


INTRO TO BINARY SYSTEMS

Previous Lecture Review

- Different numeral systems (decimal, binary, hexa).
 - Converting Between Counting Systems
 - importance of binary and hexa
 - Main memory units (mem_content vs mem_address)
 - Some important notes:
 - n bits $\rightarrow 2^n$ possibilities (n -bit address can refer to 2^n diff mem. locations)
 - $2^{n+m} = 2^n \times 2^m$
 - $\log_2(n \times m) = \log_2 n + \log_2 m$
- 
$$2^{\text{num_add_bits}} \rightarrow \text{mem_siz}$$
$$\log(\text{mem_size}) \rightarrow \text{num_add_bits}$$

(short, int, long)

signed

(float, double, long double)

$(7)_d \rightarrow$

$(10)_d \rightarrow$

$(258)_d \rightarrow$

0	0	0	0	0	0	0	1	0	0	0	0	0	0	1	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Numbers

Integer Types

(short, int, long)

unsigned

signed

(2's complement)

Floating Point Types

(float, double, long double)

$(+7)_d \rightarrow$

0	0	0	0	0	1	1	1
---	---	---	---	---	---	---	---

$(-7)_d \rightarrow$

1	1	1	1	1	0	0	1
---	---	---	---	---	---	---	---

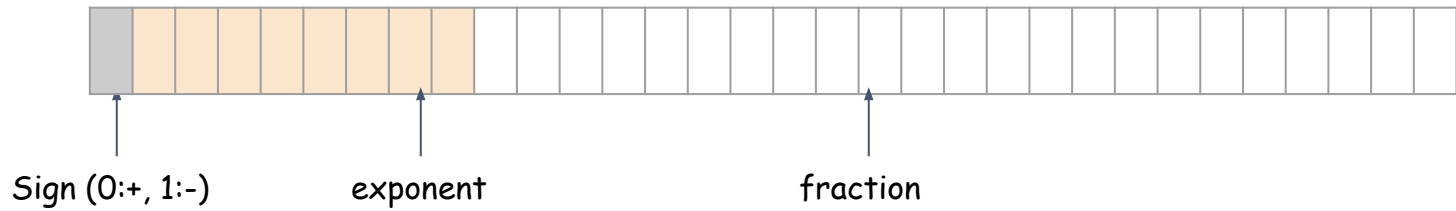
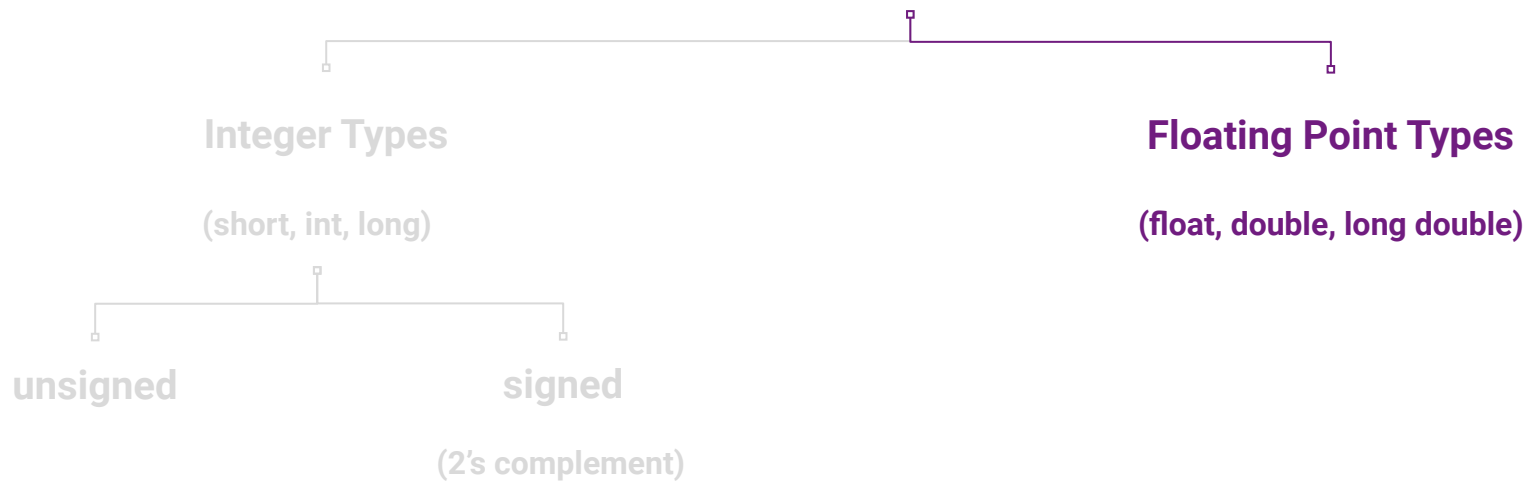
$(+40)_d \rightarrow$

