

Master Method

Let $T(n)$ be a monotonically increasing function (a function that is increasing and non-decreasing).

If the recurrence is of the form $T(n) = aT(n/b) + \Theta(n^k \log^p n)$, given $a \geq 1, b > 1, k \geq 0$ and p is a real number, then the complexity is defined as:

- 1) If $a > b^k$, then $T(n) = \Theta(n^{\log_b a})$
- 2) If $a = b^k$
 - a. If $p > -1$, then $T(n) = \Theta(n^{\log_b a} (\log n)^{p+1})$
 - b. If $p = -1$, then $T(n) = \Theta(n^{\log_b a} \log \log n)$
 - c. If $p < -1$, then $T(n) = \Theta(n^{\log_b a})$
- 3) If $a < b^k$
 - a. If $p \geq 0$, then $T(n) = \Theta(n^k \log^p n)$
 - b. If $p < 0$, then $T(n) = O(n^k)$