

LAB 4

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1 Report

In this lab we are trying to fit data computed using fourier series and lstsq to original functions e^x and $\cos(\cos x)$.

first we plotted e^x in semilog and $\cos(\cos x)$ in semilog and linear scales. These are shown in fig1 and fig2. The fourier series of e^x diverges from e^x since it is not periodic.

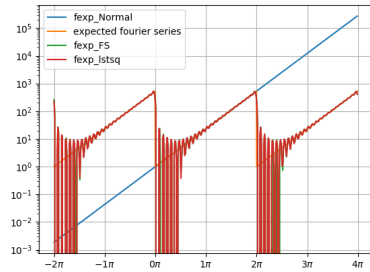


Figure 1: plot1

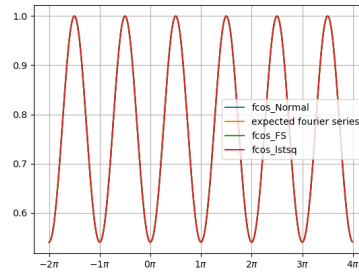


Figure 2: plot2

Then we tried to calculate fourier series coefficients of the functions and plotted them in both semilog and loglog axes. The plots for these are shown from fig3 to fig6.

Since $\cos(\cos x)$ is an even function coefficients of sine are nearly zero as $\sin(x)$ is an odd function.

Also, coefficients decay faster for $\cos(\cos x)$ because it is periodic. But for e^x , we need more frequencies to fit the function as it is not periodic.

Then we used least square method to find the fourier coefficients of the given

functions by creating a matrix A containing sine and cos harmonics upto 25^{th} order and column vector containing original values of functions called b.// By solving $Ac=b$ we can get c which contains the fourier coefficients.

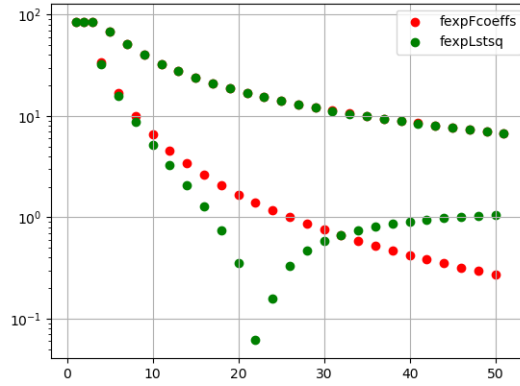


Figure 3: plot3

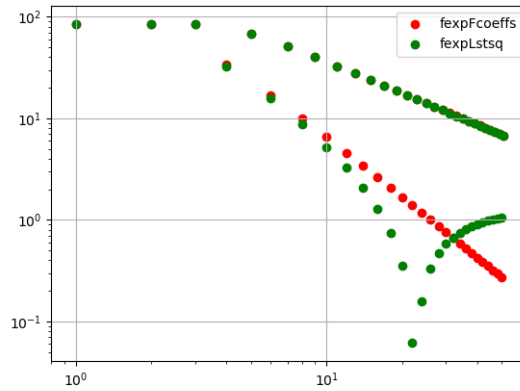


Figure 4: plot4

linearity of coefficients can be obtained by writing cos and sin in terms of e^{jw}, e^{-jw} .

Then we plotted these values from lstsq method in the corresponding plots. And hence the above plots are obtained.

Then we got the maximum deviation between coefficients calculated in both

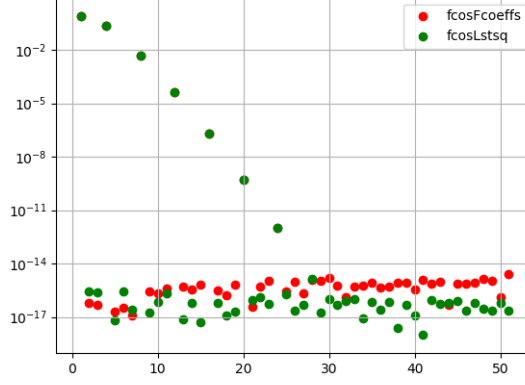


Figure 5: plot5

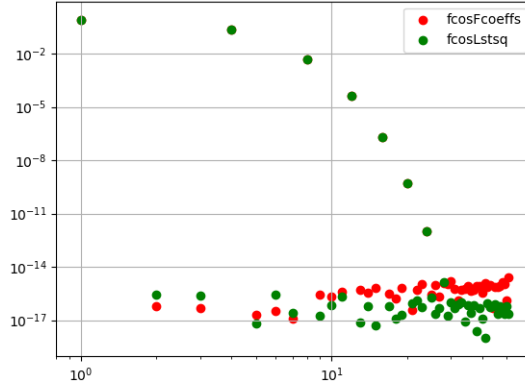


Figure 6: plot6

these methods as 1.3327308 for e^x and $2.5816134 \cdot 10^{-15}$ for $\cos(\cos x)$

Lastly, we plotted the functions using the fourier series and (least square estimate). we find that both the functions fit perfectly for $\cos(\cos x)$ but not for e^x because $\cos(\cos x)$ is periodic and e^x is not periodic. The least square is more accurate compared to fourier series