455 grmen + 02

f(1) = 2

 $f(n) = n^2 + f(n-1) + n$   $O(n^3)$  because there are 3 for loops nested within each other

 $n^2 + 3n^3 = f(n)$  c = 3  $3n^3 = c \cdot g(n)$ 

 $3n^3+n^2 \geq 3n^3 \quad \forall n \neq n \geq 0$ 

 $n^2 \geq 0$ :. f(n) = c.g(n)

.. c.g(n) is a lower bound on f(n) · S(n) & S(C.n3)

3,3+,2-0  $L_{n^2}=0$ 3n+1=0 47=-3

 $n^2 + 3n^3 = 5(n)$   $g(n) = n^3$  c = 4

 $\frac{3n^3+n^2}{3n^3+n^2} \le 4n^3$ 

3+154 1 < 1 Vn

:. fh) =(9h) 4 ≥0

i. c.g(n) is an upper board on f(n)

: 5(n) E O(n3)

: 56) 6 (n3)

3 For  $2^{n+1} + 2^n$ , every integer constant yields  $c_1 2^n \ge 2^{n+1}$  which satisfies  $O(2^n)$ 

if  $c_2 \le 2$ , then  $a_1^n \le 2^{n+1}$  satisfying  $\Omega(2^n)$   $(c_2^{2n} = 2^{n+1})$  if  $c_2 \in N$  W

So, to generalize:

ant EQ(an) because

b·a<sup>2</sup>  $\geq a^{n+1}$  iff  $b \geq a \rightarrow O(a^n)$ c·a<sup>2</sup>  $\leq a^{n+1}$  iff  $c \leq a \rightarrow \Omega(a^n)$ 

ba² à a ca² ≤ a² · a

ar

ar

ar

ar

Because of this, ant EQ(a")

For each node in the graph, we check for an eage between it and all other nodes & itself. Worst case, all nodes are checked and the graph is complete. See excel work book in repo