

Section 1

Lab Quiz #1

ECE 242: Electronic Circuits 2 (Fall 2016)
Instructor: Bosco Leung

Name:

Student ID:

Lab Session (circle one): Tuesday Wednesday Thursday

Problem 1

Circuit A and circuit B are set up as shown in Figure 1. By changing the value of the variable resistor, R_L , I_o vs V_o graph for circuit A is generated as shown in Figure 2(a) and I_o vs V_o graph for circuit B is generated as shown in Figure 2(b). The data points for figure 2 are recorded as shown in Table 1.

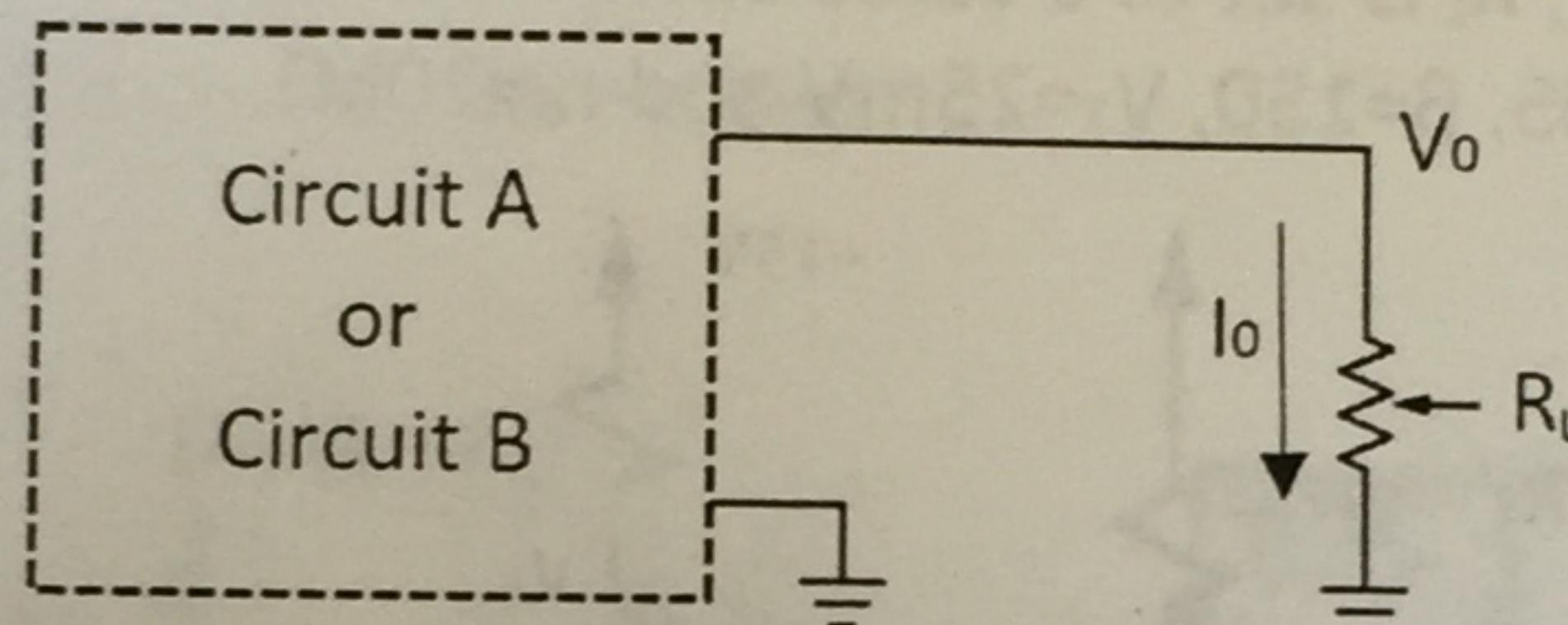


Figure 1: Laboratory Setup

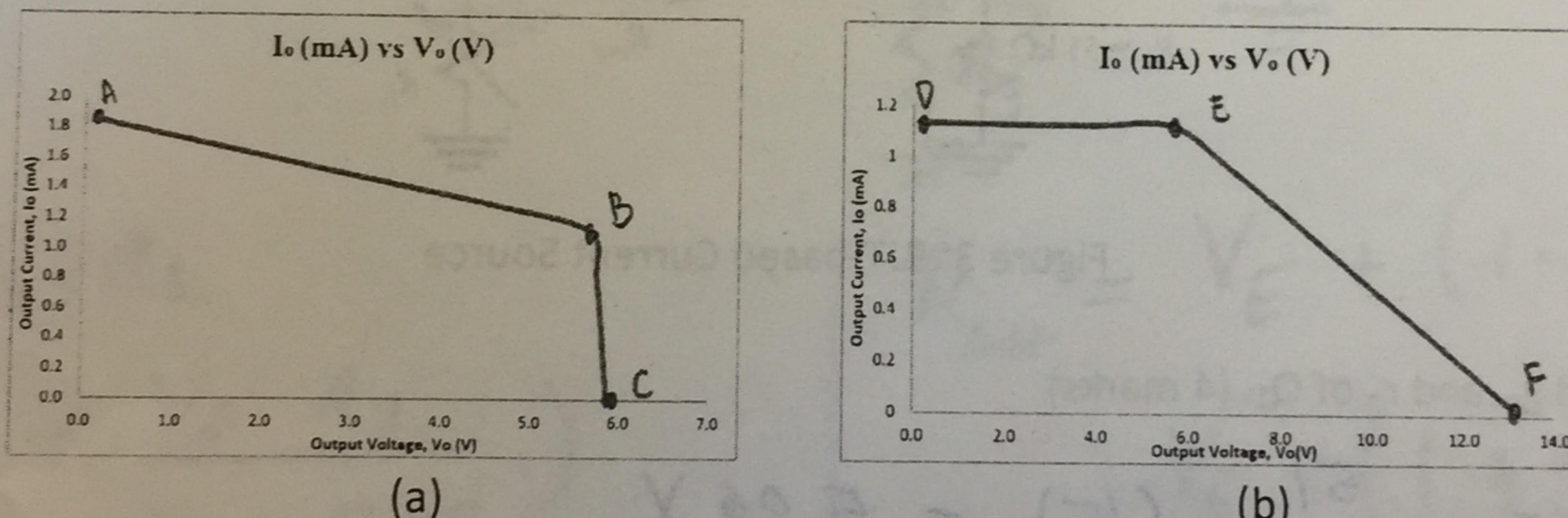


Figure 2: (a) I_o vs V_o graph of circuit A. (b) I_o vs V_o graph of circuit B

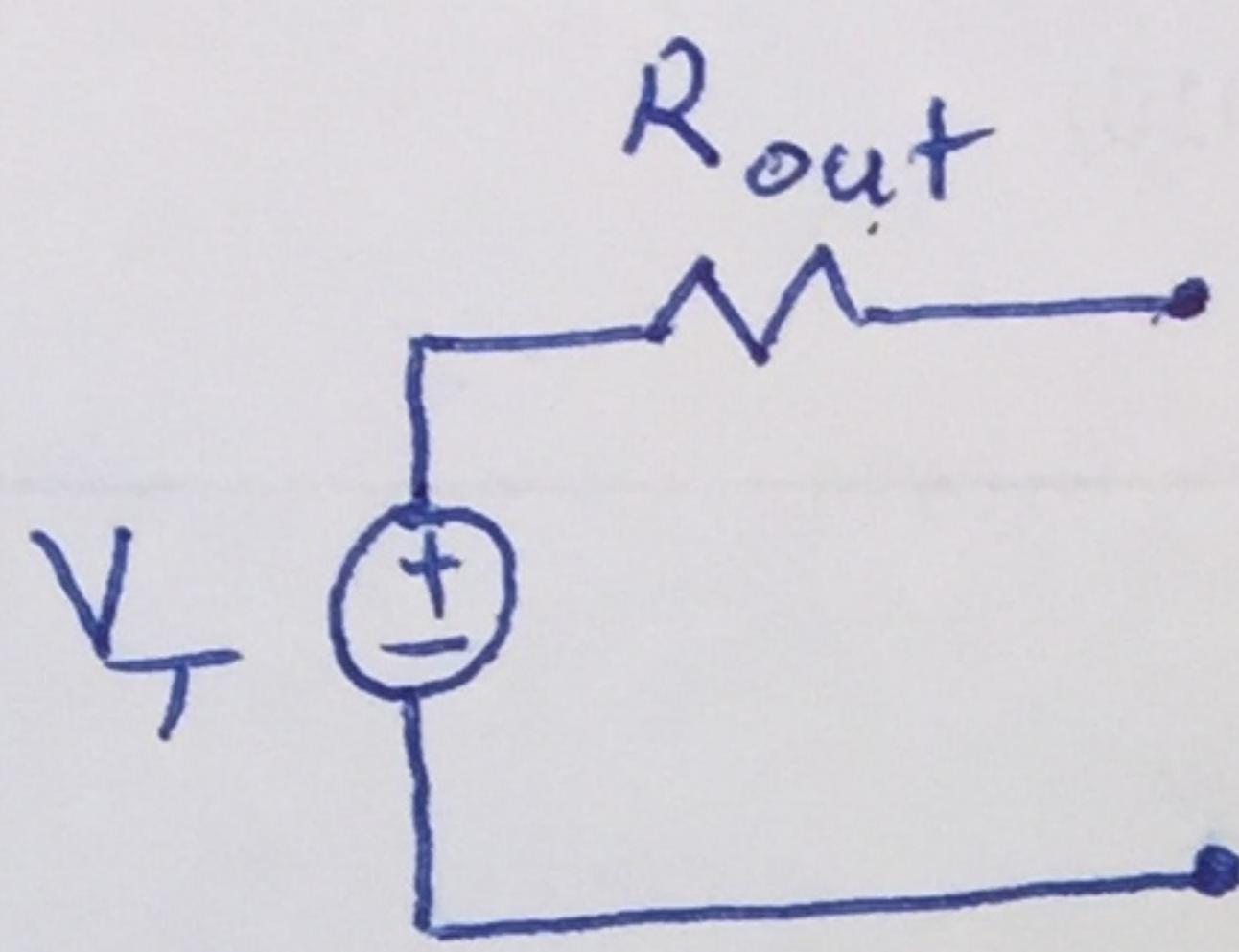
Data Points	A	B	C	D	E	F
I_o (mA)	1.83	1.19	0.0058	1.20	1.13	0.008
V_o (V)	0.025	5.70	5.86	0.022	5.85	13.4

Table 1: Data Points

- a) Which circuit is a better voltage source? Justify your answer. (2 marks)

Circuit "A". circuit "A" has smaller output resistance

- b) Draw a Norton or Thevenin (whichever appropriate) equivalent model for the circuit chosen in part (a). Label all components. (3 marks)



$$V_T = 5.86 \text{ V}$$

$$R_{out} = 135 \text{ } \mu\Omega$$

Problem 2

In Figure 3, the variable resistor, R_L is set to a value such that the BJT, Q_1 operates in forward active region. It is given that $|V_{be}|=0.65$, $\beta=150$, $V_T=25\text{mV}$ and $r_o=20\text{k}\Omega$.

