



Log-dynamics of cortical networks

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Yoshiyuki Omura (Toyama Univ)
Milena Carvalho (Univ Sao Paulo)
Vladimir Klinshov (Russian Acad Sci)
Vladimir Nekolkin (Russian Acad Sci)

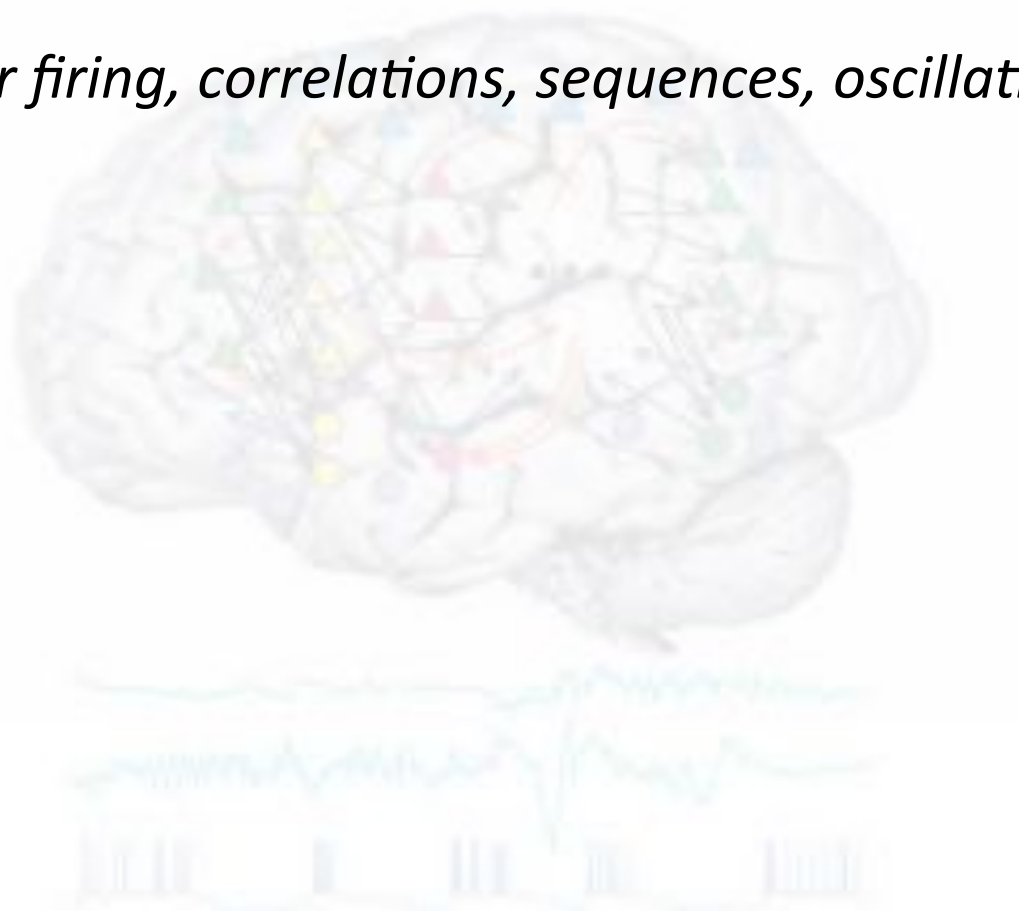
Research talk title

**Preplay and replay emerge in a recurrent
network of two-compartment neurons**

Neural code

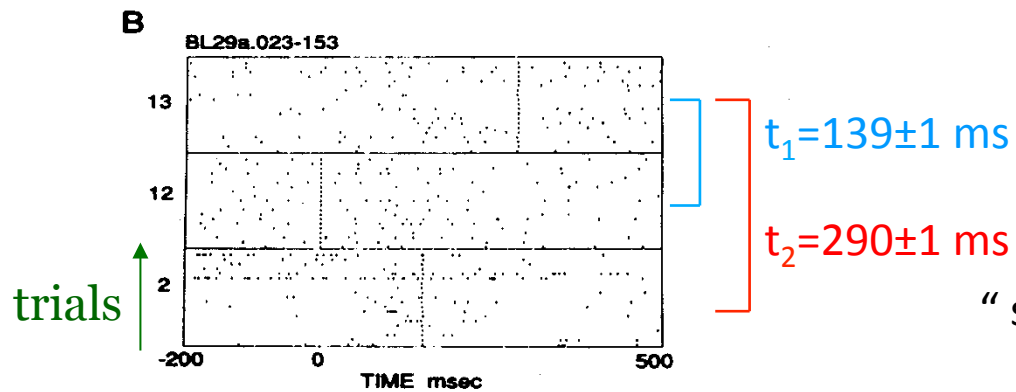
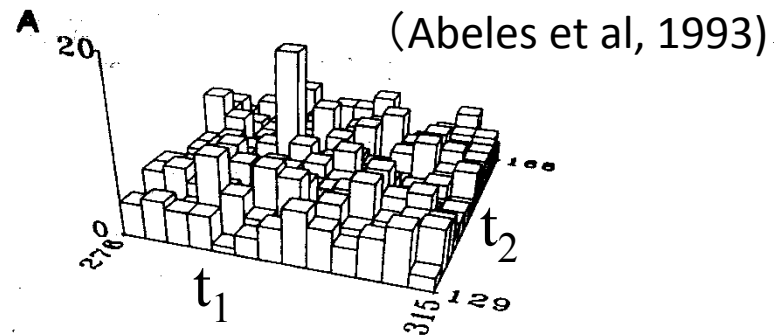
Rate, temporal, or multiplexed?

irregular firing, correlations, sequences, oscillations, ...



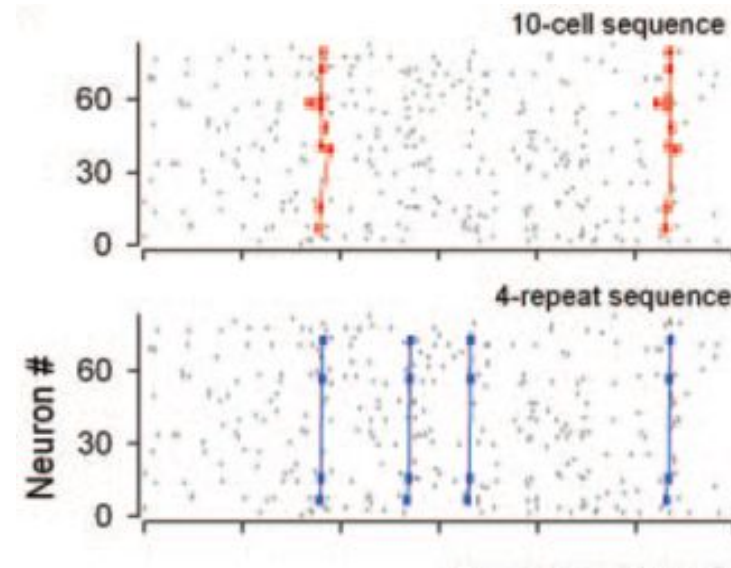
Precise spike sequence

Multiunit recordings from monkey frontal cortex

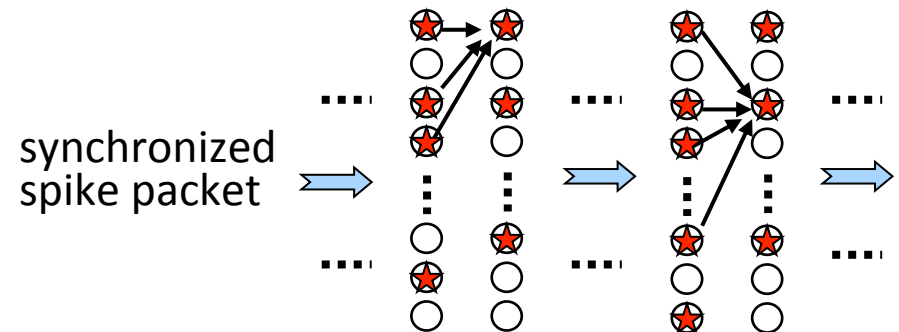


Precisely-timed spike triplets

Cortical songs (Ikegaya et al. 2004)

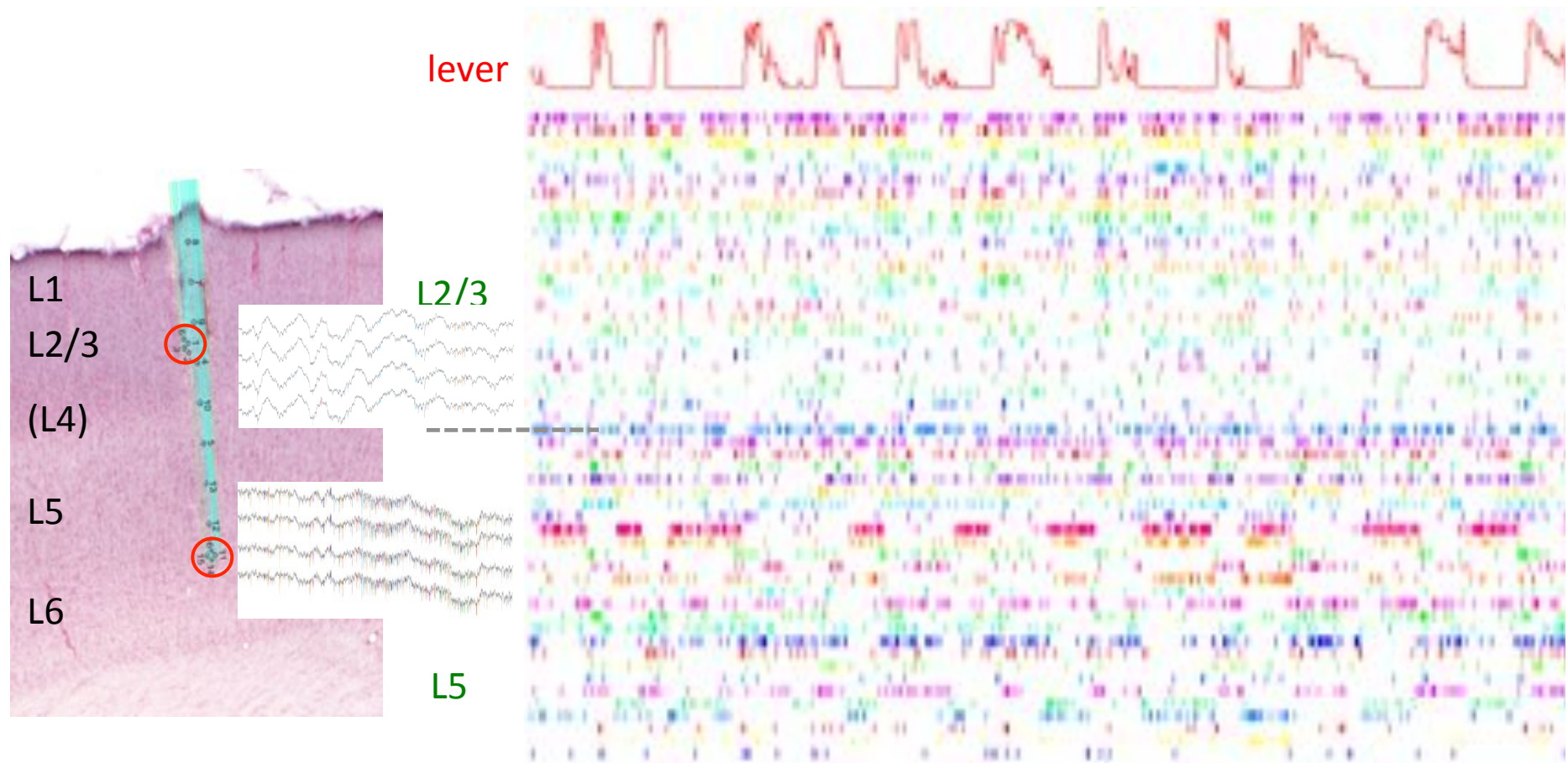


“synfire chain” (Diesmann et al., 1999)



Firing of in vivo cortical neurons is highly irregular

Rat primary motor cortex, spontaneous lever movement task, multiunit recordings (Isomura et al., Nat Neurosci 2009)



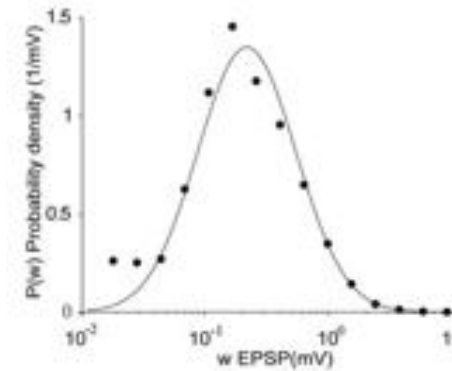
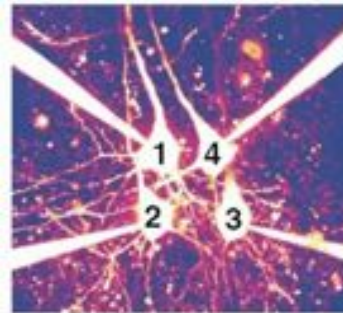
Heavy-tailed EPSP distributions of cortical synapses

Strong-sparse synapses vs. weak-dense synapses

Brain's machinery to generate noise?

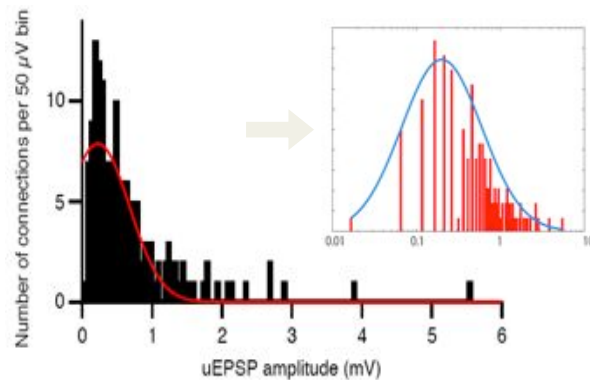
rat visual cortex

Song et al., PLoS Biol (2005)



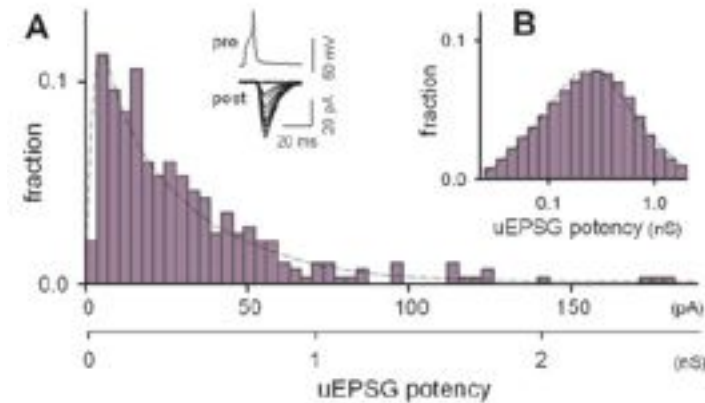
mouse somatosensory cortex

Lefort et al. Neuron (2009)



rat hippocampus

Ikegaya et al., Cereb Cortex (2013)

