

Assignment 7

HANDIN:

25.10.24



problem 1

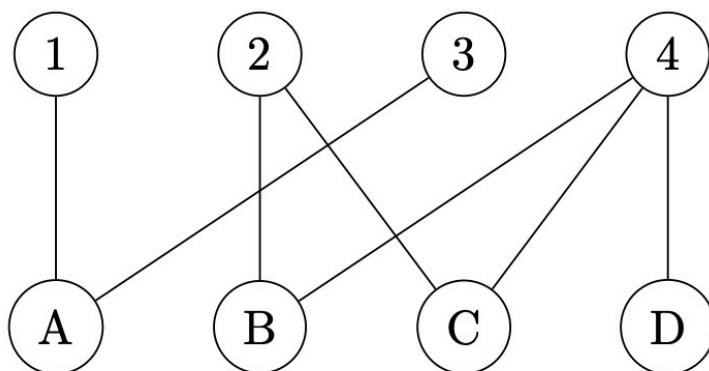
Statement 1:

Disproven \rightarrow A maximum flow does not define a unique minimum capacity cut because multiple cuts with the same capacity may exist.

Statement 2:

Proven \rightarrow A minimum capacity cut uniquely defines the maximum flow value, as the total flow cannot exceed the cut's capacity.

problem 2



Top set $X: \{1, 2, 3, 4\}$
bottom set $Y: \{A, B, C, D\}$ \Rightarrow Hall condition $|N(S)| \geq |S|$ for all $S \subseteq X$

$$S = \{1\}, N(S) = \{A\} \Rightarrow |N(S)| = 1 \geq |S| = 1$$

$$S = \{2\}, N(S) = \{B, C\} \Rightarrow |N(S)| = 2 \geq |S| = 1$$

$$S = \{3\}, N(S) = \{C\} \Rightarrow |N(S)| = 1 \geq |S| = 1$$

$$S = \{4\}, N(S) = \{C, D, B\} \Rightarrow |N(S)| = 3 \geq |S| = 1$$

larger subsets:

$$S = \{1, 2\}, N(S) = \{A, B, C\}, |N(S)| = 3 \geq |S| = 2$$

$$S = \{3, 4\}, N(S) = \{A, B, C, D\}, |N(S)| = 4 \geq |S| = 2$$

$$S = \{1, 2, 3\}, N(S) = \{A, B, C\}, |N(S)| = 3 \geq |S| = 3$$

$$S = \{1, 2, 3, 4\}, N(S) = \{A, B, C, D\}, |N(S)| = 4 \geq |S| = 4$$

Hall condition holds for all subsets

\Rightarrow a perfect matching exists \square

problem 3

* Create a Source(V) and Sink(V)

add vertices for each device d_1, d_2, \dots

and each cell tower c_1, c_2, \dots

* From source to each device, capacity is 1.

From each device d_i to nearby tower c capacity is 1

From each tower c to sink t capacity is $N(\text{tower limit})$

\rightarrow Algorithm (Ford-Fulkerson or Edmonds-Karp)

approach checks if every device can connect with the given constraints.