Assignment 2

1. Writen: Understanding word 2 vec

(a) 
$$-\sum_{w \in bab} y_w \log(\hat{y}_w) = -y_w \log(\hat{y}_{w_0}) - \dots - y_o \log(\hat{y}_o) - \dots - y_w \log(\hat{y}_{w_h}) = -\log(\hat{y}_o)$$

(b) 
$$J_{\text{naive-softmax}}(V_c, 0, U)$$

$$= -\log P(O=o \mid C=c)$$

$$= -\log\left(\frac{\exp(u_o^T V_c)}{\sum_{\mathbf{w} \in \mathbf{w}_{rob}} \exp(u_{\mathbf{w}}^T V_c)}\right)$$

$$\frac{\partial J}{\partial V_c} = -U_o + \frac{1}{\text{Eexp(U_w^TV_c)}} \frac{\partial}{\partial V_c} \frac{\sum_{x} exp(U_x^TV_c)}{\sum_{x} exp(U_x^TV_c)}$$

$$= -u_o + \frac{1}{\sum exp(u_w^T V_c)} \sum_{x} u_x \cdot exp(u_x^T V_c)$$

$$= -u_0 + \stackrel{=}{\underset{\sim}{=}} u_x \cdot \frac{\exp(u_x^T V_c)}{\underset{\sim}{\underset{\sim}{=}} \exp(u_\omega^T V_c)}$$

$$= -U^{\mathsf{T}} y + U^{\mathsf{T}} \hat{y}$$

$$= U^{\mathsf{T}}(\hat{\mathcal{G}} - \mathsf{y})$$

(C) When 
$$w=0$$
,

$$\frac{\partial J}{\partial u_w} = -V_c + \frac{1}{Zep(u_w^T V_c)} exp(u_o^T V_c) V_c$$

$$= - V_c + \mathcal{G} \cdot V_c$$

$$=(\hat{y}_0-1)\cdot V_c$$

when 
$$w \neq 0$$
,

$$= \frac{1}{\sum e^{x} p(u_{x}^{T} v_{c})} \cdot \sum_{x \neq 0} e^{x} p(u_{x}^{T} v_{c}) \cdot v_{c}^{T}$$

$$= \sum_{x \neq 0} \sum_{w} e_{x} e_{x} u_{x}^{T} u_{x}^{T} \cdot v_{c}^{T}$$

$$= \left(\sum_{x \neq 0} y_{x}^{T}\right) \cdot v_{c}^{T}, \quad \text{if } w = 0$$

$$\left(\sum_{x \neq 0} y_{x}^{T}\right) \cdot v_{c}^{T}, \quad \text{otherwise}$$

$$= \left(\widehat{g} - y\right) \cdot v_{c}^{T}$$

$$(d) \quad \mathcal{S}(x) = \frac{1}{1 + e^{-x}}$$

$$= \left(1 + e^{-x}\right)^{-2} \cdot \frac{\partial}{\partial x} \left(1 + e^{-x}\right)$$

$$= -\left(1 + e^{-x}\right)^{-2} \cdot \left(-e^{-x}\right)$$

$$= \frac{e^{-x}}{(1 + e^{-x})^{2}}$$

$$= \frac{e^{-x}}{(1 + e^{$$