0	0	0	0	0	0	0	0	0	0	0	1	0	1	0	0	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

$(-40)_d \rightarrow$

1	1	1	1	1	1	1	1	1	1	1	0	1	1	0	0	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Numbers



Numbers

Integer Types

(short, int, long)

unsigned

signed

(2's complement)

Floating Point Types

(float, double, long double)

5.75

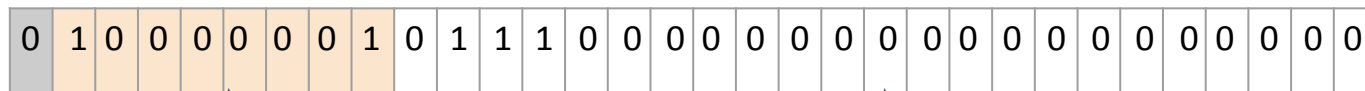
→

101.11

→

1.0111 × 2²

+127



exponent

fraction

Numbers

Integer Types

(short, int, long)

unsigned

signed

(2's complement)

Floating Point Types

(float, double, long double)

85.125

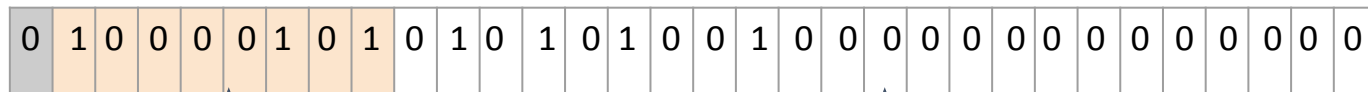
→

1010101.001

→

1.010101001 × 2⁶

+127



Sign (0:+, 1:-)

exponent

fraction

Numbers

Integer Types

(short, int, long)

unsigned

signed

(2's complement)

Floating Point Types

(float, double, long double)

0.75



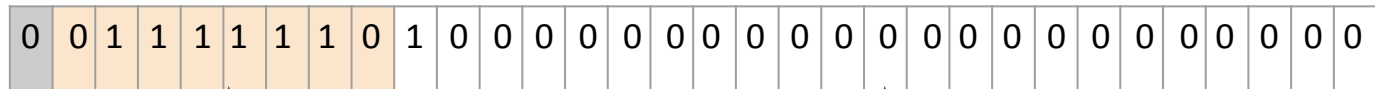
0.11



normalization

$$1.1 \times 2^{-1}$$

127-1



Sign (0:+, 1:-)

exponent

fraction

Numbers

Integer Types

(short, int, long)

unsigned

signed

(2's complement)

Floating Point Types

(float, double, long double)

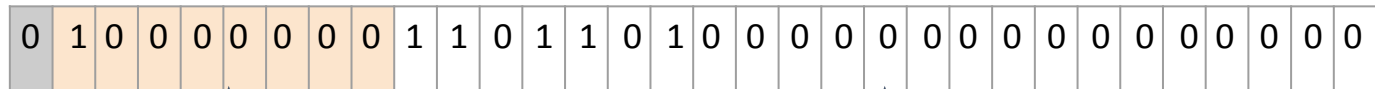
3.703125

11.101101

1.1101101 × 2¹

normalization

127+1



Sign (0:+, 1:-)

exponent

fraction

Numbers

Integer Types

(char, short, int, long)

unsigned

$(5)_d$	/	%
5/2	2	1
2/2	1	0
1/2	0	1

0 0 0 0 0 1 0 1

signed

(2's complement)

$(+5)_d$	/	%
5/2	2	1
2/2	1	0
1/2	0	1

0 0 0 0 0 1 0 1

$(-5)_d$

1 1 1 1 1 0 1 1

Floating Point Types

(float, double, long double)

