



# COMP231

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## Join Algorithm

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# Example

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- Consider the following SQL query.
  - E.g., student (sid, sname, age)  
take (sid, cid)

```
select sname  
from student S, take T  
where S.sid = T.sid
```

Student: 500 pages, 80 tuples/page, 50 bytes/tuple  
Take: 1000 pages, 100 tuples/page, 40 bytes/tuple

- 200 courses in table Take  
- 1, 2, ..., 40 in attribute Age  
of table Student



# Example

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- Assuming the following table sizes:
  - Student: 500 pages, 80 tuples/page, 50 bytes/tuple
  - Take: 1000 pages, 100 tuples/page, 40 bytes/tuple
- Assume that there are 200 courses in table Take



# Outline

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- Simple-Nested Loop Join
- Block-Nested Loop Join
- Sort-Merge Join
- Index-Nested Loop Join
- Hash Join

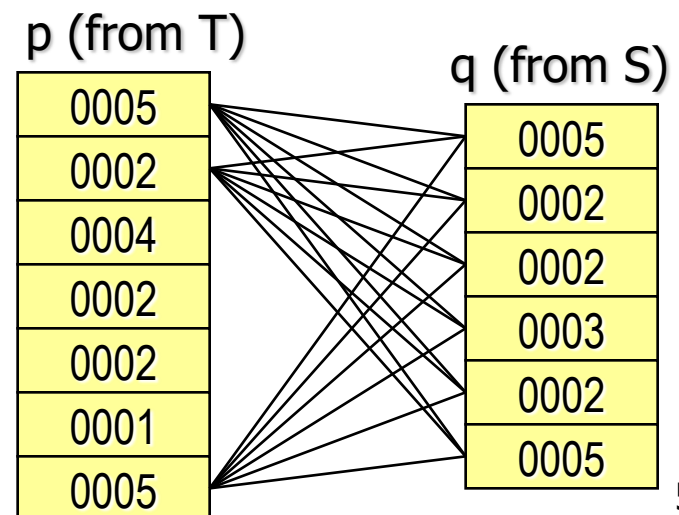
Student: 500 pages, 80 tuples/page, 50 bytes/tuple  
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- 200 courses in table Take  
- 1, 2, ..., 40 in attribute Age of table Student

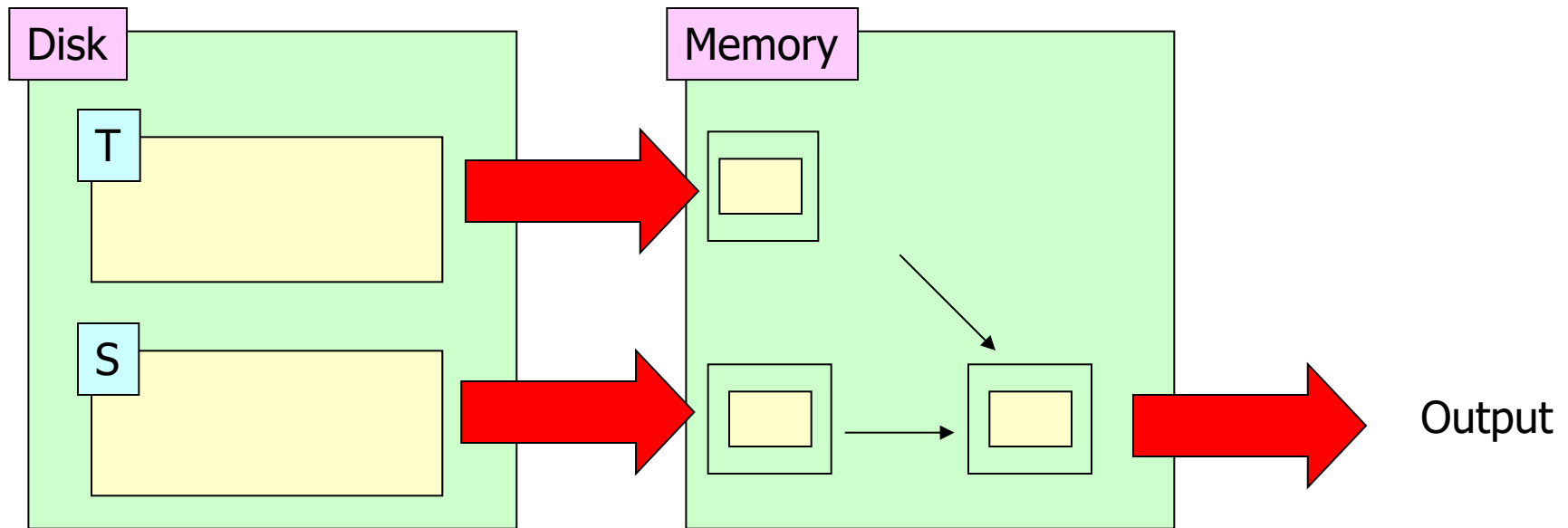
# Simple-Nested Loop Join

For each page  $p$  of  $T$  (T is called *outer relation*)  
  for each page  $q$  of  $S$  (S is called *inner relation*)  
    for each tuple  $t \in p$  and each tuple  $s \in q$   
      such that  $t.sid = s.sid$   
      output  $\langle t, s \rangle$  to the output

