this strategy as a submodule in planning paths for tethered pairs of robots in which the robots alternate exploring and providing support to their counterpart.*

In this proposal, we consider a tethered pair of robots of arbitrary design. As such, our approach is applicable to any tethered pair of rovers provided that they have a means of: (1) actuating the tether at its contact points with each rover and (2) measuring the forces exerted on each rover at the tether’s contact points. Likely the most similar system that we’ve presented so far in this proposal is the DuAxel design, which fits these specifications already. However, one can also apply this approach to a pair of Lemur IIb robots free-climbing a vertical and jagged cliff face or even a pair of traditional wheeled rovers descending a steep and rocky mountainside.

#### Research Problem 1: Coordinated control of a soft tether

*Goal: In presence of imperfect terrain information, we require a strategy for dealing with both unforeseen obstacles and unplanned tether entanglements on rocky elements of the terrain.*

In the following, we consider several potentially difficult situations that are likely to arise when planning for a tethered pair under imperfect information about the terrain. In addressing this problem in the full 3D workspace, we require a strategy which can deal with two important potential failure cases. First, while performing the exploratory role, a rover encounters an unknown obstacle obstructing its planned path, which we’ll call the “reevaluation” case (addressed in the planar case in [8]). Second, while the exploratory rover is

moving along its planned obstacle-free path, the tether comes in contact with and becomes entangled on uneven terrain (the “snagging” case).

In the snagging case [Fig. 3], we propose to develop a low-level control law capable of inducing a traveling wave in the tether by employing an oscillatory control policy at the actuated tether contact of the rover closest to the tether snag location. This approach is similar to the strategy used by humans when they encounter the same situation while mountain climbing. The challenge in this strategy however, is that once the tether is free it’s likely to impart a substantial force on the robot’s stabilizing counterpart, potentially resulting in dangerous jerking in a partially known environment. A promising solution to this problem would be to induce in response a counteracting wave from the stabilizing rover’s actuated tether contact. To this end, we would propose to explore first building a model (potentially analytically) of the expected forces exerted by the induced wave on the counterpart robot. We would then use this model in, e.g., a model predictive control-based solution where the low-level control policy optimizes its current control with respect to counteracting the incurred force over a finite time horizon of future predictions. It may also be advantageous to explore model-free approaches (e.g., designing an admittance controller), as it’s possible that reacting to forces incurred is a more feasible solution than accurately predicting them ahead of time.

In the reevaluation case of encountering an unmodeled obstacle in our path, what we must first decide is whether or not we can configure our tether such that we are able to place the tether in an arbitrary configuration on either side of the obstacle once we have moved past it. The reason we need to know this before moving forward is that while the unmodeled obstacle may not cause significant problems for our current rover’s descent, planning the current stabilizing rover’s traversal of the same slope is much more constrained as it does not have a stabilizing tether. Being able to place the tether on either side of the obstacle would then allow us to first plan the descent of the current stabilizing rover (incorporating this new obstacle), and then use the traversing rover to place the tether on the side of the obstacle that is easiest for the stabilizing rover to traverse.

There are two tools at our disposal to determine whether this new obstacle is surmountable. By considering the height of the obstacle, we can search for configurations of the tethered pair which raise the tether above the obstacle. Alternatively, we can extend our snagging strategy outlined above – simulating the effects of various parameterizations of our wave-inducing control policies to find one that would be able to surmount the obstacle. If we successfully find such a policy, we can then combine this policy with a motion plan to move

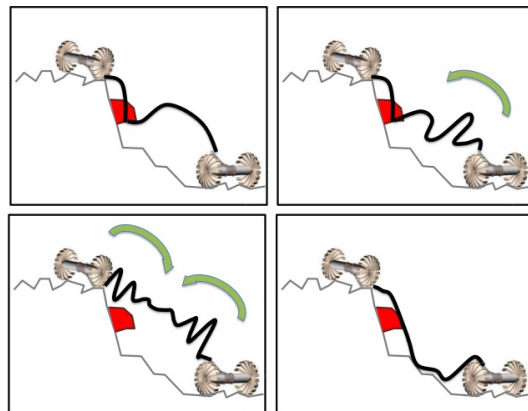


Figure 3: During a coordinated descent down a rocky extra-planetary surface, the tethered rover pair encounters an unplanned snag of the tether with a rock in the terrain (red). The situation is resolved by using the coordinated wave-inducing control strategy (green arrows indicate controls applied) to free the tether.

the exploratory rover to the desired side of the new obstacle, terminating the control policy once we've successfully reached the target state.