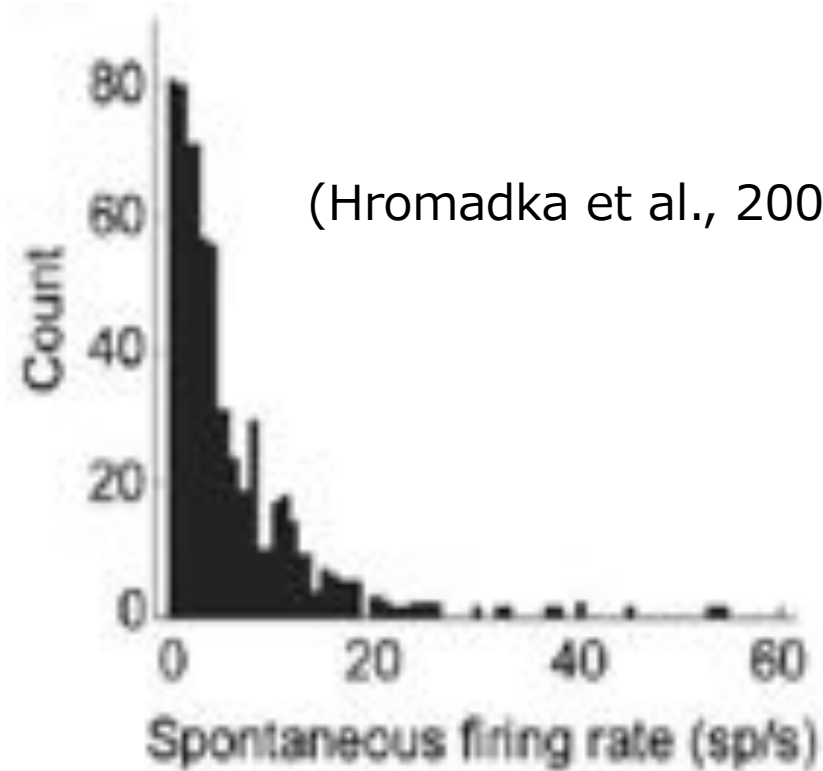


Models of spiking neurons and their networks

1. Spiking neuron models
2. Spontaneous cortical activity
3. A lognormal associative model
4. Synchronous bursting activity in the hippocampus
5. Explore cell assemblies in real data (if time allows)

Q1. Sparse asynchronous irregular states

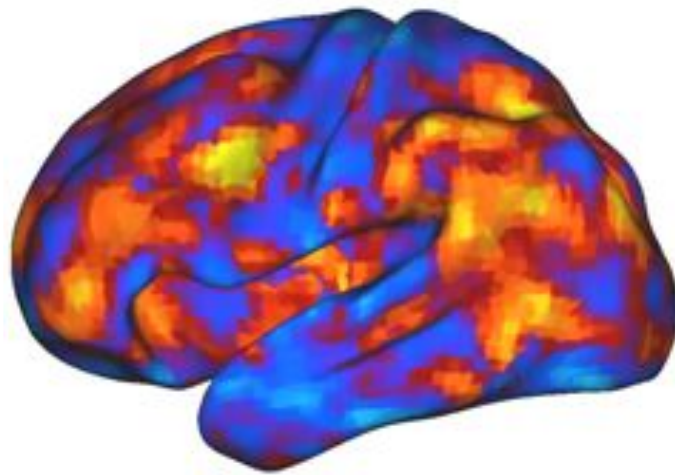
Q2. Sequence vs asynchronous irregular firing



(Hromadka et al., 2008)



Bed 22%
 Park 18%
 Washroom 7%
 Toilet 32%
 Bathroom 29%
 Bus 17%
 Stage 1%
 Airport 4%
 Poolside 2%
 Meeting room 0%



The brain is spontaneously cycling through distributed patterns of activity, which mimic activity patterns associated with sensory, motor, or cognitive events.

Asynchronous sparse irregular firing
(1~2 Hz)

Vincent et al., J Neurophysiol (2006)

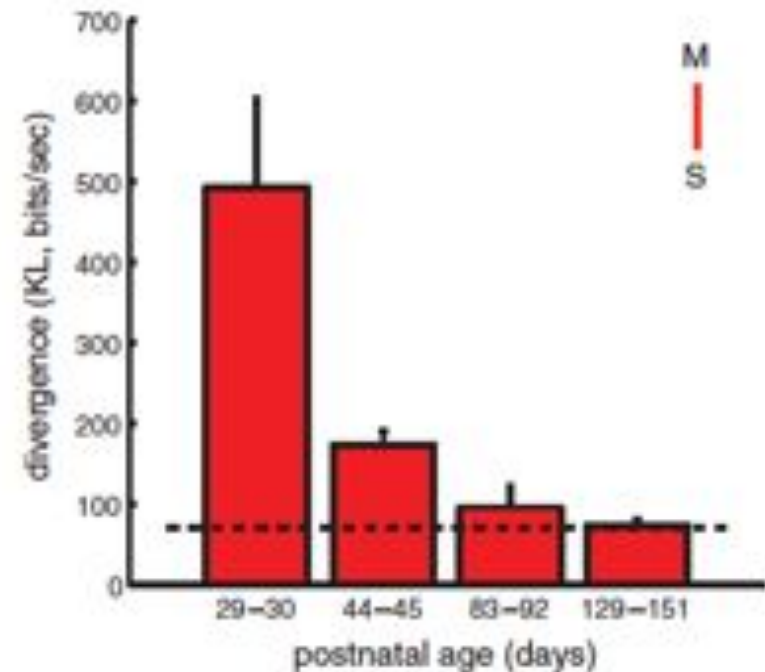
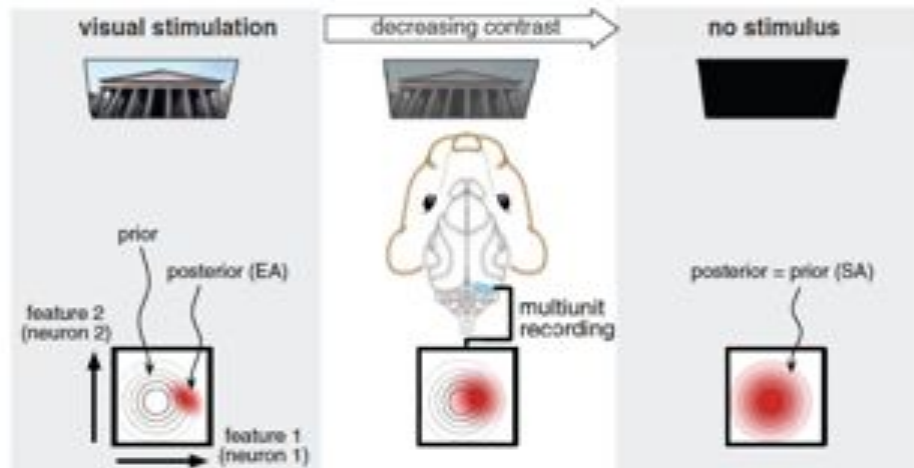
Spontaneous activity gives prior knowledge on external world

Spontaneous Cortical Activity Reveals Hallmarks of an Optimal Internal Model of the Environment

Pietro Berkes,^{1†} Gergő Orbán,^{1,2,3} Máté Lengyel,^{3*} József Fiser^{1,4,5*}

Science 2011

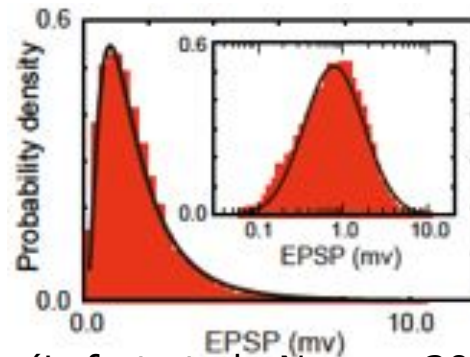
$$\langle P(\text{features} | \text{input}, \text{model}) \rangle_{P(\text{input})} \approx P(\text{features} | \text{model})$$



Asynchronous irregular firing in recurrent networks

(Teramae, Tsubo and Fukai, Sci Rep, 2012)

- 10000 excitatory + 2000 inhibitory LIF neurons



(Lefort et al., Neuron 2009)

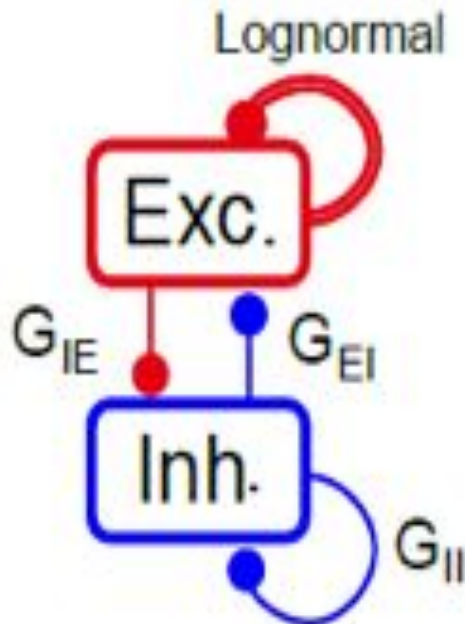
- AMPA synapses

Lognormal weight distribution
for E-E connections

EPSP size-dependent
transmission failure rate

- GABA-A synapses

Gaussian



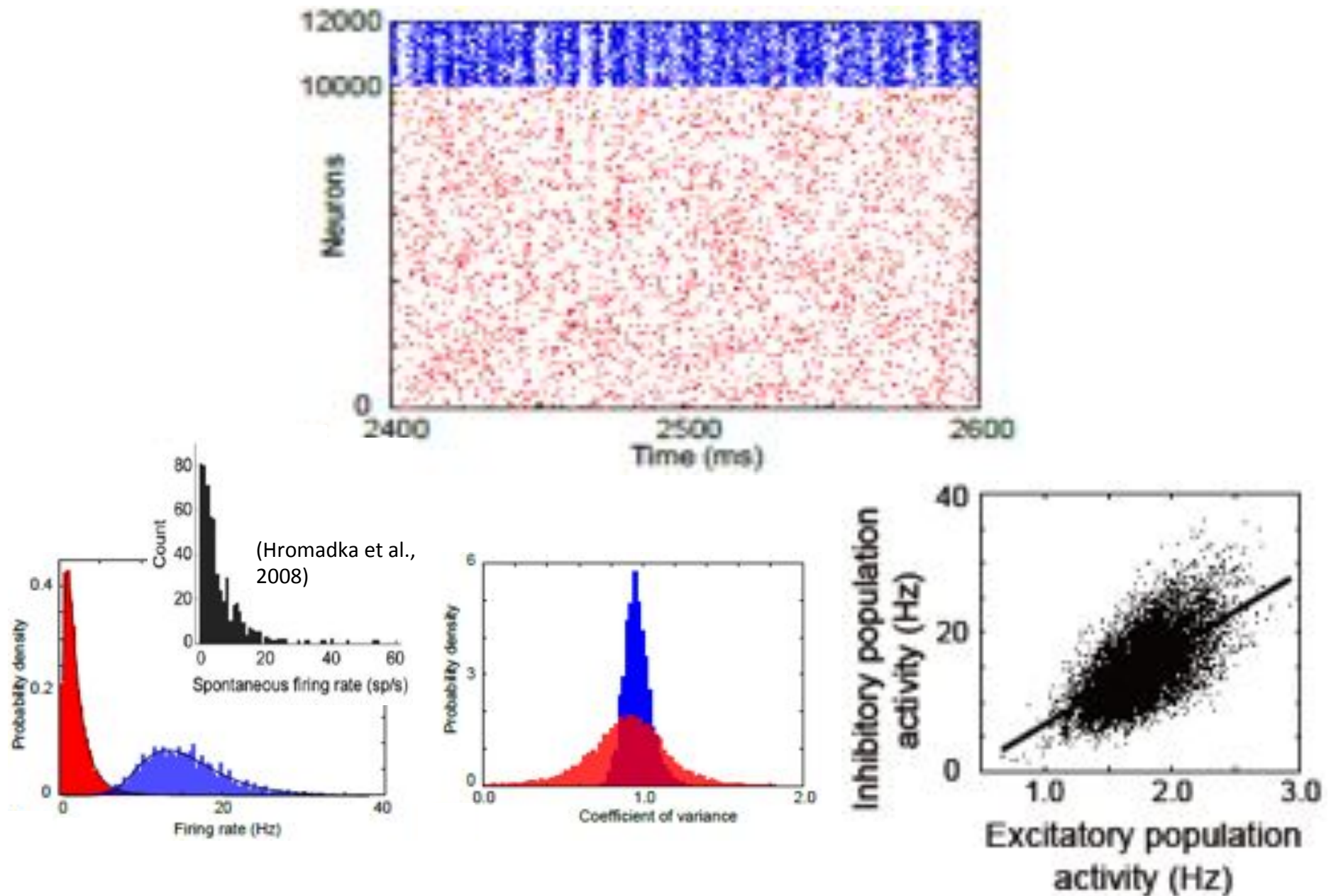
- Transmission delays are 1~3 ms

- No external input

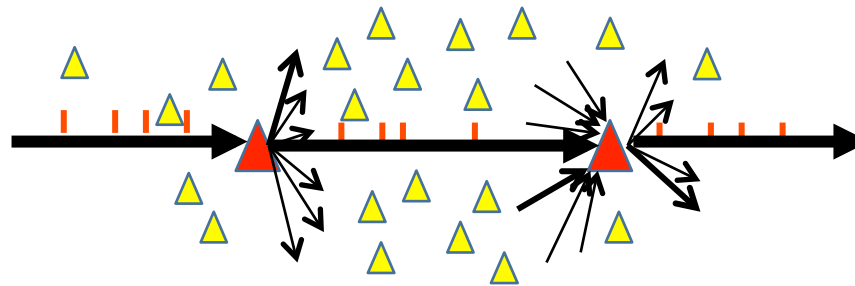
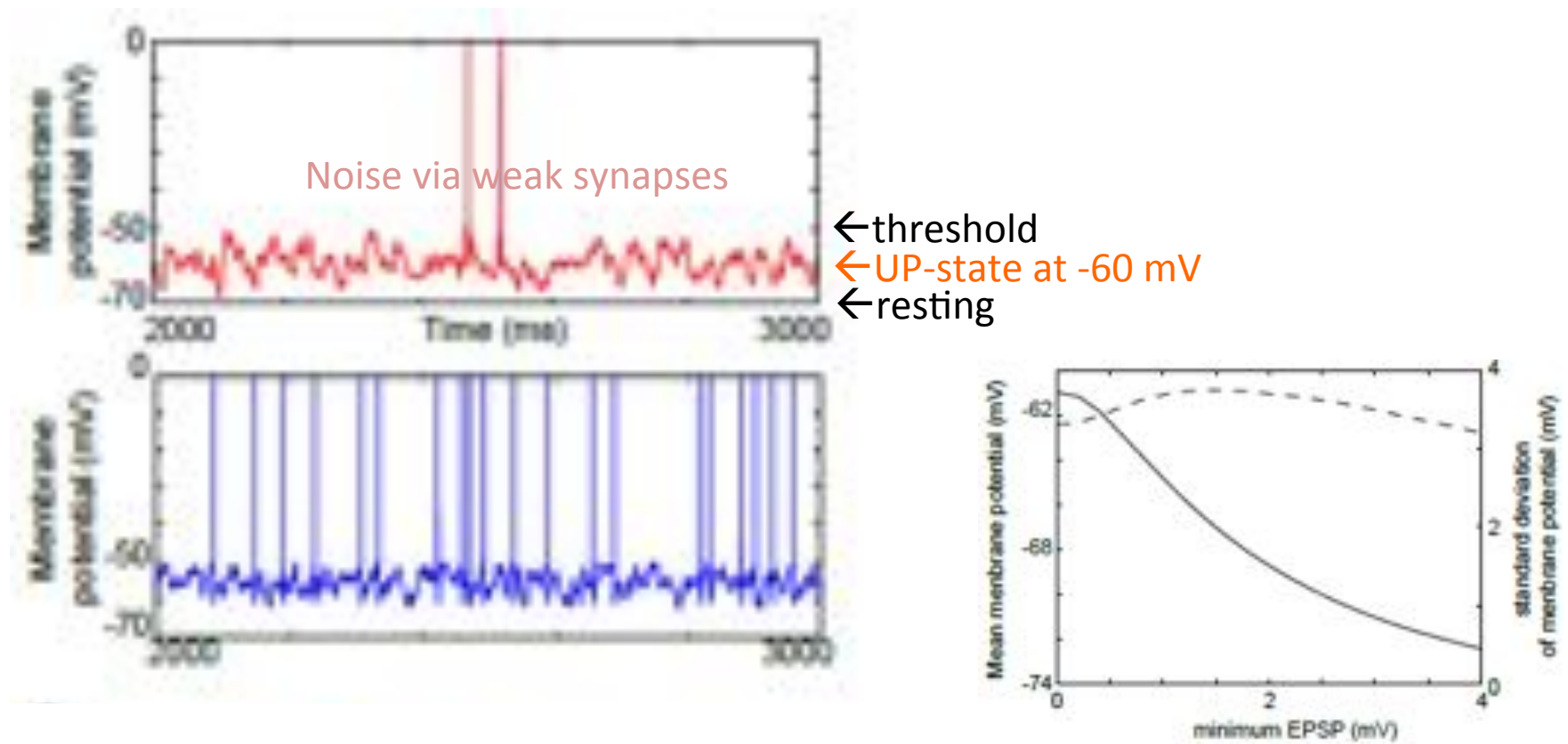


