

Unidad 5

Rasterización

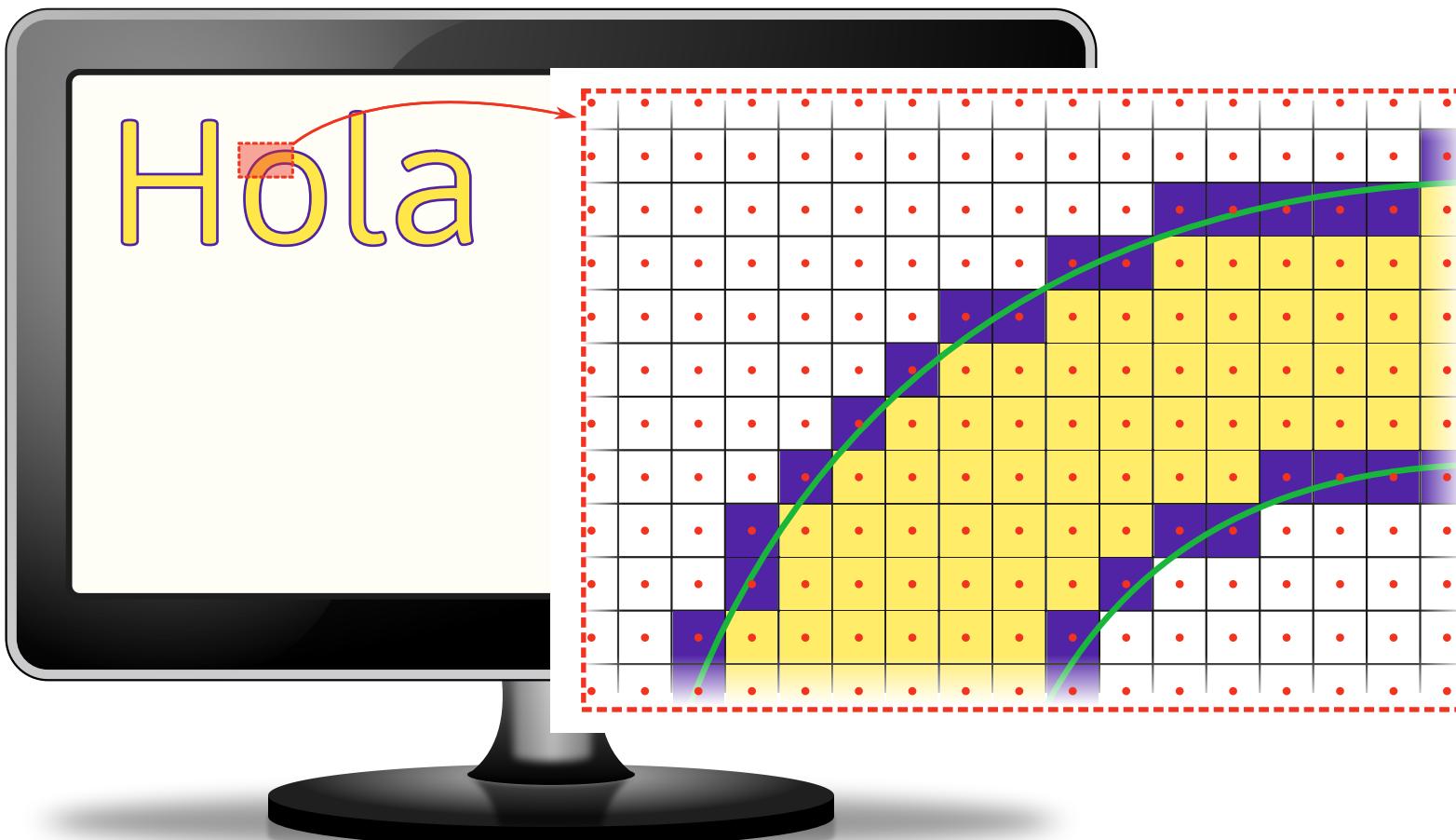
Raster vs Vector

Raster

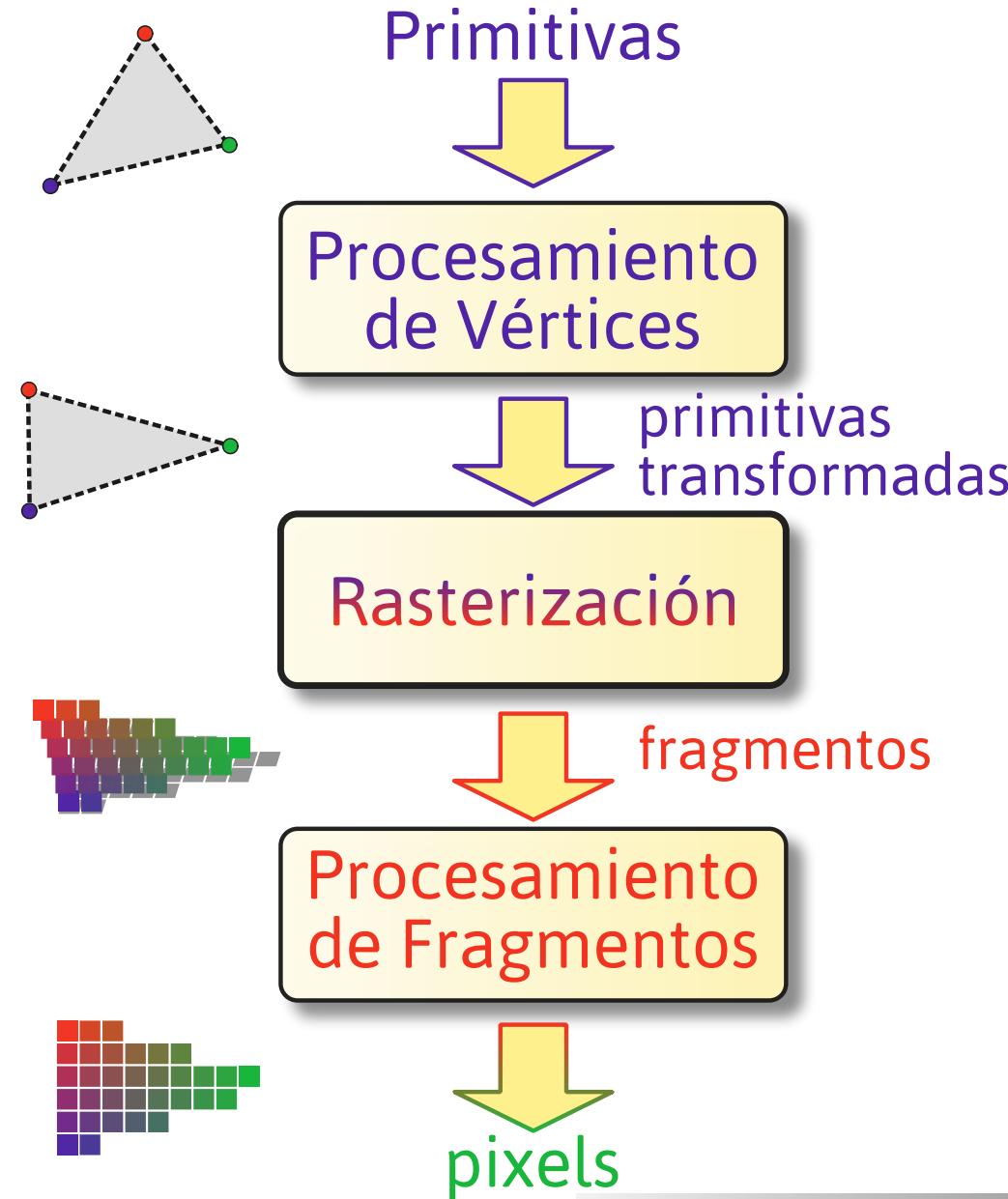
vs

Vector

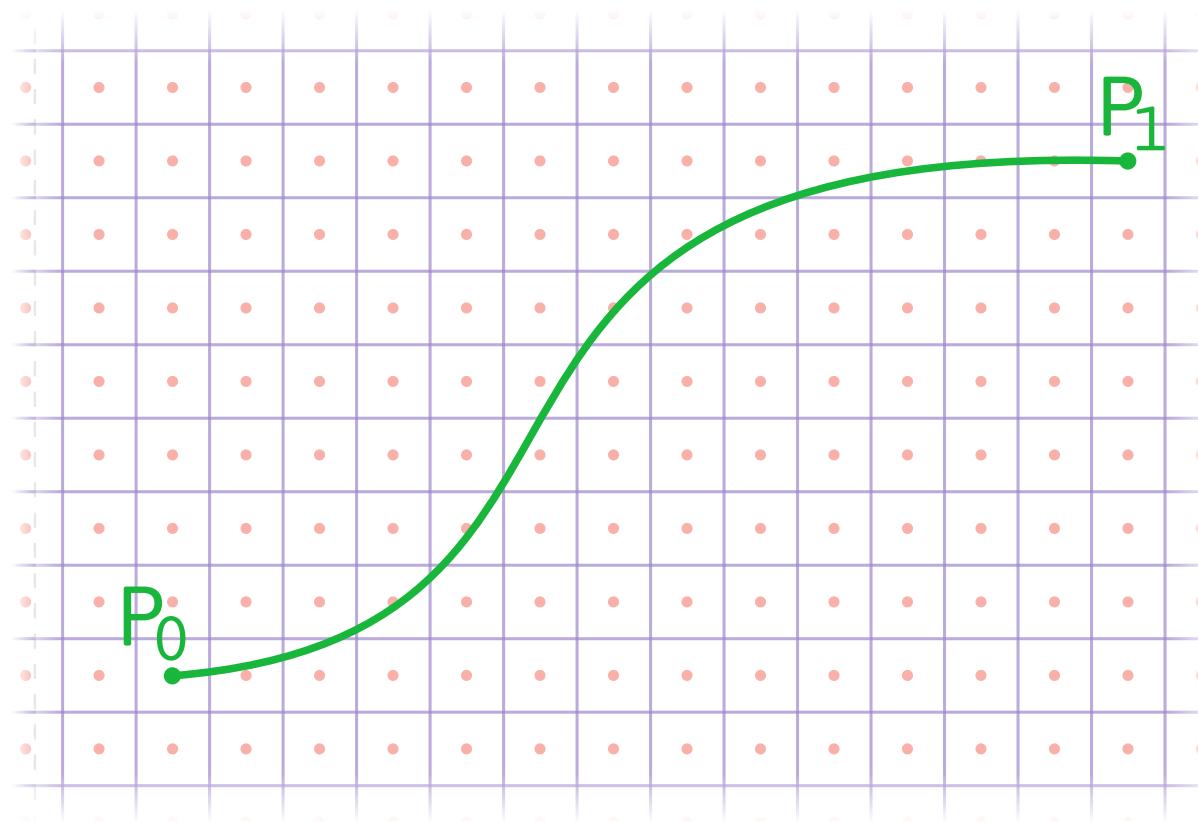
Rasterización o Scan-Conversion



La Rasterización en el Pipeline



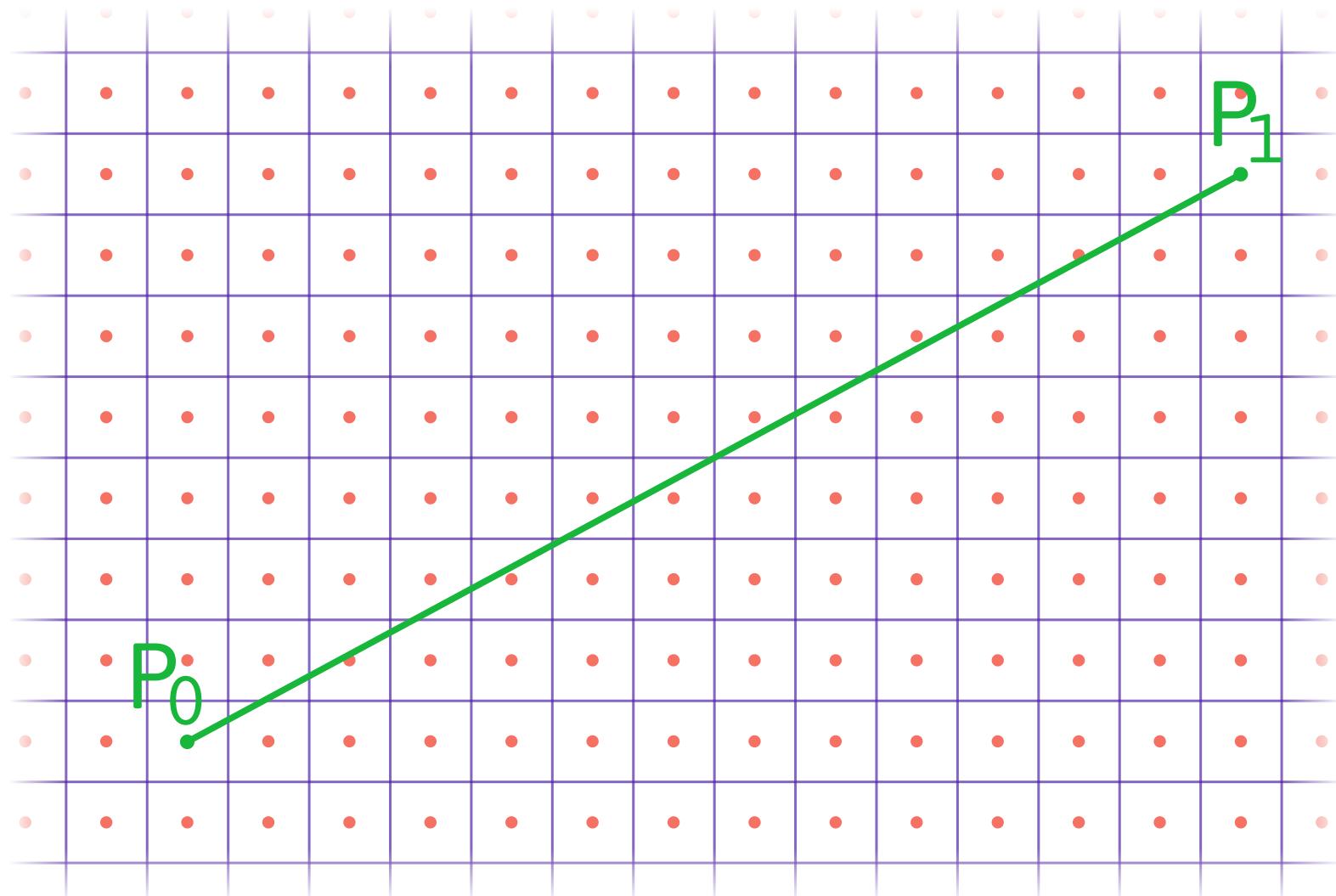
Requerimientos



