

INTRO TO BINARY SYSTEMS

Main Numeral Systems

Decimal	(Base 10)	Number System	0, 1, 2, 3, 4, 5, 6, 7, 8, 9
Binary	(Base 2)	Number System	0, 1
Ternary	(Base 3)	Number System	0, 1, 2
Quaternary	(Base 4)	Number System	0, 1, 2, 3
.....			
Hexadecimal	(Base 16)	Number System	0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F

Converting Between Counting Systems

Decimal	Hex	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
10	A	1010
11	B	1011
12	C	1100
13	D	1101
14	E	1110
15	F	1111

$$(10110)_b = 1 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 \rightarrow (22)_d$$

$$(10010)_b = 1 \times 2^4 + 0 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 \rightarrow (18)_d$$

$$(AE3)_{hex} = A \times 16^2 + E \times 16^1 + 3 \times 16^0 \rightarrow (2787)_d$$

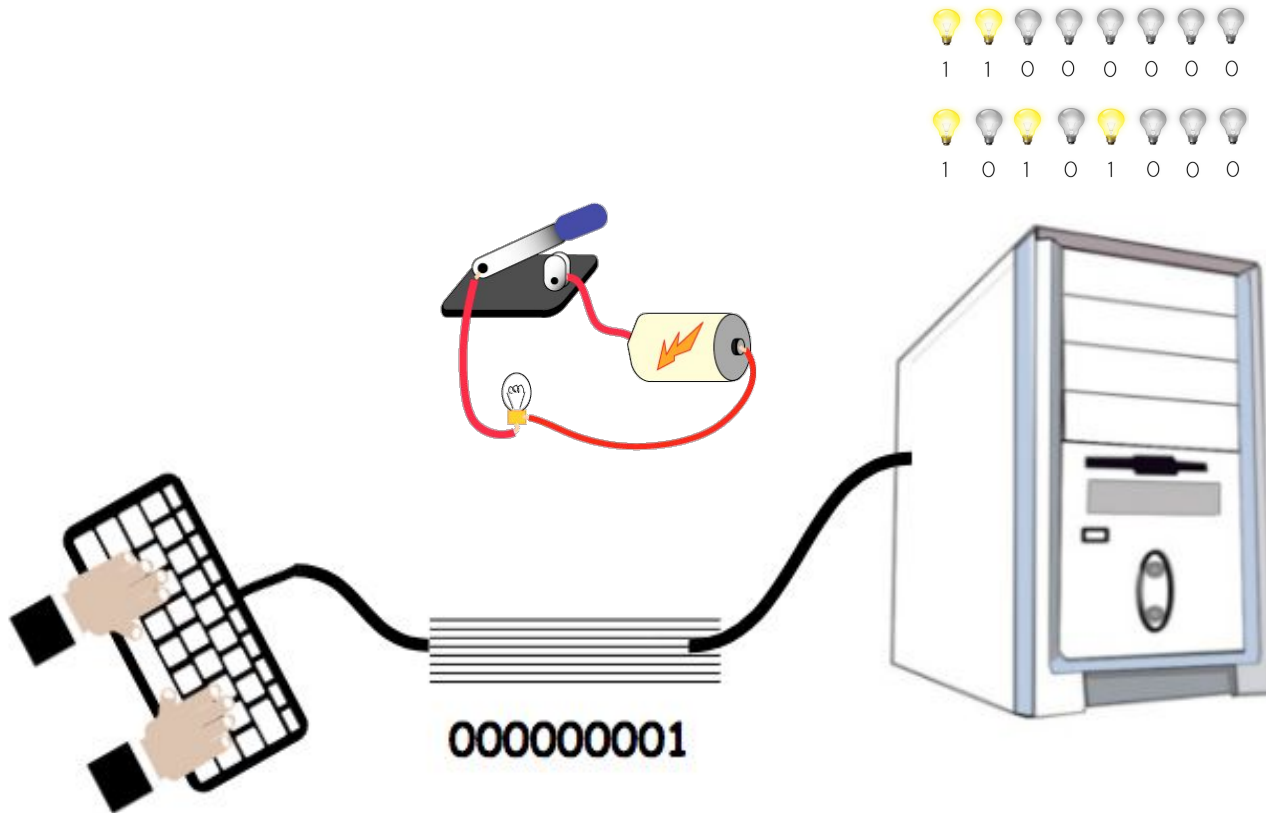
$$(B2F)_{hex} = B \times 16^2 + 2 \times 16^1 + F \times 16^0 \rightarrow (2863)_d$$

