```
import numpy as np
import matplotlib.pyplot as plt
N = 30
np.random.seed(0)
X = np.random.randn(2,N)
y = np.sign(X[0,:]**2+X[1,:]**2 -0.7)
theta = 0.5
c, s = np.cos(theta), np.sin(theta)
X = np.array ([[c, -s], [s, c]])@X
X = X + np.array([[1],[1]])
## initialize weight
Theta = np.random.randn(5)
## make new data
X_{kernel} = []
for p in X.T:
  row = [1]
  row += [p[0],p[0]**2,p[1],p[1]**2]
  X_kernel.append(row)
X_{kernel} = np.array(X_{kernel})
## draw initial bound
xx = np.linspace(-4, 4, 1024)
yy = np.linspace(-4, 4, 1024)
xx, yy = np.meshgrid(xx, yy)
w = Theta[:]
Z = w[0] + (w[1] * xx + w[2] * xx**2) + (w[3] * yy + w[4] * yy**2)
plt.contour(xx, yy, Z, 0, colors='k',)
## SGD with SVM
def calculate loss(x,y,theta):
  return np.average(np.max( 1-y*(x@theta) , 0)) + lamb*np.sum(theta**2)
max_iter = 50000
Ir = 0.01
lamb = 0.0001
## store loss each iteration
loss = []
## training
for i in range(max_iter):
  # choose random 1 data
  index = np.random.randint(0,N)
  # just temporary instance
  val = y[index]*X_kernel[index]@Theta
```

```
if val >= 1: gradient = 0
  else: gradient = -y[index]*X_kernel[index]
  # regularization part
  gradient += 2*lamb*Theta
  loss.append(calculate_loss(X_kernel,y,Theta))
  Theta -= Ir*gradient
w = Theta[:]
Z = w[0] + (w[1] * xx + w[2] * xx**2) + (w[3] * yy + w[4] * yy**2)
plt.contour(xx, yy, Z, 0, )
# plot the points
plt.scatter(X[0][y>0], X[1][y>0], c='r')
plt.scatter(X[0][y<0], X[1][y<0], c='b')
box1 = {'boxstyle': 'round',
     'ec': (0, 0, 0),
     'fc': (1, 1, 1)}
box2 = {'boxstyle': 'round',
     'ec': (0, 0.5, 0),
     'fc': (1, 1, 1)}
plt.text(-3.8,3.5, 'black line: initial weight', bbox=box1)
plt.text(-3.8,3, f'green line: {max_iter} iter later', bbox=box2)
plt.savefig('p3_visualization.png')
plt.show()
```