1. Representación Adecuada
2. Contigüidad (water-tight)
3. Eficiencia y Robustez

$$\max(\Delta x, \Delta y) \leq 1$$

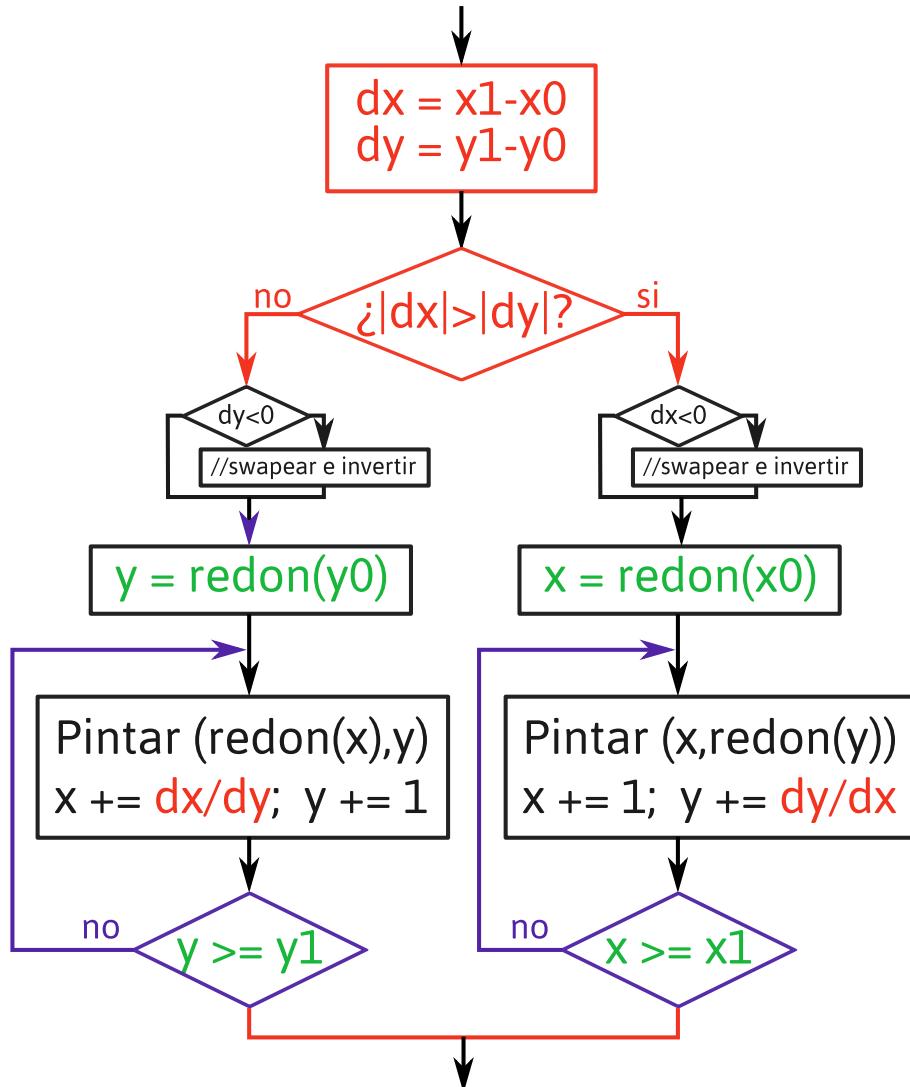
Rasterización o Scan-Conversion



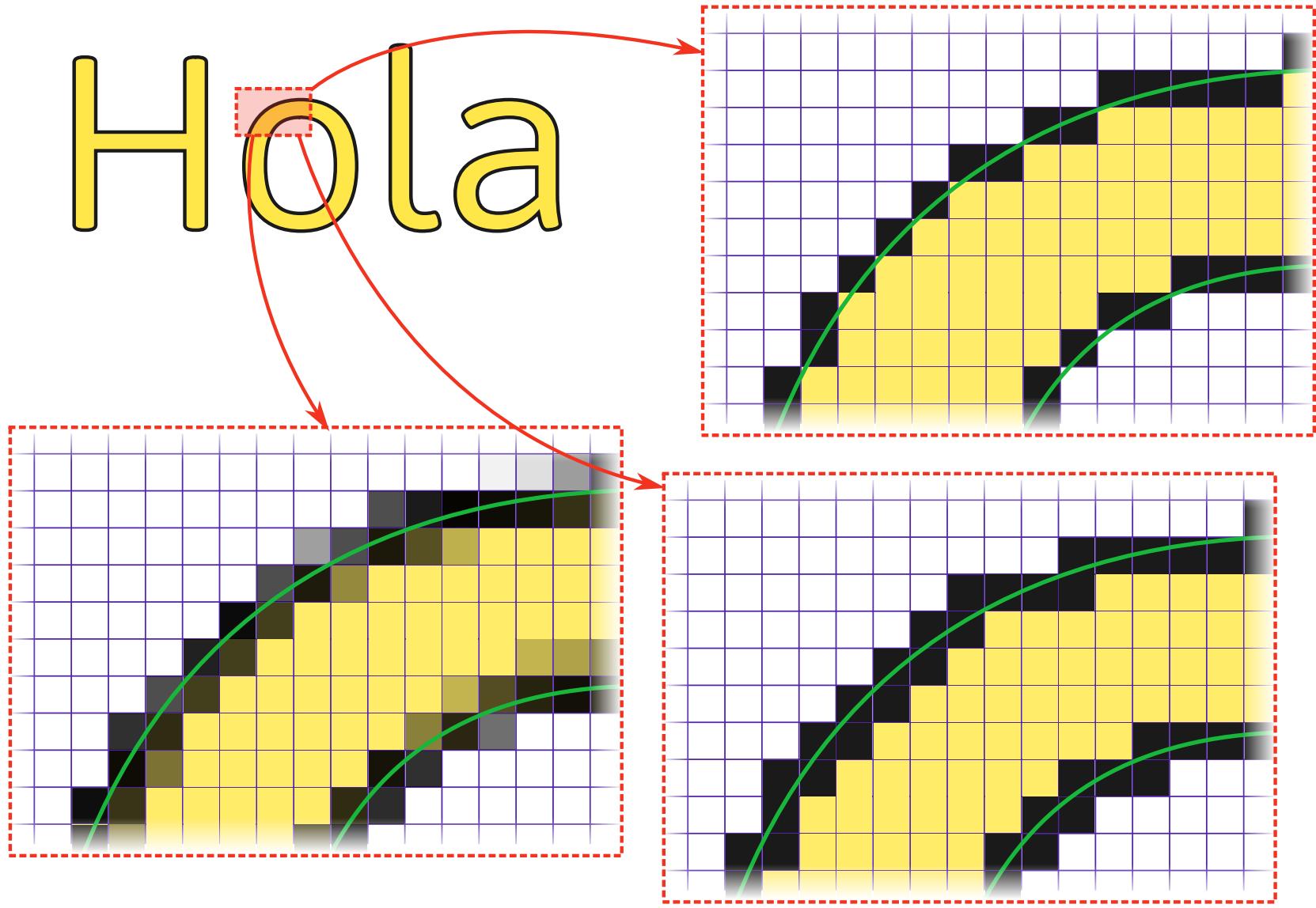
Linea DDA

Linea DDA

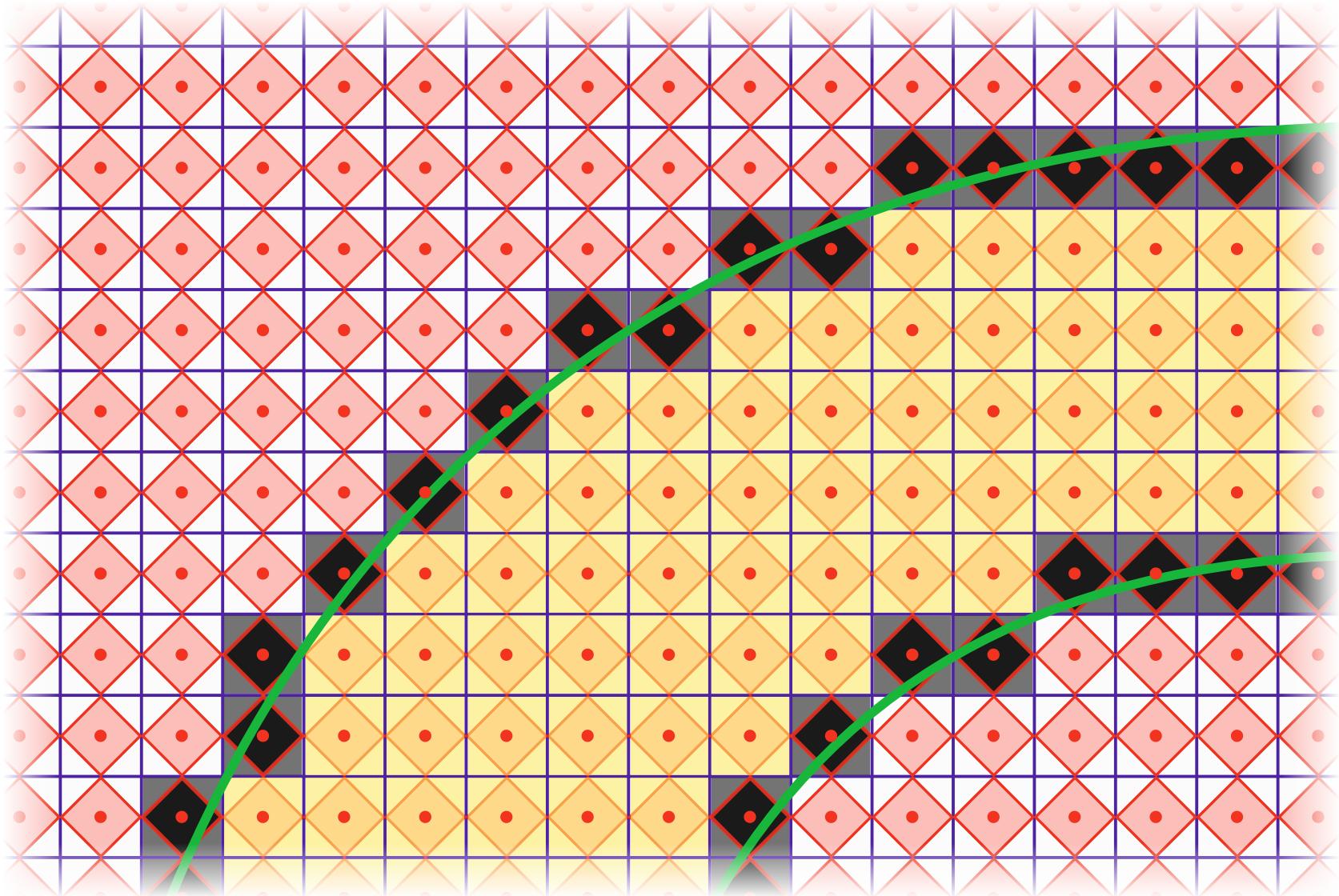
in: x_0, y_0, x_1, y_1