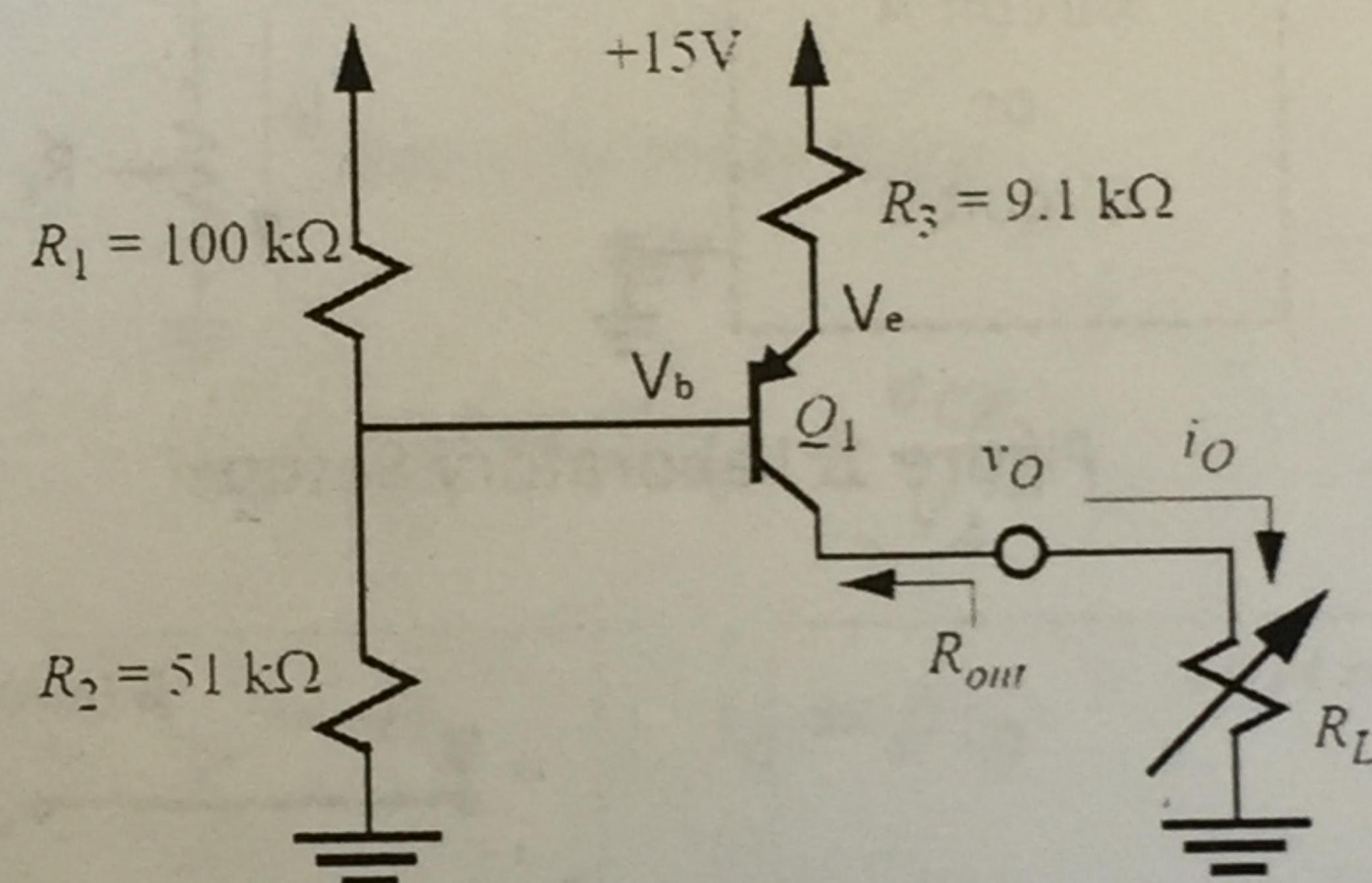


Figure 3: BJT-based Current Source

- (a) Find g_m and r_π of Q_1 . (4 marks)