5.75

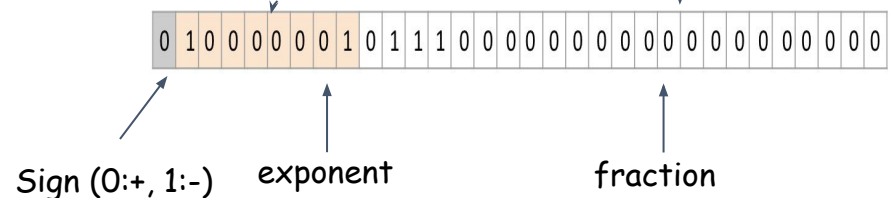
$(5)_d$	/	%
5/2	2	1
2/2	1	0
1/2	0	1

$(0.75)_d$	x	
0.75×2	1.50	1
0.50×2	1.0	1

normalization

5.75 \rightarrow 101.11 \rightarrow 1.0111 $\times 2^2$

+bias



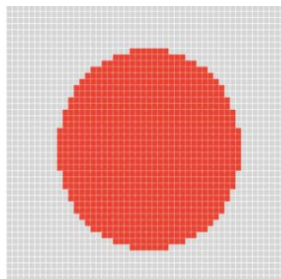
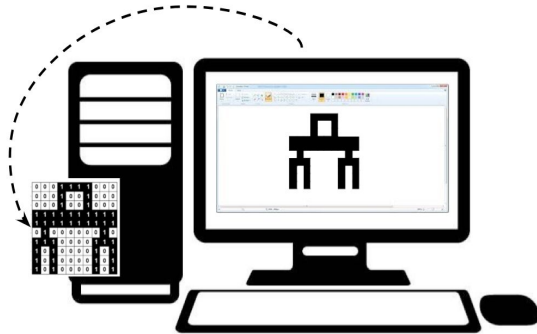
Ranges

IEEE 754 Format	Sign	Exponent	Mantissa	Exponent Bias
32 bit single precision	1 bit	8 bits	23 bits (+ 1 not stored)	$2^{(8-1)} - 1 = 127$
64 bit double precision	1 bit	11 bits	52 bits (+ 1 not stored)	$2^{(11-1)} - 1 = 1023$
128 bit quadruple precision	1 bit	15 bits	112 bits (+ 1 not stored)	$2^{(15-1)} - 1 = 16383$

Reserved Exponent Values

Exponent Value	Mantissa	Represents
11111111	All zeros	Infinity (∞)
11111111	Not all zeros	Not a number (NaN)
00000000	All zeros	Zero
00000000	Not all zeros	Subnormal (very small)

Representation of Images



RASTER

COMPRISED OF PIXELS

LOSES QUALITY WHEN SCALED

CAN'T CONVERT TO VECTOR

BMP, JPG, GIF, PNG

BW = 1 SET OF DIGITS		
1	0	1
0	1	0
1	0	1

GRAY = 1 SET OF DIGITS		
11111111	11100110	11001101
10110100	10011011	01110011
01010000	00101000	00000000

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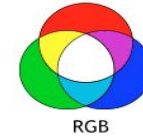
1-BIT COLOR



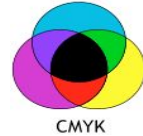
GRAYSCALE

'RGB' = 3 SETS OF DIGITS		
11111111	01100110	00110011
00000000	01100110	11001100
00000000	11111111	10011001
11111111	11111111	00110011
11111111	00000000	11001100
01100110	11001100	11111111
00110011	00110011	11111111
00110011	00110011	10011001
00000000	10011001	10011001

'CMYK' = 4 SETS OF DIGITS		
00000000	01000000	01010010
11000101	00111001	00000000
10111000	00000000	00110110
00000000	00000000	00000000
00000000	00000000	01010011
00000000	01001010	00000000
00111100	00000000	00000100
00000000	00000000	00000000
01001100	01100000	00000000
00111110	01011010	00110010
01011100	00000000	00011010
00110110	00000000	00000000



RGB



CMYK

10 x 10



20 x 20



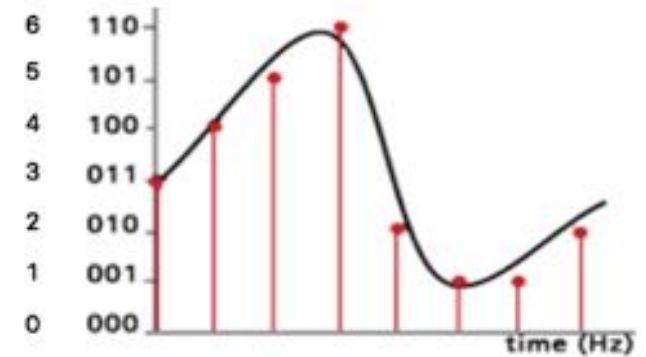
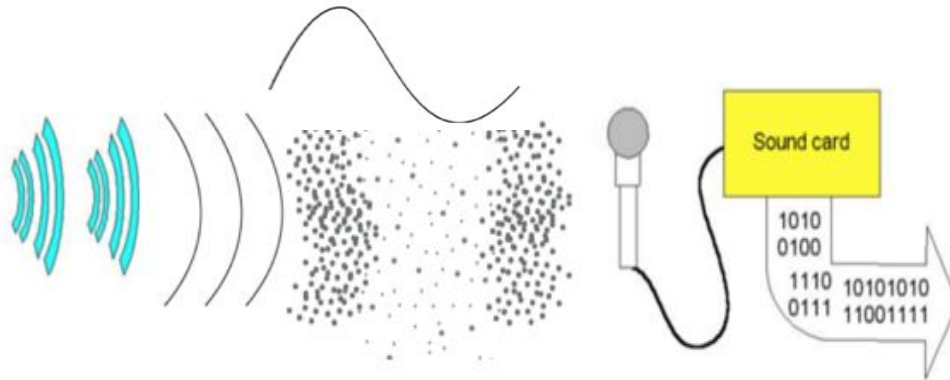
50 x 50