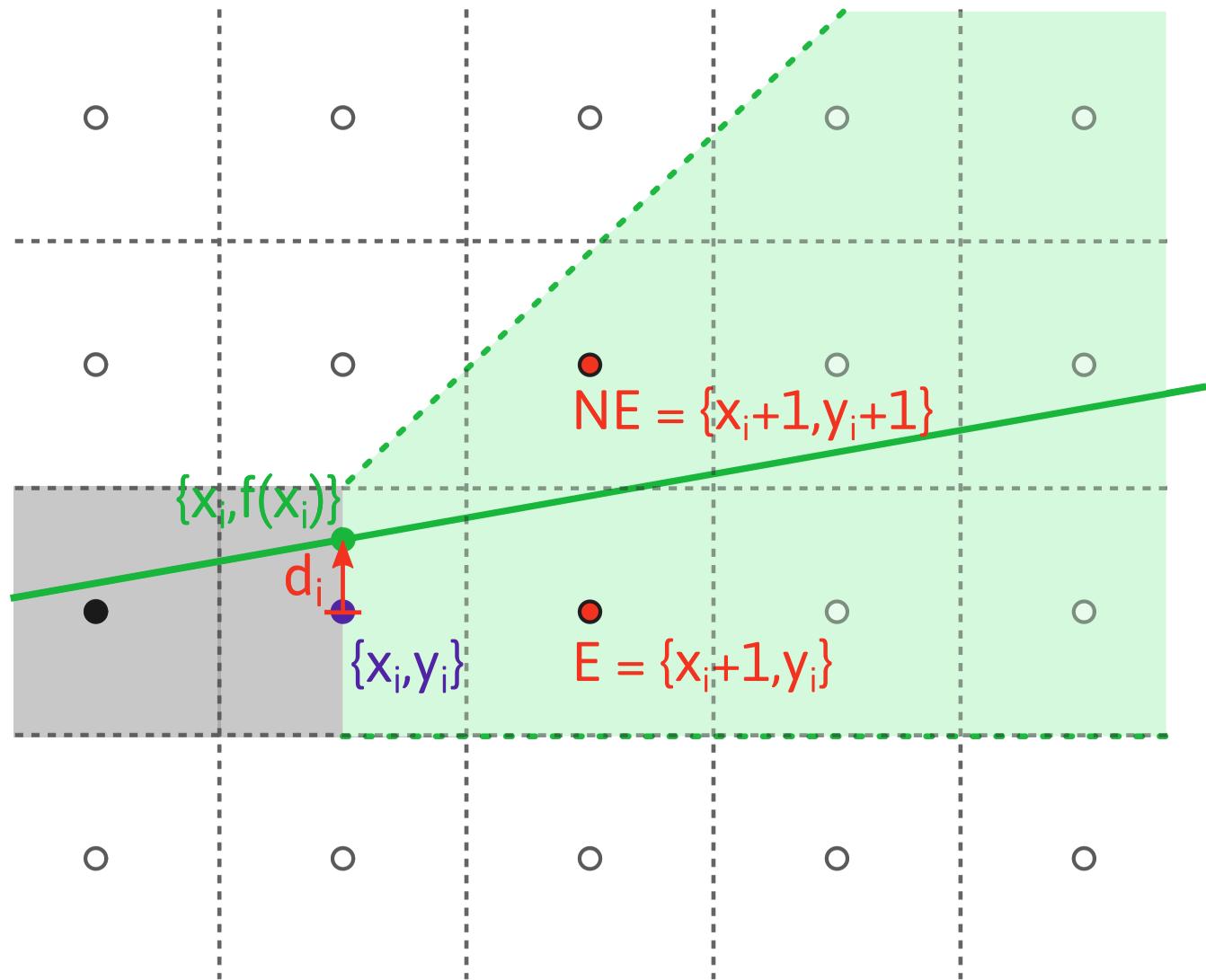
Rasterización o Scan-Conversion



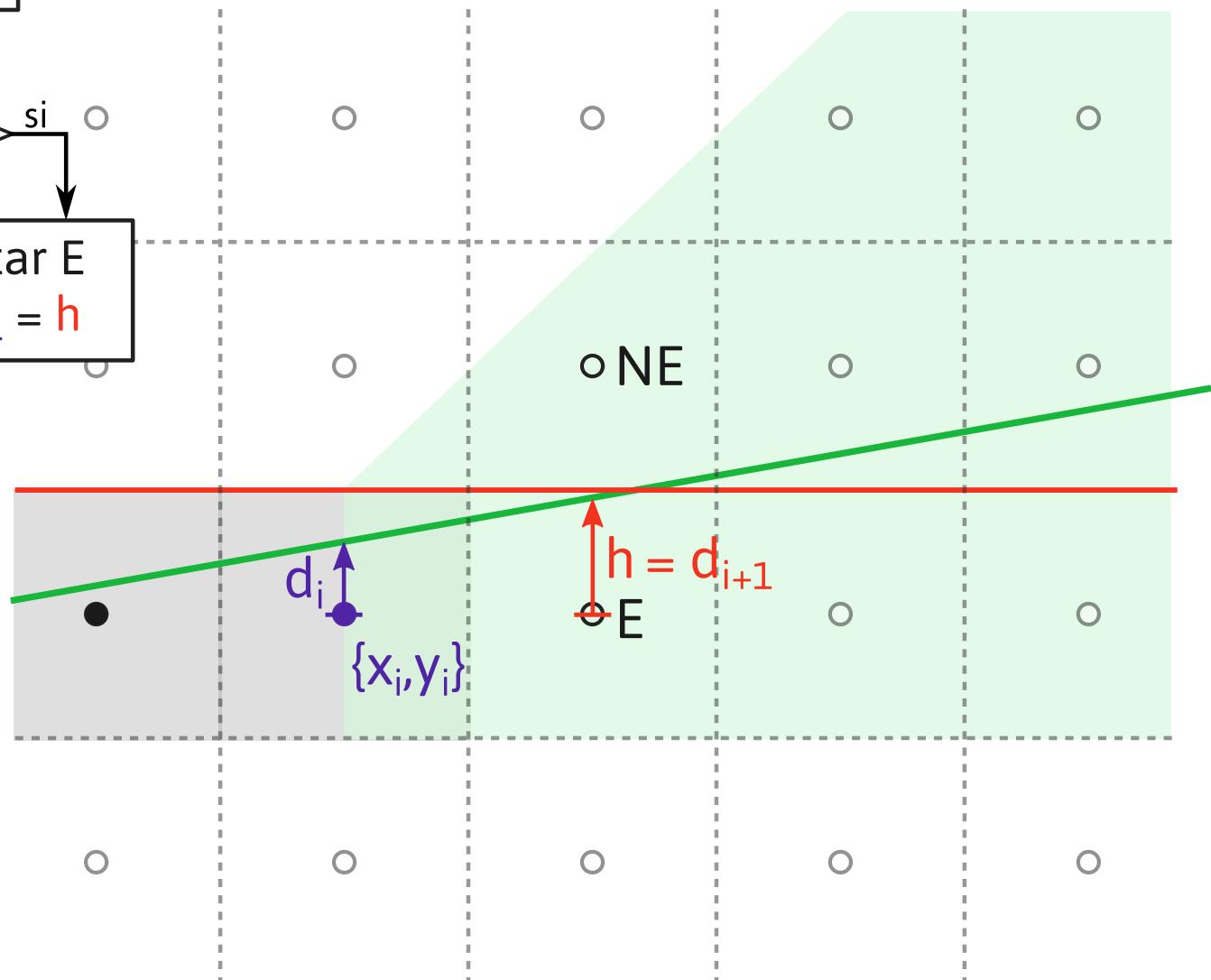
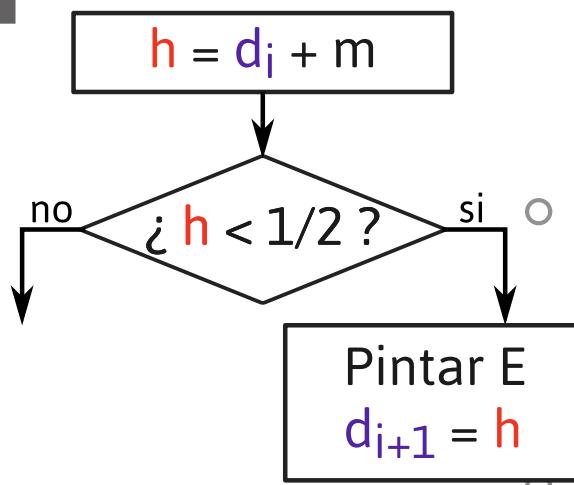
Rasterización o Scan-Conversion



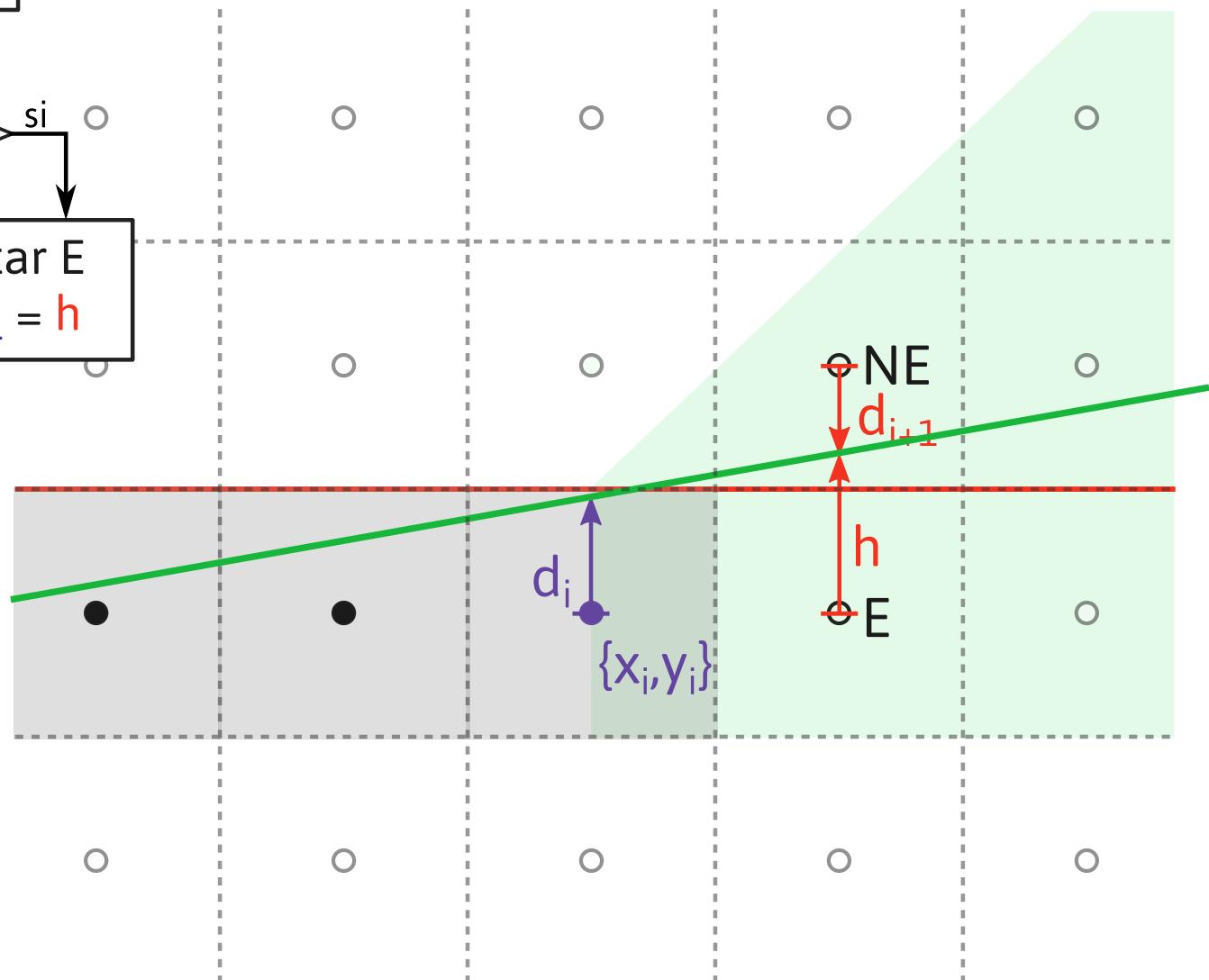
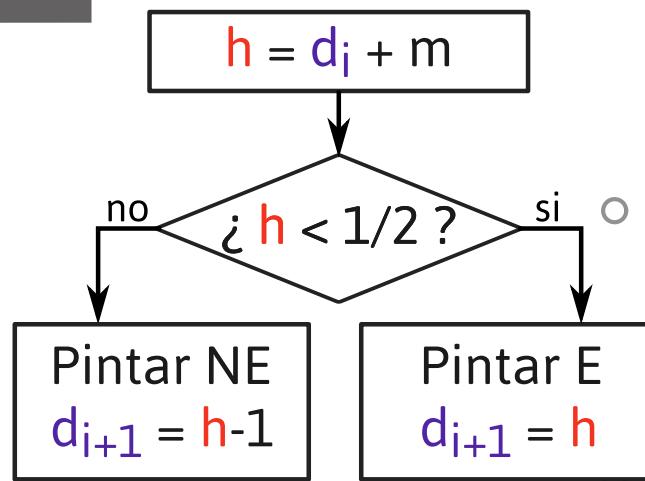
Algoritmo de linea de Bresenham



