# Tutorial of Oz 2 and the DFKI Oz System

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# **Abstract**

This tutorial introduces the programming language Oz 2. Oz 2 is a multiparadigm programming language. It is a high level programming language that is designed for advanced, concurrent, networked, soft real-time, and reactive applications. Oz 2 combines the salient features of object-oriented programming by providing state, abstract data types, classes, objects and inheritance. It provides features of functional programming by providing compositional syntax, first class procedures, and lexical scoping. It provides the salient features of logic and constraint programming such as logic variables, constraints, disjunctions, and programmable search mechanisms. Oz 2 is a concurrent language where users can create dynamically any number of sequential threads. Oz 2 threads are dataflow whose execution proceeds only when data dependencies on variables involved are resolved.

The tutorial covers most of the concepts of Oz 2 in an informal way. It is a suitable as first reading for programmers that want to be able to start quickly writing applications without any particular theoretical background. The document is deliberately informal and, thus complements other DFKI Oz 2 documentations.

#### 1.1 Introduction

A very good starting point is to ask why Oz 2. Well, one rough short answer is that, compared to other existing languages, it is magic! It provides the programmers and system developers with a wide range of programming abstractions to enable them to develop complex applications quickly and robustly. Oz 2 tries to merge several directions of programming language designs into a single coherent one. Yet, Oz 2 is a simple and coherent design. Most of us know the benefits of the various programming paradigms whether object-oriented, functional or constraint logic programming. When we start writing programs in any existing language, we quickly find ourselves confined by the concepts of the underlying paradigm. Oz tries to attack this problem by a coherent design of a language that combines the programming abstractions of various paradigms in clean and simple way.

So, before answering the above question, let us see what Oz 2 is. This is again a difficult question to answer in a few sentences. So, here is the first shot. It is a high level programming language that is designed for modern advanced, concurrent, intelligent, networked, soft real-time, parallel, interactive and pro-active applications. As you see, it is still hard to know what all this jargon means.

- Oz 2 combines the salient features of object-oriented programming, by providing state, abstract data types, classes, objects and inheritance.
- It provides the salient features of functional programming by providing a compositional syntax, first class procedures, and lexical scoping. In fact, every Oz 2 entity is first class, including procedures, threads, classes, methods, and objects.
- It provides the salient features of logic and constraint programming by providing logical variables, disjunctions, flexible search mechanisms and constraint programming.
- It is also a concurrent language where users can create dynamically any number of sequential threads that can interact with each other. However, in contrast to conventional concurrent languages, each Oz 2 thread is a data-flow thread. Executing a statement in Oz 2 proceeds only when all *real* data-flow dependencies on the variables involved are resolved.

Oz 2 has its roots in a paradigm that is known as *concurrent constraint programming*<sup>1</sup>. It is a successor to the programming language Oz and its programming system DFKI Oz. This earlier language and system will be called Oz 1 from now on, while the language will be called Oz. There are a number of differences between Oz 1 and Oz 2. The main difference, however, is that Oz 1 is a fine-grained concurrent language where potentially every statement could be executed in its own thread. Oz 2 abandoned this decision and returns to conventional sequential control structure. In spite of this, threads can be created easily and cheaply in Oz 2. Oz 2 is a data-flow language. This feature is retained from Oz 1.

<sup>&</sup>lt;sup>1</sup> Vijay Saraswat, Concurrent Constraint Programming, MIT press, 1994.

#### 1.2 Variables Declaration

We will initially restrict ourselves to the sequential programming style of Oz. You can think of Oz computations as performed by one sequential process that executes one statement after the other. We call this process a *thread*. This thread has access to a memory called the *store*. It is able to manipulate the store by reading, adding, and updating information. Information is accessed through the notion of *variables*. A thread can access information only through the variables visible to it, directly or indirectly. Oz variables are *single-assignment* variables. In imperative languages like C and Java, a variable can assigned multiple times. In contrast, single assignment variables can be assigned only once. This notion is known from many languages including data flow, and concurrent logic programming languages. A single assignment variable has a number of phases in its lifetime. Initially it is introduced with unknown value, and later it might be assigned a value, in which case the variable becomes *bound*. Once a variable is bound, it cannot itself be changed. However this does not mean that you cannot model state-change because a variable, as you will see later, could be bound to a cell, which is stateful, i.e. the content of cell can be changed.

A thread executing the statement:

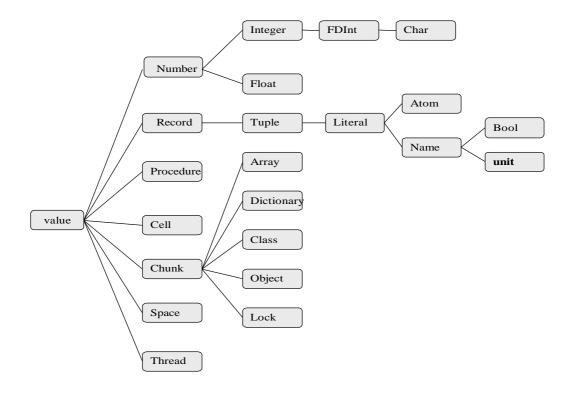
## local X Y Z in S end

Will introduce three single assignment variables X,Y and Z and execute S in the scope of these variables. A variable normally starts with an upper-case letter, possibly followed by an arbitrary number of alphanumeric characters. Variables may be also presented textually as any string of printable characters enclosed within back-quote characters, e.g. `this \$ is a variable`. Before the execution of S the variables declared, will not have any associated values. We say that the variables are *unbound*. Any variable in an Oz program must be introduced, except for certain pattern matching constructs to be shown later.

Another form of declaration is:

# declare $X \ Y \ Z$ in S

This is an open-ended declaration that makes X,Y and Z visible globally in S, as well as all statements the follows S textually, unless overridden again by another variable declaration of the same textual variables.



• Figure 1 Oz Type Hierarchy

# 1.3 Primary Oz Types

Oz is a dynamically typed language. Figure 1 shows the type hierarchy of Oz. Any variable, if it ever gets a value, will be bound to a value of one of these types. Most of the types seem familiar to experienced programmers, except probably *Chunk*, *Cell*, *Space*, *FDInt* and *Name*. We will discuss all of these types in due course. For the impatient reader here are some hints. The *Chunk* data type allows users to introduce new abstract data types. *Cell* introduces the primitive notion of state-container and state modification. *Space* will be needed for advanced problem solving using search techniques. FDInt is the type of finite domain that is used frequently in constraint programming, constraint satisfaction, and operational research. *Name* introduces anonymous unique unforgeable tokens.

The language is dynamically typed in the sense that when a variable is introduced its type, as well as its value, is unknown. Only when the variable is bound to an Oz value, its type becomes determined.

# Hello World

Let us do like everybody else. If you are unfamiliar with Oz, here is your first Oz program. Start your oz system. You typically start it by writing the command: oz and return. This will start the system having the Emacs editor as your interface. You will see two buffers. The upper buffer is called Oz, where you can enter programs and the lower buffer is called \*Oz Compiler\* where you can see the result of compiling Oz

programs. There is also a third buffer \*Oz Emulator\* showing the status of the emulator. This buffer is your standard input, and standard output. You may switch between the compiler and the emulator buffer through the Oz pull-down menu that appears in your EMACS menu bar. Use the entry Show/Hide to switch between the compiler and the emulator buffer.

If you feed the program show below:

```
{Show 'Hello World'}
```

It will print the string 'Hello World' in your standard output. In fact, the main reason for showing this program is to get you accustomed with one of the unconventional syntactic aspects of Oz, namely the syntax of *procedure calls/applications*. {Show 'Hello World'} is a procedure application of Show on the single atom argument 'Hello World'. Show is actually a pre-declared global variable in your initial environment that got bound to the printing procedure when the System module was loaded at the start of the Oz system. Procedure application in Oz syntactically follows other functional languages, e.g. SCHEME, with the exception of using braces instead of parentheses.

The DFKI Oz system provides a number of interesting tools that are accessible through the Oz menu, or can be called from your Oz Program. Instead of using Show try Browse.

You can learn about the DFKI Oz programming system, its user interface and associated tools by looking to 'The DFKI Oz User's Manual', *The Oz documentation series*.

The module System is defined in 'The DFKI Oz User's Manual'.

#### **Adding Information**

In Oz, there are few ways of adding information to the store or (said differently) of binding a variable to a value. The most common form is using the *equality* infix operator =. For example, given that the variable x is declared the following statement:

$$X = 1$$

will bind the unbound variable X to the integer 1, and add this information to the store. Now, if X is already assigned the value 1, the operation is considered as performing a test on X. If X is already bound to an incompatible value, i.e. to any other value different from 1, a proper *exception* will be raised. Exception handling is described later.

## 1.4 Data Types with Structural Equality

The hierarchy starting from Number and Record in Figure 1 defines the data types of Oz whose members (values) are equal only if they are structurally similar. For example two numbers are equal if they have the same type, or one is a subtype of the other, and have the same value. For example, both are integers and are the same number, or both are lists and their head elements are equal as well as their respective tail lists. Structural equality allows values to be equivalent even if they are replicas occupying different physical memory location.

#### 1.5 Numbers

The following program, introduces three variables  ${\tt I}$ ,  ${\tt F}$  and  ${\tt C}$ . It assigns  ${\tt I}$  an integer,  ${\tt F}$  a float, and  ${\tt C}$  the character 't' in this order. It then displays the list consisting of  ${\tt I}$ ,  ${\tt F}$ , and  ${\tt C}$ .

```
local I F C in
    I = 5
    F = 5.5
    C = &t
    {Browse [I F C]}
end
```

```
~3.141 4.5E3 ~12.0e~2
```

In Oz, there is no automatic type conversion, so 5.0 = 5 will raise an exception. Of course, there are primitive procedures for explicit type conversion. These and many others can be found in [7] Characters are a subtype of integers in the range of  $0, \ldots, 255$ . The standard ISO 8859-1 coding is used (not unicode). Printable characters have external representation, e.g. &0 is actually the integer 48, and &a is 97. Some control characters have also a representation e.g. &\n is a new line. All characters can be written as &\ooo, where o is an octal digit.

Operations on characters, integers, and floats can be found in the library modules Char, Float, and Int. Additional generic operations on all numbers are found in the module Number.

#### 1.6 Literals

Another important category of atomic types, i.e. types whose members have no internal structure, is the category of literals. Literals are divided into atoms and names. An Atom is symbolic entity that has an identity made up of a sequence of alphanumeric characters starting with a lower case letter, or arbitrary printable characters enclosed in quotes. For example:

```
a foo '=' ':=' 'OZ 2.0' 'Hello World'
```

Atoms have an ordering based on lexicographic ordering.

Another category of elementary entities is Name. The only way to create a name is by calling the procedure {NewName X} where X is assigned a new name that is guaranteed to be worldwide unique. Names cannot be forged or printed. As will be seen later, names play an important role in the security of Oz programs. A subtype of Name is Bool, which consists of two names protected from being redefined by having the reserved keywords true and false. Thus a user program cannot redefine them, and mess up all programs relying on their definition. There is also the type Unit that consists of the single name unit. This is used as synchronization token in many concurrent programs.

```
local X Y B in
   X = foo
   {NewName Y}
   B = true
   {Browse [X Y B]}
end
```

# **Records and Tuples**

Records are structured compound entities. A record has a *label* and a fixed number of components or arguments. There are also records with a variable number of arguments that are called *open records*. For now, we restrict ourselves to 'closed' records. The following is a record:

```
tree(key: I value: Y left: LT right: RT)
```

It has four arguments, and the label tree. Each argument consists of a pair *Feature:Field*, so the features of the above record is key, value, left, and right. The corresponding fields are the variables I, Y, LT, and RT. It is possible to omit the features of a record reducing it to what is known from logic programming as a compound term. In Oz, this is called a *tuple*. So, the following tuple has the same label and fields as the above record:

```
tree(I Y LT RT)
```

It is just a syntactic notation for the record:

```
tree(1:I 2:Y 3:LT 4:RT)
```

where the features are integers starting from 1 up to the number of fields in the tuple. The following program will display a list consisting of two elements one is a record, and the other is tuple having the same label and fields:

```
declare T I Y LT RT W in
    T = tree(key:I value:Y left:LT right:RT)
    I = seif
    Y = 43
    LT = nil
    RT = nil
    W = tree(I Y LT RT)
    {Browse [T W]}

The display will show:
    [tree(key:seif value:43 left:nil right:nil)
```

## **Operations on records**

We discuss some basic operations on records. Most operations are found in the module Record. To select a field of a record component, we use the infix operator '.'