For each tuple  $r$  in page  $p$   
  For each tuple  $s$  in page  $q$ ,  
    If  $r.sid = s.sid$  then  
      output the tuple joined from  
      tuple  $r$  and tuple  $s$



# Simple-Nested Loop Join



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Take: 1000 pages, 100 tuples/page, 40 bytes/tuple

- 200 courses in table Take  
- 1, 2, ..., 40 in attribute Age  
of table Student

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    for each page  $q$  of  $S$  (S is called *inner relation*)  
        for each tuple  $t \in p$  and each tuple  $s \in q$   
            such that  $t.sid = s.sid$   
            output  $\langle t, s \rangle$  to the output

We need 3 pages for buffer

1 page for  $p$  (from  $T$ )

1 page for  $q$  (from  $S$ )

1 page for the output

Student: 500 pages, 80 tuples/page, 50 bytes/tuple  
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of table Student

# Simple-Nested Loop Join

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    for each page  $q$  of  $S$  (S is called *inner relation*)  
        for each tuple  $t \in p$  and each tuple  $s \in q$   
            such that  $t.sid = s.sid$   
            output  $\langle t, s \rangle$  to the output

Cost of Reading  $T = 1000$  pages

The total number of times that  $S$  is read = 1000

Cost of Reading  $S$  (with multiple times) =  $1000 * 500 = 500000$  pages

Total Cost =  $1000 + 500000 = 501000$  pages





# Outline

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- Simple-Nested Loop Join
- < Block-Nested Loop Join >
- Sort-Merge Join
- Index-Nested Loop Join
- Hash Join

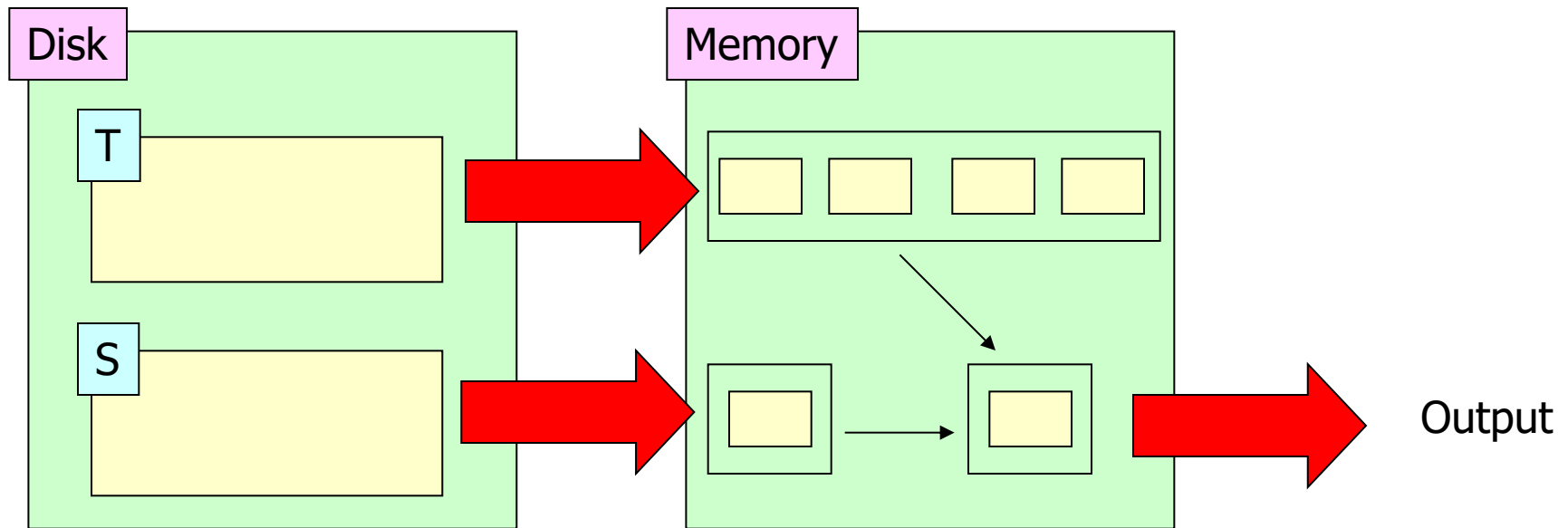
Student: 500 pages, 80 tuples/page, 50 bytes/tuple  
Take: 1000 pages, 100 tuples/page, 40 bytes/tuple