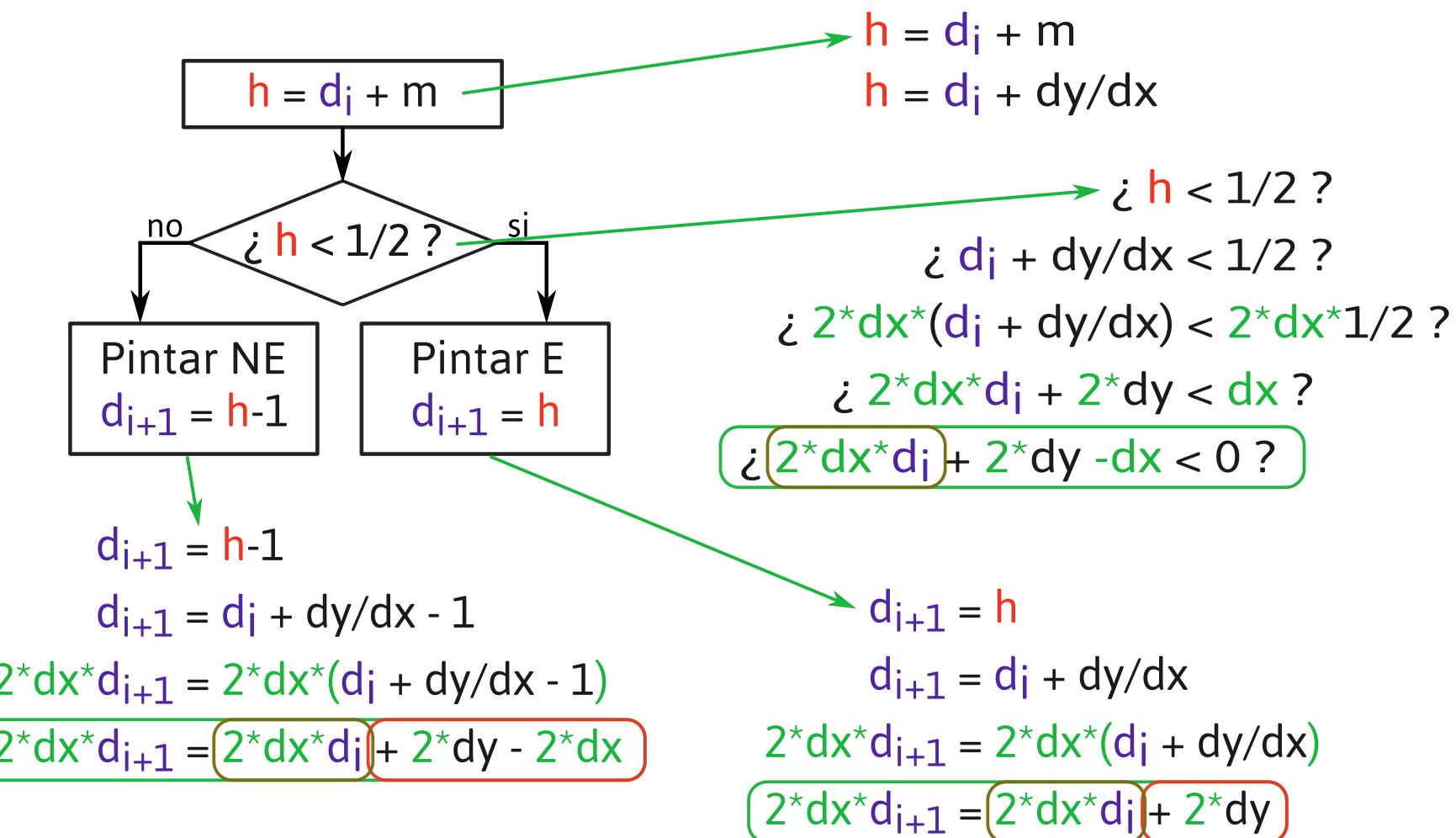
Algoritmo de linea de Bresenham



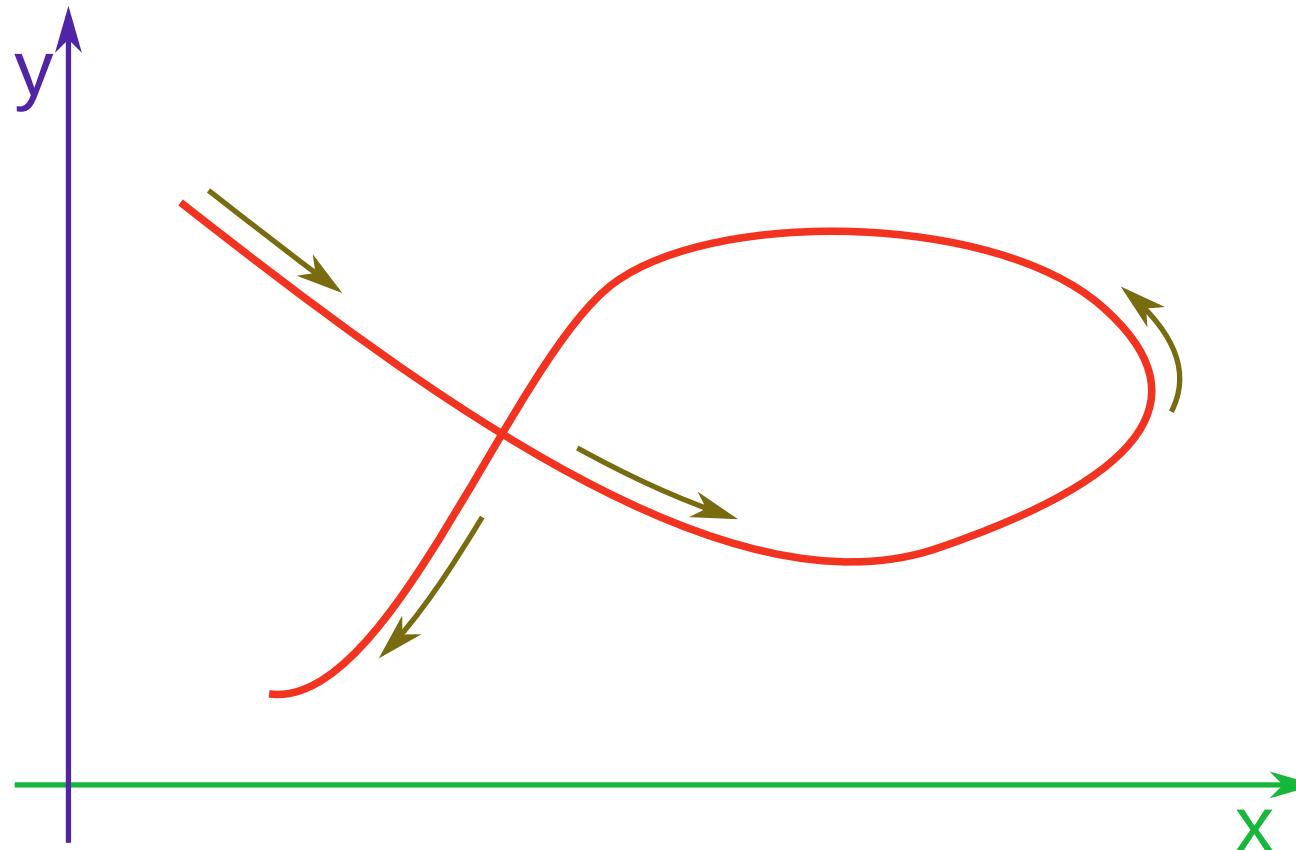
Algoritmo de linea de Bresenham



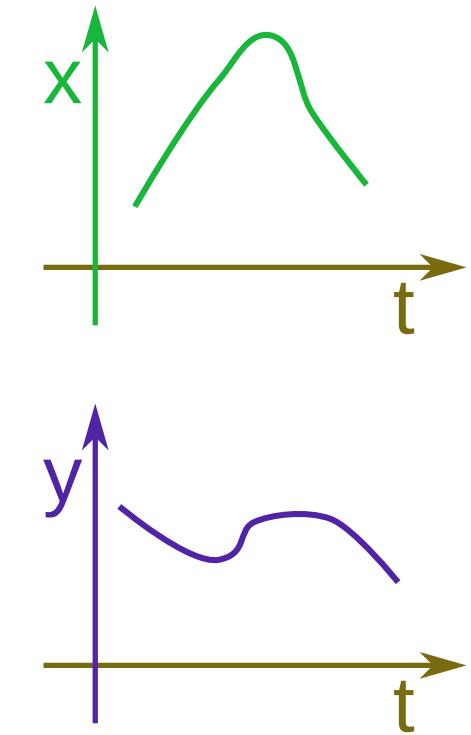
Algoritmo de linea de Bresenham



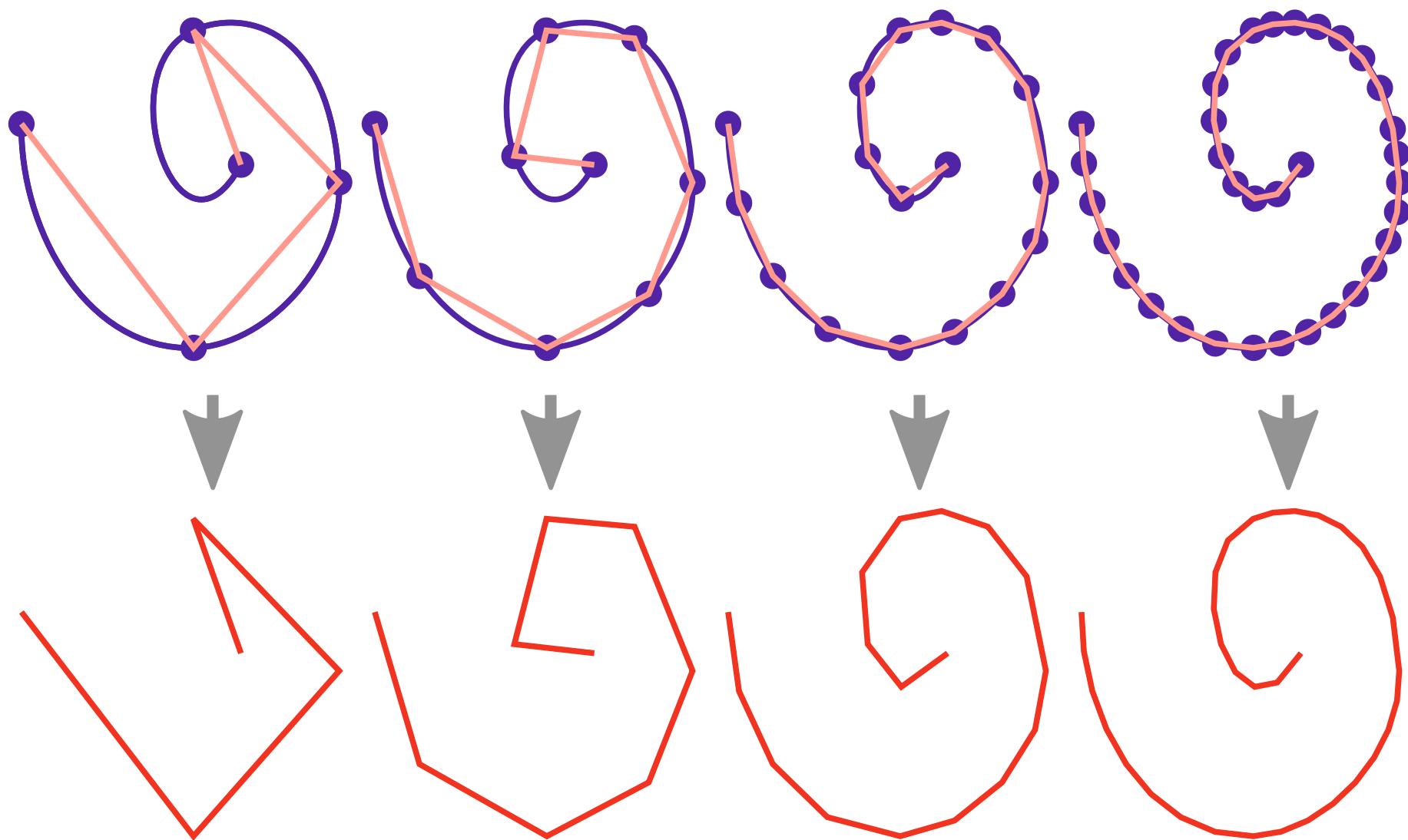
Curvas Paramétricas



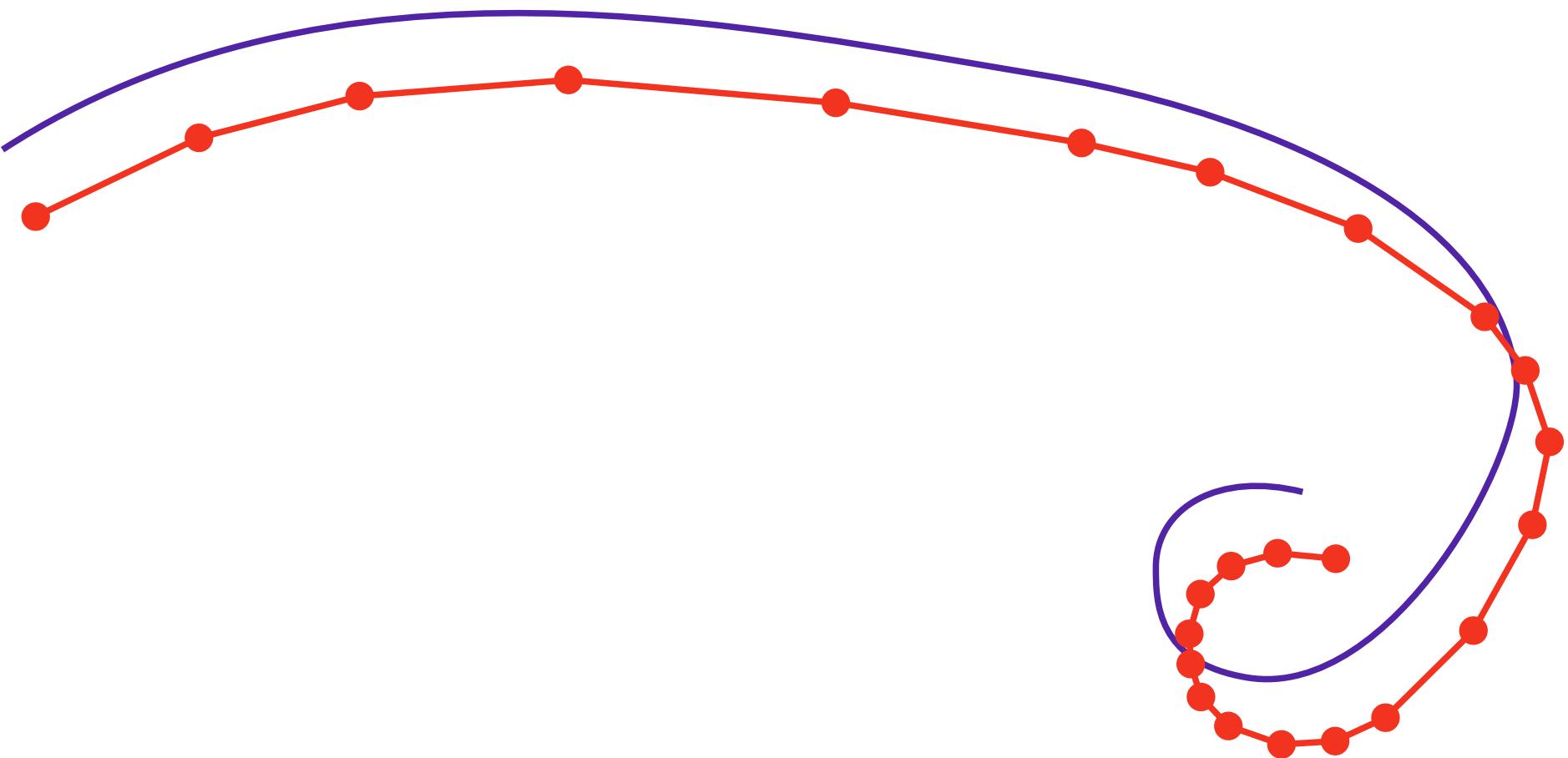
$$y=f(t) \quad x = g(t) \quad t \in [t_0; t_1]$$



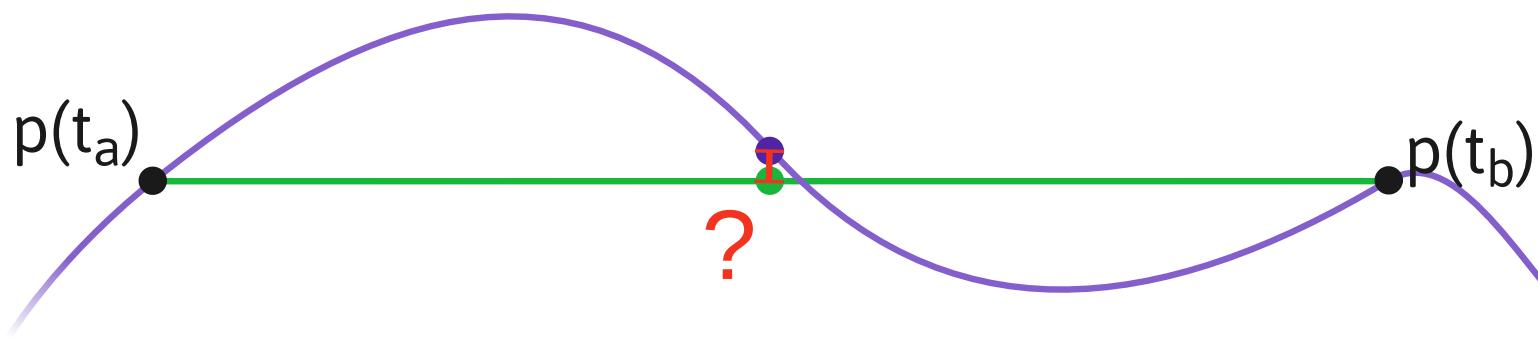
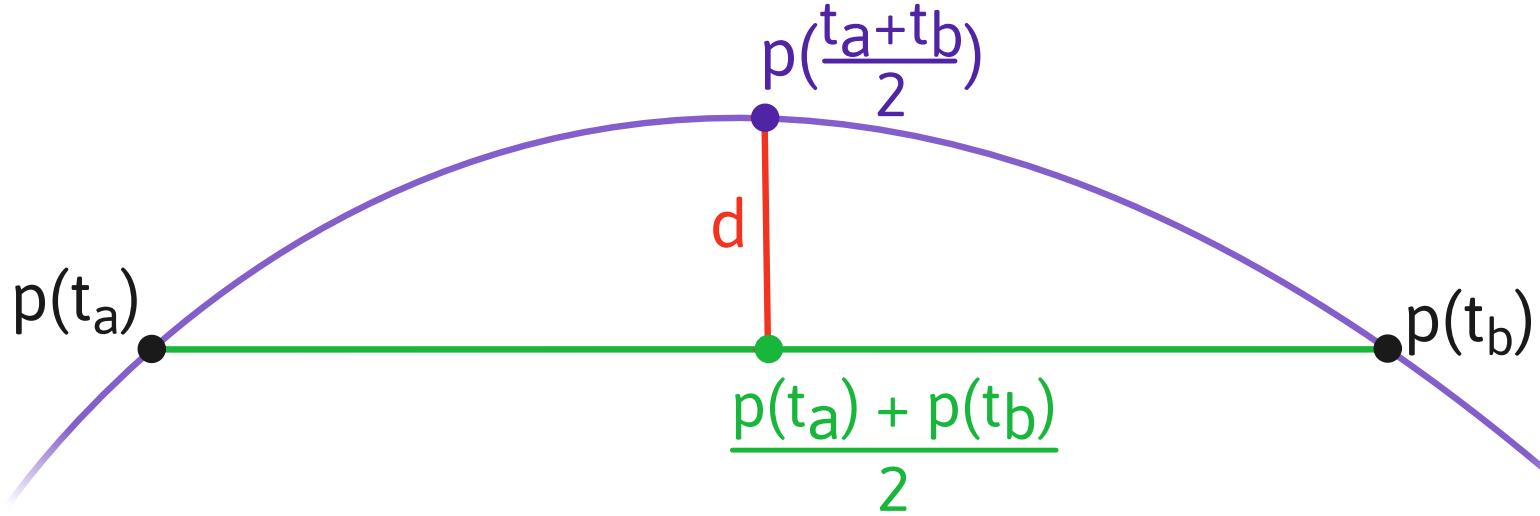
Rasterización por Subdivisiones