#### Research Problem 2: Motion planning for dynamic tethered rover pairs

*Goal: Integrating the control strategy outlined above as a subroutine in cases of environmental obstacles and tether entanglements, we aim to develop a robust motion planning framework for a tethered pair of rovers. This framework will be capable of planning the coordinated traversal of difficult terrain while the rovers alternate exploratory and stabilizing roles.*

Making use of the control strategy presented above when faced with unforeseen obstacles and situations, we can now outline our strategy for robustly solving the motion planning problem of the coordinated traversal (ascent or descent) of difficult and partially known extra-planetary terrain. Beginning with our (incomplete) knowledge of the environment, we first select a set of maximally stable waypoints throughout the terrain. We then proceed iteratively and in an alternating fashion, first planning the descent of one of the rover pair to the first stable waypoint, then the other to some next stable waypoint closer to the goal. The waypoints can then be thought of as "role reversal" locations. When we encounter unforeseen obstacles (or snags), we call upon our control strategy as a submodule and then re-plan. Importantly, re-planning under this strategy only requires re-computing the path between the current set of waypoints, as opposed to the trajectory of the entire traversal.

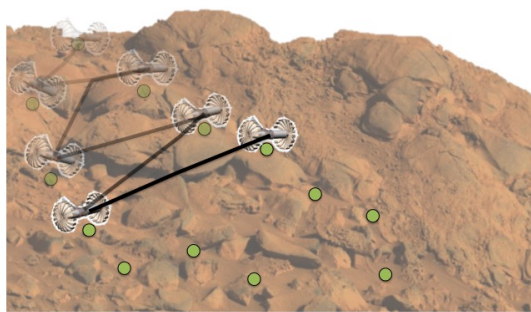


Figure 4: Conceptualized time lapse of coordinated descent of a tethered robot pair. Tether shown in black, computed waypoints in green.

Planning between two waypoints in the full 3D workspace and taking into account the dynamics of the tethered system can be addressed using traditional sampling-based motion planning methods, which have been successfully applied to solve similarly high dimensional problems [9]. The typical complaint with these methods, however, is the required time and computation required to randomly sample enough points to converge to a solution. Considering that we require our methods to be able to re-plan in a variety of situations, a motivating desire is to decrease the amount of time required to find solutions while still addressing this problem in its full state space.

Several techniques can be drawn upon in such a scenario. The first set of approaches involve biasing the sampling of states in ways that utilize our in-depth knowledge of the problem we desire to solve. For example, by computing the "most stable" support position of the stabilizing rover (i.e., perpendicular to the current position of the exploratory rover) and biasing our sampling toward samples that lie in this space. We would propose to additionally explore whether or not it is effective to solve this problem in a 2D projection first, defining a mapping from 2D space back to the full state space and using this solution

to bias samples in the full space.

Additionally, we would explore the possibility that by dissecting the problem into multiple subproblem manifolds we can achieve reliable solutions much faster than in the full space. This has been achieved through use of machine learning techniques, where the authors train a model to learn the important sub-manifolds of a particular system's state space while also learning to predict which static configurations for other state dimensions would be most effective for solving the current problem [10].



---

**References**

- [1] M. Krishna, J. Bares, and E. Mutschler, “Tethering System Design for Dante II,” *Proceedings of the IEEE*, pp. 1100–1105, 1997.
- [2] J. E. Bares, “Dante II: Technical Description, Results, and Lessons Learned,” *The International Journal of Robotics Research*, vol. 18, no. 7, pp. 621–649, 1999.
- [3] I. A. D. Nesnas, P. Abad-Manterola, J. A. Edlund, and J. W. Burdick, “Axel mobility platform for steep terrain excursions and sampling on planetary surfaces,” *IEEE Aerospace Conference Proceedings*, 2008.
- [4] M. Bibuli, M. Caccia, and L. Lapierre, “Path-following algorithms and experiments for an autonomous surface vehicle,” *IFAC Proceedings Volumes (IFAC-PapersOnline)*, vol. 7, no. PART 1, pp. 81–86, 2007.
- [5] S. Hert and V. Lumelsky, “The ties that bind: Motion planning for multiple tethered robots,” *Robotics and Autonomous Systems*, vol. 17, no. 3, pp. 187–215, 1996.
- [6] J. Hershberger and J. Snoeyink, “Computing minimum length paths of a given homotopy class,” *Computational geometry*, vol. 4, no. 2, pp. 63–97, 1994.
- [7] P. Abad-Manterola, I. A. D. Nesnas, and J. W. Burdick, “Motion planning on steep terrain for the tethered axel rover,” *Proceedings - IEEE International Conference on Robotics and Automation*, pp. 4188–4195, 2011.
- [8] M. M. Tanner, J. W. Burdick, and I. A. D. Nesnas, “Online motion planning for tethered robots in extreme terrain,” in *ICRA*, 2013.
- [9] Y. Li, Z. Littlefield, and K. E. Bekris, “Asymptotically optimal sampling-based kinodynamic planning,” *International Journal of Robotics Research (IJRR)*, vol. 35, pp. 528–564, 04/2016 2016.
- [10] J. Rowekamper, G. D. Tipaldi, and W. Burgard, “Learning to guide random tree planners in high dimensional spaces,” *IEEE International Conference on Intelligent Robots and Systems*, pp. 1752–1757, 2013.