Jun-nosuke Teramae
(-> Osaka Univ)

LogN network generates biologically realistic spontaneous activity

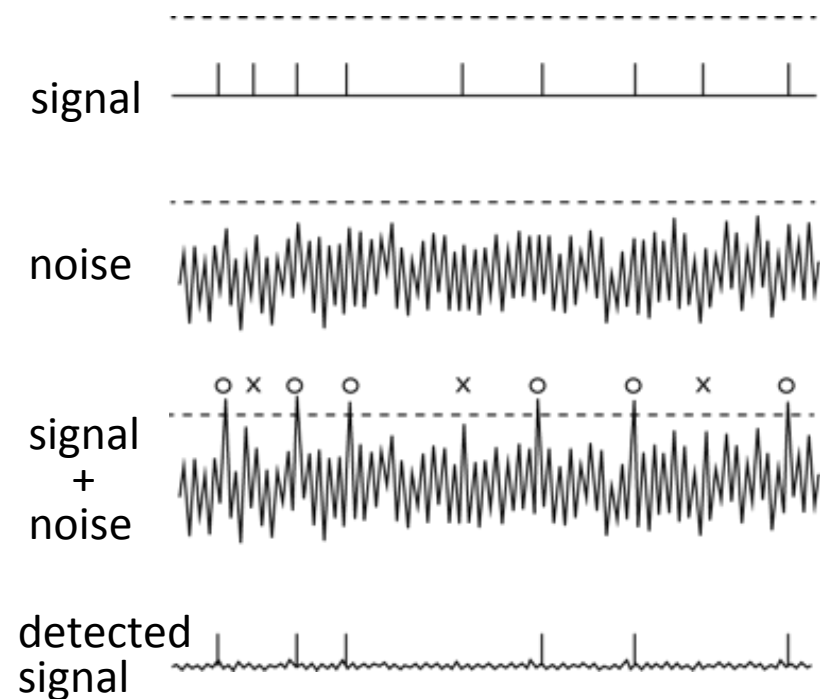
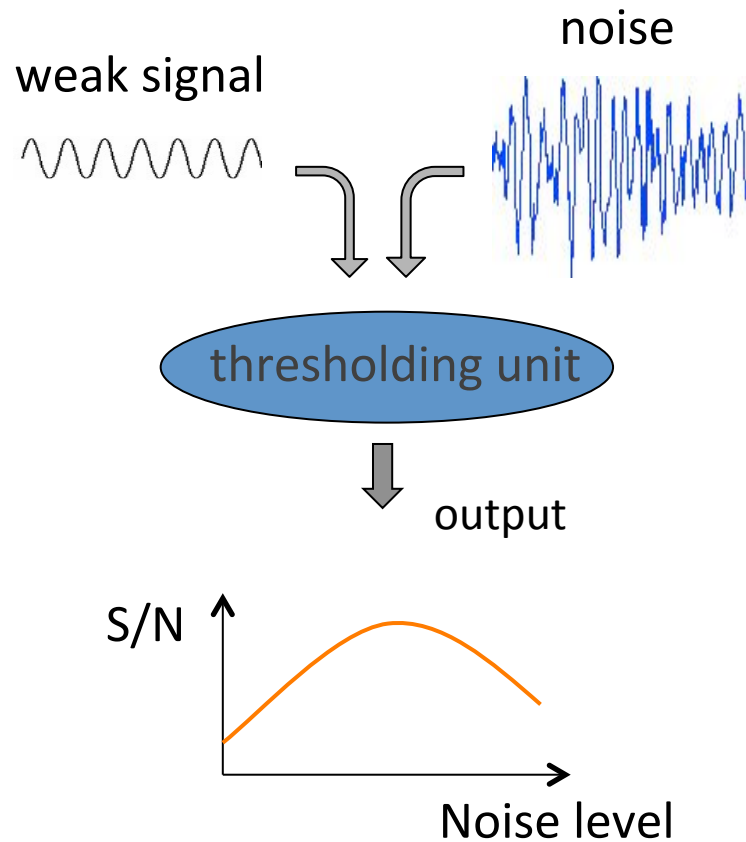


Membrane potential fluctuates around -60 mV



Stochastic resonance (確率共鳴)

Optimal noise helps detection of weak signals

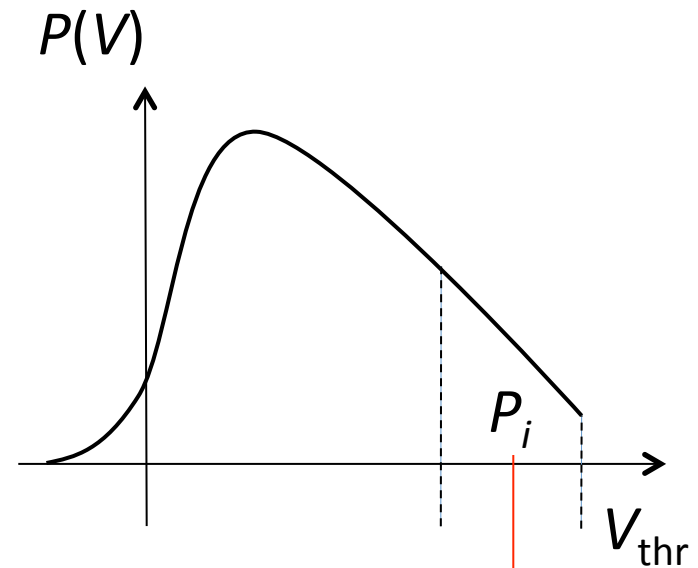
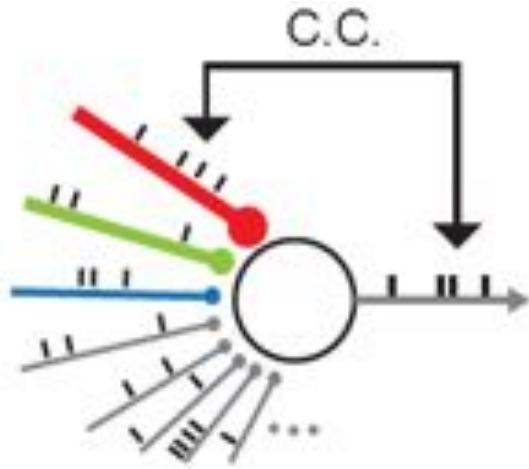


Noise improves our visual perception!



E. Simonotto et al., Phys Rev Lett (1997)

Analysis of spike transmission



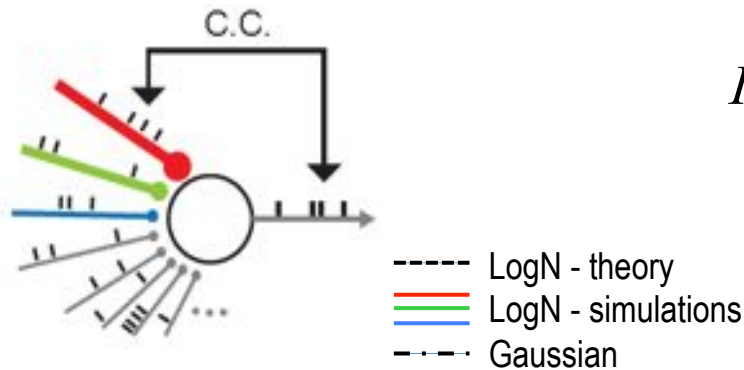
$$C.C. = P_i(x_{out} | x_{i,in}) \sqrt{\frac{r_{i,in}}{r_{out}}}$$

$$P_i(E_i) = \int_{\frac{(V_E - V_L)V_{thr} + \beta E_i V_E}{(V_E - V_L) + \beta E_i}}^{V_{thr}} P(V) dV$$

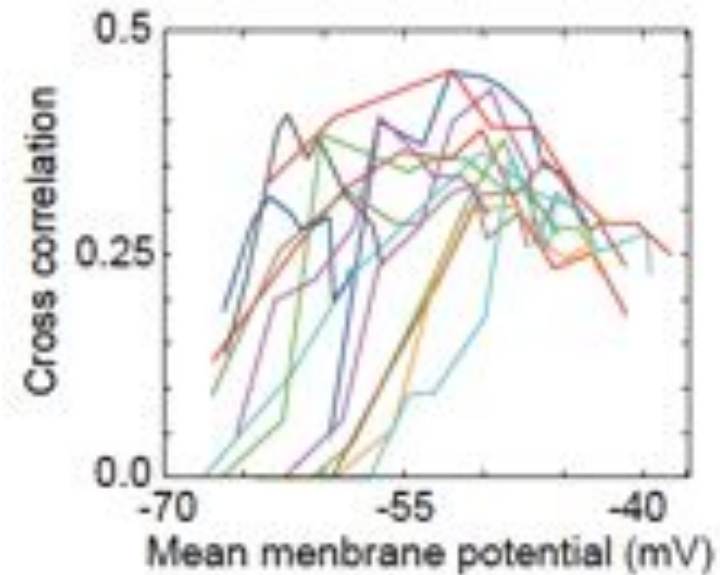
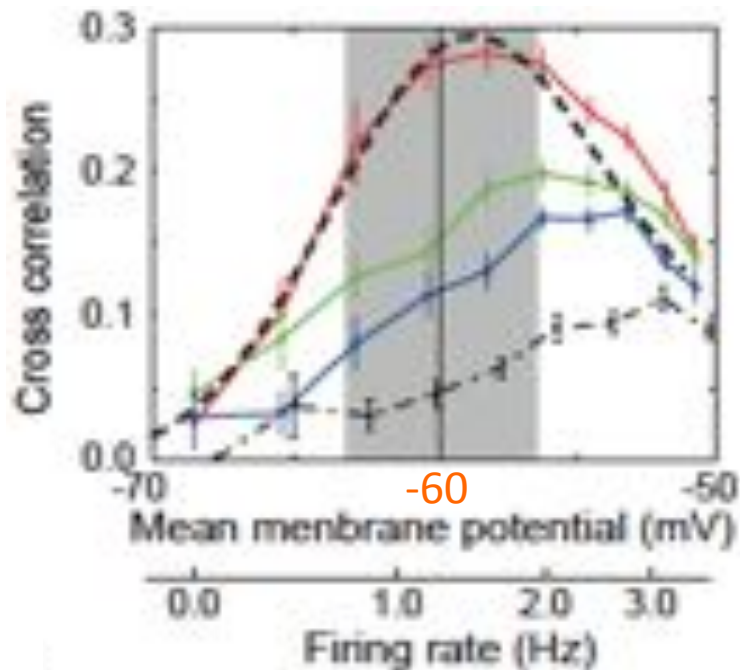
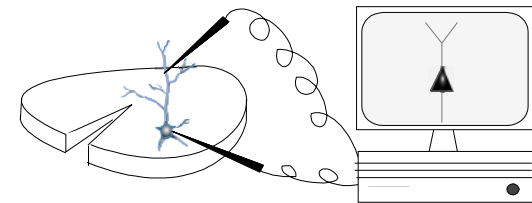
E_i = EPSP amplitude of input synapse

Lognormal EPSP distribution generates *optimal internal* noise in recurrent circuits

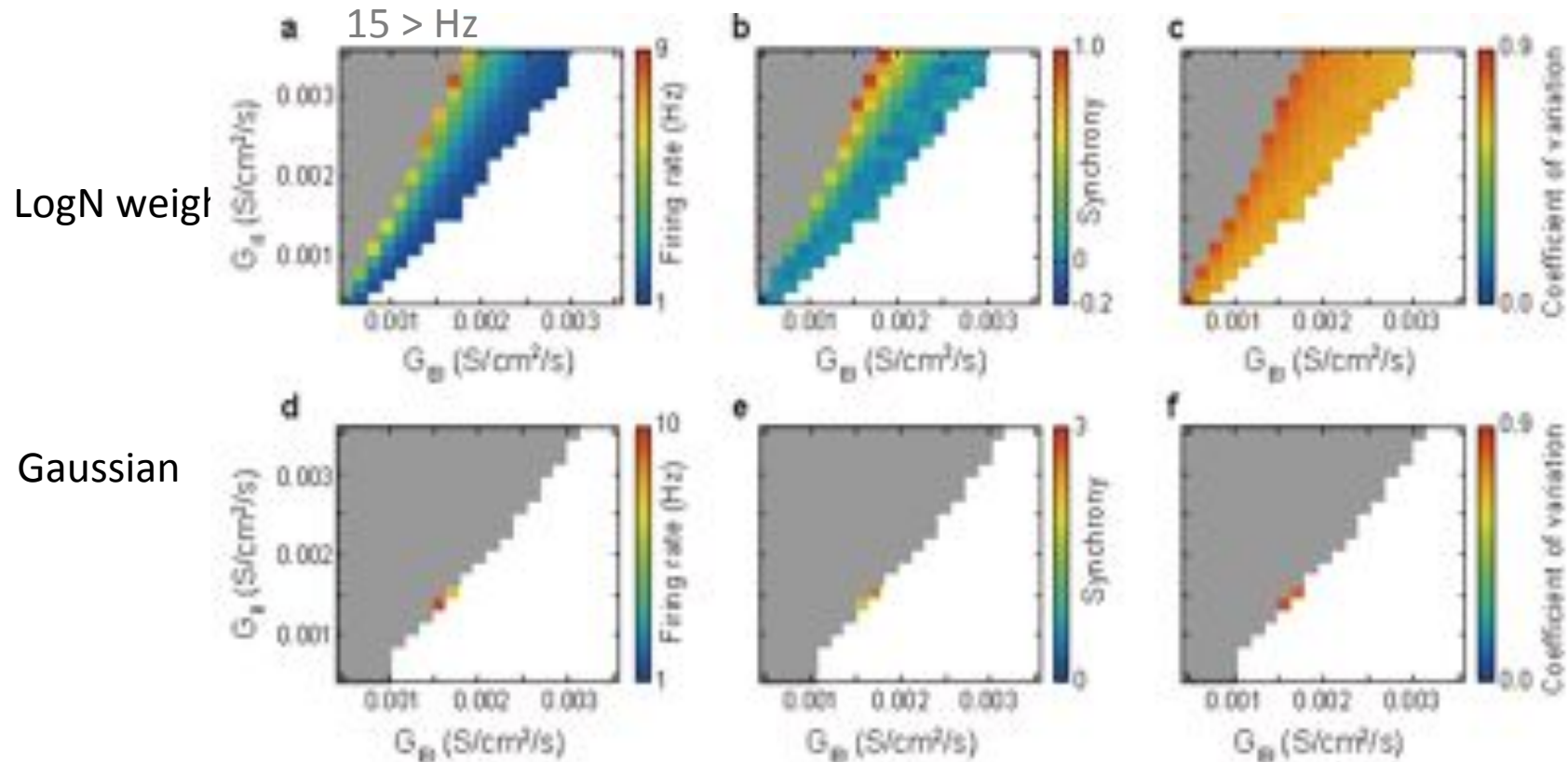
Dynamic clamp



$$I_{\text{syn}}(t) = -\sum_j g_{E_j}(t)(V - E_E) - \sum_j g_{I_j}(t)(V - E_I)$$

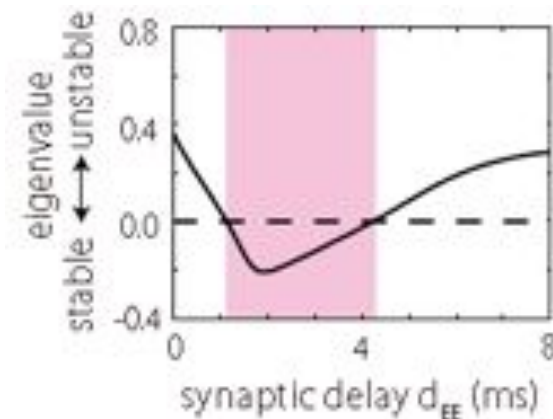


Synaptic delay enhances the stability (LIF neuron)