- 200 courses in table Take  
- 1, 2, ..., 40 in attribute Age  
of table Student

# Block-Nested Loop Join

For each block P of T (T is called *outer relation*)  
  for each page q of S (S is called *inner relation*)  
    for each tuple  $t \in P$  and each tuple  $s \in q$   
      such that  $r.sid = s.sid$   
      output  $\langle t, s \rangle$  to the output

# Block-Nested Loop Join



Student: 500 pages, 80 tuples/page, 50 bytes/tuple  
Take: 1000 pages, 100 tuples/page, 40 bytes/tuple

- 200 courses in table Take  
- 1, 2, ..., 40 in attribute Age  
of table Student

# Block-Nested Loop Join

Suppose that  $B = 6$  pages

For each block  $P$  of  $T$  (T is called *outer relation*)  
    for each page  $q$  of  $S$  (S is called *inner relation*)  
        for each tuple  $t \in P$  and each tuple  $s \in q$   
            such that  $t.sid = s.sid$   
            output  $\langle t, s \rangle$  to the output

Suppose we have  $B$  pages in memory (or  $B$  buffer pages)

$B-2$  pages for  $P$  (from  $T$ )

1 page for  $q$  (from  $S$ )

1 page for the output

Student: 500 pages, 80 tuples/page, 50 bytes/tuple  
Take: 1000 pages, 100 tuples/page, 40 bytes/tuple

- 200 courses in table Take  
- 1, 2, ..., 40 in attribute Age  
of table Student

# Block-Nested Loop Join

Suppose that B = 6 pages

For each block P of T (T is called *outer relation*)  
    for each page q of S (S is called *inner relation*)  
        for each tuple  $t \in P$  and each tuple  $s \in q$   
            such that  $t.sid = s.sid$   
            output  $\langle t, s \rangle$  to the output

Cost of Reading T = 1000 pages

The total number of times that S is read =  $\lceil 1000/(6-2) \rceil = 250$

Cost of Reading S (with multiple times) =  $250 * 500 = 125000$  pages

Total Cost =  $1000 + 125000 = 126000$  pages

Student: 500 pages, 80 tuples/page, 50 bytes/tuple  
Take: 1000 pages, 100 tuples/page, 40 bytes/tuple

- 200 courses in table Take  
- 1, 2, ..., 40 in attribute Age  
of table Student

# Block-Nested Loop Join

Suppose that  $B = 6$  pages

- T is the outer relation
- S is the inner relation
- How about the following?
  - T is the inner relation
  - S is the outer relation

Student: 500 pages, 80 tuples/page, 50 bytes/tuple  
Take: 1000 pages, 100 tuples/page, 40 bytes/tuple

- 200 courses in table Take  
- 1, 2, ..., 40 in attribute Age  
of table Student

# Block-Nested Loop Join

Suppose that  $B = 6$  pages

For each block  $P$  of  $S$  ( $S$  is called *outer relation*)  
    for each page  $q$  of  $T$  ( $T$  is called *inner relation*)  
        for each tuple  $s \in P$  and each tuple  $t \in q$   
            such that  $t.sid = s.sid$   
            output  $\langle t, s \rangle$  to the output

Cost of Reading  $S = 500$  pages

The total number of times that  $T$  is read =  $\lceil 500/(6-2) \rceil = 125$

Cost of Reading  $T$  (with multiple times) =  $125 * 1000 = 125000$  pages

Total Cost =  $500 + 125000 = 125500$  pages



# Block-Nested Loop Join

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- Execution 1
  - T is the outer relation
  - S is the inner relation
  - Cost = 126000 pages
- Execution 2
  - S is the inner relation
  - T is the outer relation
  - Cost = 125500 pages
- Which one is better?





# Outline

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- Simple-Nested Loop Join
- Block-Nested Loop Join
- Sort-Merge Join
- Index-Nested Loop Join
- Hash Join



# Sort-Merge Join

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1. Sort table T according to sid
2. Sort table S according to sid
3. Merge table T and table S

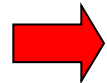
T
0004
0005
0001
0002
0002
0005
0002

S
0003
0002
0005
0002
0005
0002



# Sort-Merge Join

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1. Sort table T according to sid
2. Sort table S according to sid
3. Merge table T and table S