The value of a number is often expressed in hex

The 16-bit number **FFFF** hex corresponds to -----> $(1111\ 1111\ 1111\ 1111)_b$

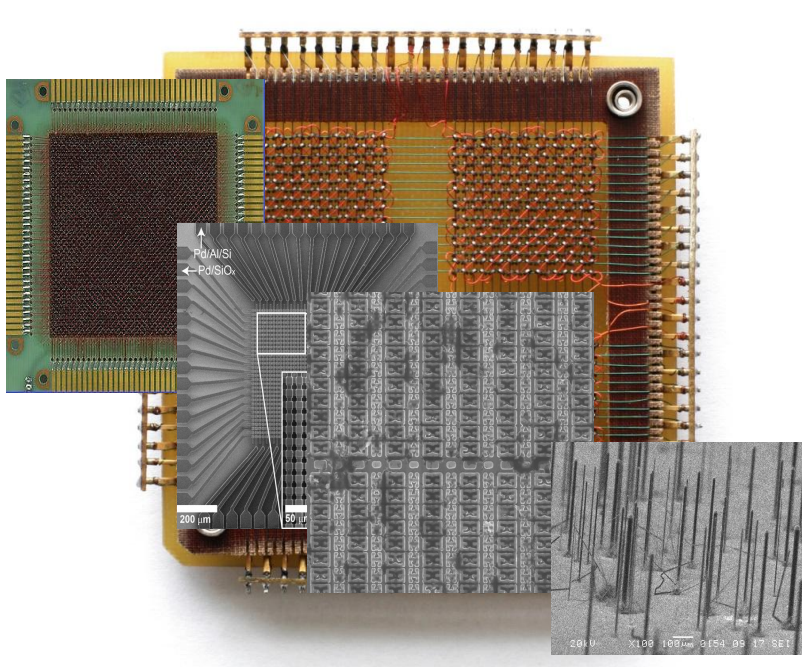
The 16-bit number **4AE3** hex corresponds to -----> $(0100\ 1010\ 1110\ 0011)_b$

Computer Language



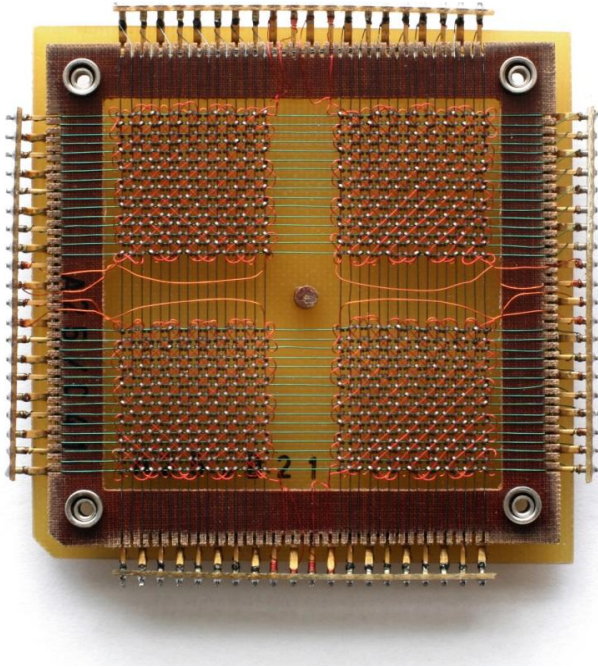
Computer Memory

- Memory — A collection of storage cells together with the necessary circuits to transfer information to and from them.



byte	b	8 bits	1 byte
kilobyte	Kb	1024 bytes	1 024 bytes
megabyte	MB	1024 KB	1 048 576 bytes
gigabyte	GB	1024 MB	1 073 741 824 bytes
terabyte	TB	1024 GB	1 099 511 627 776 bytes

Mem Content vs Mem Address



- n -bit memory location can store one of 2^n different numbers.
 - A 32-bit variable can store any of 2^{32} different numbers.
-
- n -bit address can refer to any of 2^n different memory locations.
 - A 16-bit address can refer to any of $2^{16} = 64K$ different memory locations.