#### Record.Feature

```
% Selecting a Component
    {Browse T.key}
    {Browse W.1}
% will show seif twice on the display.
seif
seif
```

tree(seif 43 nil nil)]

The *arity* of a record is a list of the features of the record sorted lexicographically. To display the arity of a record we use the procedure Arity. The procedure application

 $\{Arity \ R \ X\}$  will execute once R is assigned a record, and will bind X to the arity of the record. Executing the following statements

```
% Getting the Arity of a Record
local X in {Arity T X} {Browse X} end
local X in {Arity W X} {Browse X} end
will display
  [key left right value]
[1 2 3 4]
```

Another useful operation is conditionally selecting a field of a record. The operation CondSelect takes a record R, a feature F, and a default field-value D, and a result argument X. If the feature F exists in R, R.F is assigned to X, otherwise the default value D is assigned to X. CondSelect is not really a primitive operation. It is definable in Oz. The following statements:

```
% Selecting a component conditionally
    local X in {CondSelect W key eeva X} {Browse X} end
    local X in {CondSelect T key eeva X} {Browse X} end
will display
    eeva
    seif
```

A common infix tuple-operator used in Oz is  $\ '\#'$ . So, 1#2 is a tuple of two elements, and observe that 1#2#3 is a single tuple of three elements:

```
'#'(1 2 3)
```

and not 1#(2#3). With the '#' operator there is no empty tuple notation, and single element tuple is written as '#'(X).

The operation  $\{AdjoinList\ R\ LP\ S\}$  takes a record R a list of feature-field pairs, and returns in S a new record such that:

- The label of R is equal to the label of S.
- S has the components that are specified in LP in addition to all components in R that do not have a feature occurring in LP.

```
local S in
    {AdjoinList tree(a:1 b:2) [a#3 c#4] S}
    {Show S}
end
% gives S=tree(a:3 b:2 c:4)
```

#### Lists

As in many other symbolic programming languages, e.g. Scheme and Prolog, *lists* forms an important class of data structures in Oz. The category of lists does not belong to a single data type in Oz. They are rather conceptual structure. A list is either the atom nil representing the empty list, or is a tuple using the infix operator '|' and two arguments which are respectively the head and the tail of the list. Thus, a list of the first three natural numbers is represented as:

```
1|2|3|nil
```

Another convenient special notation for a *closed list*, i.e. list with determined number of elements is:

```
[1 2 3]
```

The above notation is used only for closed list, so a list whose first two elements are a and b, but whose tail is the variable x looks like:

```
1 | 2 | X
```

One can also use the standard notation for lists:

```
'|'(1 '|'(2 X))
```

Further notational variant is allowed for lists whose elements correspond to character codes. Lists written in this notation are called *strings*, e.g.

```
"OZ 2.0"
is the list
[79 90 32 50 46 48]
```

# 1.7 Virtual Strings

A virtual string is special a tuple that represents a string with virtual concatenation, i.e. the concatenation is performed when really needed. Virtual strings are used for I/O with files, sockets, and windows. All atoms, except nil and #, as well as numbers, strings, or #-labeled tuples can be used to compose virtual strings. Here is one example:

```
123#"-"#23#" is "#100 represents the string
"123-23 is 100"
```

For each data type discussed in section, there is a corresponding module in the DFKI Oz systems. The modules define operations on the corresponding data type. You can find more about these operation in 'The Oz Standard Modules', *The Oz documentation series*.

We have so far shown simple examples of the equality statement, e.g.

```
W = tree(I Y LT LR)
```

These were simple enough to understand intuitively what is going on. However, what happens when two unbound variables are equated X = Y, or when two large data structures are equated. Here is a short explanation. We may think of the store as a dynamically expanding array of memory cells. Each cell is labeled by a single-assignment variable. When a variable X is introduced a cell is created in the store, labeled by X, and its value is *unknown*. At this point, the cell does not possess any value; it is empty as a container that might be filled later.

A variable with an empty cell is an *unbound* variable. The cell is flexible enough to contain any arbitrary Oz value. The operation

```
W = tree(1:I 2:Y 3:LT 4:LR)
```

stores the record structure in the cell associated with W. Notice that we are just getting a graph structure. The cell contains a record with four fields. The fields contain arcs pointing to the cells labeled by I, Y, LT, and LR respectively. Each arc in turn is labeled by the corresponding feature of the record. Given two variables X and Y, X = Y will try to *merge* their respective cells. Now we are in a position to give a reasonable account for the merge operation of X = Y, known as the *incremental tell* operation.

- X and Y label the same cell: the operation is completed successfully.
- X (Y) is unbound: merge the cell of X (Y) with the cell of Y (X). Merging is done by making the cell of X point to that of Y; X and Y are now considered to be labeling the same cell. Conceptually the original cell of X has been discarded.

X and Y are labels of different cells containing the records R<sub>x</sub> and R<sub>y</sub> respectively:

- Arr and  $R_y$  have different labels, arities, or both: the operation is completed, and an exception is raised.
- lacktriangle Otherwise, the arguments of  $R_x$  and  $R_y$  with the same feature are pair-wise merged in arbitrary order.

In general the two graphs, to be merged, could have cycles. However any correct implementation of the merge operation will remember cell pairs for which an attempt to merge has been made earlier, can consider the operation to be successfully performed.

When a variable is no longer accessible, the cell and its associated variable is reclaimed by a process known as garbage collection.

Here are some examples of successful equality operations:

```
local X Y Z in
    f(1:X 2:b) = f(a Y)
    f(Z a) = Z
    {Browse [X Y Z]}
end
```

will show [a b R14=f(R14 a)] in the browser. R14=f(R14 a) is the external representation of a cyclic graph.

To be able to see the finite representation of Z, you have to switch the browser to **Minimal Graph** presentation mode. Choose the Option menu, Representation field, and click on Minimal Graph.

The Browser is described in 'The DFKI Oz User's Manual'.

The following example shows, what happens when variables with incompatible values are equated.

```
declare X Y Z in
    X = f(c a)
    Y = f(Z b)
    X = Y
```

The incremental tell of X = Y will assign Z the value c, but will also raise an exception that is caught by the system, when it tries to equate a and b.

# equality test operator ==

The basic procedure  $\{ = X Y R \}$  tries to test whether X and Y are equal or not, and returns the result in R.

- It returns the Boolean value true, if the graphs starting from the cells of X and Y have the same structure, with each pair-wise corresponding cells having identical Oz values or are the same cell.
- It returns the Boolean value false, if the graphs have different structure, or some pair-wise corresponding cells have different values.
- It suspends when it arrives at pair-wise corresponding cells that are different, but at least one of them is unbound.

Now remember if a procedure suspends, the whole thread suspends! This does not seem useful however, as you will see later, it becomes a very useful operation when multiple thread start interacting with each other.

The equality test is normally used as a functional expression, rather than a statement. As shown is the following example:

```
% See, lists are just tuples, which are just records
local L1 L2 L3 Head Tail in
   L1 = Head|Tail
   Head = 1
   Tail = 2|nil

L2 = [1 2]
   {Browse L1==L2}

L3 = '|'(1:1 2:'|'(2 nil))
   {Browse L1==L3}
end
```

# 3 Basic Control Structures

We have already seen basic statements in Oz. Introducing new variables and sequencing of statements:

$$S_1 S_2$$

Reiterating again, a thread executes statements in a sequential order. However a thread, contrary to conventional languages, may suspend in some statement, so above a thread has to complete execution of  $S_1$ , before starting  $S_2$ . In fact,  $S_2$  may not be executed at all, if an exception is raised in  $S_1$ .

## **3.1** skip

The statement **skip** is the empty statement.

#### 3.2 Conditionals

Simple Conditionals. A statement having the following form:

if 
$$X_1 \cdots X_n$$
 in C then  $S_1$  else  $S_2$  end

where C is a sequence of simple equalities, is called a simple conditional. The subexpression  $\mathbf{if}\ X_1\cdots X_N\ \mathbf{in}\ C\ \mathbf{then}\ S_1$  is usually called a *clause*, and  $\mathbf{if}\ X_1\cdots X_N\ \mathbf{in}\ C$  is the *condition* of the clause. A thread executing such as conditional will first check whether the condition: "There are  $X_1\cdots X_N$  such that C is true" is satisfied or falsified by the current state of the store. If the condition is satisfied, statement  $S_1$  is executed; if it is falsified, the thread executes  $S_2$ ; and if neither hold, the thread suspends.

A simple equality have in general the form x = t where t is a record or a variable. Examples of simple conditions follow.

**Comparison Procedures.** Oz provides a number of built-in tertiary procedures used for comparison. These include == that we have seen earlier as well as  $\setminus =$ , =<, <, >=, >, andthen, and orelse. Common to these procedures is that they are used as Boolean functions in an infix notation. The following example illustrates the use of a conditional in conjunction with the greater-than operator >. In this example z is bound to the maximum of x and y, i.e. to y:

```
local X Y F Z in
    X = 5
    Y = 10
    F = X > Y
    if F = true then Z = X
    else Z = Y end
end
```

Parallel Conditional. A parallel conditional is of the from:

```
\begin{array}{cccc} \textbf{if} & C_1 \textbf{ then } S_1 \\ [] & C_2 \textbf{ then } S_2 \\ & \vdots \\ \\ \textbf{else } S_N \textbf{ end} \end{array}
```

A parallel conditional is executed by evaluating all conditions  $C_1 \cdots C_{N-1}$  in an arbitrary order, possibly concurrently. If one of the conditions say  $C_i$  is true, its corresponding statement  $S_i$  is chosen. If all conditions are false, the else statement  $S_N$  is chosen, otherwise the executing thread suspends. Parallel conditionals are useful mostly in concurrent programming, e.g. for programming time-out on certain events. However, it is often used in a deterministic manner with mutually exclusive conditions. So, the above example could be written as:

```
local X Y F Z in
    X = 5
    Y = 10
    F = X >= Y
    if F = true then
        Z = X
[] F = false then
        Z = Y
    end
end
```

Notice that the else part is missing. This is just a shorthand notation for an else clause that raises an exception.

**Case Statement.** Oz provides an alternative conditional syntax that encourages the use of the simple form of conditions. This is called the *case* statement. The following is the simplest form:

```
case B then S_1 else S_2 end
```

where B is a simple condition that should be evaluated to a Boolean value. If B is **true**  $S_1$  is executed, otherwise if B is **false**  $S_2$  is executed. This is equivalent to:

if 
$$B = \text{true}$$
 then  $S_1$  else  $S_2$  end

Our example using if-statement could be now written as shown below.

```
local X Y Z in
   X = 5 Y = 10
   case X >= Y then Z = X else Z = Y end
end
```

Figure 2 using a case statement.

Since a case-statement is defined in terms of an if-statement, it is merely a notational convenience.

#### 3.3 Procedural Abstraction

**Procedure definitions**. Procedure definition is a primary abstraction in Oz. A procedure can be defined, passed around as argument to another procedure, or stored in a record. A procedure definition is a statement that has the following structure.

$$\texttt{proc}\ \{P\,X_{\scriptscriptstyle 1}\!\cdots X_{\scriptscriptstyle N}\}\,S\ \texttt{end}$$

Assume that the variable P is already introduced; executing the above statement will create a procedure, consisting of a unique name  $\alpha$  and an abstraction  $I(X_1 \cdots X_N) \cdot S$ . This pair is stored in the memory cell labeled by P. A procedure in Oz has a unique identity, given by its name, and is distinct from all other procedures. Two procedure definitions are always different, even if they look similar. Procedures are the first Oz values that we encounter, whose equality is based on name equality. Others include threads, cells, and chunks.

