

```
import numpy as np
```

```
class Convolution1d :
```

```
    def __init__(self, filt) :
```

```
        self.__filt = filt
```

```
        self.__r = filt.size
```

```
        self.T = TransposedConvolution1d(self.__filt)
```

```
    def __matmul__(self, vector) :
```

```
        r, n = self.__r, vector.size
```

```
        return np.asarray([np.sum(self.__filt*vector[i:i+r]) for i in range(n-r+1)]) # IMPLEMENT THIS
```

```
class TransposedConvolution1d :
```

```
# Transpose of 1-dimensional convolution operator used for the
```

```
# transpose-convolution operation  $A.T@(\dots)$ 
```

```
    def __init__(self, filt) :
```

```
        self.__filt = filt
```

```
        self.__r = filt.size
```

```
    def __matmul__(self, vector) :
```

```
        r = self.__r
```

```
        n = vector.size + r - 1
```

```
        flip_filt = self.__filt[::-1]
```

```
        return np.asarray([np.sum(flip_filt[np.maximum(0,r-1-i):min(n-i,r)]  
                                *vector[np.maximum(0,i+1-r):min(i+1,n-r+1)]) for i in range(n)]) # IMPLEMENT THIS
```

```
def huber_loss(x) :
```

```
    return np.sum( (1/2)*(x**2)*(np.abs(x)<=1) + (np.sign(x)*x-1/2)*(np.abs(x)>1) )
```

```
def huber_grad(x) :
```

```
    return x*(np.abs(x)<=1) + np.sign(x)*(np.abs(x)>1)
```

```
r, n, lam = 3, 20, 0.1
```

```
np.random.seed(0)
```

```
k = np.random.randn(r)
```

```
b = np.random.randn(n-r+1)
```

```
A = Convolution1d(k)
```

```
#from scipy.linalg import circulant
```

```
#A = circulant(np.concatenate((np.flip(k),np.zeros(n-r))))[r-1:,:]
```

```
x = np.zeros(n)
```

```
alpha = 0.01
```

```
for _ in range(100) :
```

```
    x = x - alpha*(A.T@(huber_grad(A@x-b))+lam*x)
```

```
print(huber_loss(A@x-b)+0.5*lam*np.linalg.norm(x)**2)
```

Result

```
~ python conv1D.py  
0.4587586843129764
```