

# Break Chocolate Bar into 1x1 pieces

Piece

Input:  $n, m$ , chocolate  $[n][m]$ , squares  $[nm]$  (ref/global)

Output:  $nm$  pieces in squares container; void

if  $n > 1$

$A[\lceil n/2 \rceil][m]$

$B[\lceil n/2 \rceil][m]$

for  $i = 0 \dots n-1$

for  $j = 0 \dots m-1$

if  $i \leq n/2$

$A[i][j] \leftarrow \text{chocolate}[i][j]$

else

$B[i][j] \leftarrow \text{chocolate}[i][j]$

→ exit for

→ exit for; Piece( $n/2, m, A, \text{squares}$ ); Piece( $n/2, m, B, \text{squares}$ );

else if  $m > 1$

$A[n][\lceil m/2 \rceil]$

$B[n][\lceil m/2 \rceil]$

for  $j = 0 \dots m-1$

for  $i = 0 \dots n-1$

if  $j \leq m/2$

$A[i][j] \leftarrow \text{chocolate}[i][j]$

else

$B[i][j] \leftarrow \text{chocolate}[i][j]$

→ exit for

→ exit for; Piece( $n, m/2, A, \text{squares}$ ); Piece( $n, m/2, B, \text{squares}$ );

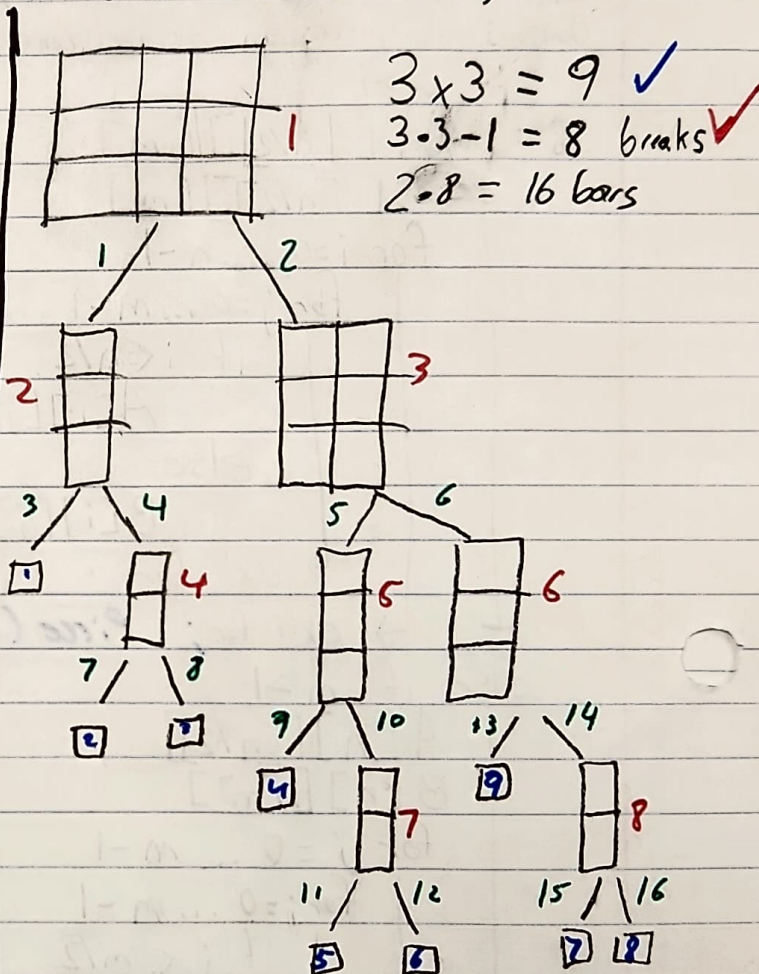
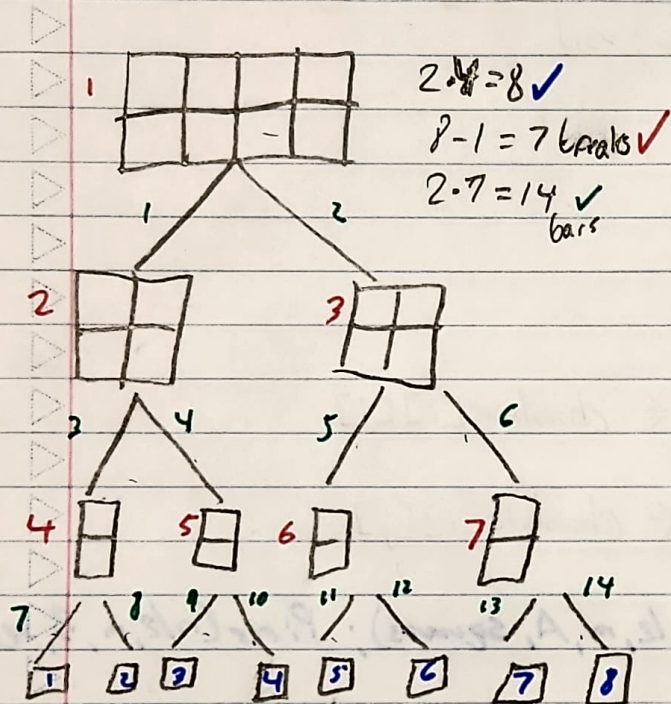
else if  $n = 1 \wedge m = 1$

push chocolate[0][0] onto squares

return



Because every cut yields two pieces, this has the structure of a binary tree / full binary tree



This behavior means # of bars is the same as half the number of edges in a FBT.

$$\text{edges} = 2 \cdot \text{nodes with 2 children}$$

$$\text{bars} = 2 \cdot \text{breaks}$$

# of leaves/squares is always = #nodes with 2 children + 1 (breaks)

$$nm = b + 1$$

$$nm - 1 = b$$

$$2 \cdot 4 = 8$$

$$\begin{array}{r} -1 \\ \hline 7 \text{ breaks} \end{array}$$