On Lexical Scoping. In general, the statement S in a procedure definition will have many 'syntactic' variable occurrences. A syntactic variable is called an identifier to distinguish it from the single assignment variable that is created at runtime. Some identifier occurrences in S are *syntactically bound* while others are *free*. An identifier occurrence X in S is bound if it is in the scope of the procedure formal-parameter X, or is in the scope of a variable introduction statement that introduces  $X^2$ . Otherwise, the identifier occurrence is free. Each free identifier occurrence in an program is eventually bound by the closest textually surrounding identifier-binding construct.

We have already seen how to apply (call) a procedure. Let us now show our first procedure definition. In Figure 2, we have seen how to compute the maximum of two numbers or literals. We abstract this code into a procedure.

<sup>&</sup>lt;sup>2</sup> This rule is approximate, since class methods and patterns bind identifier occurrences.

```
local Max X Y Z in
   proc {Max X Y Z}
      case X >= Y then
      Z = X
      else Z = Y end
   end
   X = 5 Y = 10
  {Max X Y Z} {Browse Z}
```

## 3.4 Anonymous Procedures and Variable Initialization

One could ask why is a variable bound to a procedure in a way that is different from the variable being bound to record: X = Value? The answer is that what you see is just a syntactic variant of the equivalent form

$$P = \operatorname{proc} \{ X_1 \cdots X_N \} S \text{ end}$$

where the R.H.S. defines an anonymous procedural value. This is equivalent to

$$proc \{PX_1 \cdots X_N\} S$$
 end

In Oz, we can initialize a variable immediately while it is being introduced by using a variable-initialization equality

```
X = Value or R = Value (X occurs in the record R)
```

between local and in, in the statement local ... in ... end. So the previous example could be written as follows, where we also use anonymous procedures.

Now let us understand variable initialization in more detail. The general rule says that: in a variable-initialization equality, only the variables occurring on the L.H.S. of the equality are the ones being introduced. Consider the following example:

```
local
    Y = 1
in
    local
        M = f(M Y)
        [X1 Y] = L
        L = [1 2]
    in {Browse [M L]} end
end
```

First Y is introduced and initialized in the outer local ... in ... end. Then, in the inner local ... in ... end all variables on the L.H.S. are introduced, i.e. M, Y, X1, and L. Therefore the outer variable Y is invisible in the innermost local ... end statement. The above statement is equivalent to:

```
local Y in
    Y = 1
    local M X1 Y L in
        M = f(M Y)
        L = [X1 Y]
        L = [1 2]
        {Browse [M L]}
    end
end
```

If we want Y to denote the variable in the outer scope, we have to suppress the introduction of the inner Y in the L.H.S. of the initializing equality by using an exclamation mark '!' as follows. An exclamation mark '!' is only meaningful in the L.H.S. of an initializing equality.

```
local
    Y = 1
in
    local
        M = f(M Y)
        [X1 !Y] = L
        L = [1 2]
    in {Browse [M L]}
    end
end
```

## 3.5 Pattern Matching

Let us consider a very simple example: insertion of elements in a binary tree. A binary tree is either empty, represented by nil, or is a tuple of the form tree(Key Value TreeL TreeR), where Key is a key of the node with the corresponding value Value, and TreeL is the left subtree having keys less than Key, and TreeR is the right subtree having keys greater than key. The procedure Insert takes four arguments, three of them are input arguments Key, Value and TreeIn, and one output argument TreeOut to be bound to the resulting tree after insertion.

The program is shown in Figure 3. The symbol '?' before TreeOut is a voluntary documentation comment denoting that the argument plays the role of an output argument. The procedure works by cases as obvious. First depending on whether the tree is empty or not, and in the latter case depending on a comparison between the key of the node in the tree and the input key. Notice the use of case ... then ... elsecase ... else ... end with the obvious meaning.

```
declare
proc {Insert Key Value TreeIn ?TreeOut}
   if TreeIn = nil then TreeOut = tree(Key Value nil nil)
   [] K1 V1 T1 T2 in TreeIn = tree(K1 V1 T1 T2) then
      case Key == K1 then TreeOut = tree(Key Value T1 T2)
      elsecase Key < K1 then
       local T in
          TreeOut = tree(K1 V1 T T2)
          {Insert Key Value T1 T}
       end
      else
       local T in
          TreeOut = tree(K1 V1 T1 T)
          {Insert Key Value T2 T}
       end
      end
   end
end
```

Figure 3Tree insertion.

In Figure 3, it is tedious to introduce the local variables in the clause

```
[] K1 V1 T1 T2 in TreeIn = tree(K1 V1 T1 T2) then ...
```

Oz provides a pattern-matching **case** statement, which allows implicit introduction of variables in the patterns. Two forms exist for the case-statement:

```
case E
of Pattern_1 then S_1
elseof Pattern_2 then S_2
elseof \cdots
else S end

and

case E
of Pattern_1 then S_1
[] Pattern_2 then S_2
[] \cdots
else S end
```

All variables introduced in  $Pattern_i$  are implicitly declared, and have a scope stretching over the corresponding clause. In the first case-matching statement, the patterns are tested in order. In the second, called parallel case-matching statement, the order is indeterminate. The else part may be omitted, in which case an exception is raised if all matches fail. Again, in each pattern one may suppress the introduction of new local variable by using '!'. For example, in the following example:

```
case f(X1 X2) of f(!Y Z) then ... else ... end
```

x1 is matched is against the value of the external variable Y. Now remember again that the case statement and its executing thread may suspend if x1 is insufficiently instantiated to decide the result of the matching. Have all this said, Figure 4 shows the tree-insertion procedure using a matching case-statement. We have also reduced the syntactic nesting by abbreviating:

```
% case for pattern matching
proc {Insert Key Value TreeIn ?TreeOut}
    case TreeIn
    of nil then TreeOut = tree(Key Value nil nil)
[] tree(K1 V1 T1 T2) then
        case Key == K1 then TreeOut = tree(Key Value T1 T2)
        elsecase Key < K1 then T in
            TreeOut = tree(K1 V1 T T2)
            {Insert Key Value T1 T}
        else T in
            TreeOut = tree(K1 V1 T1 T)
            {Insert Key Value T2 T}
        end
    end
end</pre>
```

• Figure 4 Tree insertion using case statement.

The expression E we may match against, could be any record structure, and not just a variable. This allows multiple argument matching, as shown in Figure 5, which depicts a classical nondeterministic stream-merge procedure. Here the use of parallel-case statement is essential.

```
proc {Merge Xs Ys ?Zs}
  case Xs#Ys
  of nil#Ys then Zs = Ys
  [] Xs#nil then Zs = Xs
  [] (X|Xr)#Ys then Zr in
     Zs = X|Zr
     {Merge Ys Xr Zr}
  [] Xs#(Y|Yr) then Zr in
     Zs = Y|Zr
     {Merge Yr Xs Zr}
  end
end
```

Figure 5 Binary Merge of two lists.

#### 3.6 Nesting

Let us use our Insert procedure as defined in Figure 4. The following statement inserts a few nodes in an initially empty tree. Note that we had to introduce a number of intermediate variables to perform our sequence of procedure calls.

```
local T0 T1 T2 T3 in
    {Insert seif 43 nil T0}
    {Insert eeva 45 T0 T1}
    {Insert rebecca 20 T1 T2}
    {Insert alex 17 T2 T3}
    {Browse T3}
```

Oz provides syntactic support for nesting one procedure call inside another statement at an expression position. So, in general:

```
local Y in
    {P ... Y ...}
    {Q Y ... }
end
```

could be written as:

```
{Q {P ... $ ...} ... }
```

using '\$' as a *nesting marker*, and thereby the variable Y is eliminated. The rule, to revert to the flattened syntax is that, a nested procedure call, inside a procedure call, is moved *before* the current statement; and a new variable is introduced with one occurrence replacing the nested procedure call, and the other occurrence replacing the nesting marker.

# 3.6.1 Functional Nesting

Another form of nesting is called functional nesting: a procedure  $\{P \mid X \mid ... \mid R\}$  could be considered as a function; its result is the argument R. Therefore

 $\{P \ X...\}$  could considered as a function call that can be inserted in any expression instead of the result argument R. So  $\{Q \ \{P \ X \ ... \} \ ... \}$  is equivalent to:

```
local R in
    {P X ... R}
    {Q R ... }
end
```

Now back to our example, a more concise form using functional nesting is:

There is one more rule to remember. It has to do with a nested application inside a record or a tuple as in:

```
Zs = X | \{Merge Xr Ys \$\}
```

Here, the nested application goes after the record construction statement; do you see why? Therefore, we get

```
local Zr in
   Zs = X | Zr
   {Merge Xr Ys Zr}
```

We can now rewrite our Merge procedure as shown in Figure 5, where we use nested application.

```
proc {Merge Xs Ys ?Zs}
    case Xs#Ys
    of nil#Ys then Zs = Ys
    [] Xs#nil then Zs = Xs
    [] (X|Xr)#Ys then Zs = X|{Merge Ys Xr $}
    [] Xs#(Y|Yr) then Zs = Y|{Merge Yr Xs $}
    end
end
```

Figure 6 Binary merge of two lists in nested form.

#### 3.7 Procedures as Values

Since we have been inserting elements in binary trees, let us define a program that checks if is a data structure is actually a binary tree. The procedure BinaryTree shown in Figure 7 checks a structure to verify whether it is a binary tree or not, and accordingly returns **true** or **false** in its result argument B.

Notice that we also defined the auxiliary local procedure And.

```
% What is a binary tree?
local
  proc {And B1 B2 ?B}
    case B1 then
    case B2 then B = true else B = false end
  else B = false end
end
in proc {BinaryTree T ?B}
  case T
  of nil then B = true
  [] tree(K V T1 T2) then
    {And {BinaryTree T1} {BinaryTree T2} B}
  else B = false end
end
```

• Figure 7. Checking a binary tree.

Consider the call {And {BinaryTree T1} {BinaryTree T2} B}. It is certainly doing unnecessary work. According to our nesting rules, it evaluates its second argument even if the first is false. One can fix this problem by making a new procedure AndThen that takes as its first two arguments two procedures, and calls the second procedure only if the first returns false; thus, getting the effect of delaying the evaluation of its arguments until really needed. The procedure is shown Figure 8. AndThen is the first example of a higher-order procedure, i.e. a procedure that takes other procedures as arguments, and may return other procedures as results. In our case, AndThen just returns a Boolean value. However, in general, we are going to see other examples where procedures return procedures as result. As in functional languages, higher order procedures are invaluable abstraction devices that help creating generic reusable components.

```
local
  proc {AndThen BP1 BP2 ?B}
      case {BP1} then
       case {BP2} then B = true else B = false end
      else B = false end
   end
in proc {BinaryTree T ?B}
      case T
      of nil then B = true
      [] tree(K V T1 T2) then
       {AndThen proc {$ B1}{BinaryTree T1 B1} end
                proc {$ B2}{BinaryTree T2 B2} end
                B}
      else B = false end
   end
end
```

Figure 8. Checking a binary tree lazily.

#### 3.8 Control Abstractions

Higher-order procedures are used in Oz to define various control abstractions. In modules Control and List as well as many others, you will find many control abstractions. Here are some examples. The procedure  $\{For\ From\ To\ Step\ P\}$  is an iterator abstraction that applies the unary procedure P (normally saying the procedure P/1 instead) to integers from From to To proceeding in steps Step. Notice that use of the empty statement **skip**. Executing  $\{For\ 1\ 10\ 1\ Browse\}$  will display the integers 1 2 ... 10.

```
local
   proc {HelpPlus C To Step P}
      case C=<To then {P C} {HelpPlus C+Step To Step P}
      else skip end
   end
   proc {HelpMinus C To Step P}
      case C>=To then {P C} {HelpMinus C+Step To Step P}
      else skip end
   end
in proc {For From To Step P}
      case Step>0 then {HelpPlus From To Step P}
      else {HelpMinus From To Step P} end
   end
end
```

Another control abstraction that is often used is the ForAll/2 iterator defined in the List module. ForAll/2 applies a unary procedure on all the elements of a list, in the order defined by the list. Think what happens if the list is produced incrementally by another concurrent thread?

