cs805 Assignment 1

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Abstract

This assignment is written in literate programming style, generated by noweb, rendered by LaTex, and compiled by clang++ with c++ 11 standard.

1 Question 1

Let n be a 3 tuple vector, and given that it is along $V1$. It is trivial that we can imply:

$$n = \frac{V1}{[|V1|, |V1|, |V1|]}$$

where $|V1| = \sqrt{V1_x^2 + V1_y^2 + V1_z^2}$

Thus n is now known.

By the definition of cross product, denoted as $\times$ here, knowning that $V1$ and $V2$ is non-collinear, we can also derive:

$$u = \frac{V2 \times V1}{[|V2 \times V1|, |V2 \times V1|, |V2 \times V1|]}$$

Finally, it is also trivial that:

$$v = n \times u$$

2 Question 2

According to the requirement, we need a function that gets the new coordination U, V, N from our two vectors.

First, assuming we have the function already. Thus giving it two points, our function will get the U, V, N from them.

```
<<src/main.cpp>>=
#include <iostream>
#include <typeinfo>//debugging only
#include "util.h"

int main () {
  Point V1;
  decltype(V1) V2;// V2 is of same type of V1

  V1 = {0,0,1000};
  V2 = {0,1,1};

  auto uvn = get_uvn(V1, V2);// compiler will replace 'auto' with the right type

  for (auto point : uvn) {//for each point in uvn
    for (auto num : point) {//for each number in point
      std::cout<<num<<',';
    }
    std::cout<<std::endl;
  }

  return 0;
}
@
```

I use a header file for typedefs and function declarations for more readable code.

```
<<src/util.h>>=
#ifndef POINTS_HPP
#define POINTS_HPP
```

```
#include <tr1/array>
typedef std::tr1::array<float, 3> Point;
typedef std::tr1::array<Point, 3> UVN;
UVN get_uvn(Point V1, Point V2);
float get_length(Point);
Point cross_product(Point, Point);
Point normalize(Point);
#endif
@
```

Finally, here is the function.

```
<<src/util.cpp>>=
#include "util.h"
#include <math.h>

//get u,v,n from two non-collinear vectors
UVN get_uvn(Point V1, Point V2) {
  //get n, which is just normalized V1
  Point n = normalize(V1);

  //get u, which is normalized V2 x V1
  Point u = normalize(cross_product(V2, V1));

  //get v, which is normalized n x u
  Point v = normalize(cross_product(n, u));

  return {u,v,n};
}

//normalize a point
Point normalize(Point x) {
  return { x[0]/get_length(x),
           x[1]/get_length(x),
           x[2]/get_length(x) };
}

//calculates cross product of two points
Point cross_product(Point x, Point y) {
```

```
  return { x[1]*y[2] - x[2]*y[1],
           x[2]*y[0] - x[0]*y[2],
           x[0]*y[1] - x[1]*y[0]};
}

//calculates length of a point
float get_length(Point x) {
  return sqrt(pow(x[0],2)+pow(x[1],2)+pow(x[2],2));
}
@
```

Furthermore, this is the command to link these files. Notice that I am using -std=c++11 flag to enable c++ 11 features. The output binary executable is bin/get_uvn_test

```
<<compile.sh>>=
clang++ -std=c++11 -o bin/get_uvn_test src/main.cpp src/util.cpp
@
```

3 Question 3

3.1 part a

By definition of matrix multiplication,

$$T \times T^{-1} =$$

$$\begin{bmatrix} 1+0+0+0 & 0+0+0+0 & 0+0+0+0 & VRP_x+0+0+-VRP_x \\ 0+0+0+0 & 0+1+0+0 & 0+0+0+0 & 0+VRP_y+0+-VRP_y \\ 0+0+0+0 & 0+0+0+0 & 0+0+1+0 & 0+0+VRP_z+-VRP_z \\ 0+0+0+0 & 0+0+0+0 & 0+0+0+0 & 0+0+0+1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} = I$$

It is also trivial that any n-tuple vector VRP in n-demensional space will fall into this pattern.

3.2 part b

Similarly, by definition of matrix multiplication,

$$R \times R^{-1} =$$

$$] \, [$$