

PRINCIPAL COMPONENT ANALYSIS

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Principal Component Analysis (PCA)

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- PCA: Data Analysis Technique

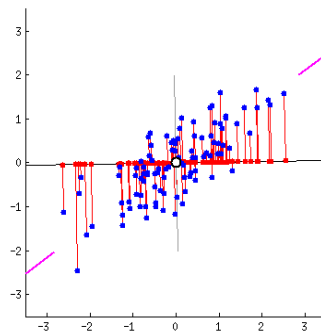
PCA

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PCA

3

- The optimal direction: The direction of maximum variance of the projected data



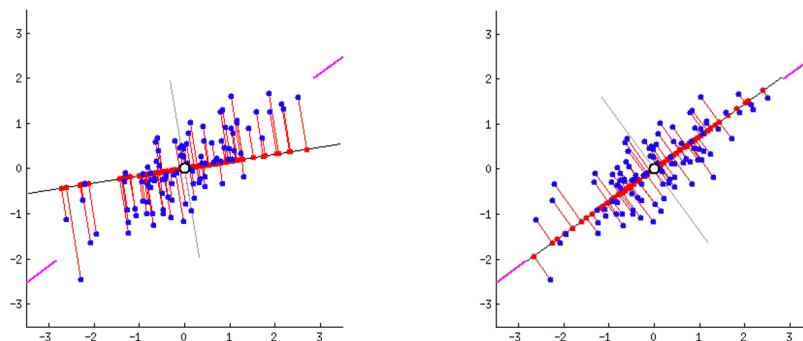
PCA

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PCA

4

- The optimal direction: The direction of maximum variance of the projected data



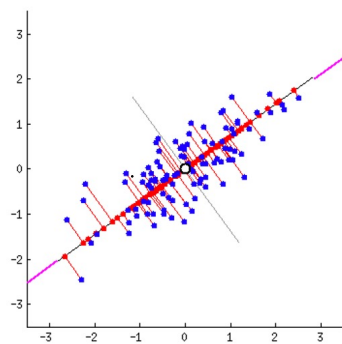
PCA

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PCA

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- The optimal direction: The direction of maximum variance of the projected data



Principal eigenvector of the covariance matrix of the data
 >> Direction of maximum variance of data

Eigenvalue determines the projection variance of the corresponding eigenvector

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PCA: Fundamental Concepts

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- Variance of a random variable fluctuating about its mean value
 - ▣ Average of the square of the fluctuations
- Covariance for a pair of random variables, each fluctuating about its mean value
 - ▣ Average of product of fluctuations
- N random variables: Covariance matrix
 - ▣ N x N symmetric matrix
 - ▣ Diagonal elements are variances of individual random variables

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PCA: Fundamental Concepts

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- Eigenvalues and eigenvectors of a square matrix A satisfy the following

$$Av_i = \lambda_i v_i$$

- Principal eigenvector
 - Eigen vector corresponding to maximal eigenvalue

Principal eigenvector of the covariance matrix of the data >>
Direction of maximum variance of data

Eigenvalue determines the **projection variance** of the corresponding eigenvector

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PCA Example

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- Dataset

$$(1, 1), (2, 2), (3, 3), (4, 4), (5, 5), (6, 6)$$

- Covariance matrix

	Column 1	Column 2
Column 1	2.91666667	
Column 2	2.91666667	2.91666667

- Eigen values

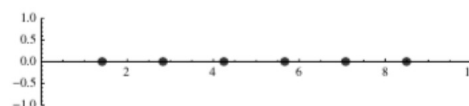
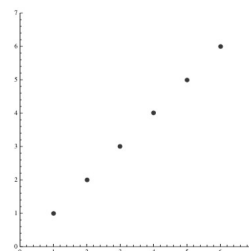
$$\lambda_1 = \frac{2917}{500}$$

- Eigen vectors

$$\lambda_2 = 0$$

$$v_1 = (1, 1)$$

$$v_2 = (-1, 1)$$



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PCA: Applications

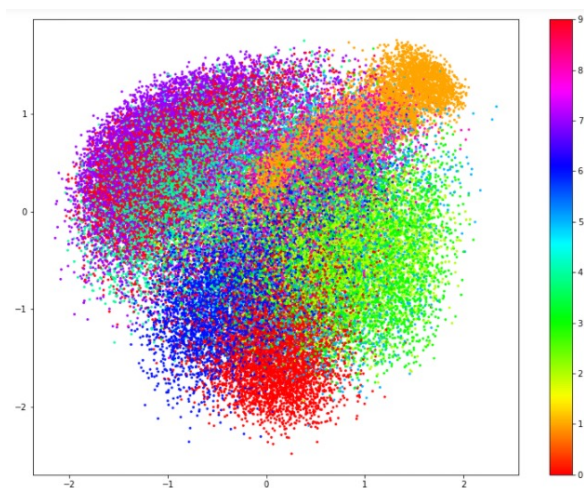
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- General Dimensionality Reduction
 - ▣ Feature vector
- Visualization of High-dimensional Data
 - ▣ Feature space visualization

PCA

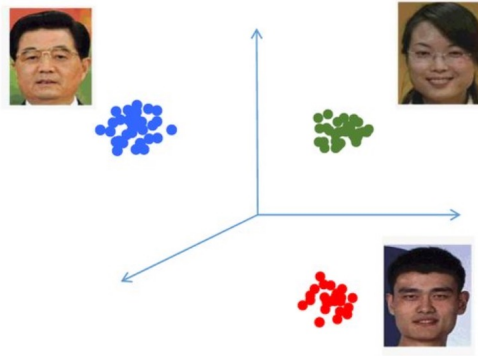
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PCA for Feature Space Visualization



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PCA for Feature Space Visualization



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Thank You!

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