

Notes on Combinatorial Optimization

Hao Su

July 1, 2025

Contents

1	Optimization Problems	1
---	-----------------------	---

Chapter 1

Optimization Problems

Defn 1.1 An *instance* of an *optimization problem* is a pair (F, c) , where F is any set, the domain of feasible points and c the cost function, a mapping $c : F \rightarrow \mathbb{R}$. The problem is to find an $f \in F$ for which $c(f) \leq c(y)$ for all $y \in F$. Such a point f is called a *globally optimal* (or simply *optimal*) solution to the given instance. \diamond