$$V_b = \frac{51}{51 + 100} (15) = 5.06 \text{ V}$$

$$V_e = 5.06 + 0.65 = 5.71 \text{ V}$$

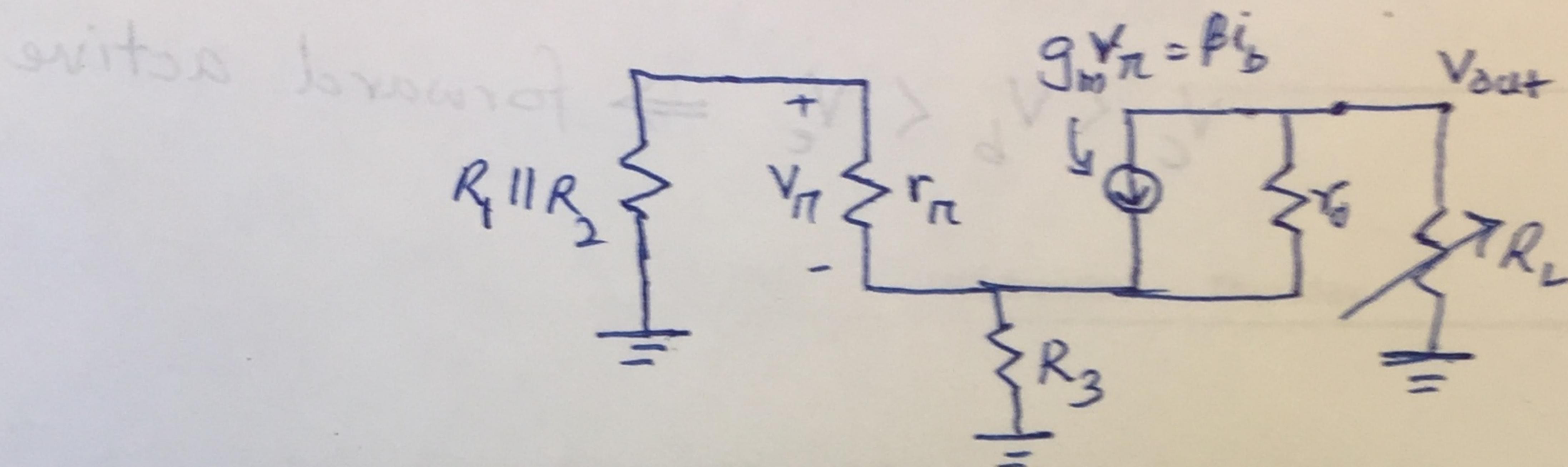
$$I_E = \frac{15 - V_e}{R_3} = \frac{15 - 5.71}{9.1 \text{ k}} = 1.02 \text{ mA}$$

$$I_{C_1} = \frac{\beta}{1 + \beta} I_E = \frac{150}{151} (1.02 \text{ mA}) = 1.013 \text{ mA}$$