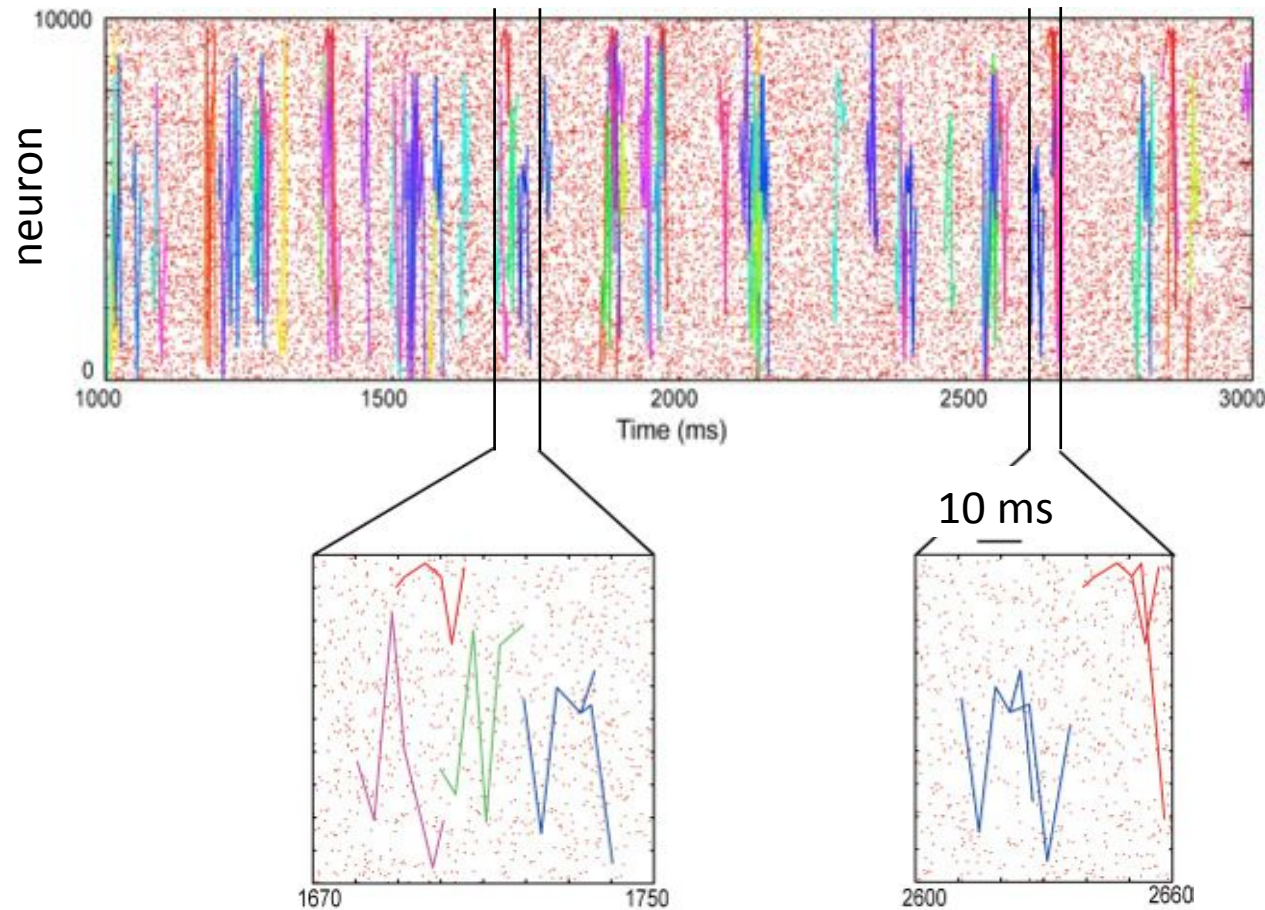


Inhibition arrives a little earlier than excitation

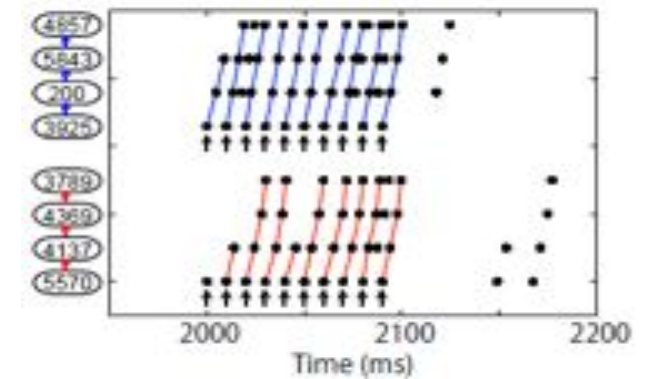
$$d_{EE} (\sim 2\text{ms}) > d_{EI}, d_{IE}, d_{II} (\sim 1\text{ms})$$



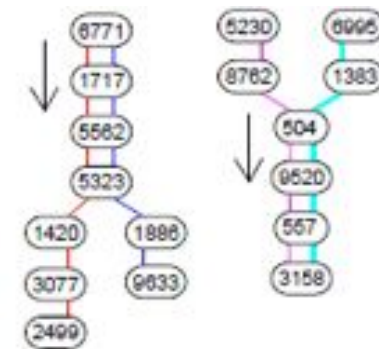
The AI state consists of vast many spike sequences



- Sequence propagation is probabilistic.



- Sequences can branch or merge.

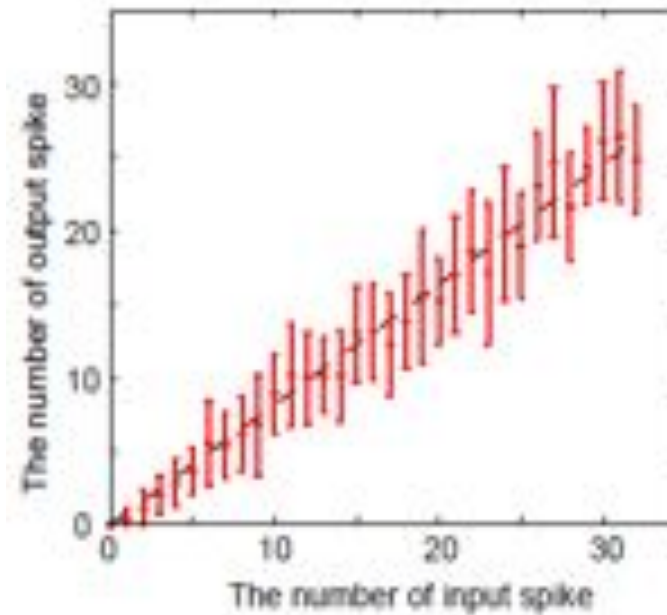


- Sequences can be stretched or compressed.

logN network can propagate firing rate information

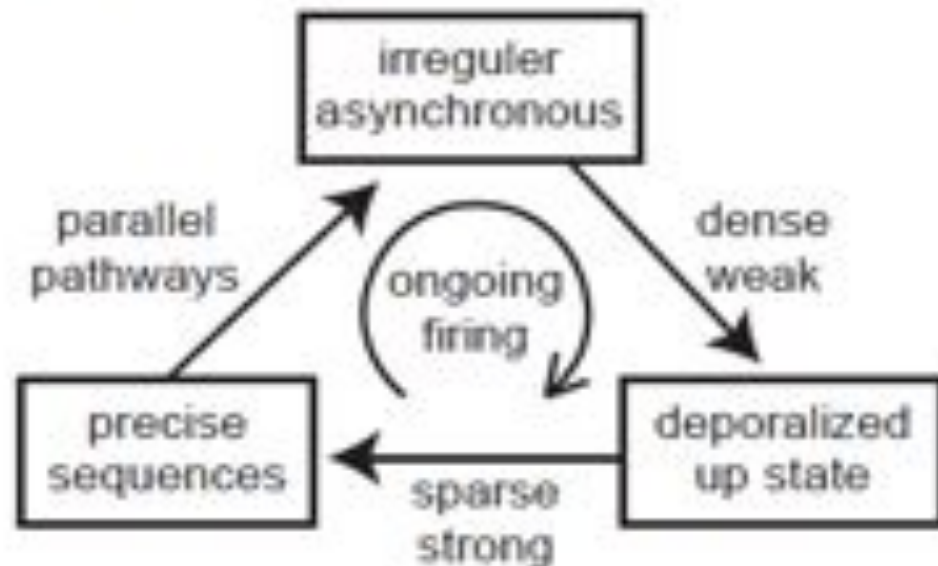


Efficient spike routing is possible
along strong synaptic pathways



Interim Summary

- Long-tailed (lognormal) EPSP distributions achieves asynchronous irregular states by sequences.
- Rate information propagates the pathways of strong synapses.
- Precise spike sequences and irregular firing are two sides of the same coin.



Buzsáki G, Mizuseki K.

The log-dynamic brain: how skewed distributions affect network operations.

Nat Rev Neurosci 15:264-278 (2014).

Lognormal networks for associative memory

(Hiratani et al., Front Comput Neurosci, 2013)

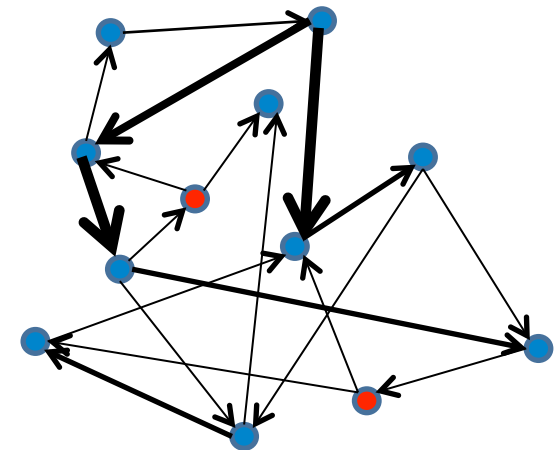


sparse binary memory patterns

$$\text{Prob} [\xi_i^\mu = 1] = a, \text{Prob} [\xi_i^\mu = 0] = 1 - a$$

$$J_{ij} = \frac{1}{N} \sum_{\mu=1}^P \xi_i^\mu \xi_j^\mu \sim \text{Gaussian}$$

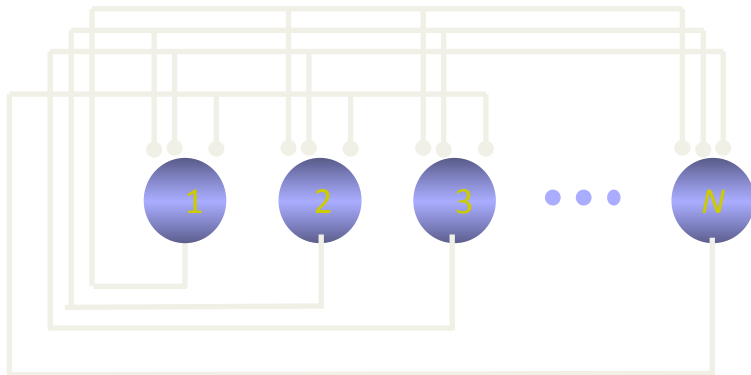
Use cumulative distributions to map J_{ij} onto a logN distribution, preserving the relative orders between matrix elements



N_E : # of excitatory cells
 p : # of stored patterns
 a : sparseness ($0 < a < 1$)

Lognormal associative memory model

(Hiratani et al., Front Comput Neurosci, 2013)



Sparse binary memory patterns

Hebb rule

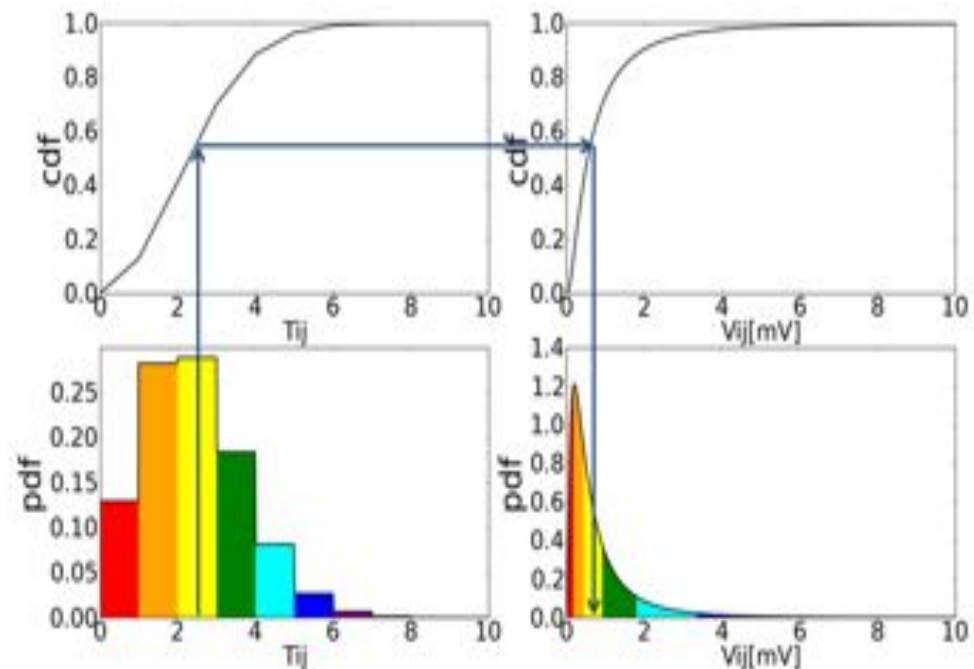
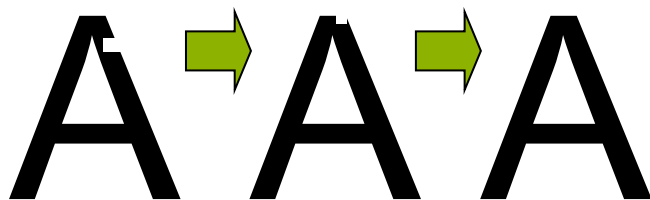
$$G_{ij} = \frac{1}{N} \sum_{\mu=1}^P \xi_i^{\mu} \xi_j^{\mu}$$

$p/N \rightarrow \infty$

Gaussian

Lognormal

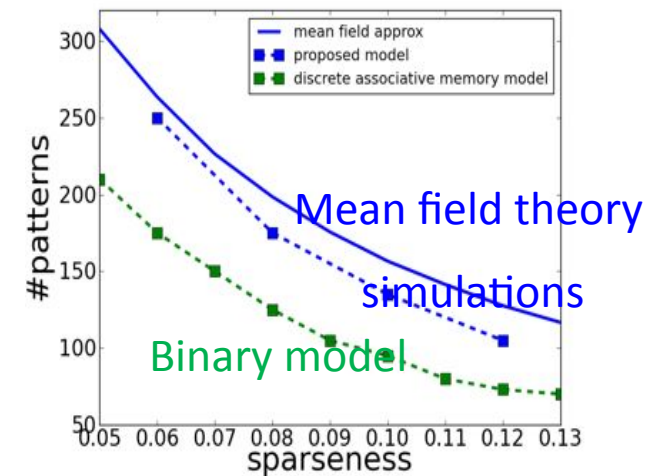
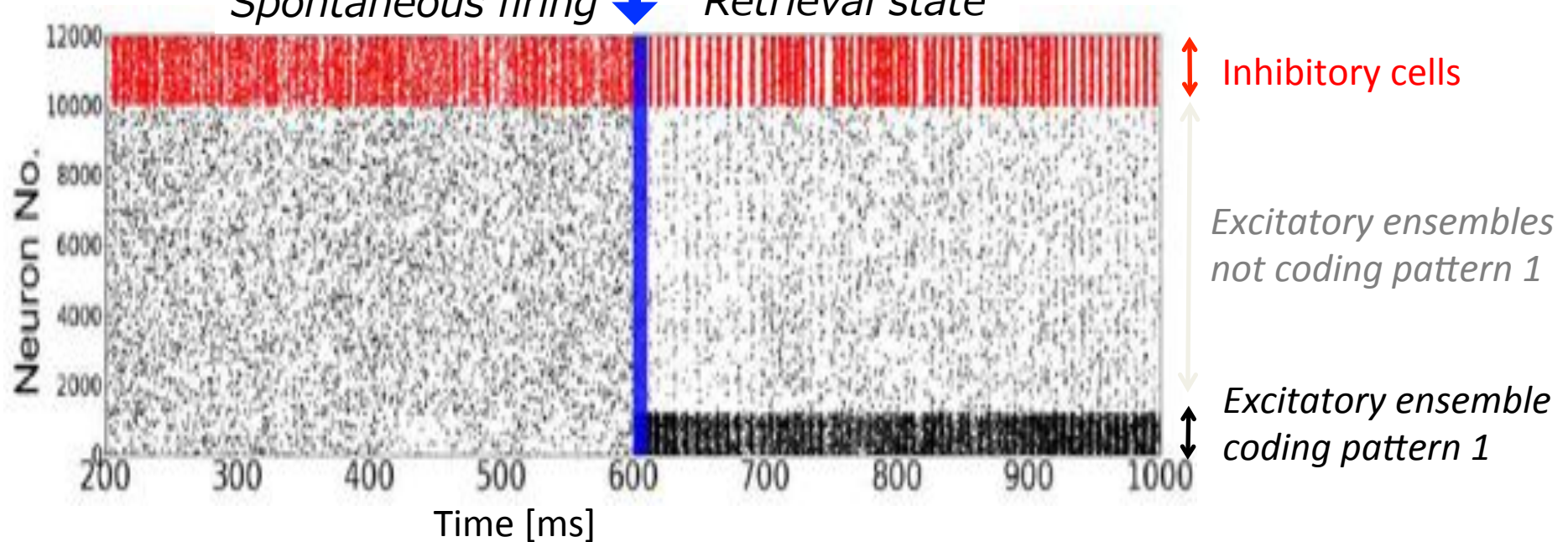
“Pattern completion”



