

BANKURA UNIVERSITY

B.Sc (HONS) FIFTH SEMESTER EXAMINATIONS, 2021-22

Subject: Computer Science

Course ID: 51512

Course Title: Theory of Computation

Full Marks: 40

Time: 2 Hrs

The figures in the margin indicate full marks

Answer all the questions.

UNIT I

1. Answer any five of the following questions: (5x2=10)
- a) Write two differences between nfa and dfa.
 - b) Define regular expression? Give example.
 - c) Find all strings of length 5 or less in the regular set represented by $(ab+a)^*(aa+b)$
 - d) State pumping lemma of regular languages.
 - e) Define simple grammar. Give example.
 - f) What is context free language? Give example.
 - g) Define Turing Machine.
 - h) Draw an nfa for $L=a^*b^*$

UNIT II

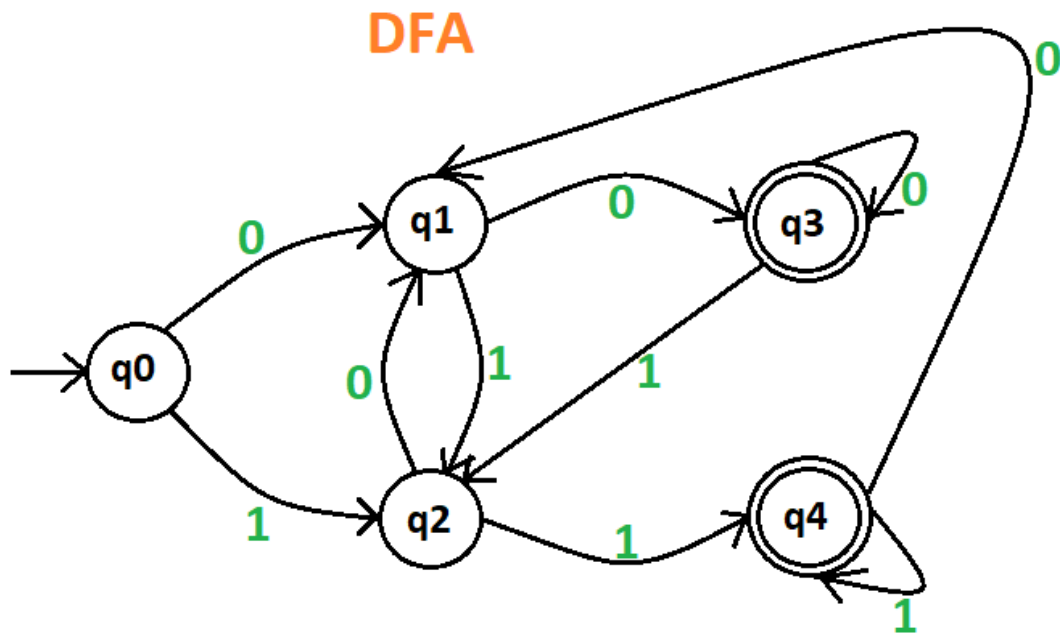
2. Answer any Four of the following questions: (5x4=20)
- a) Find regular expression for the following languages
 - I. Set of all strings of $\{0, 1\}$ not ended with 01.
 - II. $L=vwv$ such that $|v|=2$ and $v,w \in \{a, b\}^*$
 - III. Write differences between acceptor and transducer. 1.5x2+2=5
 - b) Draw dfa for the following languages:
 - I. $L = (ab+ba)^*bb$
 - II. Strings of $\{0, 1\}$ ended with 01. 2.5x2=5
 - c) Design a pda for $L=\{a^n b^{2n} : n>0\}$. Explain functioning of it with instantaneous description. 4+1=5
 - d) Write context free grammars for $L_1=\{a^n b^m c^n : n>0, m>0\}$ & $L_2=\{a^n b^n : n>0\}$ 2.5x2=5
 - e) Design a Turing machine for $L=\{a^n b^n c^n : n>0\}$.
 - f) Prove that $L=\{a^p : p \text{ is a prime}\}$ is not regular. State pigeonhole principle. 4+1=5

UNIT III

3. Answer any one of the following questions:

(10x1=10)

a) Find a regular expression for the following dfa.



Prove the following theorem by method of induction

$$1+2+3+\dots+n = n(n+1)/2$$

$$6+4=10$$

b) Use pumping lemma for context free languages to prove that following languages are not context free.

I. $L = \{ a^n b^n c^n : n > 0 \}.$

II. $L = \{ a^n b^m \mid n = m^2 \}$

$$5+5=10$$