cs805 Assignment 1

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Abstract

This assignment is written in literate programming style, generated by noweb, rendered by LaTex, and compiled by clang++ with c++ 11 standard.

1 Question 1

Let n be a 3 tuple vector, and given that it is along V1. It is trivial that we can imply:

$$n = \frac{V1}{[|V1|, |V1|, |V1|]}$$

where $|V1| = \sqrt{V1_x^2 + V1_y^2 + V1_z^2}$

Thus n is now known.

By the definition of cross product, denoted as \times here, knowning that V1 and V2 is non-collinear, we can also derive:

$$u = \frac{V2 \times V1}{[|V2 \times V1|, |V2 \times V1|, |V2 \times V1|]}$$

Finally, it is also trivial that:

$$v = n \times u$$

2 Question 2

According to the requirement, we need a function that gets the new coordination U, V, N from our two vectors.

First, assuming we have the function already. Thus giving it two points, our function will get the U, V, N from them.

```
<<src/main.cpp>>=
#include <iostream>
#include <typeinfo>//debugging only
#include "util.h"
int main () {
 Point V1;
  decltype(V1) V2;// V2 is of same type of V1
  V1 = \{0,0,1000\};
  V2 = \{0,1,1\};
  auto uvn = get_uvn(V1, V2);// compiler will replace 'auto' with the right type
  for (auto point : uvn) {//for each point in uvn
    for (auto num : point) {//for each number in point
      std::cout<<num<<',';
    std::cout<<std::endl;
  }
  return 0;
}
I use a header file for typedefs and function declarations for more readable
code.
<<src/util.h>>=
#ifndef POINTS_HPP
#define POINTS_HPP
```

```
#include <tr1/array>
typedef std::tr1::array<float, 3> Point;
typedef std::tr1::array<Point, 3> UVN;
UVN get_uvn(Point V1, Point V2);
float get_length(Point);
Point cross_product(Point, Point);
Point normalize(Point);
#endif
Finally, here is the function.
<<src/util.cpp>>=
#include "util.h"
#include <math.h>
//get u,v,n from two non-collinear vectors
UVN get_uvn(Point V1, Point V2) {
  //get n, which is just normalized V1
 Point n = normalize(V1);
  //get u, which is normalized V2 x V1
  Point u = normalize(cross_product(V2, V1));
  //get v, which is normalized n x u
  Point v = normalize(cross_product(n, u));
 return {u,v,n};
}
//normalize a point
Point normalize(Point x) {
  return { x[0]/get_length(x),
           x[1]/get_length(x),
           x[2]/get_length(x) };
}
//calculates cross product of two points
Point cross_product(Point x, Point y) {
```

Furthermore, this is the command to link these files. Notice that I am using -std=c++11 flag to enable c++ 11 features. The output binary executable is bin/get_uvn_test

```
<<compile.sh>>=
clang++ -std=c++11 -o bin/get_uvn_test src/main.cpp src/util.cpp
@
```

3 Question 3

3.1 part a

By definition of matrix multiplication,

$$T \times T^{-1} =$$

$$\begin{bmatrix} 1+0+0+0&0&0+0+0&0&0+0+0&VRP_x+0+0+-VRP_x\\0+0+0+0&0&0+1+0+0&0+0+0&0+VRP_y+0+-VRP_y\\0+0+0+0&0&0+0+0&0&0+0+1+0&0+0+VRP_z+-VRP_z\\0+0+0+0&0&0+0+0&0&0+0+0+0&0&0+0+1 \end{bmatrix} =$$

$$\begin{bmatrix} 1&0&0&0\\0&1&0&0\\0&0&1&0\\0&0&0&1 \end{bmatrix} = I$$

It is also trivial that any n-tuple vector VRP in n-demensional space will fall into this pattern.

3.2 part b

Similarly, by definition of matrix multiplication,

$$R \times R^{-1} =$$

$$\begin{bmatrix} u_x^2 + u_y^2 + u_z^2 & u_x \times v_x + u_y \times v_y + u_z \times v_y & u_x \times n_x + u_y \times n_y + u_z \times n_y & 0 \\ v_x \times u_x + v_y \times u_y + v_z \times u_z & v_x^2 + v_y^2 + v_z^2 & v_x \times n_x + v_y \times n_y + v_z \times n_z & 0 \end{bmatrix}$$