Figure 9. The For iterator.

```
proc {ForAll Xs P}
  case Xs
  of nil then skip
[] X|Xr then
  {P X}
  {ForAll Xr P}
  end
end
```

# 3.9 Exception Handling

Oz incorporates an exception handling mechanism that allows safeguarding programs against exceptional and/or unforeseeable situations at run-time. It is also possible to raise and handle user-defined exceptions.

An exception is any expression  $\,E\,.$  To raise the exception  $\,E\,,$  one executes the following statement:

```
raise E end
```

He is a simple example:

```
proc {Eval E ?R}
  case E
  of plus(X Y) then {Browse X+Y}
  [] times(X Y) then {Browse X*Y}
  else raise illFormedExpression(E) end
  end
end
```

The basic exception handling statement is called a try-statement, and has the following form:

```
\begin{array}{c} \textbf{try } S \, \textbf{catch} \\ Pattern_1 \, \textbf{then } S_1 \\ \vdots \\ Pattern_2 \, \textbf{then } S_2 \\ \vdots \\ Pattern_N \, \textbf{then } S_N \end{array} \right\} \, optional \\ \textbf{end}
```

Execution of this statement is equivalent to executing S if S does not raise an exception. If S raises exception E and E matches one of the patterns  $Pattern_i$ , control is passed to the corresponding statement  $S_i$ . If E does not match any pattern the exception is propagated outside the try-statement until eventually caught by the system, which catches all escaped exceptions.

```
try
    {ForAll [plus(5 10) times(6 11) min(7 10)] Eval}
catch
    illFormedExpression(X) then {Browse '** X **'}
end
```

A try-statement may also specify a final statement  $S_{\it FINAL}$  , which is executed on normal as well as on exceptional exit.

```
\begin{array}{c} \textbf{try } S \, \textbf{catch} \\ Pattern_1 \, \textbf{then } S_1 \\ [] \, Pattern_2 \, \textbf{then } S_2 \\ \vdots \\ [] \, Pattern_N \, \textbf{then } S_N \\ \\ \textbf{finally } S_{FINAL} \, \textbf{end} \end{array} \right\} \, optional
```

Assume that 'F'<sup>3</sup> is an opened file; the procedure Process/1 manipulates the file in some way; and the procedure CloseFile/1 closes the file. The following program ensures that the F is closed upon normal or exceptional exit.

```
try
   {Process F}
catch
   illFormedExpression(X) then {Browse '** X **'}
finally {CloseFile F} end
```

## **System Exceptions**

The exceptions raised by the Oz system are records with one of the labels: failure, error, and system.

- failure: indicates the attempt to perform an inconsistent equality operation on the store of Oz, recall section 2.
- error: indicates a runtime error which should not occur.
- system: indicates a runtime condition, i.e., an unforeseeable situation like a closed file or window.

The exact format of Oz system-exceptions is in an experimental state and therefore remains the user is only advised to rely of the label only as in the following example:

```
try 1=2
catch
    failure(...)then {Show caughtFailure}
end
```

Here the pattern failure(...) catches any record whose label is failure. When an exception is raised but not handled, an error message is printed in the emulator window (standard output).

<sup>&</sup>lt;sup>3</sup> We will see how input/output is handled later.

# 4 Functional Notation

Oz provides functional notation as syntactic convenience. We have seen that a procedure call:

$$\{PX_1...X_NR\}$$

could be used in a nested expression as a function call:

$$\{PX_1...X_N\}$$

Oz also allows functional abstractions directly as syntactic notation for procedures. Therefore, the following function definition:

fun 
$$\{FX_1...X_N\}$$
  $SE$  end

where S is a statement and E is an expression corresponds to the following procedure definition:

$$\texttt{proc} \ \{F X_1 \dots X_N R\} \ S R = E \ \texttt{end}$$

The exact syntax for functions as well as their unfolding into procedure definitions is defined in Oz Notation, the Oz Documentation Series.

Here we rely on the reader's intuition. Roughly speaking, the general rule for syntax formation of functions looks very similar to how procedures are formed. With the exception that, whenever a thread of control in a procedure ends in a statement, the corresponding function ends in an expression.

The program shown in Figure 10 is the functional equivalent to the program shown in Figure 8. Notice how the function AndThen/2 is unfolded into the procedure AndThen/3. Below we show a number of steps that give some intuition of the transformation process. All the intermediate forms are legal Oz programs.

```
fun {AndThen BP1 BP2}
   case {BP1} then
    case {BP2} then true else false end
   else false end
end
```

Make a procedure by introducing a result variable B:

```
proc {AndThen BP1 BP2 B}
    B = case {BP1} then
        case {BP2} then true else false end
        else false end
end
```

Move the result variable into the outer *case-expression* to make it a *case-statement*:

```
proc {AndThen BP1 BP2 B}
  case {BP1} then
    B = case {BP2} then true else false end
  else B = false end
end
```

Move the result variable into the inner *case-expression* to make it a *case-statement*, and we are done:

```
proc {AndThen BP1 BP2 B}
      case {BP1} then
        case {BP2} then B = true else B = false end
      else B = false end
   end
% Syntax Convenience: functional notation
local
   fun {AndThen BP1 BP2}
      case {BP1} then
         case {BP2} then true else false end
      else false end
   end
   fun {BinaryTree T}
      case T
      of nil then true
      [] tree(K V T1 T2) then
       {AndThen fun {$}{BinaryTree T1} end
                fun {$}{BinaryTree T2} end}
      else false end
   end
end
```

Figure 10. Checking a binary tree lazily.

If you are a functional programmer, you can cheer up! You have your functions, including higher-order ones, and similar to lazy functional languages Oz allows certain forms of tail-recursion optimizations that are not found in certain strict functional languages including Standard ML, Scheme, and the concurrent functional language Erlang. However, functions in Oz are not lazy. This property is easily programmed using the concurrency constructs of Oz and the single assignment variables. Here is an example of the well-known higher order function Map/2. It is tail recursive in Oz but not in Standard ML or in Scheme.

```
fun {Map Xs F}
   case Xs
   of nil then nil
   [] X|Xr then {F X}|{Map Xr F}
   end
end
{Browse {Map [1 2 3 4] fun {$ X} X*X end}}
```

#### andthen and orelse

After all, we have been doing a lot of work for nothing! Oz already provides the Boolean lazy (non-strict) versions of the functions And/2 and Or/2 as the Boolean operators andthen and orelse respectively. The former behaves like the function AndThen/2, and the latter evaluates its second argument only if the first argument

<sup>&</sup>lt;sup>4</sup> Strict functional languages evaluate all its argument first before executing the function.

evaluates **false**. As usual, these operators are not primitives, they are defined in Oz. Figure 11 defines the final version of the function BinaryTree.

```
fun {BinaryTree T}
    case T of nil then true
    [] tree(K V T1 T2) then
        {BinaryTree T1} andthen {BinaryTree T2}
    else false end
end
```

Figure 11 Checking a binary tree lazily.

**To Function or not to function**? The question is when to use functional notation, and when not. The honest answer is that it is up to you! I will tell you my personal opinion. Here are some rules of thumb:

- First, what I do not like. Given that you defined a procedure P do not call it as a function, i.e. do not use functional nesting for procedures. Use instead procedural nesting, with nesting marker, as in the Merge example. Moreover, given that you defined a function, call it as function.
- I tend to use function definitions when things are really functional, i.e. there is one output and, possibly many inputs, and the output is a mathematical function of the input arguments.
- I tend to use procedures in most of the other cases, i.e. multiple outputs or nonfunctional definition due to stateful data types or nondeterministic definitions<sup>5</sup>.
- One may relax the previous rule and use functions when there is a clear direction of information-flow although the definition is not strictly functional. Hence, by this rule we can write the binary-merge in Figure 6 as a function although it is definitely not. After all functions are concise.

<sup>&</sup>lt;sup>5</sup> In fact, I use mostly objects except for typical constraint based applications.

## 5 Modules and Interfaces

Modules, also known as packages, are collection of procedures and other values<sup>6</sup> that are constructed together to provide certain related functionality. A module typically has a number of private procedures that are not visible outside the module and a number of interface procedures that provides the external services of the module. The interface procedures provide the services of the module. In Oz, there is no syntactic support for modules or interfaces. Instead, the lexical scoping of the language and the record data-type suffices to construct modules. The general a module construction looks as follows. Assume that we would like to construct a module called List that provides a number of interface procedures for appending, sorting and testing membership of lists. This would look as follows.

Access to Append procedure outside of the module List is done by using the field append from the 'record' List: List.append. Notice that in the above example the procedure MergeSort is private to the module. Most of the library modules of DFKI Oz follow the above structure.

Often some of the procedures in a module are made global without the module prefix. There are several ways to do this. Here is one way to make Append externally visible:

Modules are often stored on files, for example the List module could be stored on the file 'List.oz'. This file may be inserted into another file by using the compiler directive \insert 'List.oz'.

<sup>&</sup>lt;sup>6</sup> Classes, objects, etc.

You can investigate the libraries accompanying the system in the EMACS OZ menu. Click on the entry Find, and select Modules File.

The List module is defined in the 'Oz Standard Modules' documentation.

Compiler directives are defined in 'The DFKI Oz User's Manual'.

## 6 Concurrency

So far, we have seen only one thread executing. It is time to introduce concurrency. In Oz a new concurrent thread of control is spawned by:

#### thread S end

Executing this statement, a thread is forked that runs concurrently with the current thread. The current thread resumes immediately with the next statement. Each nonterminating thread, that is not blocking, will eventually be allocated a time slice of the processor. This means that threads are executed fairly.

However, there are three priority levels: *high*, *medium*, and *low* that determine how often a runnable thread is allocated a time slice. In Oz, a high priority thread cannot starve a low priority one. Priority determines only how large piece of the processor cake a thread can get.

Each thread has a unique name. To get the name of the current thread the procedure Thread.this/1 is called. Having a reference to a thread, by using its name, enables operations on threads such as terminating a thread, or raising an exception in a thread. Thread operations are defined the standard module Thread<sup>7</sup>.

Let us see what we can do with threads. First, remember that each thread is a data flow thread that blocks on data dependency. Consider the following program:

```
declare X0 X1 X2 X3 in
thread
  local Y0 Y1 Y2 Y3 in
     {Browse [Y0 Y1 Y2 Y3]}
     Y0 = X0+1
     Y1 = X1+Y0
     Y2 = X2+Y1
     Y3 = X3+Y2
     {Browse completed}
  end
end
{Browse [X0 X1 X2 X3]}
```

If you input this program and watch the display of the Browser tool, the variables will appear unbound. If you now input the following statements one at a time:

```
X0 = 0

X1 = 1

X2 = 2

X3 = 3
```

you will see how the thread resumes and then suspends again. First when x0 is bound the thread can execute y0 = x0+1 and suspends again because it needs the value of x1 while executing y1 = x1+y0, and so on.

<sup>&</sup>lt;sup>7</sup> Christian. Schulte, et al, Oz Standard Modules, Oz documentation series.

```
fun {Map Xs F}
  case Xs
  of nil then nil
  [] X|Xr then thread {F X} end | {Map Xr F}
  end
end
```

• Figure 12 A concurrent Map function.

The program shown in Figure 12 defines a concurrent Map function. Notice that 'thread . . . end' is used here as an expression. Let us discuss the behavior of this program. If we enter the following statements:

```
declare
F X Y Z
{Browse thread {Map X F} end}
```

a thread executing Map is created. It will suspend immediately in the case-statement because X is unbound. If we thereafter enter the following statements:

```
X = 1 | 2 | Y
fun {F X} X*X end
```

the main thread will traverse the list creating two threads for the first two arguments of the list, thread  $\{F\ 1\}$  end, and thread  $\{F\ 2\}$  end, and then it will suspend again on the tail of the list Y. Finally,

```
Y = 3 | Z
Z = nil
```

will complete the computation of the main thread and the newly created thread thread {F 3} end, resulting in the final list [1 4 9]. The program shown in Figure 13 is a concurrent divide-and-conquer program, which is very inefficient way to compute the 'Fibonacci' function. This program creates an exponential number of threads! See how it is easy to create concurrent threads. You may use this program to test how many threads your Oz installation can create. Try

```
{Fib 24}
```

while using the panel program in your Oz menu to see the threads. If it works, try a larger number.

```
fun {Fib X}
  case X
  of 0 then 1
  [] 1 then 1
  else thread {Fib X-1} end + {Fib X-2} end
end
```

• Figure 13 A concurrent Fibonacci function.

```
** The Oz Panel Showing Thread Creation in {Fib 26 X}
```

The whole idea of explicit thread creation in Oz is to enable the programmer to structure his/her application in a modular way. Therefore, create threads only when the application need it, and not because concurrency is fun.