Rasterización por Subdivisiones



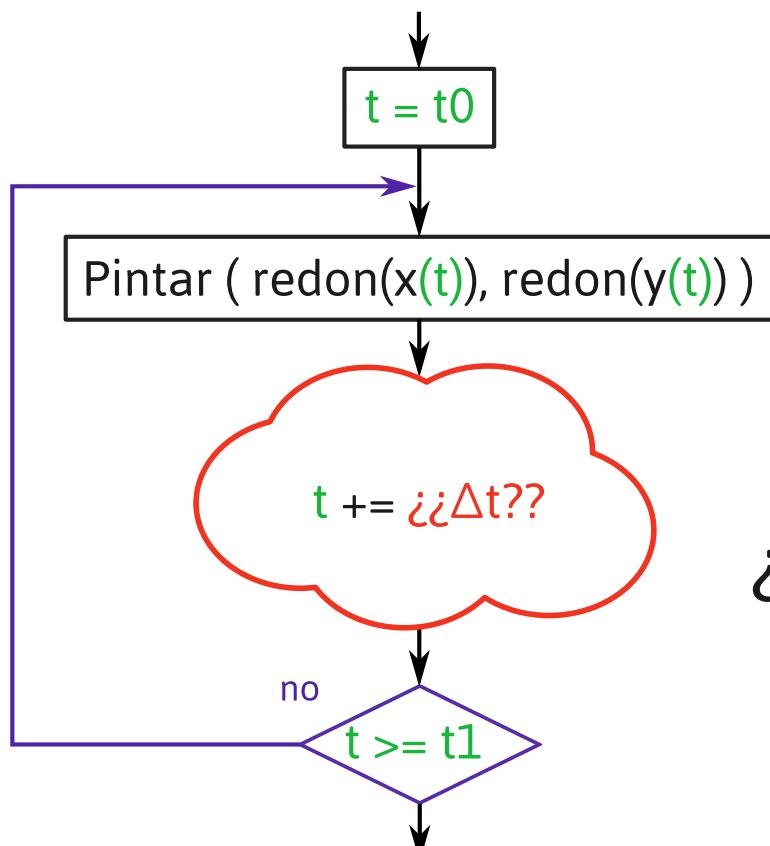
Rasterización por Subdivisiones



Rasterización de curvas por Derivadas

Curva DDA

in: $x(t)$, $y(t)$, $dx(y)$, $dy(t)$, t_0 , t_1

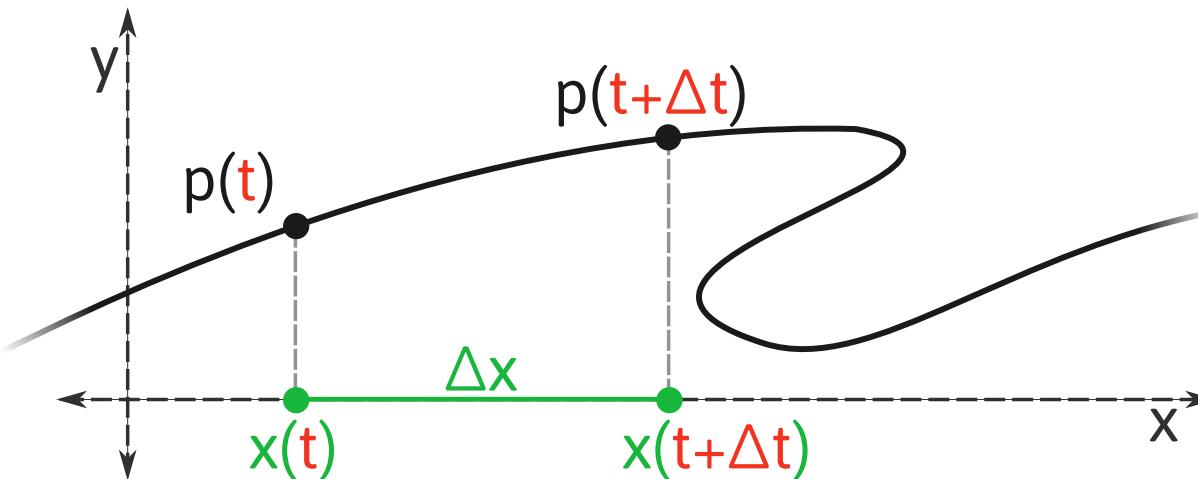


contigüidad: $\max(\Delta x, \Delta y) \leq 1$

$$\begin{aligned} \Delta t \mid \max(\Delta x, \Delta y) = 1 \\ \Delta x = 1 \quad \text{ó} \quad \Delta y = 1 \\ ? \Delta t_x = f(\Delta x) ? \\ \Delta t_x = f(1) \\ ? \Delta t_y = g(\Delta y) ? \\ \Delta t_y = g(1) \\ \Delta t = \min(\Delta t_x, \Delta t_y) \end{aligned}$$

Rasterización de curvas por Derivadas

? Δt | $\Delta x = 1$?



$$\Delta x = x(t+\Delta t) - x(t)$$

$$x(t+\Delta t) \approx x(t) + \Delta t x'(t)$$

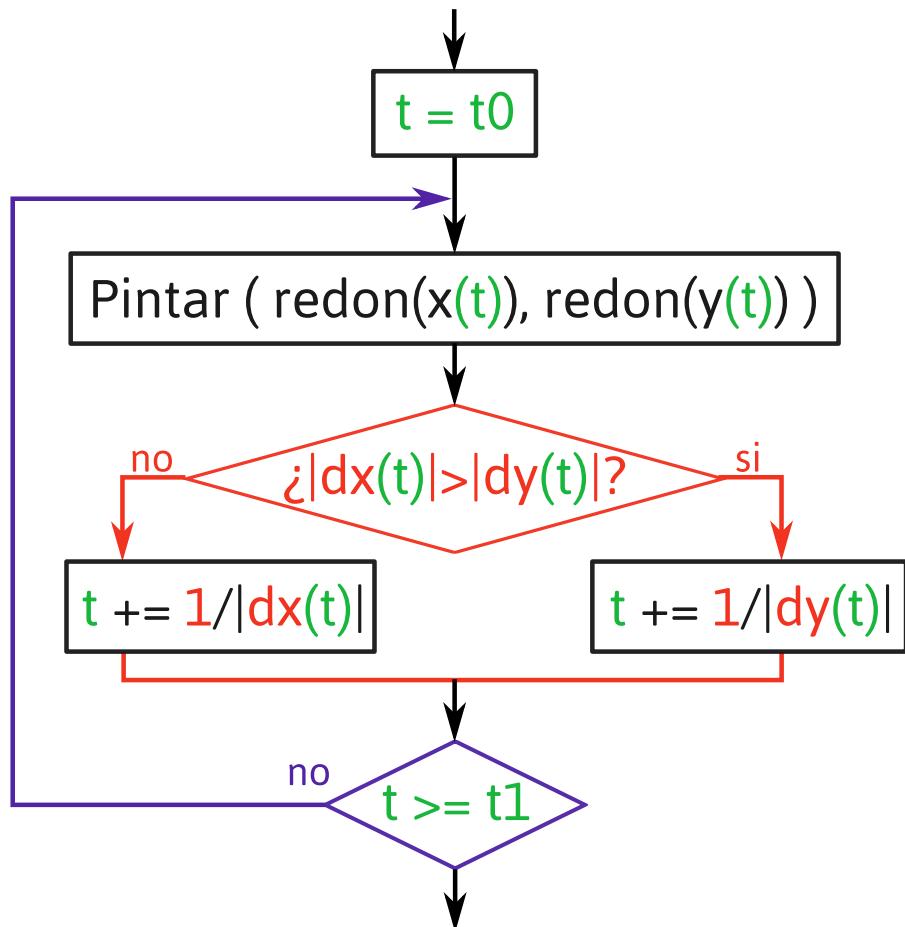
$$\Delta x \approx x(t) + \Delta t x'(t) - x(t)$$

$$\Delta x \approx \Delta t x'(t) \rightarrow 1 \approx \Delta t x'(t) \rightarrow \Delta t \approx 1 / x'(t)$$

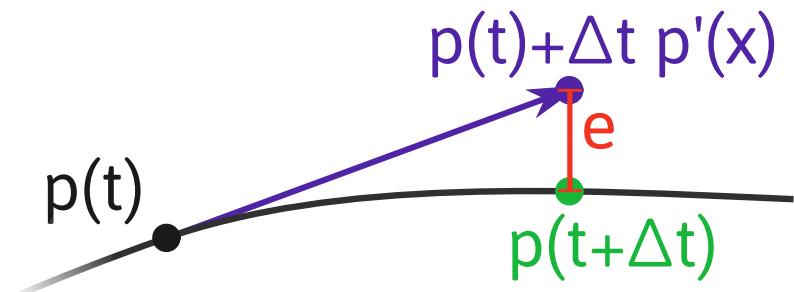
Rasterización de curvas por Derivadas

Curva DDA

in: $x(t), y(t), dx(y), dy(t), t_0, t_1$



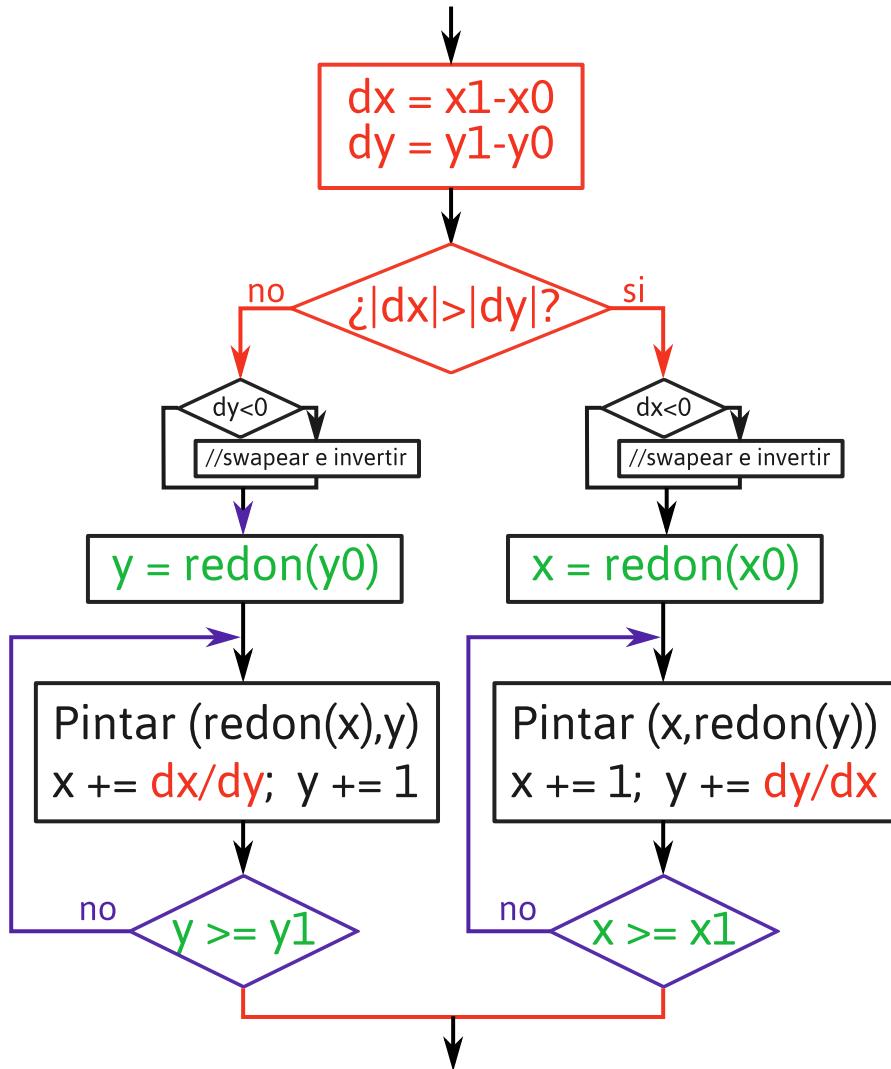
$$\begin{aligned}\Delta t &= \min(\Delta t_x, \Delta t_y) \\ \Delta t_x &\approx 1 / |x'(t)| \longrightarrow \\ \Delta t &= \min(1/|x'(t)|, 1/|y'(t)|) \\ \Delta t &= 1 / \max(|x'(t)|, |y'(t)|)\end{aligned}$$



