Using Finite Elements to Solve Kuramoto-Sivashinsky PDE

by

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Kuramoto-Sivashinsky Equation

- Flame Equation
- Non-linear PDE
- Higher-order
- Time-dependent
- Can model Flame Dynamics

• Equation: $u_t + uu_x + u_{xx} + u_{xxxx} = 0$

Weak Form

```
F = (u_n1 * v * ufl.dx - u_n * v * ufl.dx +

dt * theta * linear_operator(u_n1) * v * ufl.dx +

dt * (1 - theta) * linear_operator(u_n) * v * ufl.dx +

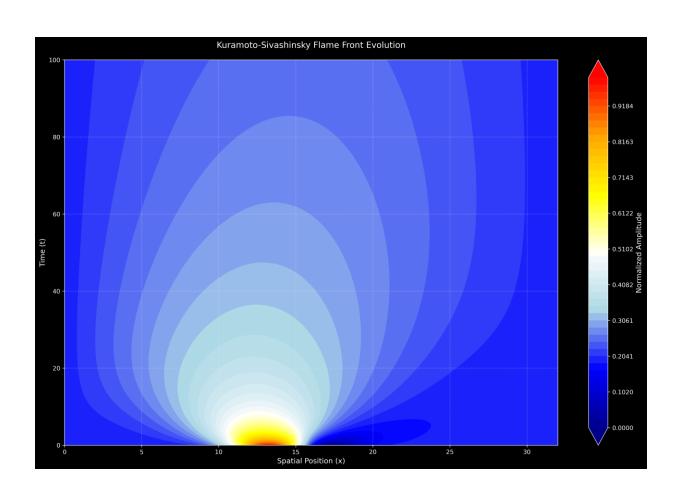
dt * nonlinear_operator(u_n1) * v * ufl.dx +

....)
```

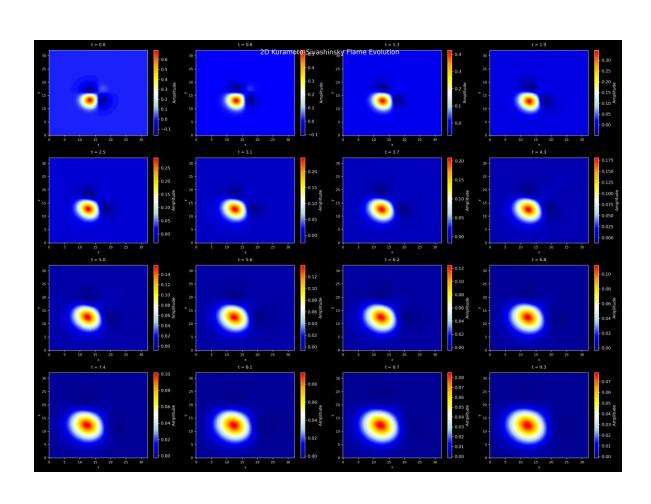
Solver – Kuramoto-Sivashinsky

- Spatial Finite Elements
- Time Crank-Nicholson
- Newton's Method
- GMRES with ILU

1D Results



2D Results



Project Checklist

- ✓ Non-linear PDE
- ✓ Derive Weak Form
- ✓ Time-marching Scheme
- ✓ Function Spaces
- ✓ Performance
- √ Verification