

## Master Method

Let  $T(n)$  be a monotonically increasing function (a function that is increasing and non-decreasing).

If the recurrence is of the form  $T(n) = aT(n/b) + \Theta(n^k \log^p n)$ , given  $a \geq 1, b > 1, k \geq 0$  and  $p$  is a real number, then the complexity is defined as:

- 1) If  $a > b^k$ , then  $T(n) = \Theta(n^{\log_b a})$
- 2) If  $a = b^k$ 
  - a. If  $p > -1$ , then  $T(n) = \Theta(n^{\log_b a} (\log n)^{p+1})$
  - b. If  $p = -1$ , then  $T(n) = \Theta(n^{\log_b a} \log \log n)$
  - c. If  $p < -1$ , then  $T(n) = \Theta(n^{\log_b a})$
- 3) If  $a < b^k$ 
  - a. If  $p \geq 0$ , then  $T(n) = \Theta(n^k \log^p n)$
  - b. If  $p < 0$ , then  $T(n) = O(n^k)$