Rasterización por DDA: Linea vs Curva

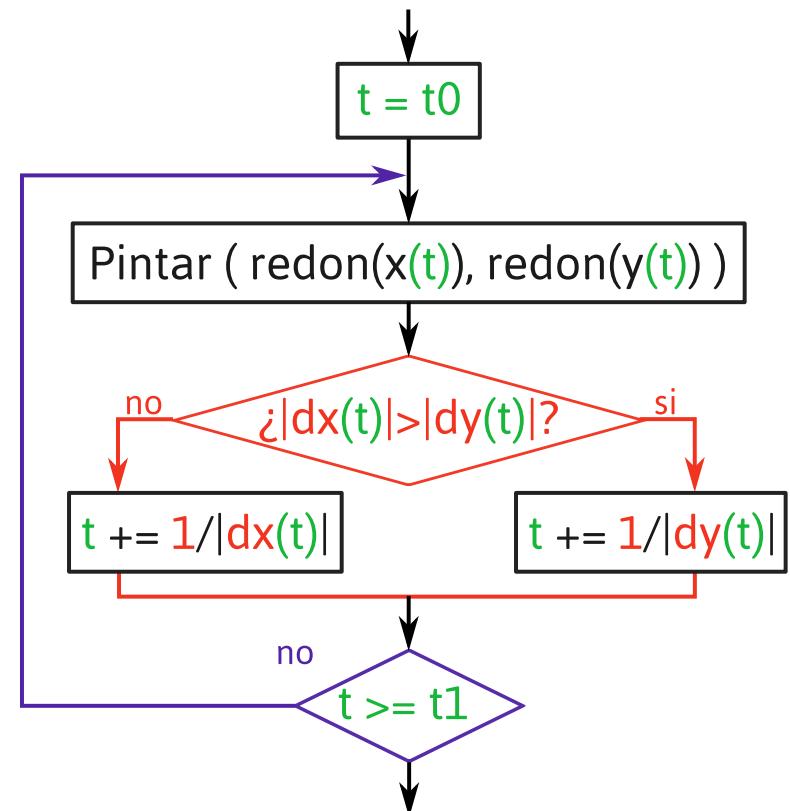
Linea DDA

in: x_0, y_0, x_1, y_1

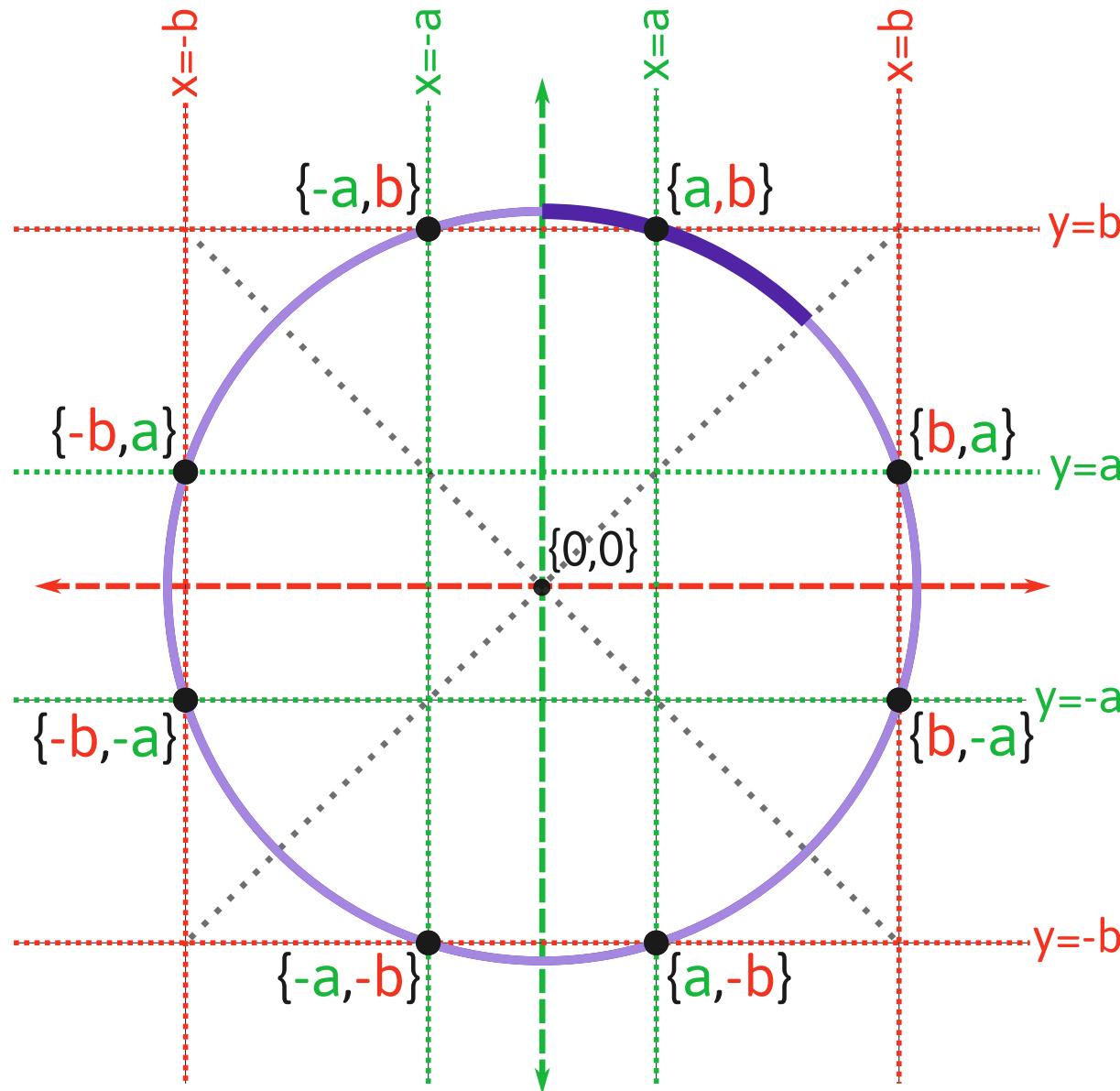


Curva DDA

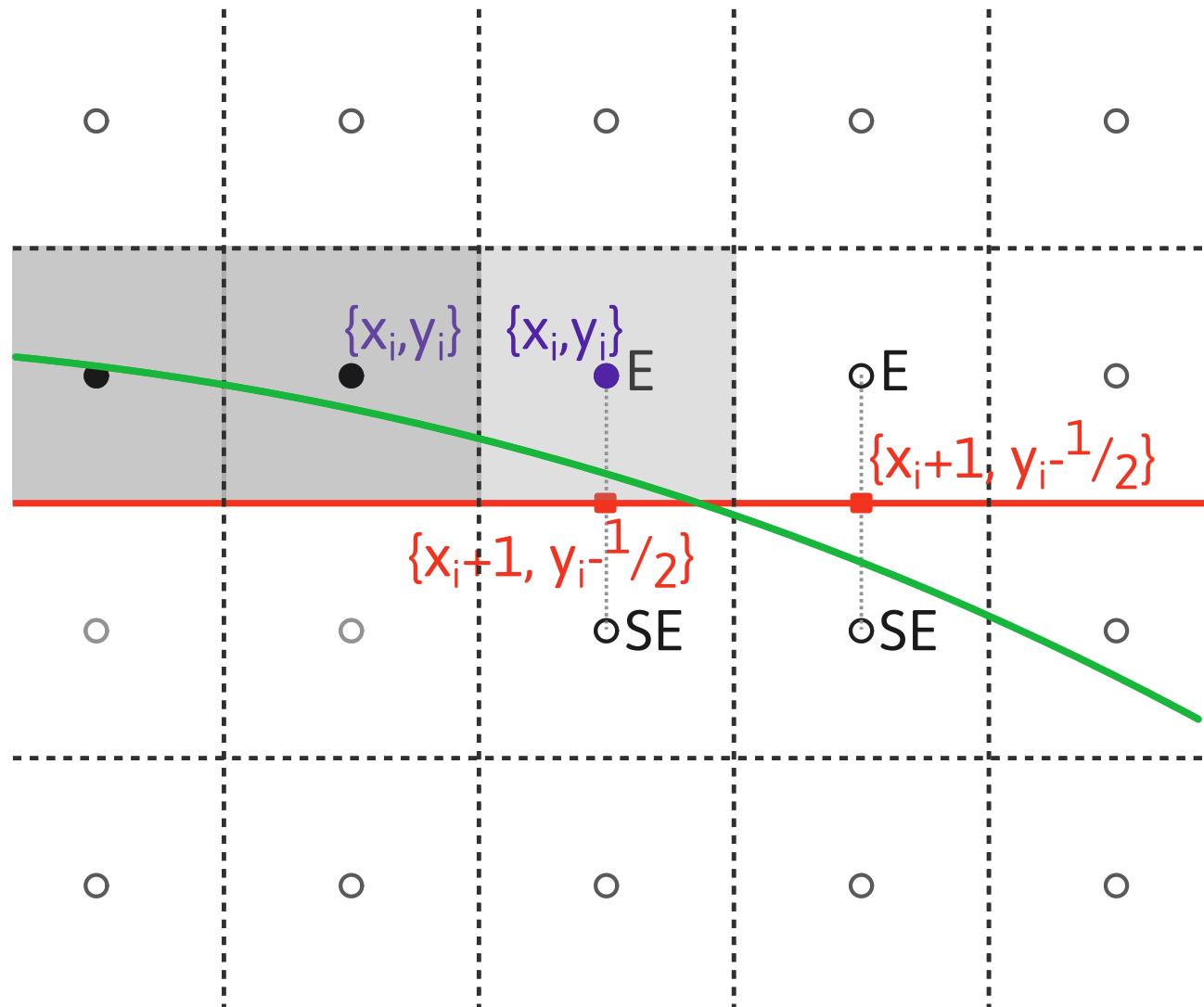
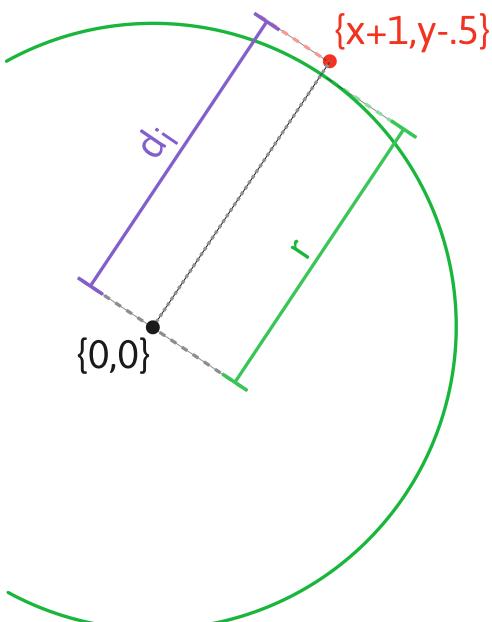
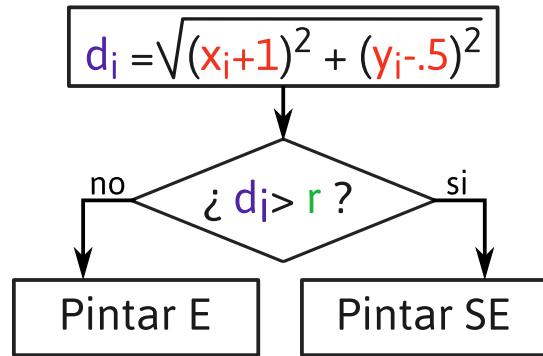
in: $x(t), y(t), dx(y), dy(t), t_0, t_1$