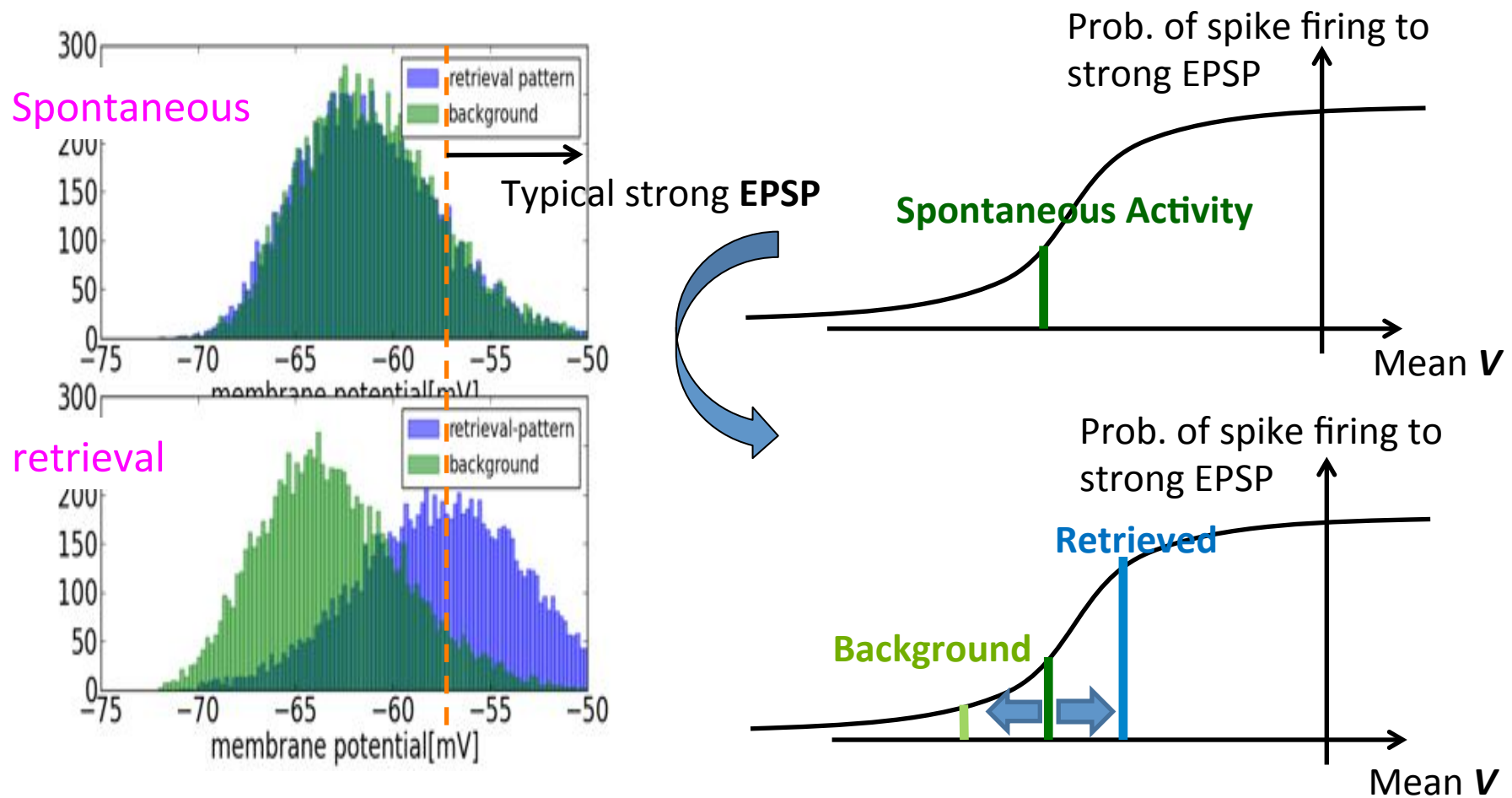
Memory recall

cue for retrieving pattern 1

Spontaneous firing ↓ Retrieval state



Internal noise structure dynamically changes during retrieval



Model of clustered cortical circuits

Klinshov, Teramae, Nekorkin, Fukai (PLoS ONE, 2014)

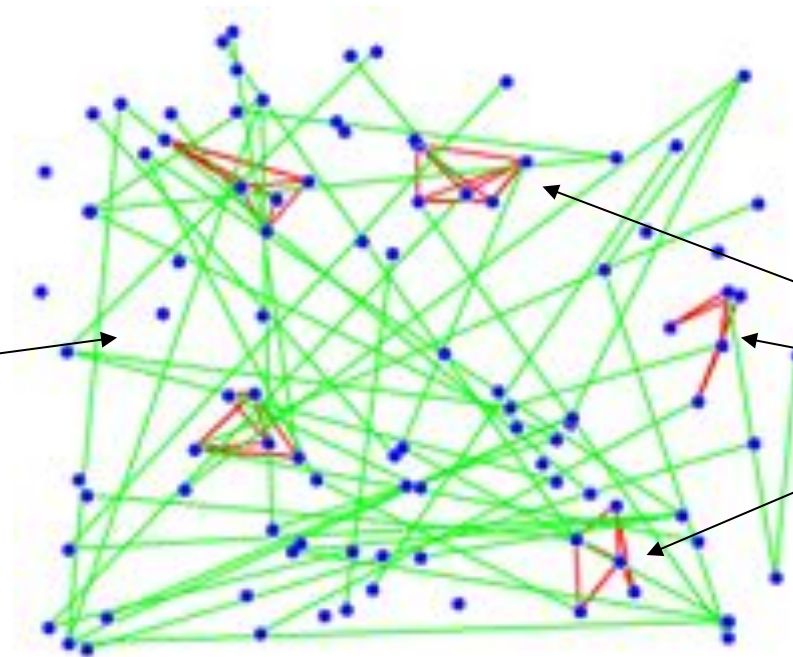
A network of N neurons including K clusters each involving M units

C_1, C_2 : connection probabilities

$f_1(w), f_2(w)$: weight distributions

Outside and
between clusters

C_1
 $f_1(w)$



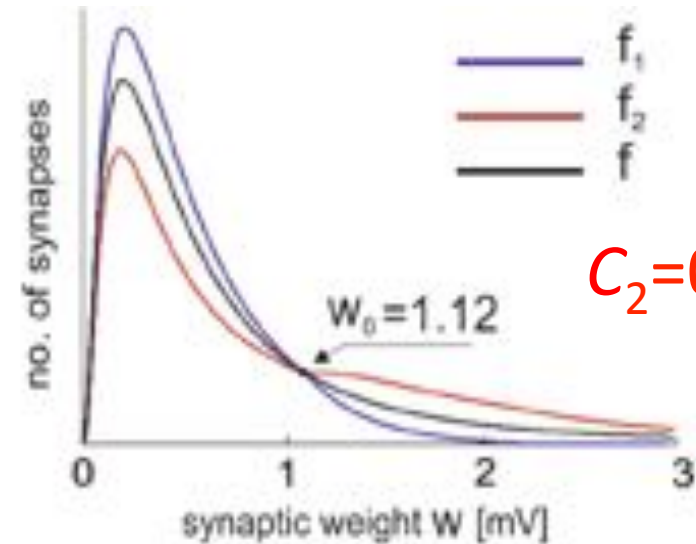
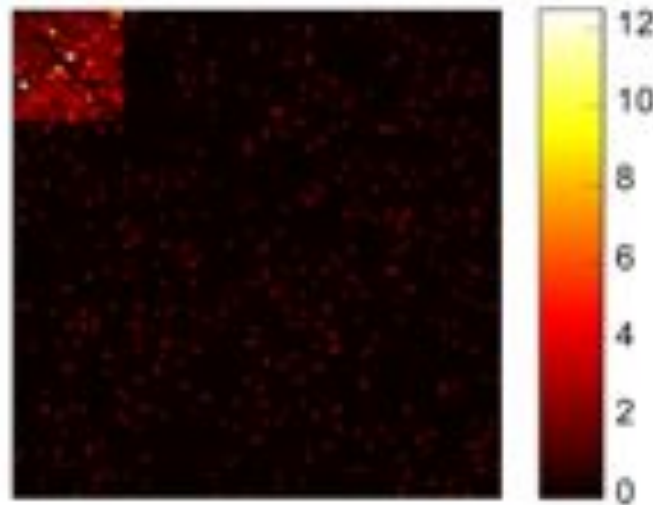
$(100 \mu m)^3$

Within a cluster

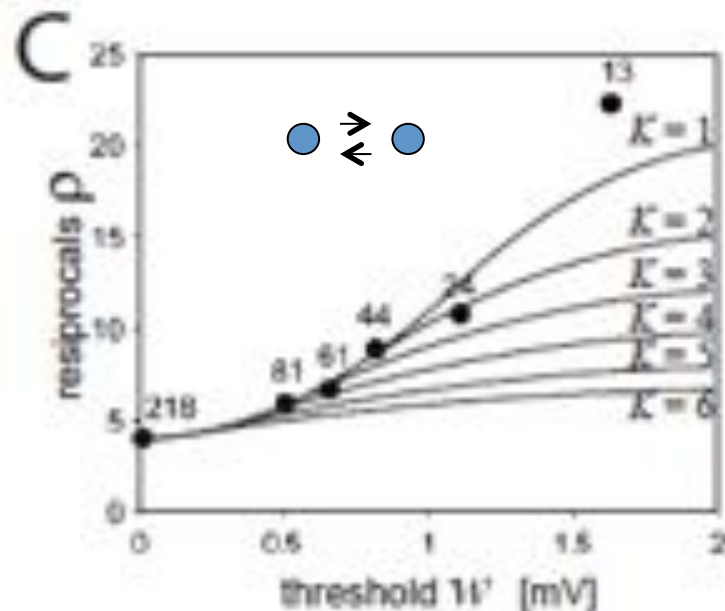
C_2
 $f_2(w)$

The clustered connection matrix

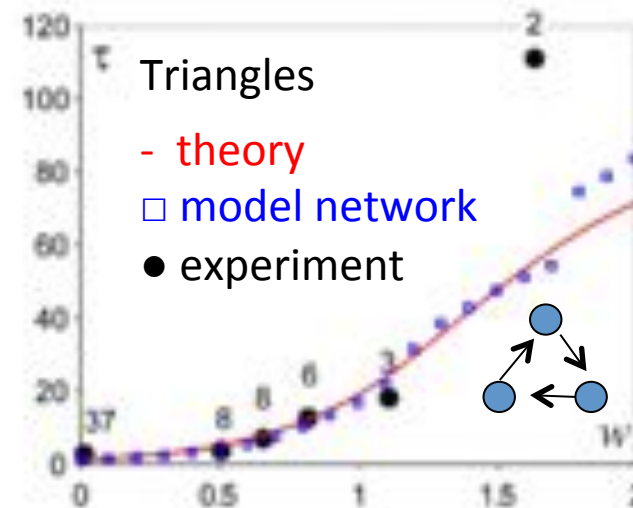
Only $K=1$ is consistent with all experimental observations.



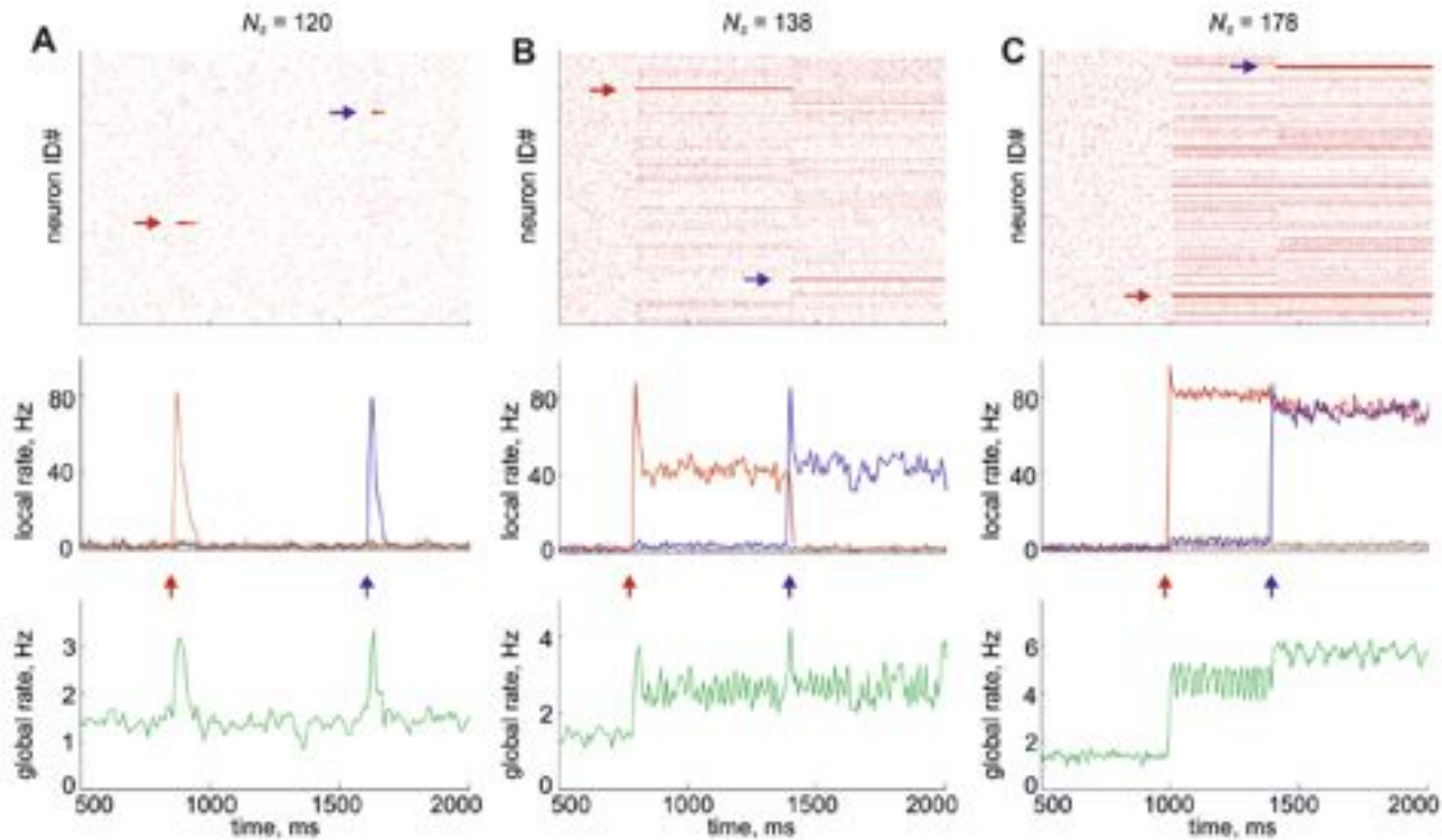
$C_2=0.88$!