Size matters!

Powers of two

$2^0 = 1$	$2^5 = 32$	$2^{10} = 1024 = 1\text{K (kilo)}$
$2^1 = 2$	$2^6 = 64$	$2^{20} = 1\text{M (mega)}$
$2^2 = 4$	$2^7 = 128$	$2^{30} = 1\text{G (giga)}$
$2^3 = 8$	$2^8 = 256$	$2^{40} = 1\text{T (tera)}$
$2^4 = 16$	$2^9 = 512$	

Rule: $2^{n+m} = 2^n \times 2^m$

Example: $2^{16} = 2^{10} \times 2^6 = 1\text{k} \times 64 = 64\text{k}$

Logarithms (base 2)

$\log_2 1 = 0$	$\log_2 32 = 5$	$\log_2 1024 = \log_2 1\text{K} = 10$
$\log_2 2 = 1$	$\log_2 64 = 6$	$\log_2 1\text{M} = 20$
$\log_2 4 = 2$	$\log_2 128 = 7$	$\log_2 1\text{G} = 30$
$\log_2 8 = 3$	$\log_2 256 = 8$	$\log_2 1\text{T} = 40$
$\log_2 16 = 4$	$\log_2 512 = 9$	

Rule: $\log_2(n \times m) = \log_2 n + \log_2 m$

Example: $\log_2 64\text{k} = \log_2 1\text{k} + \log_2 64 = 10+6 = 16$

Examples

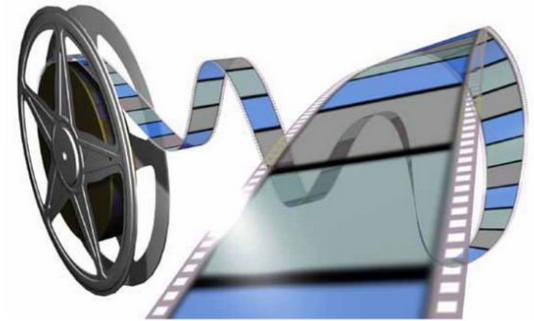
- What is the size the largest memory we can have with 45-bit address?

$$2^{45} = 2^{40} \times 2^5 = 1\text{T} \times 32 = 32\text{T}$$

- How many binary digits do we need for an address of 2G memory?

$$\log 2G = \log 2 + \text{Log } G = 1 + 30 = 31 \text{ bits}$$

Representation of Data



Representation of Symbols and Text

- **Symbols and Text**

- Each symbol can be assigned a numeric value.

ASCII Code: Character to Binary

0	0011 0000	G	0100 0111	W	0101 0111	m	0110 1101	:	0011 1010
1	0011 0001	H	0100 1000	X	0101 1000	n	0110 1110	;	0011 1011
2	0011 0010	I	0100 1001	Y	0101 1001	o	0110 1111	?	0011 1111
3	0011 0011	J	0100 1010	Z	0101 1010	p	0111 0000	!	0010 0001
4	0011 0100	K	0100 1011	a	0110 0001	q	0111 0001	'	0010 1100
5	0011 0101	L	0100 1100	b	0110 0010	r	0111 0010	"	0010 0010
6	0011 0110	M	0100 1101	c	0110 0011	s	0111 0011	(0010 1000
7	0011 0111	N	0100 1110	d	0110 0100	t	0111 0100)	0010 1001
8	0011 1000	O	0100 1111	e	0110 0101	u	0111 0101	space	0010 0000
9	0011 1001	P	0101 0000	f	0110 0110	v	0111 0110		
A	0100 0001	Q	0101 0001	g	0110 0111	w	0111 0111		
B	0100 0010	R	0101 0010	h	0110 1000	x	0111 1000		
C	0100 0011	S	0101 0011	I	0110 1001	y	0111 1001		
D	0100 0100	T	0101 0100	j	0110 1010	z	0111 1010		
E	0100 0101	U	0101 0101	k	0110 1011	.	0010 1110		
F	0100 0110	V	0101 0110	l	0110 1100	,	0010 0111		

Numbers

