

1 Tapped-C transformer

1.1 Introduction

This code returns the Tapped-c matching network's elements' values:

- Q: the required loaded Q of the resonant circuit
- Xp: either the inductive or capacitive reactance. They are equal at resonance
- Rp: the equivalent shut resistance of the inductor (Ω)
- C1: Tapped-C transformer's C1 capacitor (F)
- C2: Tapped-C transformer's C2 capacitor (F)
- L: Tapped-C transformer's L inductance (H)
- IL_: insertion loss of the network (dB)

For getting the above values, it requires the following inputs:

- fc: center frequency of the wanted resonant circuit (Hz)
- B: bandwidth of the wanted resonant circuit (Hz)
- Rs: source resistance
- RL: load resistance
- Qp: the Q of the inductor

So, the function call is,

```
» [Q,Xp,Rp,C1,C2,L,IL_dB] = tapped_c(fc,B,Rs,RL,Qp);
```

It displays the results in the command window, and it saves them a txt in the same folder it has been executed.

1.2 Example:

Here is an example of a FM band mixer's tapped c transformer:

```
» fc = 98e6;
» B = 20e6;
» Rs = 50;
» RL = 1.5e3;
» Qp = 75;

» [Q,Xp,Rp,C1,C2,L,IL_dB] = tapped_c(fc,B,Rs,RL,Qp);

***** Tapped-C resonant matching network *****
|
| Initial data:
|
| Center frequency (fc): 98.00 MHz
| Bandwidth (B): 20.00 MHz
| Serial resistance (Rs): 50.00  $\Omega$ 
| Load resistance (RL): 1.50 k $\Omega$ 
| Inductor Q at 98.00 MHz (Qp): 75
|
|
| The Tapped-C transformer's characteristic equations are the following:
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$$R_s' = R_s (1 + C_1/C_2) \exp(2) \quad (1)$$

$$C_T = C_1 C_2 / (C_1 + C_2) \quad (2)$$

Where

C_T is the equivalent capacitance that resonates with L

First we clear C_1/C_2 from (1) and we will use (2) in advance to get C_1 and C_2

Let the system:

$$Q_p = R_p / X_p \quad (3)$$

$$Q = R_{\text{total}} / X_p \quad (4)$$

Resolving the proposed system,

$$X_p: 143.06 \, \Omega$$

$$R_p: 10729.59 \, \Omega$$

Knowing that:

$$C_1 = (C_1/C_2) * C_2 \quad (5)$$

$$C_t = C_1 || C_2 \quad (6)$$

Then, solving the system above by replacing (5) in (6),

$$| L : 232.34 \, \text{nH} |$$

$$| C_1 : 62.18 \, \text{pF} |$$

$$| C_2 : 13.89 \, \text{pF} |$$

Finally, we calculate the insertion loss of the network,

$$IL = 20 \log_{10} (V_{L_resonant} / V_{L_noResonant}) \quad (7)$$

Solving (7)...

$$IL = 20 \log_{10} ((Z_L * Z_{c1} * (R_L + R_S)) / (R_L * R_S * Z_L + R_L * R_S * Z_{c1} + R_L * R_S * Z_{c2} + R_L * Z_L * Z_{c1} + R_S * Z_L * Z_{c1} + R_S * Z_L * Z_{c2} + R_L * Z_{c1} * Z_{c2} + Z_L * Z_{c1} * Z_{c2}))$$

$$| IL(\text{dB}) : 8.84 |$$