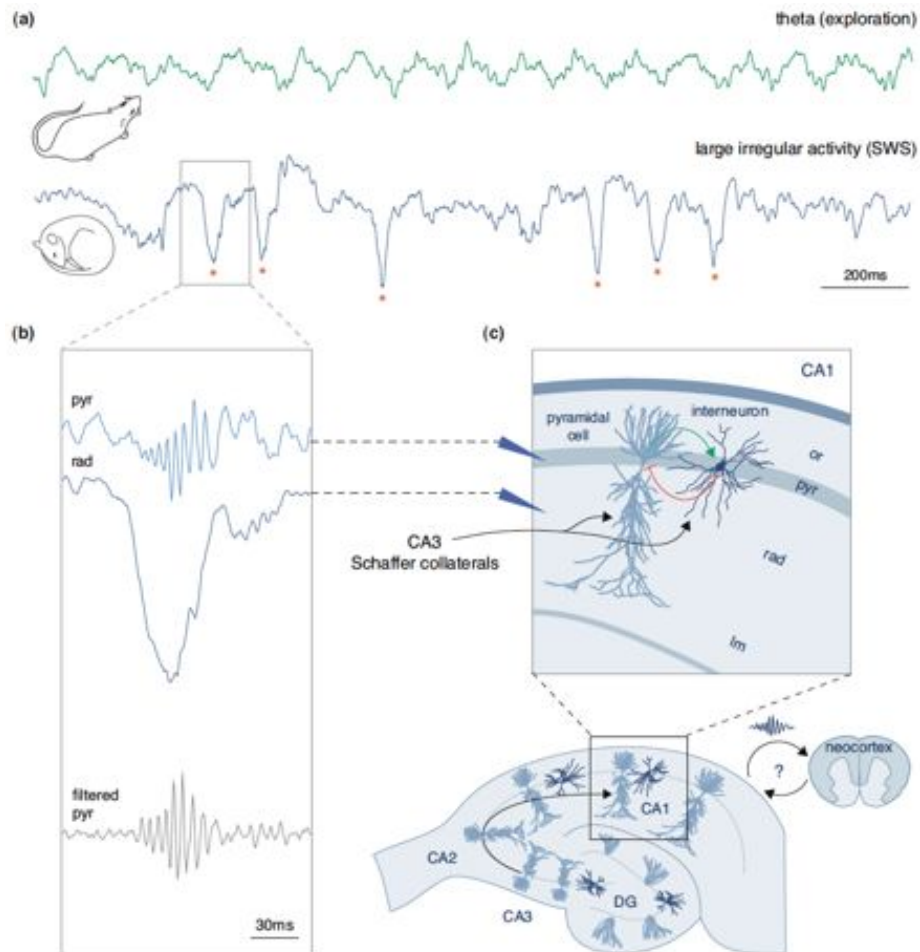
Counts relative to random



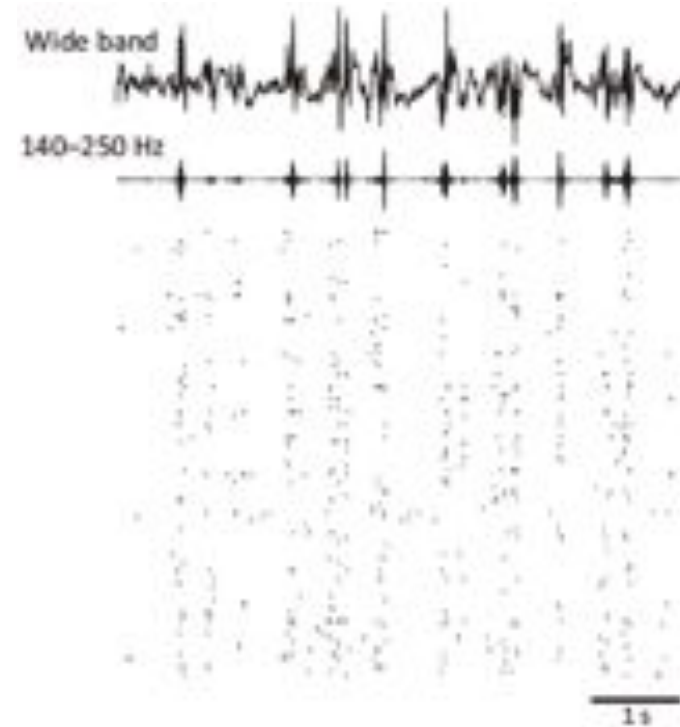
Competing working memory



Burst firing during sharp wave ripples



Girardeau and Zugaro, Curr Opin Neurobiol, 2013



McNamara et al., Nat Neurosci 2014

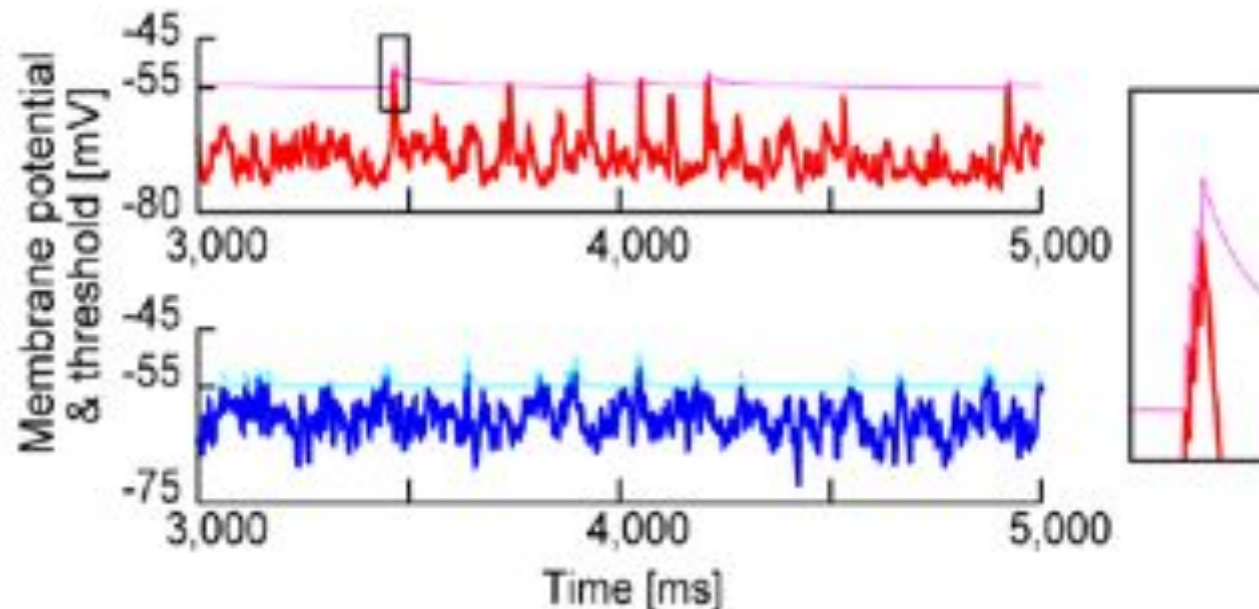
- Ripples are crucial for memory consolidation.
- Ripples are generated by CA3 input.

Multi-time scale adaptive threshold (MAT) model

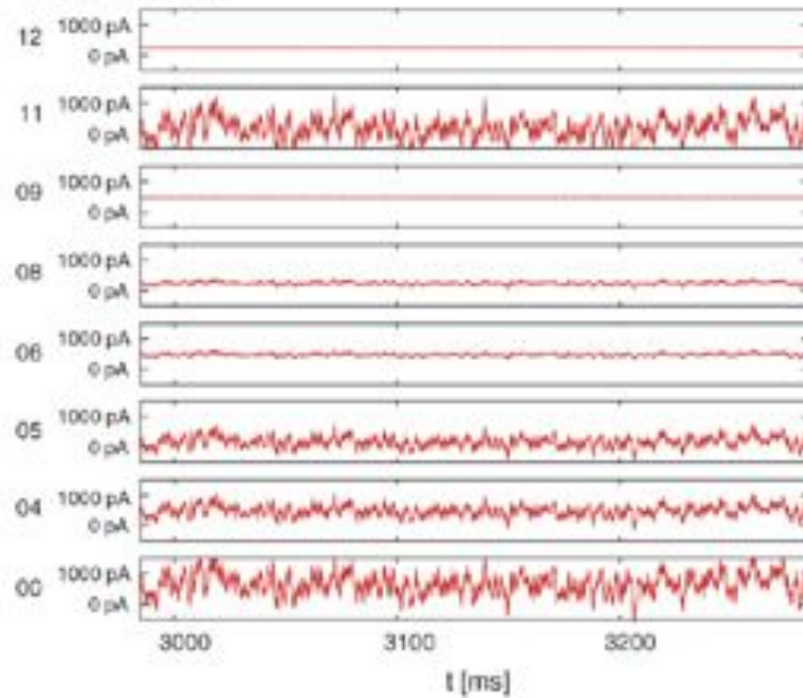
MAT neuron has dynamical threshold and fires when $V(t)$ exceeds $\theta(t)$.

$$\theta_i(t) = \sum_j H(t - t_j) + \omega \quad H_i(t) = \sum_{k=1,2} \alpha_k \exp\left(-\frac{t}{\tau_k}\right)$$

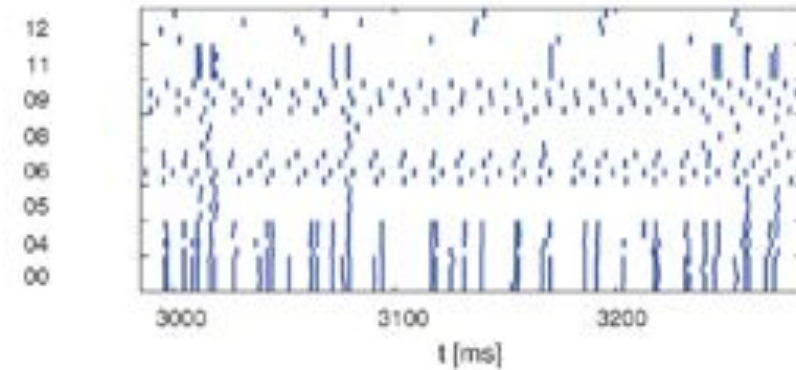
Kobayashi et al., 2009



(A) Input currents



(B) Spike times



Results of the challenge on intrinsically reliable data only

Submission	Group	Reference	Raw Γ	Performance (Γ_A)
Submission 1	Kyoto/Kobayashi (AR)	See Section 2.4.1	0.60	0.73
Submission 2	Kyoto/Shinomoto (CC)	See Section 2.4.2	0.71	0.84
Submission 3	Anonymous 1	–	0.48	0.56
Submission 4	Anonymous 2	–	0.33	0.40
Reference 1	Lausanne/Jolivet (SRM)	See Section 2.4.3	0.70	0.84
Reference 2	Lausanne/Naud (aEIF)	See Section 2.4.4	0.70	0.83

Modeling population synchrony in the hippocampus

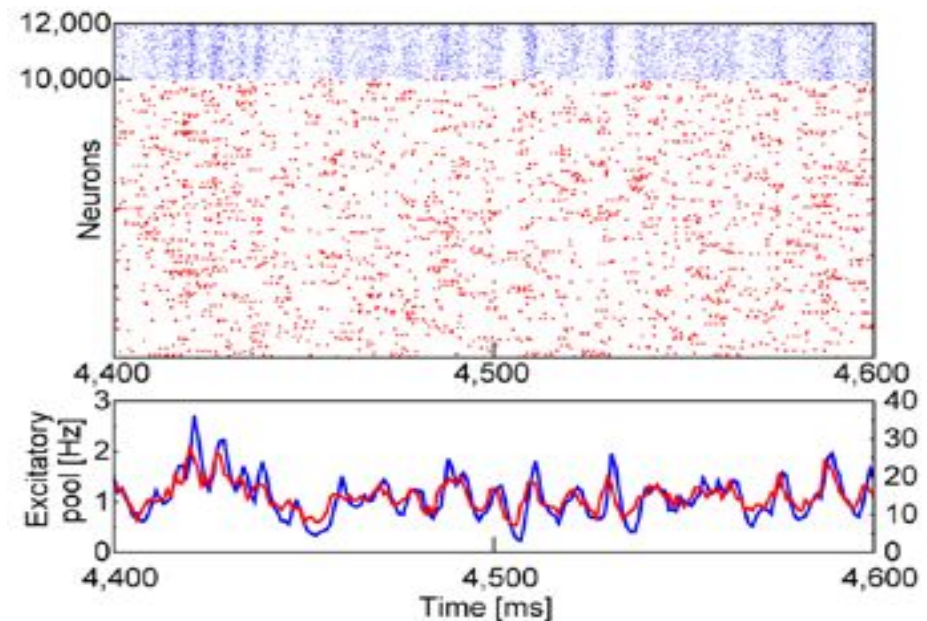
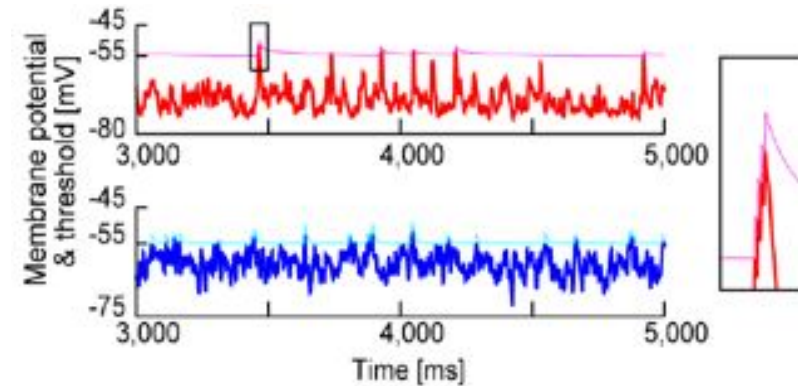
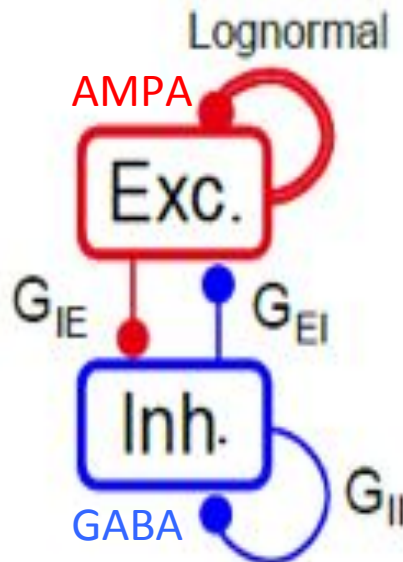
Ohmura, Carvalho, Inokuchi, Fukai (J Neurosci 2015)

Multi-time scale Adaptive Threshold (MAT) model

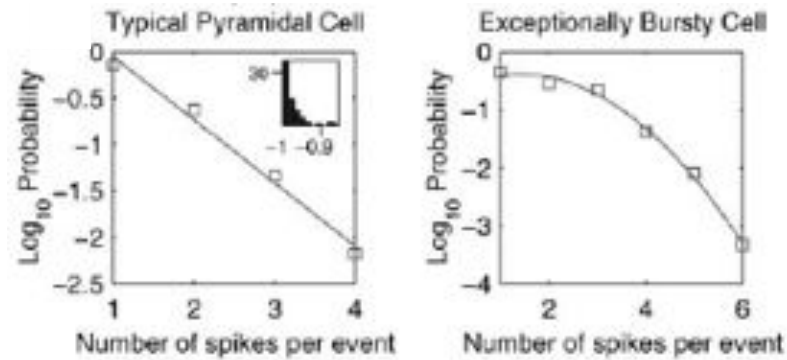
$$\theta_i(t) = \sum_j H(t - t_j) + \omega$$
$$H_i(t) = \sum_{k=1,2} \alpha_k \exp\left(-\frac{t}{\tau_k}\right)$$