### **6.1** Time

In module  $\mathtt{Time}$ , we can find a number of useful soft real-time procedures. Among them are:

- {Alarm I ?U} which creates immediately its own thread, and binds U to unit after I milliseconds.
- {Delay I} suspends the executing thread for, a least, I milliseconds and then reduces to skip.

```
local
  proc {Ping N}
    case N==0 then {Browse 'ping terminated'}
    else {Delay 500} {Browse ping} {Ping N-1} end
  end
  proc {Pong N}
    {For 1 N 1
    proc {$ I} {Delay 600} {Browse pong} end }
    {Browse 'pong terminated'}
  end
in
  {Browse 'game started'}
  thread {Ping 50} end
  thread {Pong 50} end
end
```

Figure 14 A 'Ping Pong' program.

The program shown in Figure 14 starts two threads, one displays ping periodically after 500 milliseconds, and the other pong after 600 milliseconds. Some pings will be displayed immediately after each other because of the periodicity difference.

### **6.2** Stream Communication

The data-flow property of Oz easily enables writing threads that communicate through streams in a producer-consumer pattern. A stream is a list that is created incrementally by one thread (the producer) and subsequently consumed by one or more threads (the consumers). The threads consume the same elements of the stream. For example, the program in Figure 15 is an example of stream communication, where the producer generates a list of numbers and the consumer sums all the numbers.

```
fun {Generator N}
   case N > 0 then N|{Generator N-1}
   else nil end
end
local
   fun {Sum1 L A}
     case L
     of nil then A
     [] X|Xs then {Sum1 Xs A+X}
     end
   end
in fun {Sum L} {Sum1 L 0} end
end
```

• Figure 15 Summing the elements in a list.

Try the program above by running the following program:

```
local L in
   thread L = {Generator 150000} end
   thread {Browse {Sum L}} end
end
```

It should produce the number 11250075000. Let us understand the working of stream communication. A producer incrementally creates a stream (a list) of elements as in the following example where it is producing volvo's. This happens in general in an eager fashion.

```
fun {Producer ...} ... volvo|{Producer ...} ... end
```

The consumer waits on the stream until items arrives, then the items are consumed as in:

```
proc {Consumer Ls ...}
   case Ls of volvo|Lr then 'Consume volvo'... end
   {Consumer Lr}
end
```

The data flow behavior of the *case-statement* suspends the consumer until the arrival of the next item of the stream. The recursive call allows the consumer to iterate the action over again. The following pattern avoids the use of recursion by using an iterator instead:

Figure 16 shows a simple example using this pattern. The consumer counts the cars received. Each time it receives 1000 cars it prints a message on the display of the Browser.

```
fun {Producer N}
   case N > 0 then
      volvo|{Producer N-1}
   else then nil end
end
proc {Consumer Ls}
   proc {Consumer Ls N}
      case Ls
      of nil then skip
      [] volvo Lr then
         case N mod 1000 == 0 then
              {Browse 'riding a new volvo'}
         else skip end
         {Consumer Lr N+1}
      else {Consumer Lr N} end
   end
in {Consumer Ls 1}
end
                 Figure 16 Producing volvo's.
```

You may run this program using:

```
{Consumer thread {Producer 10000} end}
```

When you feed a statement into the emulator, it is executed in its own thread. Therefore, after feeding the above statement two threads are created. The main one is for the consumer, and the forked thread is for the producer.

Notice that the consumer was written using the *recursive* pattern. Can we write this program using the iterative ForAll/2 construct? This is not possible because the consumer carries an extra argument N that accumulates a result which, is passed to the next recursive call. The argument corresponds to some kind of *state*. In general, there are two solutions. We either introduce a stateful (mutable) data structure, which we will do in Section 7, or define another iterator that passes the state around. In our case, some iterators that fit our needs exist in the module List. First, we need an iterator that filters away all items except volvo's. We can use {Filter Xs P ?Ys} which outputs in Ys all the elements that satisfies the procedure P/2 used as a Boolean function. The second construct is {List.forAllInd Xs P} which is similar to ForAll, but P/2 takes the index of the current element of the list, starting from 1, as its first argument, and the element of the list as its second argument. Here is the program:

```
proc {Consumer Ls}
   fun {IsVolvo X} X == volvo end
   Ls1
in
   thread Ls1 = {Filter Ls IsVolvo} end
   {List.forAllInd Ls1
     proc {$ N X}
        case N mod 1000 == 0 then
        {Browse 'riding a new volvo'}
        else skip end
     end}
end
```

## 6.3 Thread Priority and Real Time

Try to run the program using the following statement:

```
{Consumer thread {Producer 5000000} end}
```

Switch on the panel and observe the memory behavior of the program. You will quickly notice that this program does not behave well. The reason has to do with the asynchronous message passing. If the producer sends messages i.e. create new elements in the stream, in a faster rate than the consumer can consume, increasingly more buffering will be needed until the system starts to break down<sup>8</sup>. There are a number of ways to solve this problem. One is to create a bounded buffer between producers and consumers which we will be discussed later. Another way is to control experimentally the rate of thread execution so that the consumers get a larger time-slice than the producers do.

<sup>&</sup>lt;sup>8</sup> Ironically in our current research project PERDIO, developing next generation Oz system (an Internet-wide distributed Oz), stream communication across sites works better because of designed flow-control mechanism that suspends producers when the network buffers are full.

The modules Thread<sup>9</sup>, and System<sup>10</sup>, provide a number of operations pertinent to threads. Some of these are summarized in Table 6-1.

| Procedure                                  | Description                    |
|--|--------------------------------|
| {Thread.state +T ?A}                       | Returns current state of T     |
| {Thread.suspend +T}                        | Suspends T                     |
| {Thread.resume +T}                         | Resumes T                      |
| {Thread.terminate +T}                      | Terminates T                   |
| {Thread.injectException +T +E}             | Raises exception E in T        |
| {Thread.this +T}                           | Returns the current thread T   |
| {Thread.setPriority +T +P}                 | Sets T's priority              |
| {Thread.setThisPriority +P}                | Sets current thread's priority |
| {System.get priorities +P}                 | Gets system-priority ratios    |
| {System.set priorities(high:+X medium:+Y)} | Sets system-priority ratios    |

Table 6-1 Thread operations.

### DFKI Oz has three priority levels. The system procedure

```
{System.set priorities(high:X medium:Y)}
```

sets the processor-time ratio to X:1 between high-priority threads and medium-priority thread. It also sets the processor-time ratio to Y:1 between medium-priority threads and low-priority thread. X and Y are integers. So, if we execute

```
{System.set priorities(high:+10 medium:+10)}
```

for each 10 time-slices allocated to runnable high-priority threads, the system will allocate one time-slice for medium-priority threads, and similarly between medium and low priority threads. Within the same priority level, scheduling is fair and round-robin. Now let us make our producer-consumer program work. We give the producer low priority, and the consumer high. We also set the priority ratios to 10:1 and 10:1.

```
local L in
   {System.set priorities(high:+10 medium:+10)}
   thread
      {Thread.setThisPriority low}
      L = {Producer 5000000}
   end
   thread
      {Thread.setThisPriority high}
      {Consumer L}
   end
end
```

### 6.4 Demand-driven Execution

An extreme alternative solution is to make the producer lazy, only producing an item when the consumer requests one. A consumer, in the case, constructs the stream with unbound variables (empty boxes). The producer waits for the unbound variables (empty boxes) to appear on the stream. It then binds the variables (fills the boxes). The general pattern of the producer is as follows.

<sup>&</sup>lt;sup>9</sup> Defined in 'Oz standard Modules', Oz documentation series.

<sup>&</sup>lt;sup>10</sup> Defined in 'Oz User Manual', Oz documentation series.

```
proc {Producer Xs}
  case Xs of X|Xr then
        I in 'Produce I'
        X=I ...
        {Producer Xr}
  end
end
```

The general pattern of the consumer is as follows.

```
proc {Consumer ... Xs}
    X Xr in
    ...
    Xs = X/Xr
    'Consume X'
    ... {Consumer ... Xr}
end
```

The program shown in Figure 17 is a demand driven version of the program in Figure 16. You can run it with very large number of volvo's!

```
local
  proc {Producer L}
      case L of X | Xs then X = volvo {Producer Xs}
      [] nil then {Browse 'end of line'}
      end
   end
   proc {Consumer N L}
      case N==0 then L = nil
      else
          X \mid Xs = L
      in
         case X of volvo then
            case N mod 1000 == 0 then
             {Browse 'riding a new volvo'}
            else skip end
            {Consumer N-1 Xs}
         else {Consumer N Xs} end
      end
   end
   {Consumer 10000000 thread {Producer $} end}
end
```

Figure 17 Producing volvo's lazily.

### **Thread Termination-Detection**

We have seen how threads are forked using the statement  ${\tt thread}\ S$   ${\tt end}$ . A natural question that arises is how to join back a forked thread into the original thread of control. In fact, this is a special case of detecting termination of multiple threads, and making another thread wait on that event. The general scheme is quite easy because Oz is a data-flow language.

```
thread T_1 X_1 = unit end
thread T_2 X_2 = X_1 end
...
thread T_N X_N = X_{N-1} end
{Wait X_N}
MainThread
```

When All threads terminate the variables  $X_1$  ...  $X_N$  will be merged together labeling a single box that contains the value **unit**. {Wait  $X_N$ } suspends the main thread until  $X_N$  is bound.

In Figure 18 we define a higher-order construct (combinator), that implements the concurrent-composition control construct that has been outlined above. It takes a single argument that is a list of nullary procedures. When it is executed, the procedures are forked concurrently. The next statement is executed only when all procedures in the list terminate.

```
local
   proc {Concl Ps I O}
      case Ps of P|Pr then
          M in
          thread {P} M = I end
      {Concl Pr M O}
   [] nil then O = I
      end
   end
in
   proc {Conc Ps} {Wait {Concl Ps unit $}} end
end
```

# 7 Stateful Data Types

Oz provides set of stateful data types. These include ports, objects, arrays, and dictionaries (hash tables). These data types are abstract in the sense that they are characterized only by the set of operations performed on the members of the type. Their implementation is always hidden, and in fact different implementations exist but their corresponding behavior remains the same. For example, objects are implemented in a totally different way depending on the optimization level of the compiler. Each member is always unique by conceptually tagging it with an Oz-name upon creation. A member is created by an explicit creation operation. A type test operation always exists. In addition, a member ceases to exist when it is no longer accessible.

### **7.1** Ports

Port is such an abstract data-type. A Port P is an asynchronous communication channel that can be shared among several senders. A port has a stream associated with it. The operation:  $\{NewPort S ?P\}$  creates a port P and initially connects it to the variable S taking the role of a stream. The operation:  $\{Send P M\}$  will append the message M to the end of the stream associated with P. The port keeps track of the end of the stream as its next insertion point. The operation  $\{IsPort P ?B\}$  checks whether P is a port. The following program shows a simple example using ports: X

```
declare S P
P = {Port.new S}
{Browse S}
{Send P 1}
{Send P 2}
```

If you enter the above statements incrementally you will observe that S gets incrementally more defined.

```
S
1|
1|2|
```

Ports are more expressive abstractions than pure stream communication that was discussed in Section6.2, since they can be shared among multiple thread, and can be embedded in other data structures. Ports are the main message passing mechanism between threads in Oz.