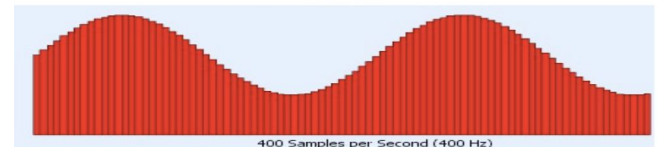
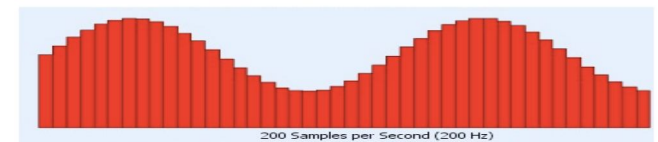
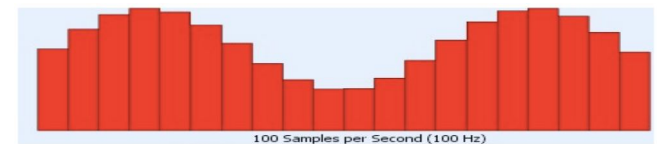
100 x 100



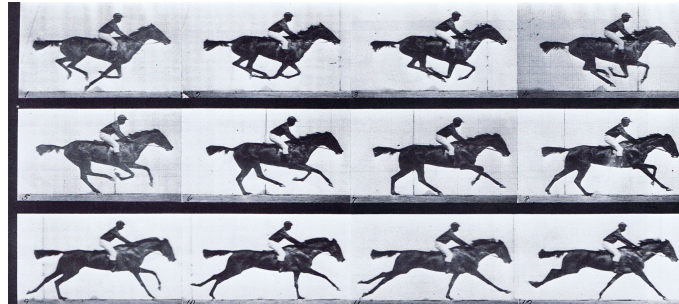
Representation of Sounds



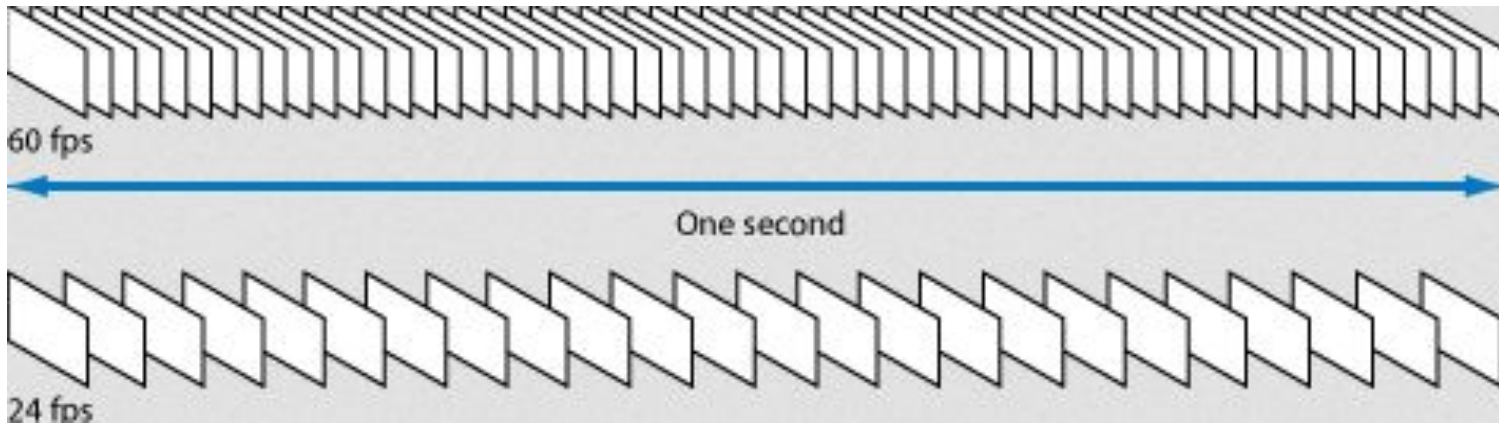
resulting sample:
011, 100, 101, 110, 010, 001, 001, 010 etc



Representation of Videos



Bits store data for each video frame



video frame rate (fps)