Jolivet et al., 2008

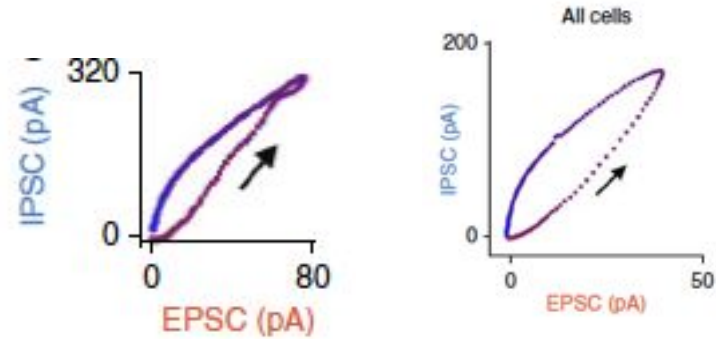
Kobayashi et al., 2009



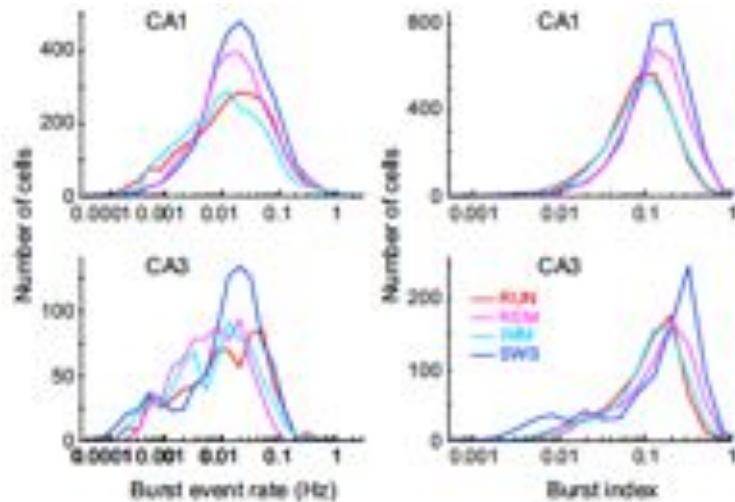
EXP



(Harris et al., Neuron 2001: CA1)

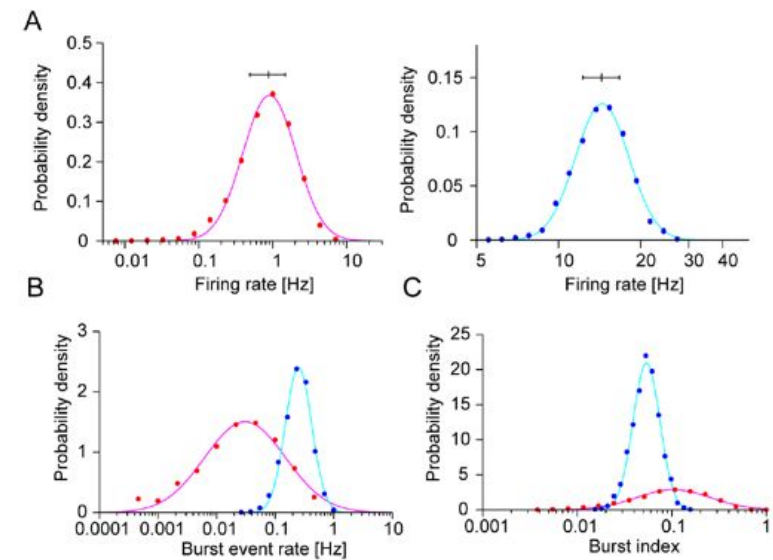
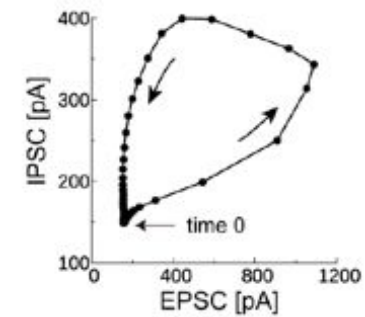
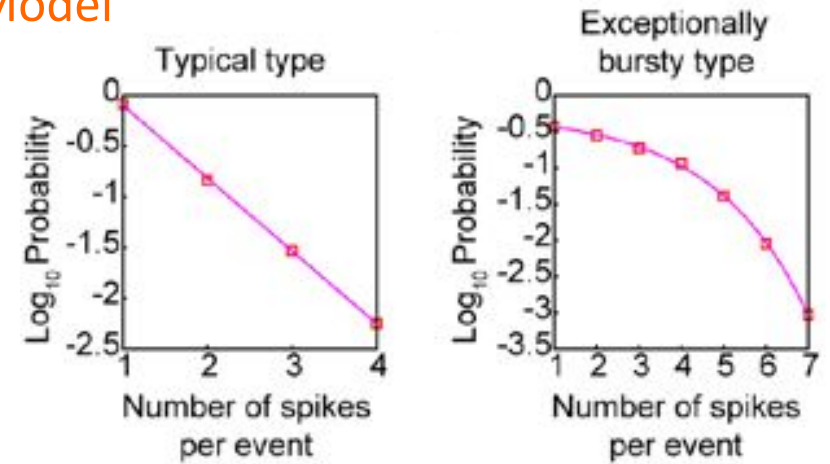


(Mizunuma et al., Nat Neurosci 2014)

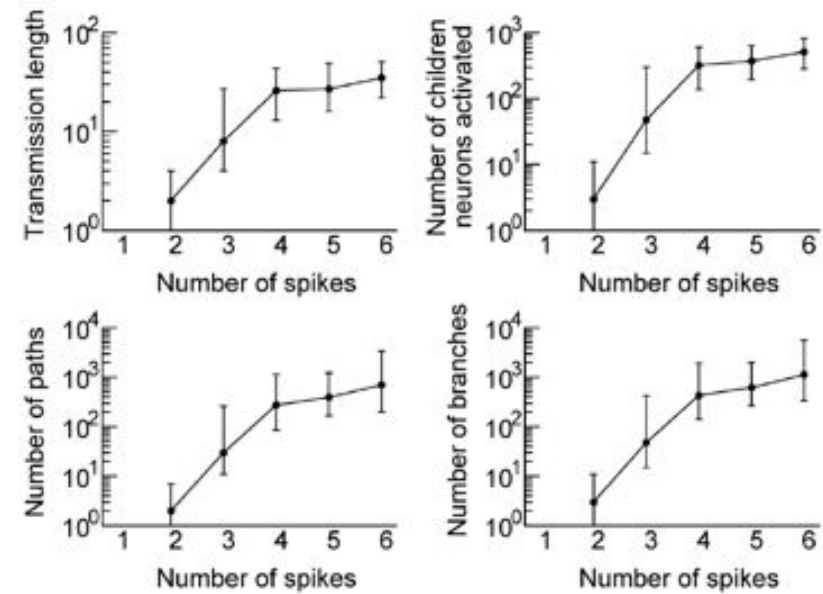
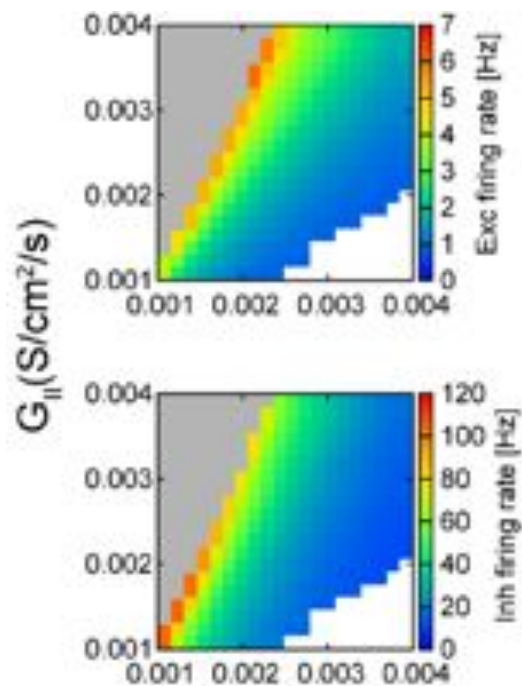
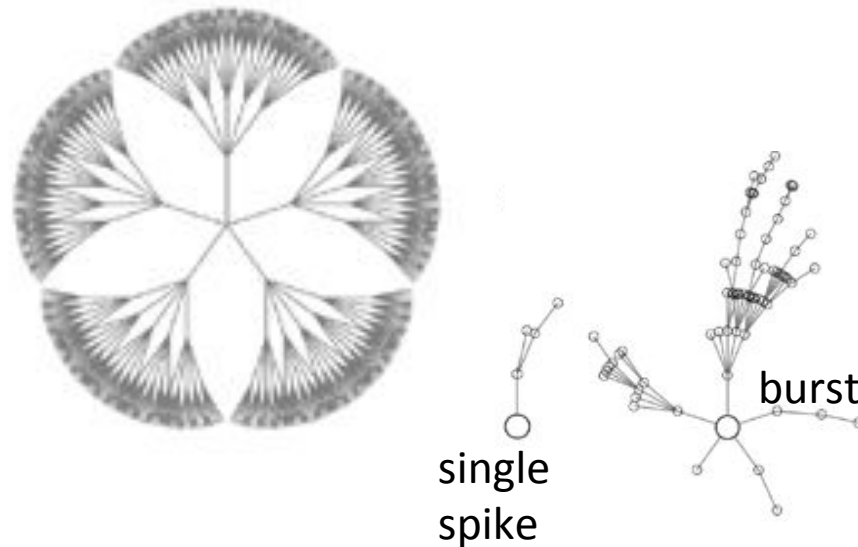


(Mizuseki and Buzsaki, Cell Rep, 2013)

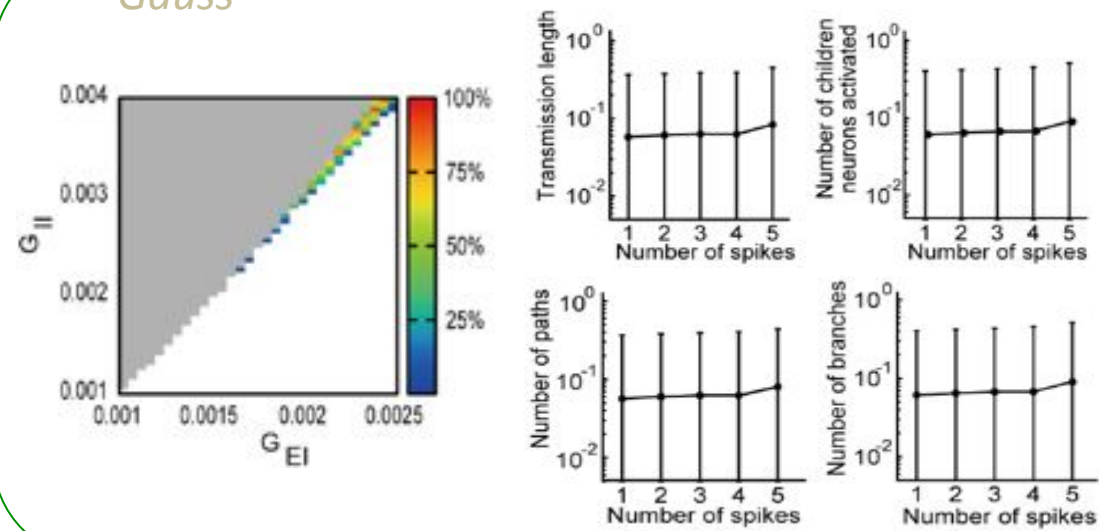
Model



Activity propagation in lognormal networks



Gauss



Summary

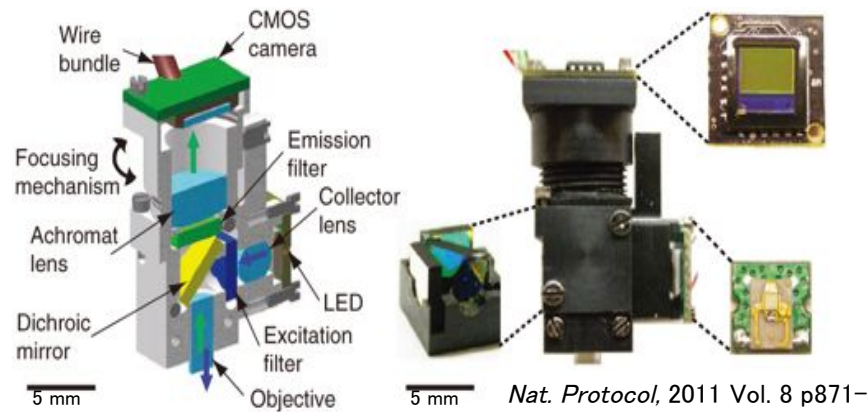
Co-existence of *strong sparse synapses* and *weak dense synapses* is a typical feature of neocortical and hippocampal circuits.

Such distributions support both irregularity and sequence in population neural activity.

Clustered networks with such distributions suggested working memory activity is cluster-size dependent.

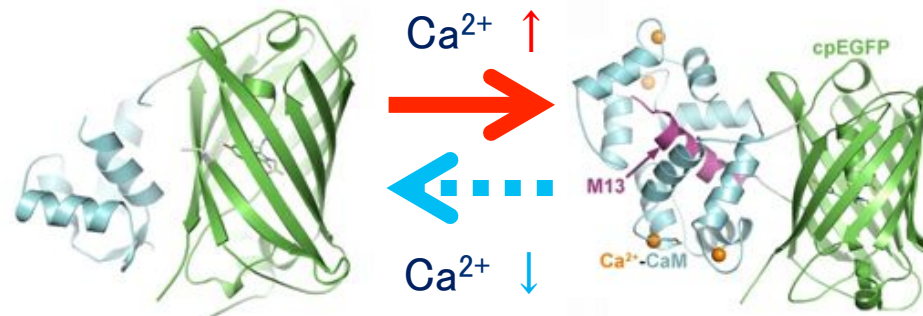
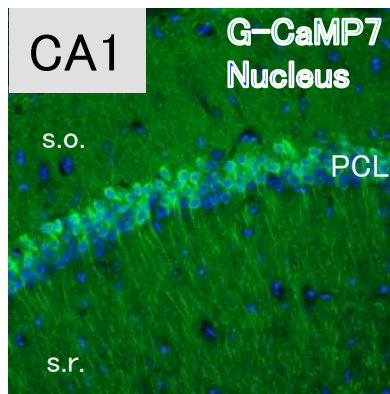
Calcium imaging with ultrasmall endomicroscope