### **Server-Clients Communication**

The program shown in Figure 19 defines a thread that acts as FIFO queue server. Using single-assignment (logic) variables makes the server insensitive to the arrival order of get messages relative put messages. get messages can arrive even when the queue is empty. A server is created by {NewQueueServer ?Q}. This procedure returns back a port Q to the server. A client thread having access to Q can request services by sending a message on the port. Notice how results are returned back through logic variables. A client requesting an Item in the queue will send the message {Send Q get(I)}. The server will eventually answer back by binding I to an item.

```
declare NewQueueServer in
local
   fun {NewQueue}
      X in q(front:X rear:X number:0)
   end
   fun {Put Q I}
      X in
      Q.rear = I | X
      {AdjoinList Q [rear#X number#(Q.number+1)]}
   end
   proc {Get Q ?I ?NQ}
      X in
      Q.front = I \mid X
      NQ = {AdjoinList Q [front#X number#(Q.number-1)]}
   end
   proc {Empty Q ?B ?NQ}
      B = (Q.number == 0) NQ = Q
   proc {QServer Xs Q}
      case Xs of X | Xr then
          NQ in
          of put(I) then NQ = {Put Q I}
          [] get(I) then {Get Q I NQ}
          [] empty(B) then {Empty Q B NQ}
          else NQ = Q end
          {QServer Xr NQ}
      [] nil then skip
      end
   end
   S P = \{NewPort S\}
in fun {NewQueueServer}
      thread {QServer S {NewQueue}} end
   end
end
```

Figure 19 Concurrent Queue server.

The following sequence of statement illustrates the working of the program.

### declare

```
Q = {NewQueueServer}
{Send Q put(1)}
{Browse {Send Q get($)}}
{Browse {Send Q get($)}}
{Browse {Send Q get($)}}
{Send Q put(2)}
{Send Q put(3)}
{Browse {Send Q empty($)}}
```

\*\*\* Explain the use of logic variables as a mechanism to returns value.

\*\*\* Explain the common pattern of using nesting markers in message passing.

### 7.2 Chunks

Ports are actually stateful data structures. A port keeps a local state internally tracking the end of its associated stream. Oz provides two primitive devices to construct abstract stateful data-types *chunks* and *cells*. All others subtypes of chunks can be defined in terms of chunks and cells.

A chunk is similar to a record except that the label of a chunk is an oz-name, and there is no arity operation available on chunks. This means one can hide certain components of a chunk if the feature of the component is an oz-name that is visible only (by lexical scoping) to user-define operations on the chunk.

A chunk is created by the procedure {NewChunk Record}. This creates a chunk with the same arguments as the record, but having a unique label. The following program creates a chunk.

```
local X in
    {Browse X={NewChunk f(c:3 a:1 b:2)}}
    {Browse X.c}
end
```

This will display the following.

```
<Ch>(a:1 b:2 c:3)
```

In Figure 20, we show an example of using the information hiding ability of chunks to implement Ports.

### **7.3** Cells

A cell could be seen as a chunk with a mutable single component. A cell is created as follows.

```
{NewCell X ?C}
```

A cell is created with the initial content x. c is bound to a cell. The Table{Cell} shows the operations on a cell.

| Operation         | Description                                   |
|-------------------|---|
| {NewCell X ?C}    | Creates a cell C with content X.              |
| $\{Access +C X\}$ | Returns the content of C in X.                |
| {Assign +C Y}     | Modifies the content of C to Y.               |
| {IsCell +C}       | Tests if C is a cell                          |
| {Exchange +C X Y} | Swaps atomically the content of C from X to Y |

Table 7-1 Cell operations.

Check the following program. The last statement increments the cell by one. If we leave out thread ... end the program deadlocks. Do you know why?

Cells and higher-order iterators allow conventional assignment-based programming in

Oz. The following program accumulates in the cell J  $\sum_{i=1}^{10} i$ .

Ports described in Subsection 7.1 can be implemented by chunks and cells in a secure way, i.e. as an abstract data type that cannot be forged. The following program shows an implementation of Ports.

```
declare NewPort IsPort Send in
local
   Port = {NewName} %New Oz name
in
   fun {NewPort S}
        C = {NewCell S}
        {NewChunk port(Port:C)}
   end
   fun {IsPort ?P}
        {ChunkHasFeature Port} %Checks a chunk feature
   end
   proc {Send P M}
        Ms Mr in
        {Exchange P.Port Ms Mr}
        Ms = M|Mr
```

end end

Figure 20. Implementation of Ports by Cells and Chunks.

Initially an Oz-name is created locally, which is accessible only by the Port operations. A port is created as a chunk that has one component, which is a cell. The cell is initialized to the stream associated with the port. The type test IsPort is done by checking the feature Port. Sending a message to a port results in updating the stream atomically, and updating the cell to point to the tail of the stream.

A Class in Oz is a chunk that contains:

- A collection of methods in a method table.
- A description of the attributes that each instance of the class will possess. Each attribute is a stateful cell that is accessed by the attribute-name, which is either an atom or an Oz-name.
- A description of the features that each instance of the class will possess. A feature is an immutable component (a variable) that is accessed by the feature-name, which is either an atom or an Oz-name.
- Classes are stateless Oz-values<sup>11</sup>. Contrary to languages like Smalltalk, or Java etc., they are just descriptions of how the objects of the class should behave.

## **Classes from First Principles**

Figure 21 shows how a class is constructed from first principles as outlined above. Here we construct a Counter class. It has a single attribute accessed by the atom val. It has a method table, which has three methods accessed through the chunk features browse, init and inc. A method is a procedure that takes a message, always a record, an extra parameter representing the state of the current object, and the object itself known internally as **self**.

```
declare Counter
local
   Attrs = [val]
   MethodTable = m(browse:MyBrowse init:Init inc:Inc)
   proc {Init M S Self}
      init(Value) = M in
      {Assign S.val Value}
   end
   proc {Inc M S Self}
      X inc(Value)=M in
         {Access S.val X} {Assign S.val X+Value}
      end
   end
   proc {MyBrowse M=browse S Self}
      {Browse {Access S.val}}
   end
in
   Counter = {NewChunk c(methods:MethodTable attrs:Atts)}
end
```

Figure 21. An Example of Class construction.

\*\*\* Talk about the example.

### **Objects from First Principles**

Figure 22 shows a generic procedure that creates an object from a given class. This procedure creates an object state from the attributes of the class. It initializes the attributes of the object, each to a cell (with unbound initial value). We use here the

<sup>&</sup>lt;sup>11</sup> In fact, classes may have some invisible state. In the current implementation, a class usually has method cache, which is stateful.

iterator Record.forAll/2 that iterates over all fields of a record. NewObject returns a procedure Object that identifies the object. Notice that the state of the object is visible only within Object. One may say that Object is a procedure that encapsulates the state<sup>12</sup>.

```
proc {NewObject Class InitialMethod ?Object}
    local
        State 0
    in
        State = {MakeRecord s Class.attrs}
        {Record.forAll State proc {$ A} {NewCell A} end}
        proc {O M}
            {Class.methods.{Label M} M State O}
        end
        {O InitialMethod}
        Object = O
    end
end
```

Figure 22. Object Construction.

We can try our program as follows

```
declare C
{NewObject Counter init(0) C}
{C inc(6)} {C inc(6)}
{C browse}
```

Try to execute the following statement.

```
local X in {C inc(X)} X=5 end {C browse}
```

You will see that nothing happens. The reason is that the object application

```
\{C inc(X)\}
```

suspends inside the procedure INC/3 that implements method inc. Do you know where exactly? If you on the other hand execute the following statement, things will work as expected.

```
local X in thread {C inc(X)} end X=5 end {C browse}
```

## 8.1 Objects and Classes for Real

Oz supports object-oriented programming following the methodology outlined above. There is also syntactic support and optimized implementation so that object application (calling a method in objects) is as cheap as procedure calls. The class Counter defined earlier has the syntactic form shown in Figure 23:

```
class Counter
  attr val
  meth browse
    {Browse @val}
  end
  meth inc(Value)
    val <- @val + Value
  end</pre>
```

<sup>&</sup>lt;sup>12</sup> This is a simplification; an object in Oz is a chunk that has the above procedure in one of its fields; other fields contain the object features.

```
meth init(Value)
     val <- Value
  end
end</pre>
```

Figure 23. Counter Class.

A class *x* is defined by:

```
class X ... end.
```

Attributes are defined using the attribute-declaration part before the method-declaration part:

```
attr A_1 \ldots A_N
```

Then follows the method declarations, each has the form:

```
meth E S end
```

where the expression E evaluates to a method head, which is a record whose label is the method name. An attribute A is accessed using the expression @A. It is assigned a value using the statement  $A \leftarrow E$ .

A class can be defined anonymously by:

```
X = class $ ... end.
```

The following shows how an object is created from a class using the procedure New/3, whose first argument is the class, the second is the initial method, and the result is the object. New/3 is a generic procedure for creating objects from classes.

```
declare C in
C = {New Counter init(0)}
{C browse}
{C inc(1)}
local X in thread {C inc(X)} end X=5 end
```

#### 8.2 Static Method Calls

Given a class C and a method head m(...), a method call has the following form:

```
C , m(...)
```

A method call invokes the method defined in the class argument. A method call can only be used inside method definitions. This is because a method call takes the current object denoted by <code>self</code> as implicit argument. The method could be defined the class or inherited from a super class. Inheritance will be explained shortly.

## Classes as Modules

Static method calls have in general the same efficiency as procedure calls. This allows classes to be used as modules. This is advantageous because classes can be built incrementally by inheritance. The program shown in Figure shows a possible class acting as a module. The class ListC defines some common list-procedures as methods. ListC defines the methods append/3, member/2, length/2, and nrev/2. Notice that a method body is similar to any Oz statement but in addition, method calls are allowed. We also see the first example of inheritance.

```
class ListC from BaseObject
```

Here the class ListC inherits from the predefined class BaseObject that has only one trivial method: meth noop skip end.

```
class ListC from BaseObject
  meth append(Xs Ys ?Zs)
      case Xs
      of nil then Ys = Zs
      [] X | Xr then Zr in
         Zs = X | Zr
         ListC , append(Xr Ys Zr)
      end
   end
  meth member(X L ?B)
      {Member X L B}
                       % This defined in List.oz
   end
  meth length(Xs ?N)
      case Xs
      of nil then N = 0
      [] _|Xr then N1 in
         ListC , length(Xr N1)
         N = N1+1
      end
   end
  meth nrev(Xs ?Ys)
      case Xs
      of nil then Ys = nil
      [] X | Xr then Yr in
         ListC , nrev(Xr Yr)
         ListC , append(Yr [X] Ys)
      end
   end
end
```

Figure 24. List Class.

To use a class as a module one need to create an object from it. This is done by:

```
declare ListM = {New ListC noop}
```

ListM is an object that acts as a module, i.e. it encapsulates a group of procedures (methods). We can try this module by performing some method calls:

```
{Browse {ListM append([1 2 3] [4 5] $)}} 
{Browse {ListM length([1 2 3] $)}} 
{Browse {ListM nrev([1 2 3] $)}}
```

### 8.3 Inheritance

Classes may inherit from one or several classes appearing after the keyword: **from**. A class B is a *superclass* of a class A if:

- $\blacksquare$  B appears in the **from** declaration of A, or
- $\blacksquare$  B is a superclass of a class appearing in the **from** declaration of A.

Inheritance is a way to construct new classes from existing classes. It defines what attributes, features<sup>13</sup>, and methods are available in the new class. We will restrict our discussion of inheritance to methods. Nonetheless, the same rules apply to features and attributes.

The methods are available in a class C (i.e. visible) are defined through a precedence relation on the methods that appear in the class hierarchy. We call this relation the *overriding relation*:

- $\blacksquare$  A method in a class C overrides any method, with the same label, in any super class if C.
- A method defined in a class B declared in the **from**-declaration of C overrides any method, with the same label, defined in a class to the left of B in the **from** declaration.

Now a class hierarchy with the super-class relation can be seen as a directed graph with the class being defined as the root. The edges are directed towards the subclasses. There are two requirements for the inheritance to be valid. First, the inheritance relation is directed and acyclic. So the following is not allowed:

```
class A from B ... end
class B from A ... end
```



Figure 25. Illegal class hierarchy.

