

```
import numpy as np
import matplotlib.pyplot as plt
```

```
np.seterr(invalid='ignore', over='ignore') # suppress warning caused by division by inf
```

```
def f(x):
    return 1/(1 + np.exp(3*(x-3))) * 10 * x**2 + 1 / (1 + np.exp(-3*(x-3))) * (0.5*(x-10)**2 + 50)
```

```
def fprime(x):
    return 1 / (1 + np.exp((-3)*(x-3))) * (x-10) + 1/(1 + np.exp(3*(x-3))) * 20 * x + (3* np.exp(9))/(np.exp(9)-1.5)
```

```
x = np.linspace(-5,20,100)
```

```
## plot all
```

```
fig, axs = plt.subplots(1, 4, figsize = (16,4))
```

```
for ax in axs:
```

```
    ax.plot(x,f(x), 'k')
```

```
max_iter = 400
```

```
alpha = [0.01, 0.01, 0.3, 4]
```

```
color = ['g', 'r', 'g', 'g']
```

```
## fixing seed
```

```
np.random.seed(13)
```

```
for i in range(4):
```

```
    x = np.random.uniform(-5,20)
```

```
    x=1
```

```
    axs[i].set_title(f'alpha = {alpha[i]}')
```

```
    axs[i].scatter(x,f(x), alpha=1, c=color[i], label = f'initial_x= {x:.1f}')
```

```
    ## iteration (GD)
```

```
    for _ in range(max_iter):
```

```
        x += -alpha[i]*fprime(x)
```

```
        axs[i].scatter(x,f(x), alpha=0.4, c='b')
```

```
    axs[i].legend()
```

```
plt.savefig('GD.png')
```

```
plt.show()
```

# Result