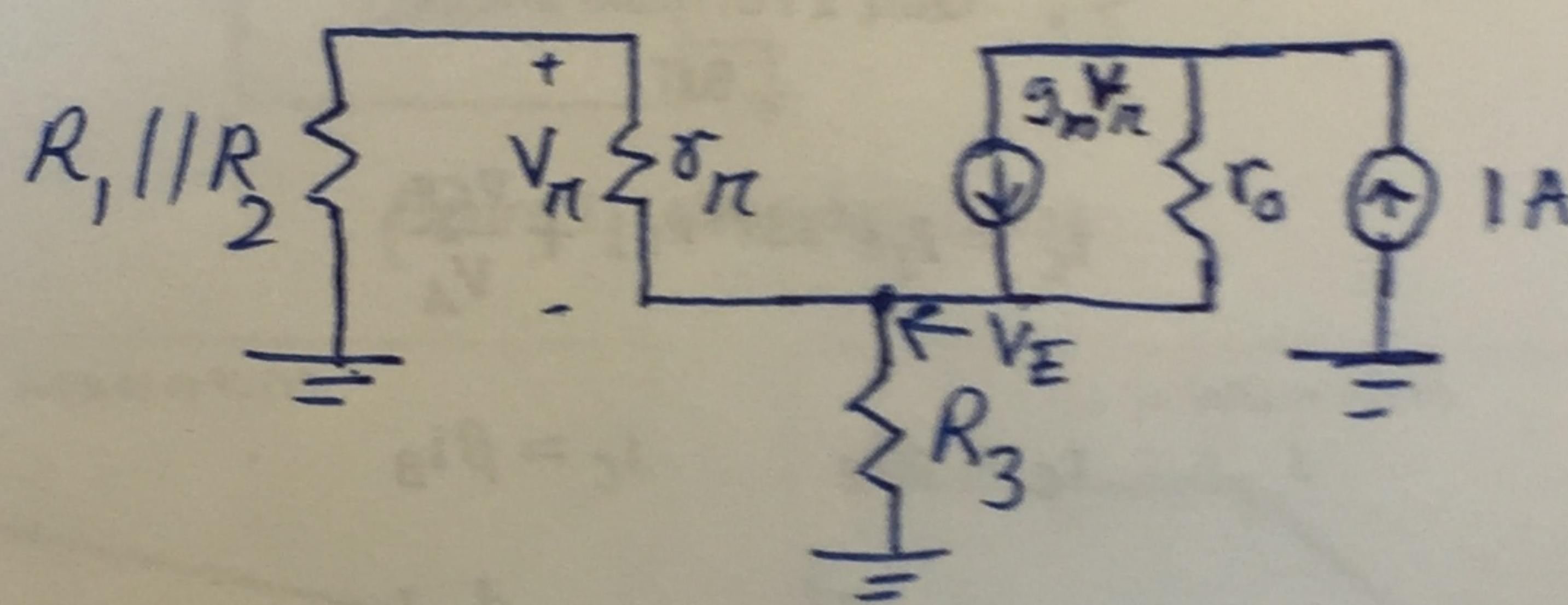
$$\therefore g_m = \frac{1.013 \text{ mA}}{25 \text{ mV}} = 0.0405 \text{ A/V}$$

$$r_\pi = \frac{\beta}{g_m} = \frac{150}{0.0405} = 3.703 \text{ k}\Omega$$

(b) Draw the small signal model for the circuit in Figure 3. Label all components. (3 marks)



c) Find the output resistance, R_{out} . (6 marks)



$$V_E = (1 - i_b) R_3$$

$$= \left(R_3 - \frac{V_E R_3}{r_\pi + R_1 || R_2} \right)$$

$$V_E \left(1 + \frac{R_3}{r_\pi + R_1 || R_2} \right) = R_3$$

$$\therefore V_E = \frac{R_3}{1 + \left(\frac{R_3}{r_\pi + R_1 || R_2} \right)} \quad *$$