Second, after striking out all overridden methods each remaining method should have a unique label and is defined only in one class in the hierarchy. Hence, class  ${\tt C}$  in the following example is not valid because the two methods labeled  ${\tt m}$  remains.

```
class A meth m(...) ... end end
class B meth m(...) ... end end
class B from B1 end
class A from A1 end
class C from A B end
```

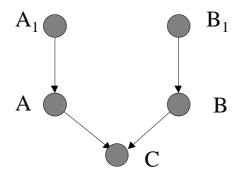


Figure 26. Illegal class hierarchy in method m.

Whereas the class C below is valid, and the method m that is available in C is that of B.

<sup>&</sup>lt;sup>13</sup> To be defined shortly.

```
class A meth m(...) ... end end class B meth m(...) ... end end class C from A B end
```

Notice that if you run a program with an invalid hierarchy, the system will not complain until an object is created that tries to access an invalid method. Only at this point of time, you are going to get a runtime exception. The reason is that classes are partially formed at compile time, and are completed by demand, using method caches, at execution time.

## **Multiple inheritance or Not**

My opinion is the following:

- In general, to use multiple inheritance correctly, one has to understand the total inheritance hierarchy, which is sometimes worth the effort.
- I do not like the existence of any overriding rule that depends on the order of classes in the **from** construct. So I would consider the latter example as invalid as the former one. The reason is that if you take A and B in the later example, and refine them to get the first example your working program will suddenly cease to work
- If there is a method-name conflict between immediate super classes, I would define the method locally to overrides the conflict-causing methods.
- There is another problem with multiple inheritance when sibling super-classes share (directly or indirectly) a common ancestor-class that is stateful (i.e. has attributes). One may get replicated operations on the same attribute. This typically happens when executing an initialization method in a class, one has to initialize its super classes. The only remedy here is to understand carefully the inheritance hierarchy to avoid such replication. Alternatively, you should only inherit from multiple classes that do not share stateful common ancestor. This problem is known as the implementation-sharing problem.

#### 8.4 Features

Objects may have features similar to records. Features are components that are specified in the class declaration:

As in a record, a feature of an object has an associated field. The field is a logic variable that can be bound to any Oz value (including cells, objects, classes etc.). Features of objects are accessed using the infix ´.´ operator. The following shows an example using features:

```
class ApartmentC from BaseObject
   meth init skip end
end
class AptC from ApartmentC
  feat
        streetName: york
        streetNumber:100
        wallColor:white
        floorSurface:wood
end
```

#### **Feature initialization**

The example shows how features could be initialized at the time the class is defined. In this case, all instances of the class AptC will have the features of the class, with their corresponding values. Therefore, the following program will display york twice.

```
declare Apt1 Apt2
Apt1 = {New AptC init}
Apt2 = {New AptC init}
{Browse Apt1.streetName}
{Browse Apt2.streetName}
```

We may leave a feature uninitialized as in:

```
class MyAptC1 from ApartmentC
   feat streetName
end
```

In this case whenever an instance is created, the field of the feature is assigned a new fresh variable. Therefore, the following program will bind the feature streetName of object Apt3 to the atom kungsgatan, and the corresponding feature of Apt4 to the atom sturegatan.

```
declare Apt3 Apt4
Apt3 = {New MyAptC1 init}
Apt4 = {New MyAptC1 init}
Apt3.streetName = kungsgatan
Apt4.streetName = sturegatan
```

One more form of initialization is available. A feature may be initialized in the class declaration to a variable or an Oz-value that has a variable. In the following, the feature is initialized to a tuple with an anonymous variable. In this case, all instances of the class will *share* the same variable. Consider the following program.

```
class MyAptC1 from ApartmentC
   feat streetName:f(_)
end ______

local Apt1 Apt2 in
Apt1 = {New MyAptC1 init}
Apt2 = {New MyAptC1 init}
{Browse Apt1.streetName}
{Browse Apt2.streetName}
Apt1.streetName = f(york)
```

If entered incrementally, will show that the statement

```
Apt1.streetName = f(york)
```

binds the corresponding feature of Apt 2 to the same value as that of Apt 1.

#### 8.5 Parameterized Classes

There are many ways to get your classes more generic, which later may be specialized for specific purposes. The common way to do this in object-oriented programming is to define first *an abstract class* in which some methods are left unspecified. Later these methods are defined in the subclasses. Suppose you have defined a generic class for sorting where the comparison operator less is needed. This operator depends on what kinds of data are being sorted. Different realizations are needed for integer, rational, or complex numbers, etc. In this case, by subclassing we can specialize the abstract class to a 'concrete' class.

In Oz, we have also another natural method for creating generic classes. Since classes are first-class values, we can instead define a function the takes some type argument(s) and return a class that is specialized for the type(s). In Figure 27, the function SortClass is defined that takes a class as its single argument and returns a sorting class specialized for the argument.

```
fun {SortClass Type}
   class $ from BaseObject
       meth qsort(Xs Ys)
          case Xs
          of nil then Ys = nil
          [] P | Xr then S L in
              {self partition(Xr P S L)}
             ListC, append(C,qsort(S $) P (C,qsort(L $)) Ys)
          end
       end
       meth partition(Xs P Ss Ls)
          case Xs
          of nil then Ss = nil Ls = nil
          [] X | Xr then Sr Lr in
             case Type,less(X P $) then
                Ss = X | Sr | Lr = Ls
             else
                 Ss = Sr Ls = X | Lr
             end
                C,partition(Xr P Sr Lr)
          end
       end
   end
 end
```

Figure 27. Parameterized Classes.

We can now define two classes for integers and rationals:

```
class Int
   meth less(X Y B)
        B = X<Y
   end
end
class Rat from Object
  meth less(X Y B)
        '/'(P Q) = X
        '/'(R S) = Y
   in
        B = P*S < Q*R
  end
end</pre>
```

Thereafter, we can execute the following statements:

```
{Browse {{New {SortClass Int} noop} qsort([1 2 5 3 4] $)}}
{Browse {{New {SortClass Rat} noop}
qsort(['/'(23 3) '/'(34 11) '/'(47 17)] $)}}
```

## 8.6 Self Application

The program in Figure 27 shows in the method qsort an object application using the keyword **self** (see below).

We use here the phrase *object-application* instead of the commonly known phrase *message sending* because message sending is misleading in a concurrent language like Oz. When we use **self** instead of a specific object as in

```
{self partition(Xr P S L)}
```

we mean that we dynamically pick the method partition that is defined (available) in the current object. Thereafter we apply the object (as a procedure) on the message. This is a form of dynamic binding common in all object-oriented languages.

### 8.7 Attributes

We have touched before on the notion of attributes. Attributes are the carriers of state in objects. Attributes are declared similar to features, but using the keyword attributeal. When an object is created each attribute is assigned a new cell as its value. These cells are initialized very much the same way as features. The difference lies in the fact that attributes are cells that can be assigned, reassigned and accessed at will. However, attributes are private to their objects. The only way to manipulate an attribute from outside an object is to force the class designer to write a method that manipulates the attribute. In the Figure{Point} we define an the class Point. Note that the attributes x and y are initialized to zero before the initial message is applied. The method move uses self-application internally.

```
class Point from BaseObject
   attr x:0 y:0
  meth init(X Y)
     x <- X
     y <- Y
                         % attribute update
   end
   meth location(L)
     L = l(x:@x y:@y) % attribute access
   meth moveHorizontal(X)
     x <- X
   end
  meth moveVertical(Y)
     y <- Y
   end
  meth move(X Y)
      { self moveHorizontal(X) }
      { self moveVertical(Y) }
   end
  meth display
      % Switch the browser to virtual string mode
      {Browse "point at ("\#@x\#", "\#@y\#")\n"}
   end
end
```

Figure 28. The class Point.

Try to create an instance of Point and apply some few messages:

```
declare P
P = {New Point init(2 0)}
{P display}
{P move(3 2)}
```

### 8.8 Private and Protected Methods

Methods may be labeled by variables instead of literals. These methods are *private* to the class in which they are defined, as in:

```
class C from ...
  meth A(X) ... end
  meth a(...) {self A(5)} ... end
  ...
end
```

The method A is visible only within the class C. In fact the notation above is just an abbreviation of the following expanded definition:

```
local A = {NewName} in
  class C from ...
   meth A(X) ... end
  meth a(...) {self A(5)} ... end
  ...
  end
end
```

where A is bound to a new name in the lexical scope of the class definition.

Some object-oriented languages have also the notion of protected methods. A method is *protected* if it is accessible only in the class it is defined or in descendant classes, i.e. subclasses and subsubclasses etc. In Oz there is no direct way to define a method to be protected. However there is a programming technique that gives the same effect. We know that attributes are only visible inside a class or to descendants of a class by inheritance. We may make a method protected by firstly making it private and secondly storing it is in an attribute. Consider the following example:

```
class C from ...
  attr pa:A
  meth A(X) ... end
  meth a(...) {self A(5)} ... end
  ...
end
```

Now, we create a subclass C1 of C and access method A as follows:

```
class C1 from C
  meth b(...) {self @pa(5)} ... end
  ...
end
```

Method b accesses method A through the attribute pa.

Let us continue our simple example in Figure 28 by defining a specialization of the class that in addition of being a point, it stores a history of the previous movement. This is shown in Figure 29.

```
class HistoryPoint from Point
   attr
      history: nil
      displayHistory: DisplayHistory
  meth init(X Y)
      Point, init(X Y) % call your super
      history <- [l(X Y)]
   end
   meth move(X Y)
      Point, move(X Y)
      history <- l(X Y) |@history
   end
   meth display
      Point, display
      {self DisplayHistory}
   end
   meth DisplayHistory % made protected method
      {Browse "with location history: "}
      {Browse @history}
   end
end
```

Figure 29. The class History Point.

There are a number of remarks on the class definition <code>HistoryPoint</code>. First observe the typical pattern of method refinement. The method <code>move</code> specializes that of class <code>Point</code>. It first calls the super method, and then does what is specific to being a <code>HistoryPoint</code> class. Second, <code>DisplayHistory</code> method is made private to the class. Moreover it is made available for subclasses, i.e. protected, by storing it in the attribute <code>displayHistory</code>. You can now try the class by the following statements:

```
declare P
P = {New HistoryPoint init(2 0)}
{P display}
{P move(3 2)}
```

# 8.9 Default Argument Values

A method head may have default argument values. Consider the following example.

```
meth m(X Y d1:Z<=0 d2:W<=0) ... end
```

A call of the method m may leave the arguments of features d1 and d2 unspecified. In this case these arguments will assume the value zero.

We continue our Point example by specializing Point in a different direction. We define the class BoundedPoint as a point that moves in a constrained rectangular area. Any attempt to move such a point outside the area will be ignored. The class is shown in {BoundedPoint}. Notice that the method init has two default arguments that give a default area if not specified in the initialization of a new instance of BoundedPoint.

```
class BoundedPoint from Point
   attr
      xbounds: 0#0
      ybounds: 0#0
      boundConstraint: BoundConstraint
   meth init(X Y xbounds:XB <= 0#10 ybounds:YB <= 0#10)</pre>
      Point, init(X Y) % call your super
      xbounds <- XB
      ybounds <- YB
   end
   meth move(X Y)
      case {self BoundConstraint(X Y $)} then
          Point, move(X Y)
      else skip end
   end
  meth BoundConstraint(X Y B)
      B = (X >= @xbounds.1 andthen
           X =< @xbounds.2 andthen
           Y >= @ybounds.1 andthen
           Y =< @ybounds.2 )
   end
   meth display
      Point, display
      { self DisplayBounds }
   end
   meth DisplayBounds
      X0#X1 = @xbounds
      Y0#Y1 = @ybounds
      S = "xbounds = ("#X0#", "#X1#"), ybounds = ("
          #Y0#","#Y1#")"
   in
      {Browse S}
   end
end
```

Figure 30 The class BoundedPoint

We conclude this section by finishing our example in a way that shows the multiple inheritance problem. We would like now a specialization of both HistoryPoint and BoundedPoint as a bounded-history point. A point that keeps track of the history and moves in a constrained area. We do this by defining the class BHPoint that inherits from the two previously defined classes. Since they both share the class Point, which contains stateful attributes, we encounter the implementation-sharing problem. We, any way, anticipated this problem and therefore created two protected methods stored in boundConstraint and displayHistory to avoid repeating the same actions. In any case, we have to refine the methods init, move, and display since they occur in the two sibling classes. The solution is shown in {BHPoint}. Notice how we use the protected methods. We did not care avoiding the repetition of initializing the attributes x? and y? since it does not make so much harm. Try the following example:

```
declare P
P = {New BHPoint init(2 0)}
{P display}
{P move(1 2)}
```

This pretty much covers most of object system. What is left is how to deal with concurrent threads sharing common space of objects.

```
class BHPoint from HistoryPoint BoundedPoint
   meth init(X Y xbounds:XB <= 0#10 ybounds:YB <= 0#10)</pre>
      % repeats init
      HistoryPoint,init(X Y)
      BoundedPoint,init(X Y xbounds:XB ybounds:YB)
   end
   meth move(X Y)
      L = @boundConstraint in
      case \{self L(X Y \$) \} then
          HistoryPoint,move(X Y)
      else skip end
   end
   meth display
      BoundedPoint, display
      {self @displayHistory}
   end
end
```

• Figure 31 The class BHPoint.