● Optical endomicroscope • *nVista*



From Inokuchi laboratory
@Toyama University

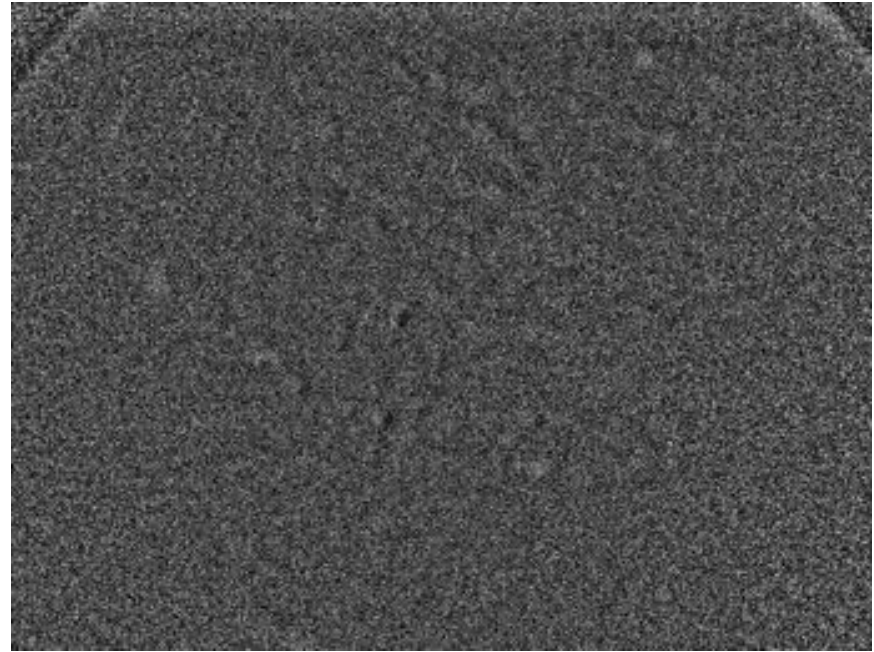
● Calcium sensor G-CaMP



Calcium imaging with an ultrasmall endomicroscope

Novel context exposure
dF/F movie

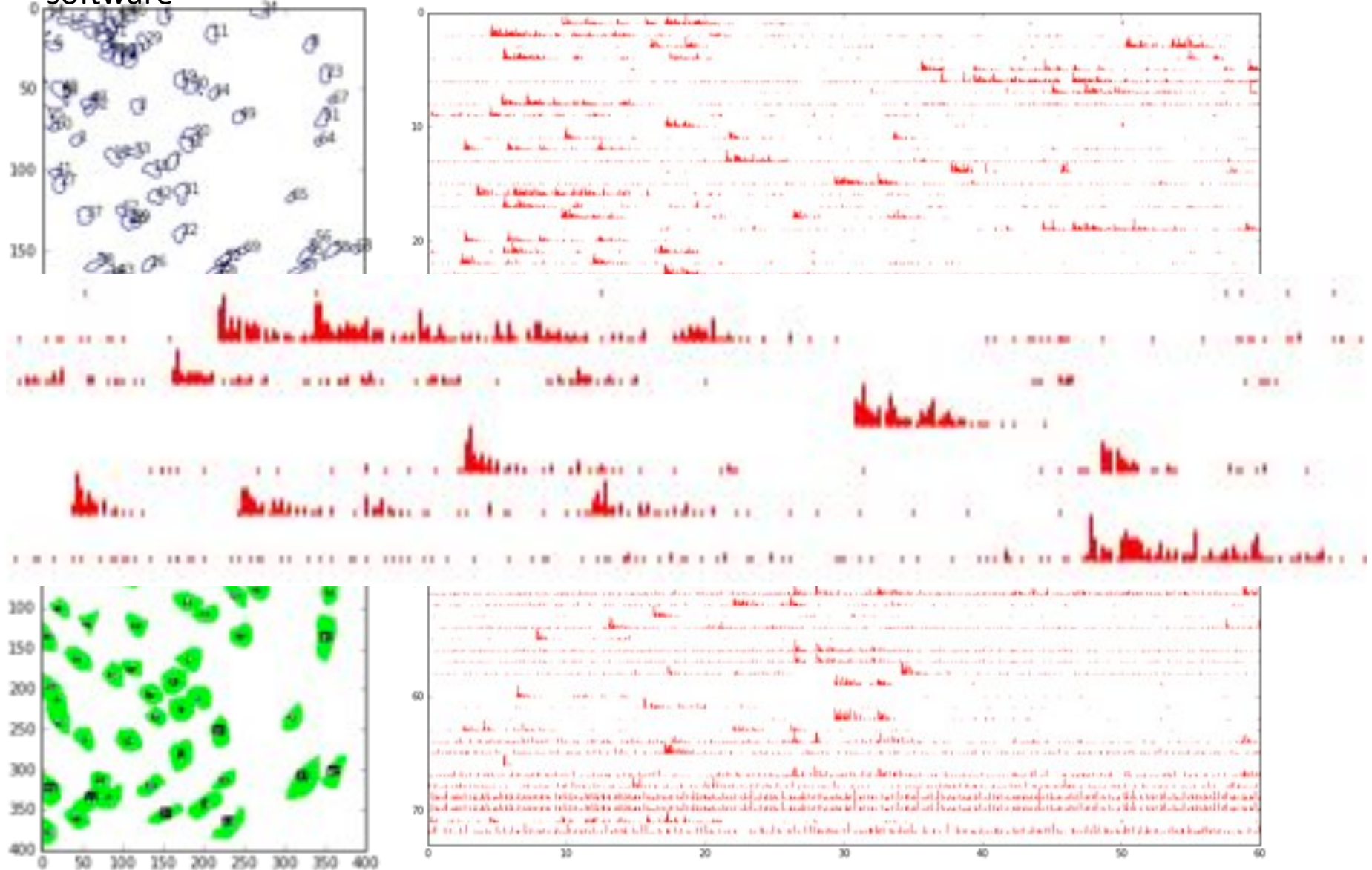
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–Novel context exposure and Ca^{2+} *dF* movie–

Examples of detected cells and activity patterns

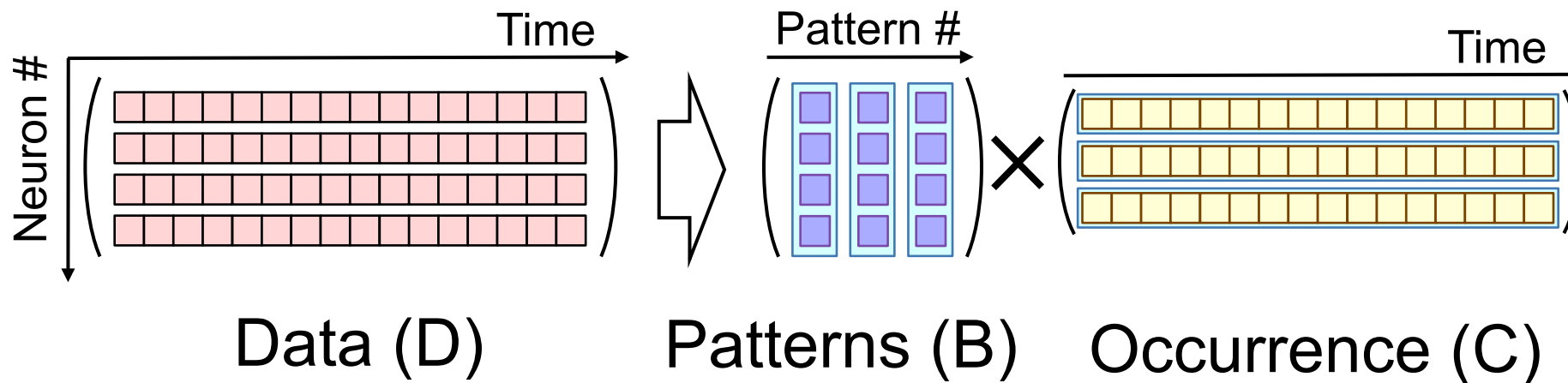
software



Non-negative matrix factorization (NMF) for cell assembly detection



Alan Fung



● Data matrix expressed by a product of non-negative matrices

● Search matrices B and C that minimize the error.

$$\mathbf{D} \approx \mathbf{BC}$$

$$E \equiv \sum_{ij} \left(D_{ij} - \sum_k B_{ik} C_{kj} \right)^2$$

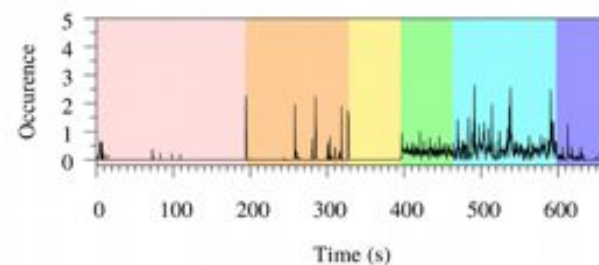
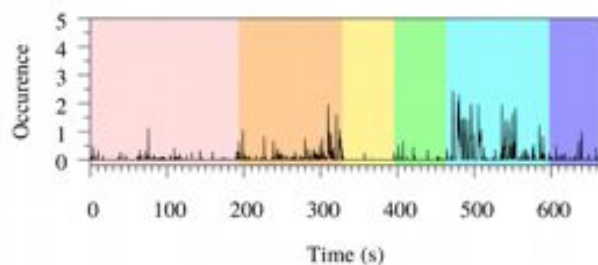
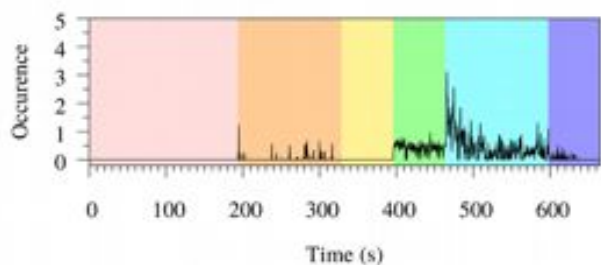
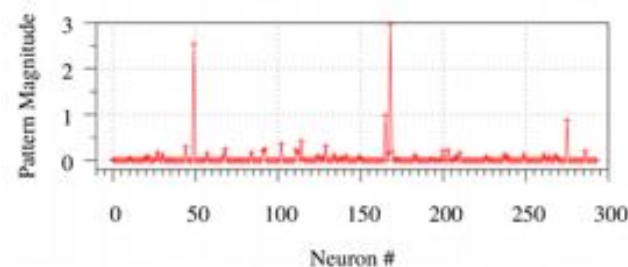
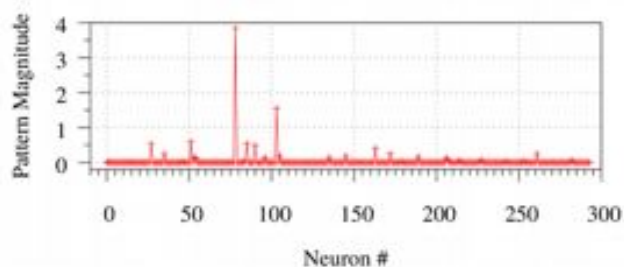
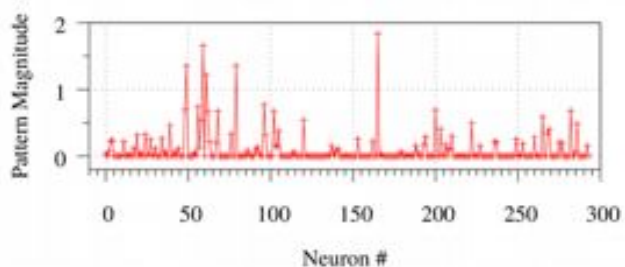
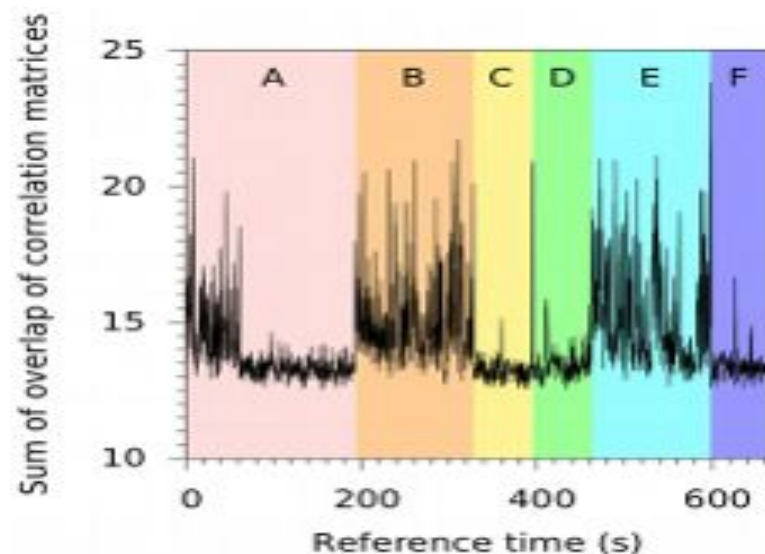
NMF of NV61

Day 1

- A Pre-exposure sleep
- B Exposure to a novel context
- C Post-exposure sleep

Day 2

- D Pre-exposure sleep
- E Exposure to a novel context
- F Post-exposure sleep



Day change
Preplay?

Preplay?
Interaction with previous experience

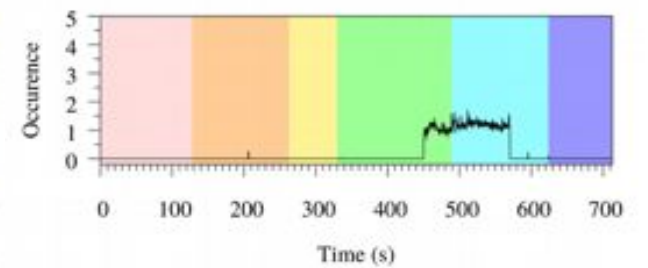
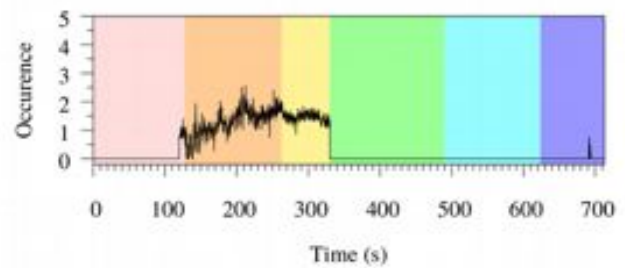
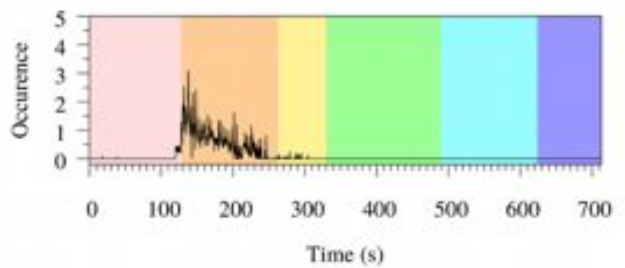
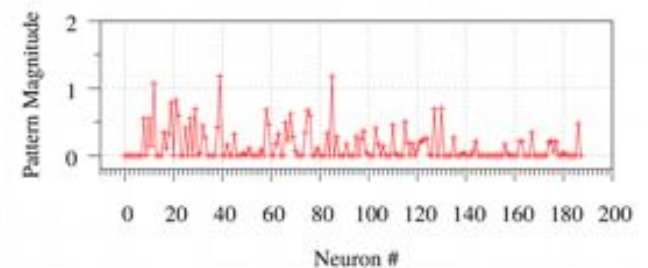
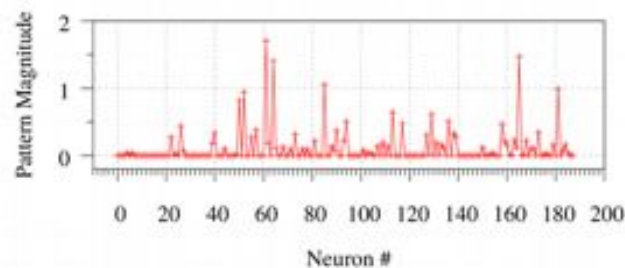
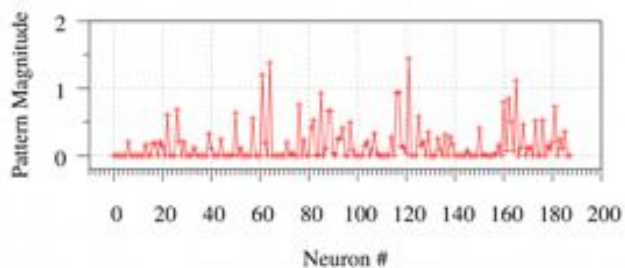
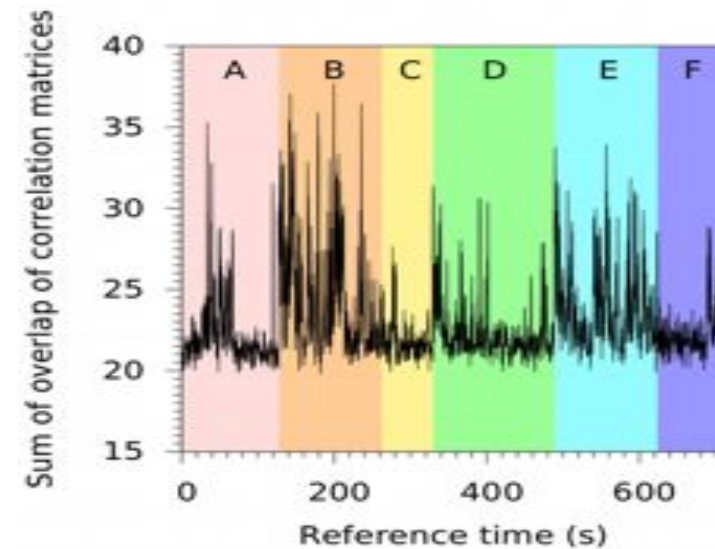
NMF of NV62

Day 1

- A Pre-exposure sleep
- B Exposure to a novel context
- C Post-exposure sleep

Day 2

- D Pre-exposure sleep
- E Exposure to a novel context
- F Post-exposure sleep



Day change
Context

Day change
Replay

Day change
Preplay

Optimal number of cell assemblies

- Too many cell assemblies does not much improve the fitting accuracy.

- Use Akaike's information criteria for determining the optimal number.