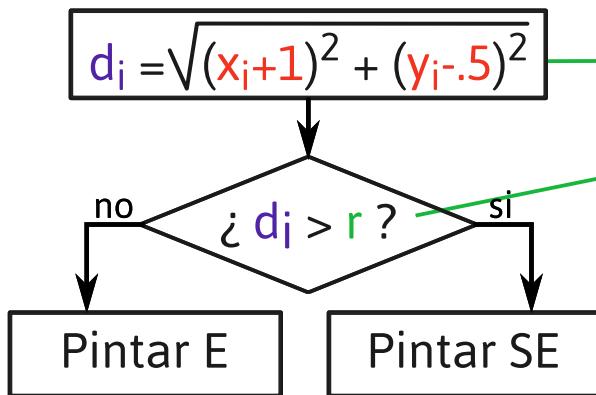
Rasterización de Circunferencias



Algoritmo de Circunferencias de Bresenham

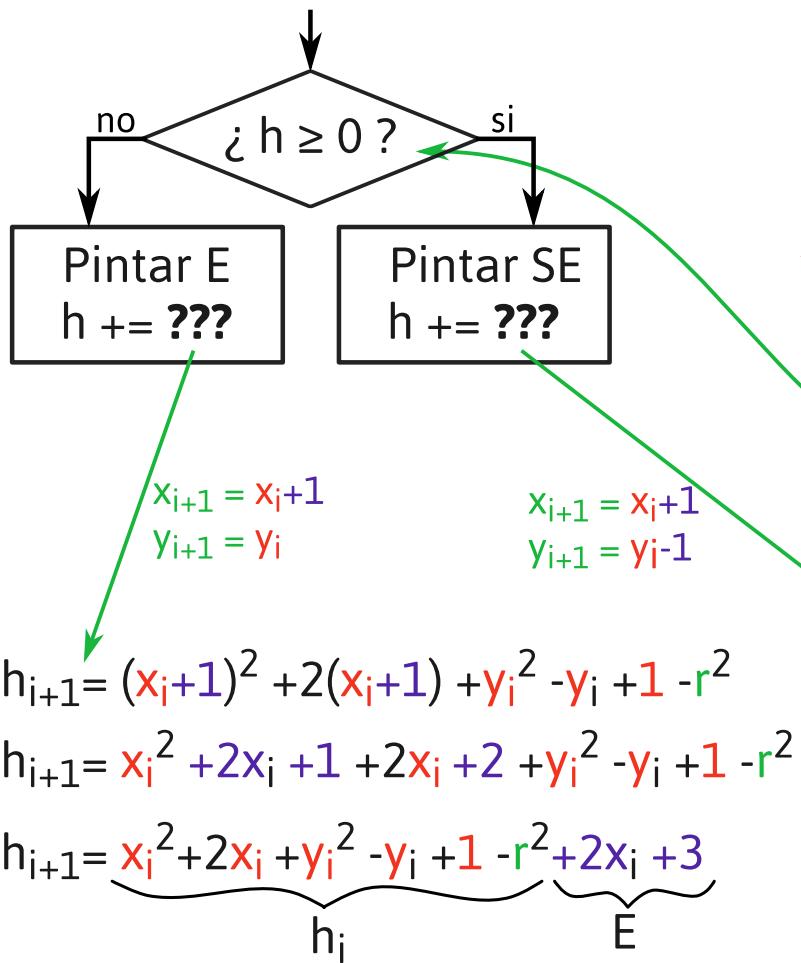


Algoritmo de Circunferencias de Bresenham



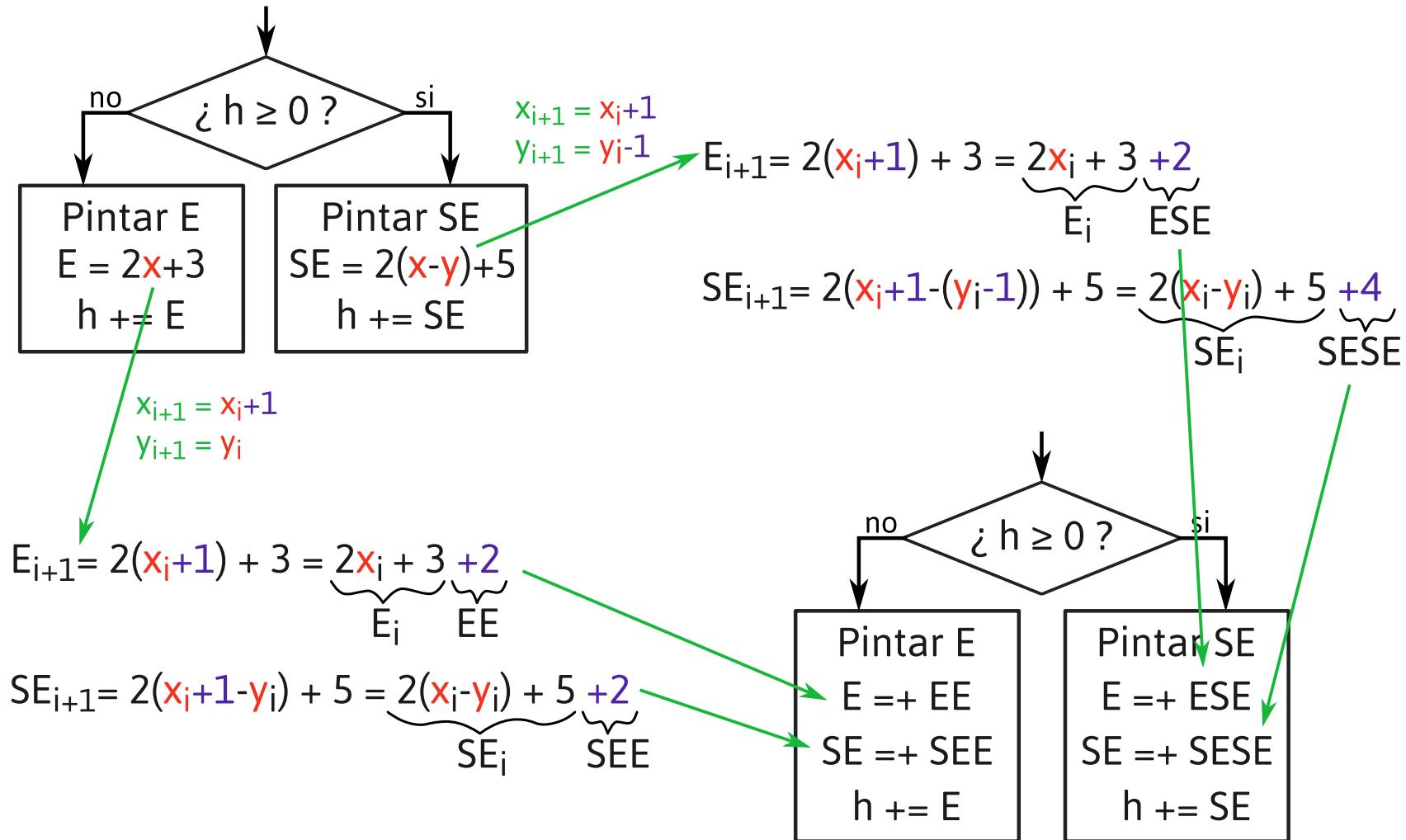
$$\begin{aligned} & \sqrt{(x_i+1)^2 + (y_i-.5)^2} > r \\ & (x_i+1)^2 + (y_i-.5)^2 > r^2 \\ & (x_i+1)^2 + (y_i-.5)^2 - r^2 > 0 \\ & x_i^2 + 2x_i + 1 + y_i^2 + 2y_i(-.5) + (-.5)^2 - r^2 > 0 \\ & x_i^2 + 2x_i + y_i^2 - y_i + 1.25 - r^2 > 0 \\ & x_i^2 + 2x_i + y_i^2 - y_i + 1 - r^2 > -0.25 \\ & \underbrace{x_i^2 + 2x_i + y_i^2 - y_i + 1 - r^2}_{h_i} \geq 0 \end{aligned}$$

Algoritmo de Circunferencias de Bresenham

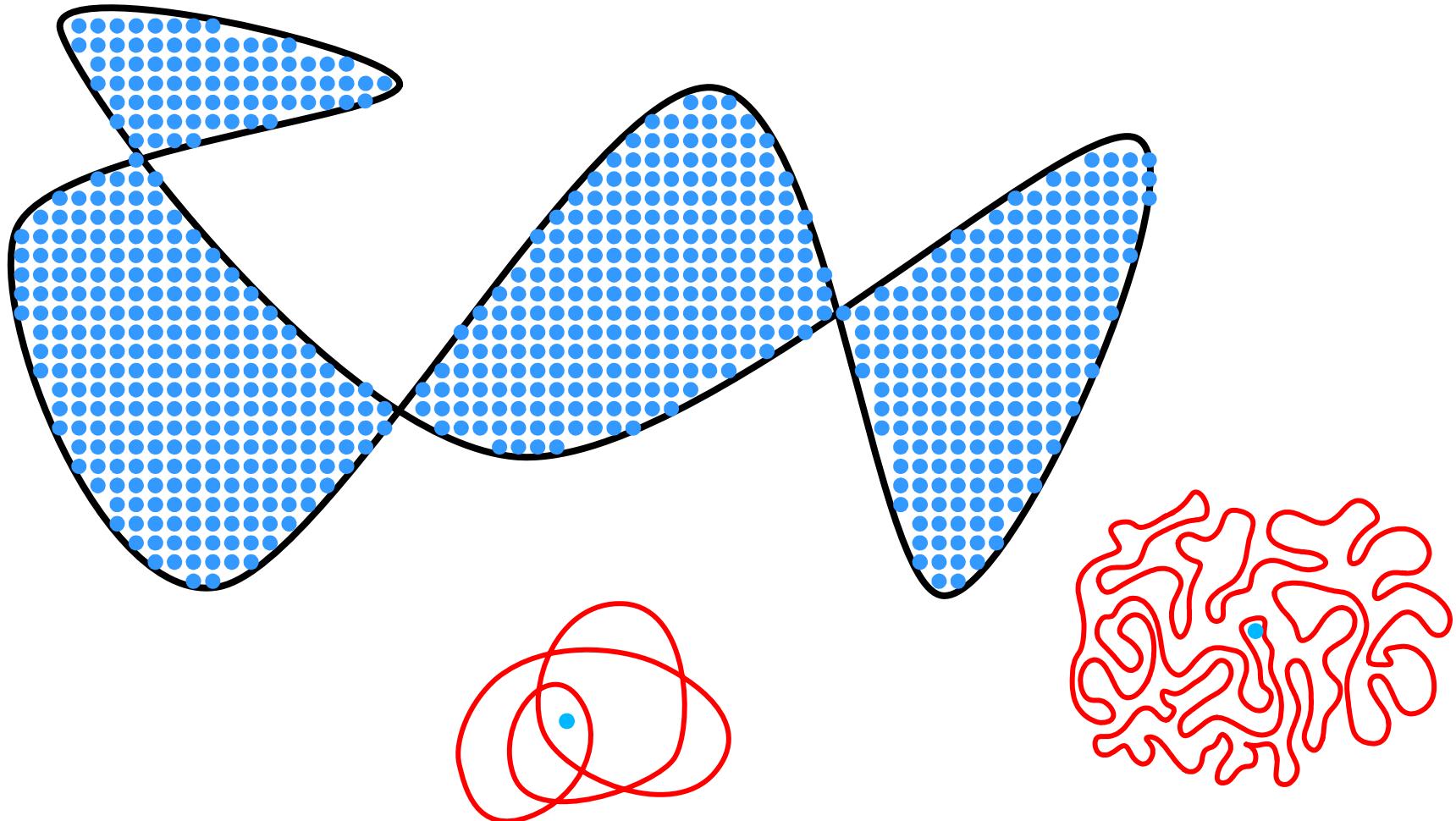


$$\begin{aligned}
 & \sqrt{(x_i+1)^2 + (y_i-0.5)^2} > r \\
 & (x_i+1)^2 + (y_i-0.5)^2 > r^2 \\
 & (x_i+1)^2 + (y_i-0.5)^2 - r^2 > 0 \\
 & x_i^2 + 2x_i + 1 + y_i^2 + 2y_i(-0.5) + (-0.5)^2 - r^2 > 0 \\
 & x_i^2 + 2x_i + y_i^2 - y_i + 1.25 - r^2 > 0 \\
 & x_i^2 + 2x_i + y_i^2 - y_i + 1 - r^2 > -0.25 \\
 & \underbrace{x_i^2 + 2x_i + y_i^2 - y_i + 1 - r^2}_{h_i} \geq 0 \\
 & h_{i+1} = (x_{i+1})^2 + 2(x_{i+1}) + (y_{i-1})^2 - (y_{i-1}) + 1 - r^2 \\
 & h_{i+1} = x_i^2 + 2x_i + 1 + 2x_i + 2 + y_i^2 - 2y_i^2 + 1 + y_i + 1 - r^2 \\
 & h_{i+1} = \underbrace{x_i^2 + 2x_i + y_i^2 + y_i + 1 - r^2}_{h_i} + \underbrace{2x_i - 2y_i + 5}_{SE}
 \end{aligned}$$

Algoritmo de Circunferencias de Bresenham

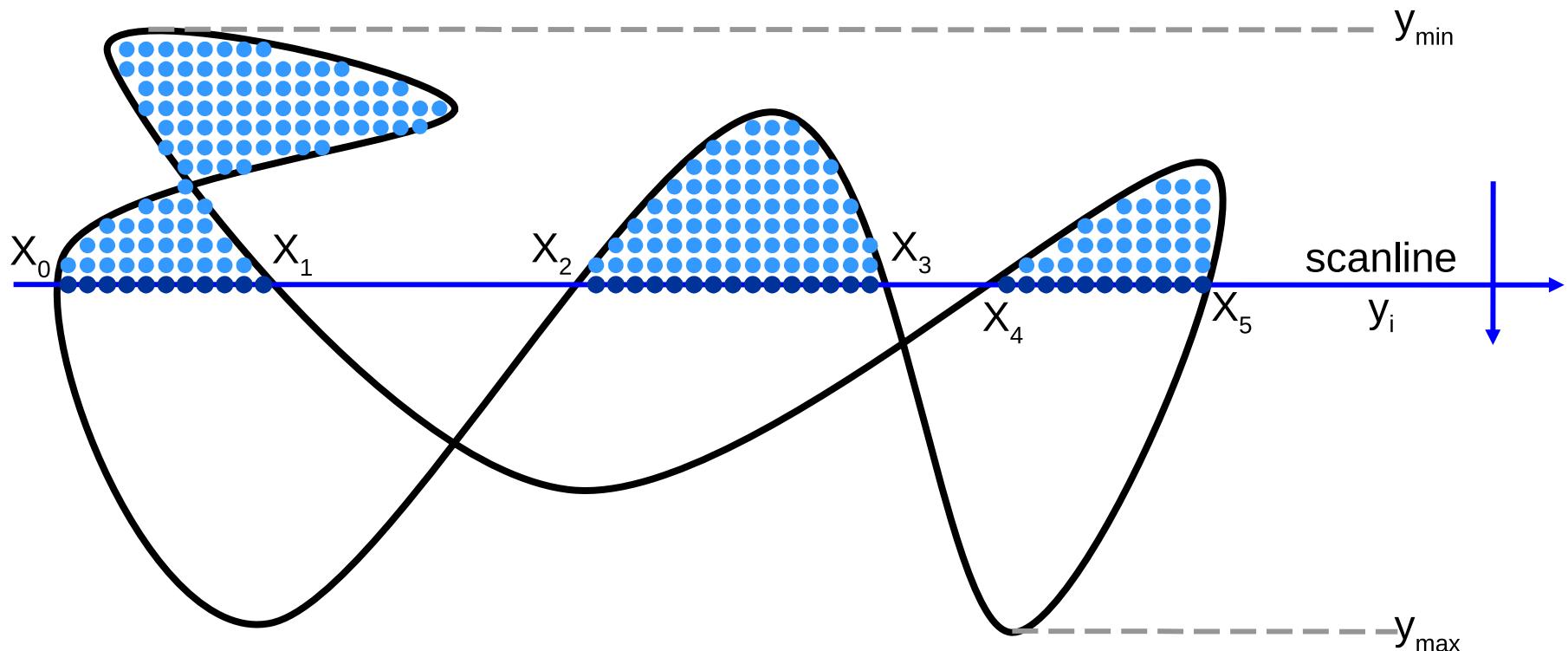


Rasterización de Figuras Cerradas



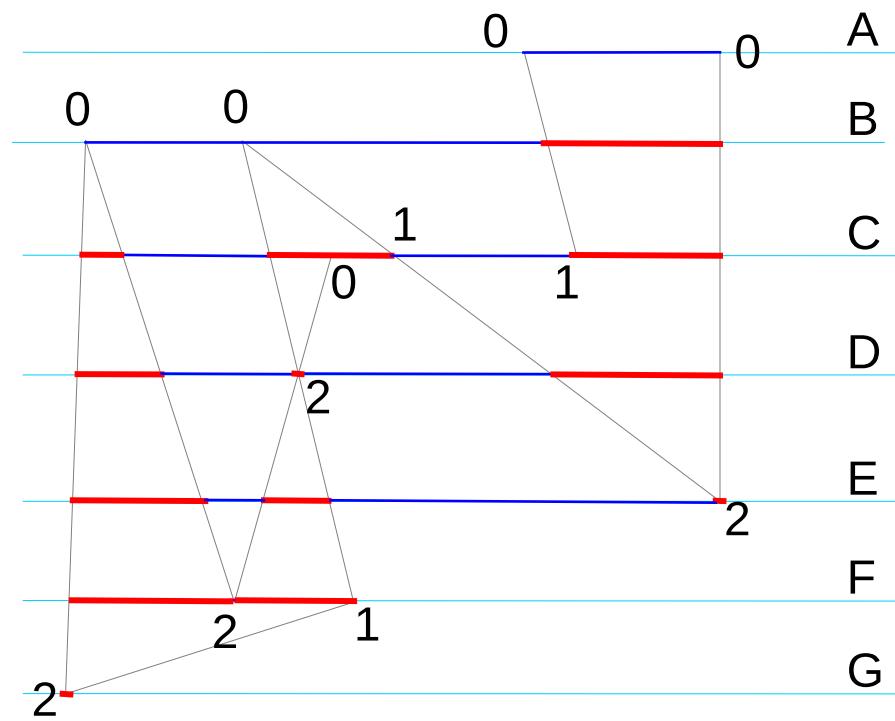
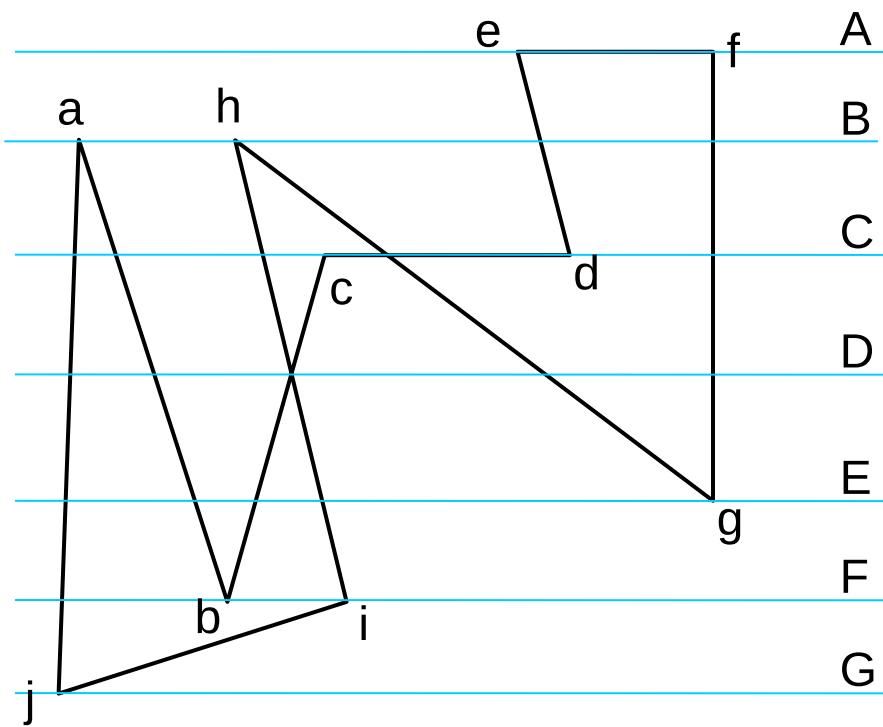
Rasterización de Figuras Cerradas

Igual que el *buffer de color* *cache friendly*



```
y=ymin+1; i=1; while(y<ymax) {  
    j=0; while(j<n[i]-1) {  
        x=X[i][j]+1; while(x<X[i][j+1]) {pinta(x,y); x++;} j+=2;  
    }  
    y++; i++;  
}
```

Rasterización de Poligonales



Pasos horizontales no se agregan a la lista.