## 9 Objects and Concurrency

As we have seen, objects in Oz are stateful data structures. Threads are the active computation entities. Threads can communicate either by message passing using ports, or through common shared objects. Communication through shared objects requires the ability to serialize concurrent operations on objects so that the object state is kept coherent after each such an operation. In Oz, we separate the issue of acquiring exclusive access of an object from the object system. This gives us the ability to perform coarse-grain atomic operation of a set of objects, a very important requirement in distributed database system. The basic mechanism in Oz to get exclusive access is through locks.

### 9.1 Locks

The purpose of a lock is to mediate exclusive access to a shared resource between threads. Such a mechanism is typically made safer and more robust by restricting this exclusive access to a critical region. On entry into the region, the lock is secured and the thread is granted exclusive access rights to the resource, and when execution leaves the region, whether normally or through an exception, the lock is released. A concurrent attempt to obtain the same lock will block until the thread currently holding it has released it.

## 9.1.1 Simple Locks

In the case of a simple lock, a nested attempt by the same thread to reacquire the same lock during the dynamic scope of a critical section guarded by the lock will block. We say *reentrancy* is not supported. Simple locks can be modeled in Oz as follows, where Code is a nullary procedure encapsulating the computation to be performed in the critical section. The lock is represented as a procedure, which when applied to so some code it tries to get the lock by waiting until Old gets bound to unit. Notice that the lock is released upon normal as well as abnormal exit.

```
proc {NewSimpleLock ?Lock}
    Cell = {NewCell unit}
in
    proc {Lock Code}
    Old New in
        try
        {Exchange Cell Old New}
        {Wait Old} {Code}
        finally New=unit end
    end
```

### **Atomic Exchange on Object Attributes**

Another implementation is using an object as shown below to implement a lock. Notice the use of the construct:

```
Old = lck <- New
```

Similar to the Exchange operation on cells, this is an atomic exchange on an object attribute.

```
class SimpleLock
  attr lck:unit
  meth init skip end
  meth lock(Code)
    Old New in
    try
        Old = lck <- New
        {Wait Old} {Code}
    finally New= unit end
  end</pre>
```

#### 9.1.2 Thread-Reentrant Locks

In Oz, the computational unit is the thread. Therefore an appropriate locking mechanism should grant exclusive access rights to threads. As a consequence the non-reentrant simple lock mechanism presented above is inadequate. A thread-reentrant lock allows the same thread to reenter the lock, i.e. to enter a dynamically nested critical region guarded by the same lock. Such a lock can be acquired by at most one thread at a time. Concurrent threads that attempt to get the same lock are queued. When the lock is released, it is granted to the thread standing first in line etc. Thread-reentrant locks can be modeled in Oz as follows:

```
class ReentrantLock from SimpleLock
   attr Current:unit
  meth lck(Code)
      ThisThread = {Thread.this} in
      case ThisThread == @Current then
         {Code}
      else
         try
            Code1 = proc {$}
                       Current <- ThisThread
                       {Code}
                     end
         in SimpleLock, lck{Code1}
         finally Current <- unit end</pre>
      end
   end
end
```

Thread reentrant locks are given syntactic and implementational support in Oz. They are implemented as subtype chunks. Oz provides the following syntax for guarded critical regions:

```
lock _E_ then _S_ end
```

where E is an expression that evaluates to a lock. The construct blocks until S is executed. If E is not a lock, then a type error is raised.

- {NewLock L} creates a new lock L.
- {IsLock E} returns true iff Eis a lock..

## **Arrays**

Oz has arrays as chunk subtype. Operations on arrays are defined in module Array.

- {NewArray +L +H +I ?A} creates an array A, where L is the lower-bound index, H is the higher-bound index, and I is the initial value of the array elements.
- {Array.low +A ?L} returns the lower index.
- {Array.high +A ?L} returns the higher index.
- {Get +A +I ?R} returns A[I] in R.
- $\{Put +A +I X\}$  assigns X to the entry A[I].

As a simple illustration of the use of locks consider the program in Figure 32. The procedure Switch transforms negative elements of an array to positive, and zero elements to the atom 'zero'! The procedure Zero resets all elements to zero.

```
declare A L in
A = \{NewArray 1 100 \sim 5\}
L = \{NewLock\}
proc {Switch A}
   {For {Array.low A} {Array.high A} 1
    proc {$ I}
       X = \{Get A I\} in
       case X<0 then {Put A I ~X}</pre>
       elsecase X == 0 then {Put A I zero} else skip end
        {Delay 100}
    end}
end
proc {Zero A}
   {For {Array.low A} {Array.high A} 1
    proc {$ I} {Put A I 0} {Delay 100} end}
end
                    Figure 32 Using Lock.
```

Try the following program.

```
local X Y in
   thread {Zero A} X = unit end
   thread {Switch A} Y = X end
   {Wait Y}
   {For 1 10 1 proc {$ I} {Browse {Get A I}} end}
end
```

The elements of the array will be mixed 0 and 'zero'.

Assume that we want to perform the procedures Zero and Switch, each atomically but in an arbitrary order. To do this we can use locks as in the following example.

```
local X Y in
    thread
    {Delay 100}
    lock L then {Zero A} end
    X = unit
    end
    thread
      lock L then {Switch A} end
      Y = X
    end
    {Wait Y}
    {For 1 10 1 proc {$ I} {Browse {Get A I}} end}
end
```

By Switching the delay statement above between the first and the second thread, we observe that all the elements of the array either will get the value zero or 0. We have no mixed values.

\*\*\* Write an example of an atomic transaction on multiple objects using multiple locks.

### 9.2 Locking Objects

To guarantee mutual exclusion on objects one may use the locks described in the previous subsection. Alternatively, we may declare in the class that its instance objects can be locked with a default lock existing in the objects when they are created. A class with an implicit lock is declared as follows:

```
class C from ....
prop locking
....
end
```

This does not automatically lock the object when one of its methods is called. Instead we have to use the construct:

```
lock S end
```

inside any method to guarantee exclusive access when  $\,{\it s}$  is executed. Remember that our locks are thread-reentrant. This implies that:

- if we take all objects that we have constructed and enclose each method body with lock... end, and
- execute our program with only one thread, then
- the program will behave exactly as before

Of course, if we use multiple threads calling methods in multiple objects, we might deadlock if there is any cyclic dependency. Writing nontrivial concurrent program needs careful understanding of the dependency patterns between threads. In such programs deadlock may occur whether locks are used or not. It suffices to have a cyclic communication pattern for deadlock to occur.

The program in Figure 23 can be refined to work in concurrent environment by refining it as follows:

```
class CCounter from Counter
  prop locking
  meth inc(Value)
     lock Counter,inc(Value) end
  end
  meth init(Value)
     lock Counter,init(Value) end
  end
end
```

Let us now study a number of interesting examples where threads not only perform atomic transactions on objects, but also synchronize through objects.

### **Concurrent FIFO Channel**

The first example shows a concurrent channel, which is shared among an arbitrary number of threads. Any producing thread may put information in the channel asynchronously. A consuming thread has to wait until information exists in the channel. Waiting threads are served fairly. Figure 33 shows one possible realization. This program relies on the use of logical variables to achieve the desired synchronization. The method put/1 inserts an element in the channel. A thread executing the method get/1 will wait until an element is put in the channel. Multiple consuming threads will reserve their place in the channel, thereby achieving fairness. Notice that {Wait I} is done outside an exclusive region. If waiting was done inside lock . . . end the program would deadlock. So, as a rule of thumb:

Do not wait inside an exclusive region, if the waking-up action has to acquire the same lock..

```
class Channel from BaseObject
  prop locking
  attr f r
  meth init
    X in f <- X r <- X
  end
  meth put(I)
    X in lock @r=I | X r<-X end
  end
  meth get(?I)
    X in lock @f=I | X f<-X end {Wait I}
  end
end
end</pre>
```

• Figure 33 An Asynchronous Channel Class

### **Monitors**

The next example shows a traditional way to write *monitors*. We start by defining a class that defines the notion of events and the monitor operations notify(Event) and wait(Event) by specializing the class Channel.

```
class Event from Channel
  meth wait
        Channel , get(_)
  end
  meth notify
        Channel , put(unit)
  end
end
```

We show here an example of a unit buffer in the traditional monitor style. The unit buffer behaves in a way very similar to a channel when it comes to consumers. Each consumer waits until the buffer is full. In the case of producers only one is allowed to insert an item in the empty buffer. Other producers have to suspend until the item is consumed. The program in Figure 34 shows a single buffer monitor. Here we had to program a signaling mechanism for producers and consumers. Observe the pattern in put/1 and get/1 methods. Most execution is done in an exclusive region. If waiting is necessary it is done outside the exclusive region. This is done by using an auxiliary variable X, which gets bound to yes. The get/1 method notifies one producer at a time by setting the empty flag and notifying one producer (if any). This is done as an atomic step. The put/1 method does the reciprocal action.

```
class UnitBufferM
   attr item empty psignal csignal
  prop locking
  meth init
      empty <- true
      psignal <- {New Event init}</pre>
      csignal <- {New Event init}</pre>
   end
  meth put(I)
      X in
      lock
        case @empty then
          item <- I
          empty <- false
          X = yes
          {@csignal notify}
        else X = no end
      end
      case X == no then
         {@psignal wait}
         {self put(I)}
      else skip end
   end
  meth get(I)
      X in
      lock
        case {Not @empty} then
          I = @item
          empty <- true
          {@psignal notify}
          X = yes
        else X = no end
      case X == no then
         {@csignal wait}
         {self get(I)}
      else skip end
   end
end
```

• Figure 34 A Unit Buffer Monitor

Try the above example by running the following code:

```
local
   UB = {New UnitBufferM init} in
   {For 1 15 1
    proc{$ I} thread {UB put(I)} {Delay 500} end end}
   {For 1 15 1
    proc{$ I} thread {UB get({Browse})}{Delay 500} end end}
end
```

## **Bounded Buffers Oz Style**

In Oz, it is very rare to write programs in the monitor style shown above. In general it is very awkward. There is a simpler way to write a UnitBuffer class that is not traditional. This is due to the combination of objects and logic variable Figure 35 shows simple definition. No locking is needed directly.

```
class UnitBuffer from BaseObject
   attr prodq buffer
  meth init
      buffer <- {New Channel init}</pre>
      prodq <- {New Event init}</pre>
      {@prodq notify}
   end
   meth put(I)
      {@prodq wait}
      {@buffer put(I)}
   end
   meth get(?I)
      {@buffer get(I)}
      {@prodq notify}
   end
end
```

Figure 35 Unit Buffer.

Simple generalization of the above program leads to an arbitrary size bounded buffer class. This is shown in below. The put and get methods are the same as before. Only the initialization method is changed.

```
class BoundedBuffer from UnitBuffer
  attr prodq buffer
  meth init(N)
     buffer <- {New Channel init}
     prodq <- {New Event init}
     {For 1 N 1 proc {$ _}} {@prodq notify} end}
  end
end</pre>
```

Figure 36 A Bounded Buffer Class.

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|---|--|--|--|--|--|--|
| Christian Schulte, et. al., 'Oz Standard Modules', the Oz documentation series. |  |  |  |  |  |  |
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