



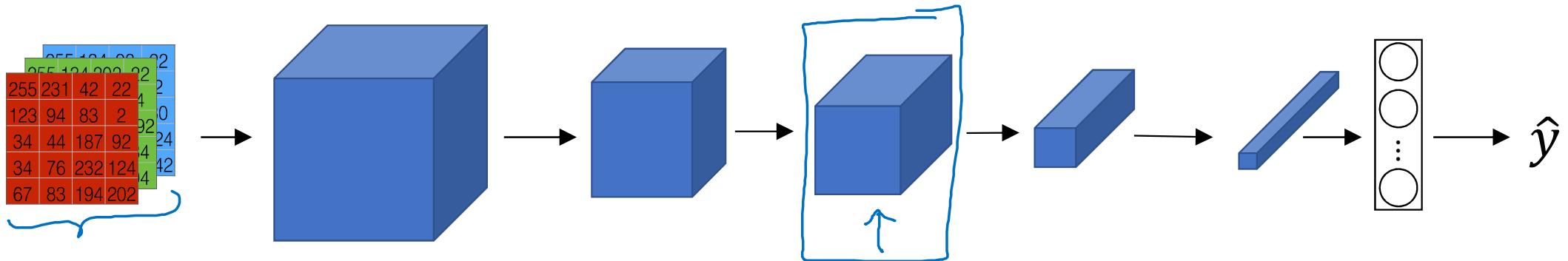
deeplearning.ai

# Neural Style Transfer

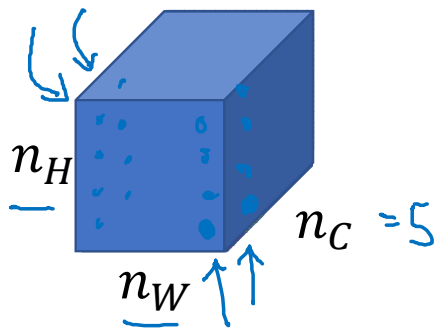
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## Style cost function

# Meaning of the “style” of an image



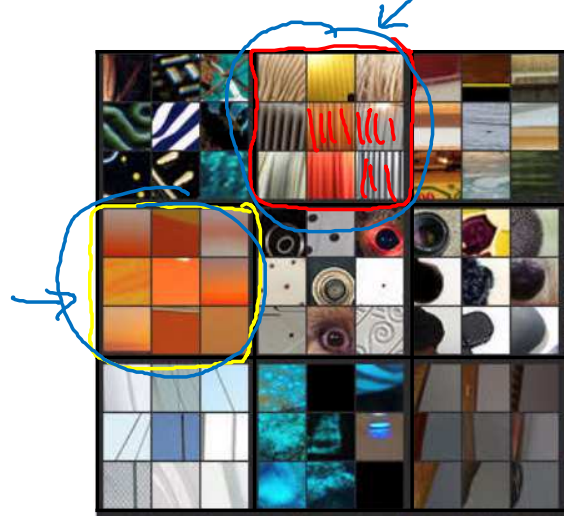
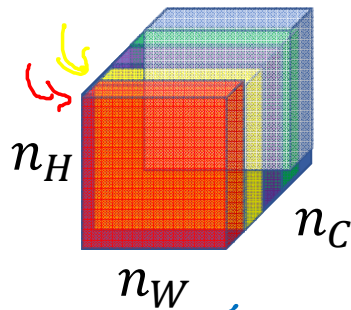
Say you are using layer  $l$ 's activation to measure “style.”  
Define style as correlation between activations across channels.



How correlated are the activations  
across different channels?

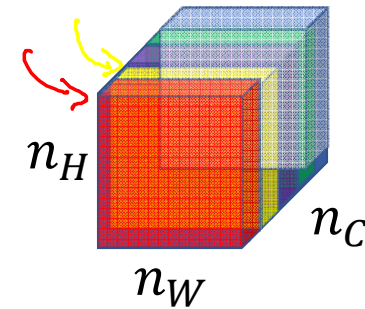
# Intuition about style of an image

Style image



Correlated?  
Uncorrelated

Generated Image



# Style matrix

Let  $a_{i,j,k}^{[l]}$  = activation at  $(i, j, k)$ .  $G^{[l]}$  is  $n_c^{[l]} \times n_c^{[l]}$

$$\begin{aligned} \rightarrow G_{kk'}^{[l](s)} &= \sum_{i=1}^{n_H^{[l]}} \sum_{j=1}^{n_W^{[l]}} a_{ijk}^{[l](s)} a_{ijk'}^{[l](s)} \\ \rightarrow G_{kk'}^{[l](G)} &= \sum_{i=1}^{n_H^{[l]}} \sum_{j=1}^{n_W^{[l]}} a_{ijk}^{[l](G)} a_{ijk}^{[l](G)} \end{aligned}$$

"Gram matrix"

$$G_{kk'}^{[l]} \quad k=1, \dots, n_c^{[l]}$$

$$\begin{aligned} \beta J_{\text{style}}^{[l]}(S, G) &= \frac{1}{(\dots)} \|G^{[l](s)} - G^{[l](G)}\|_F^2 \\ &= \frac{1}{(2n_H^{[l]} n_W^{[l]} n_c^{[l]})^2} \sum_k \sum_{k'} (G_{kk'}^{[l](s)} - G_{kk'}^{[l](G)})^2 \end{aligned}$$

# Style cost function

$$\|G^{T[L](S)} - G^{T[L](G)}\|_F^2$$

$$J_{style}^{[l]}(S, G) = \frac{1}{\left(2n_H^{[l]}n_W^{[l]}n_C^{[l]}\right)^2} \sum_k \sum_{k'} (G_{kk'}^{[l](S)} - G_{kk'}^{[l](G)})$$

$$J_{style}(S, G) = \sum_l \lambda_l^{TL} J_{style}^{TL}(S, G)$$

$$\underbrace{J(G)}_G = \alpha J_{content}(G) + \beta J_{style}(S, G)$$