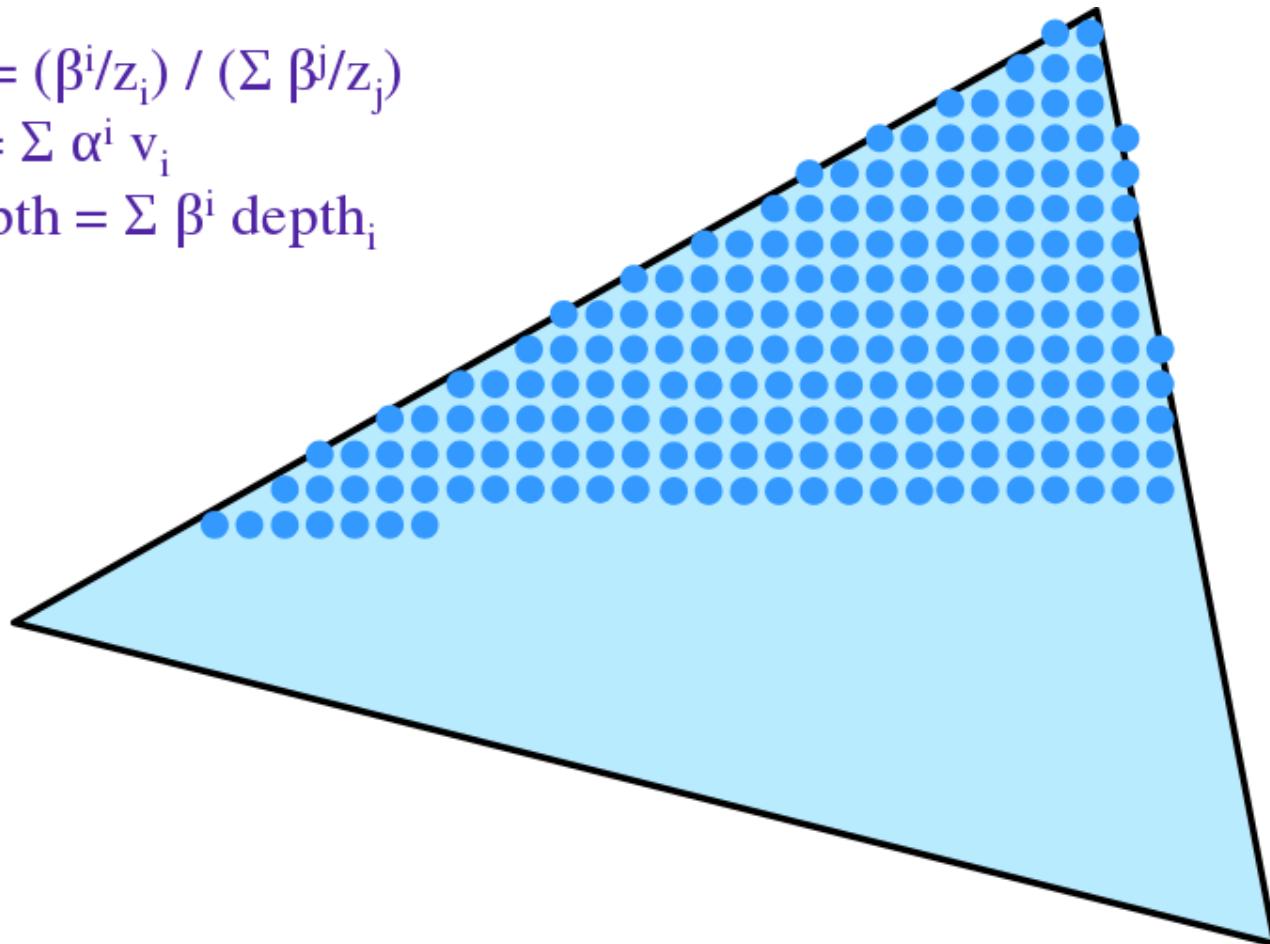
Vértices: sólo los mínimos estrictos de su segmento.

Rasterización de Triángulos

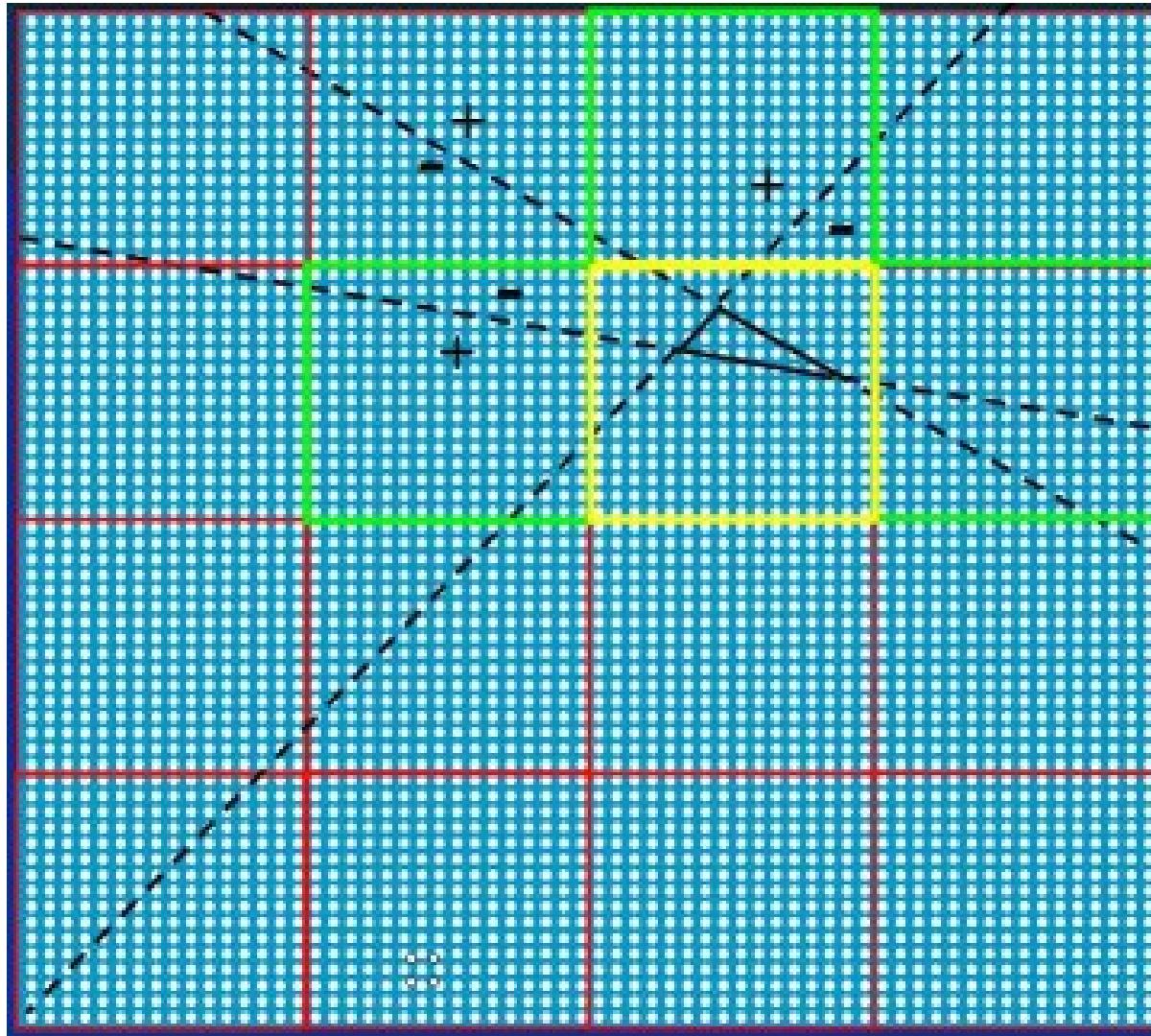
$$\alpha^i = (\beta^i/z_i) / (\sum \beta^j/z_j)$$

$$v = \sum \alpha^i v_i$$

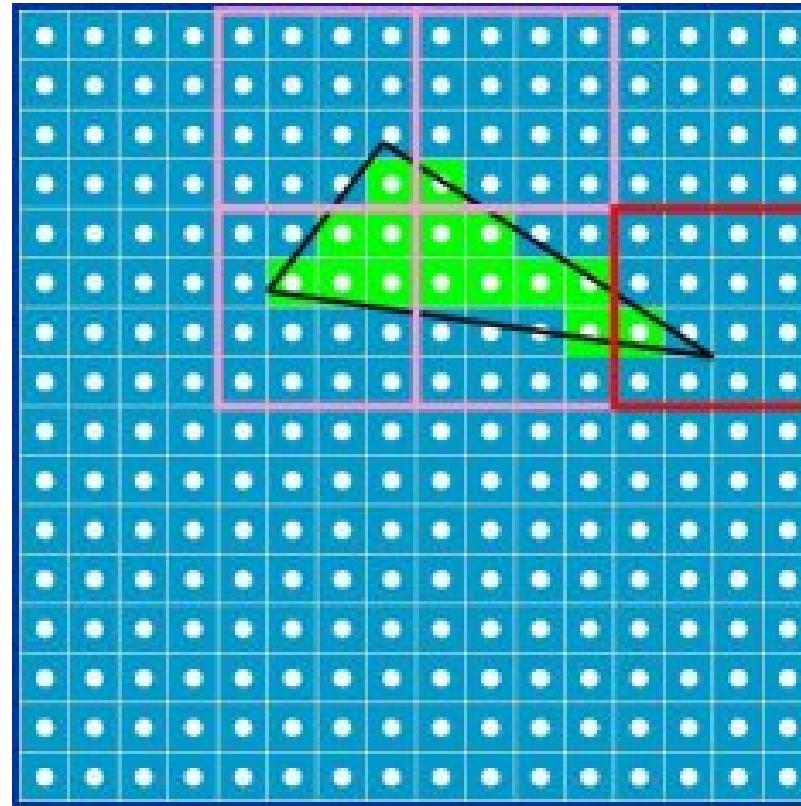
$$\text{depth} = \sum \beta^i \text{depth}_i$$



Rasterización de Triángulos



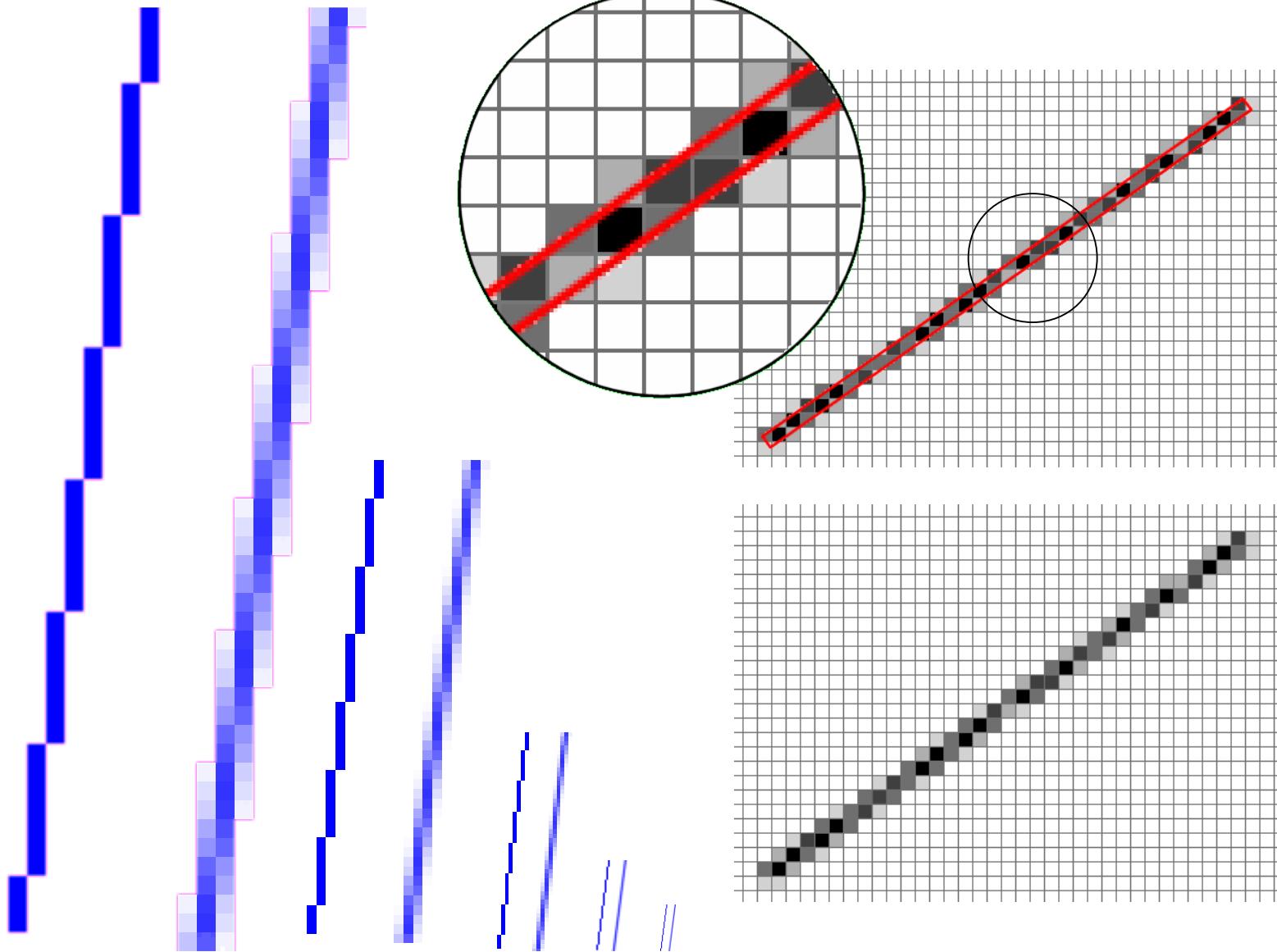
Rasterización de Triángulos



Anti-aliasing



Anti-aliasing



Anti-aliasing