$$V_E = \frac{9.1k}{1 + \left(\frac{9.1k}{3.705k + (100k || 51k)} \right)}$$

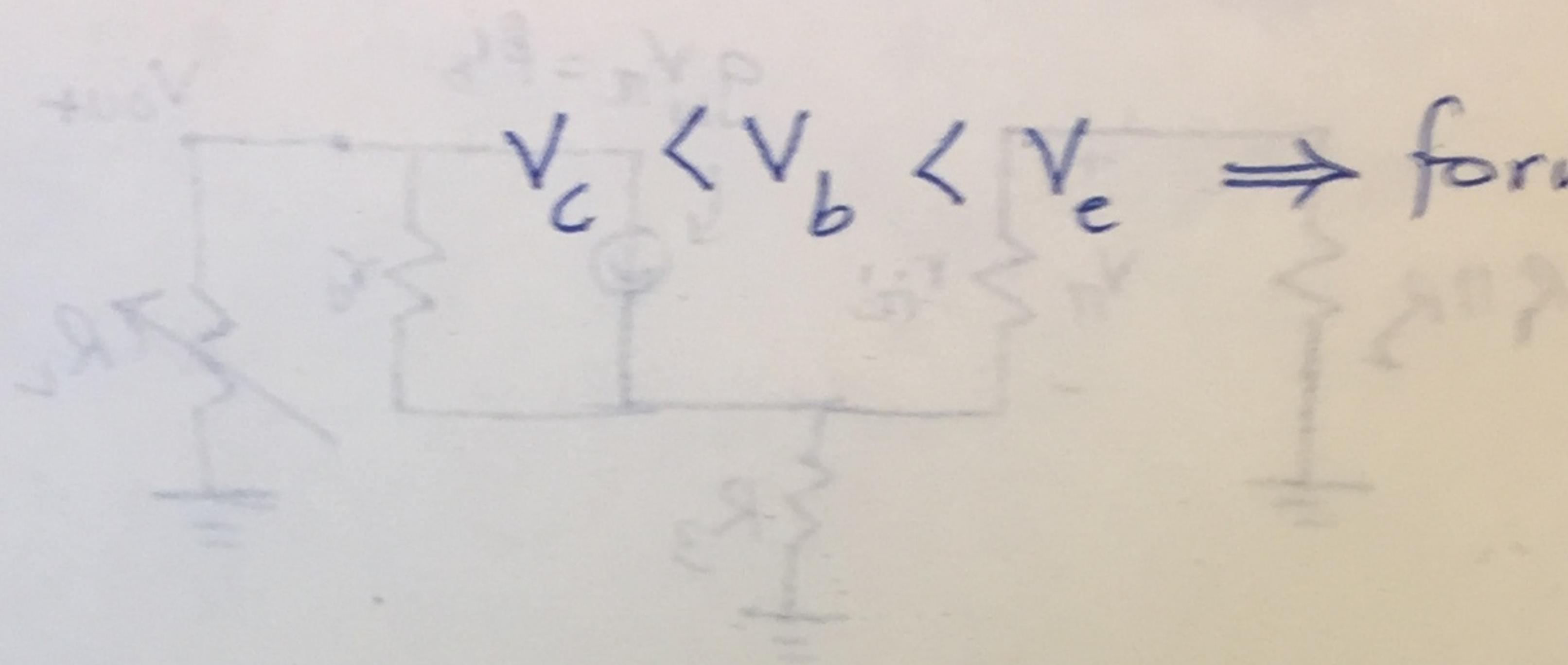
$$V_E = 7.322 kV$$

$$\begin{aligned} R_{out} &= V_E + (1 - g_m V_E) r_o \\ &= V_E + \left(1 + g_m \frac{r_\pi V_E}{r_\pi + R_1 || R_2} \right) r_o \\ &= r_o \left(1 + \frac{g_m r_\pi r_o}{r_\pi + R_1 || R_2} \right) V_E \\ R_{out} &= 20k + \left(1 + \frac{(150)(20k)}{3.703k + (100k || 50k)} \right) \\ &\quad * (7.322k) \end{aligned}$$

$$\therefore R_{out} = 0.823 M\Omega$$

d) What is the region of operation for BJT, Q₁ when R_L is set to 3kΩ. Justify your answer. (2marks)

When $R_L = 3\text{k}\Omega$; $V_o = 1.03 \text{m} \times 3\text{k} = 3.03\text{V}$



$V_c < V_b < V_e \rightarrow \text{forward active}$

Quiz 1 Formula Sheet

BJT

$$i_C = I_S e^{v_{BE}/V_T} \left(1 + \frac{v_{CE}}{V_A}\right)$$

$$i_C = \alpha i_E \quad i_C = \beta i_B$$

$$\alpha(v_{ac} - 1) + v_o = \alpha = \frac{\beta}{\beta + 1} \quad g_m = \frac{i_C}{V_T}$$

$$\alpha \left(\frac{v_o}{2V_T + \alpha} \alpha + 1 \right) + v_o = r_0 = \frac{V_A}{I_C} \quad \left(\frac{v_o}{2V_T + \alpha} - \alpha \right) =$$

$$r_o = \frac{V_T}{I_S} = \frac{\beta}{g_m} = (\beta + 1)r_e$$

$$r_e = \frac{V_T}{I_E} = \frac{\alpha}{g_m}$$

$$\left(\frac{(0.02)(0.2)}{(0.02)(0.2) + 3.03} + 1 \right) + 3.03 = +0.2$$

$$(3.03)^2 =$$

$$0.04808 = 0.02^2$$