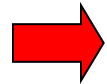
T
0001
0002
0002
0002
0004
0005
0005

S
0003
0002
0005
0002
0005
0002



# Sort-Merge Join

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


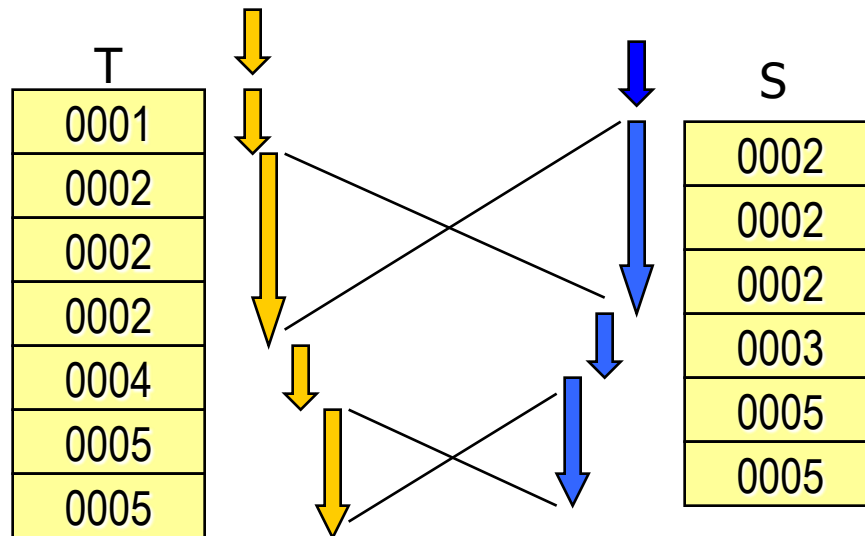
1. Sort table T according to sid
2. Sort table S according to sid
3. Merge table T and table S

T
0001
0002
0002
0002
0004
0005
0005

S
0002
0002
0002
0003
0005
0005

# Sort-Merge Join

- 
1. Sort table T according to sid
  2. Sort table S according to sid
  3. Merge table T and table S





# Sort-Merge Join

---

1. Sort table T according to sid
2. Sort table S according to sid
3. Merge table T and table S

Cost of Sorting =  $2N * (\# \text{ of passes})$

where no. of passes =  $1 + \lceil \log_{B-1} \lceil N / B \rceil \rceil$

Student: 500 pages, 80 tuples/page, 50 bytes/tuple  
Take: 1000 pages, 100 tuples/page, 40 bytes/tuple

- 200 courses in table Take  
- 1, 2, ..., 40 in attribute Age  
of table Student

# Sort-Merge Join

Suppose that B = 6 pages

1. Sort table T according to sid
2. Sort table S according to sid
3. Merge table T and table S

$$\begin{aligned}\text{Cost of Sorting T} &= 2 * 1000 * (1 + \lceil \log_{6-1} \lceil 1000 / 6 \rceil \rceil) \\ &= 10000\end{aligned}$$

$$\begin{aligned}\text{Cost of Sorting S} &= 2 * 500 * (1 + \lceil \log_{6-1} \lceil 500 / 6 \rceil \rceil) \\ &= 4000\end{aligned}$$

$$\begin{aligned}\text{Cost of Merging} &= \text{Cost of Reading T} + \text{Cost of Reading S} \\ &= 1000 + 500 \\ &= 1500\end{aligned}$$

$$\text{Total Cost} = 10000 + 4000 + 1500 = 15500 \text{ pages}$$



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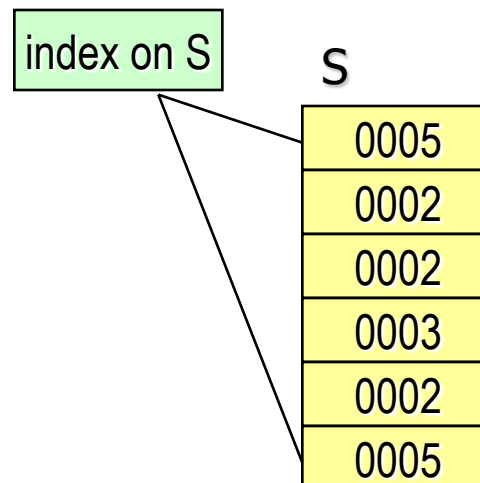


Student: 500 pages, 80 tuples/page, 50 bytes/tuple  
Take: 1000 pages, 100 tuples/page, 40 bytes/tuple

- 200 courses in table Take  
- 1, 2, ..., 40 in attribute Age  
of table Student

# Index-Nested Loop Join

- Assume that there is an index built on attribute sid for table Student
- E.g., If we search for the tuples with sid = 0005



# Index-Nested Loop Join

For each tuple  $t$  of  $T$

$ID \leftarrow t.sid$

use the index to obtain a tuple  $s$  (or tuples) in  $S$

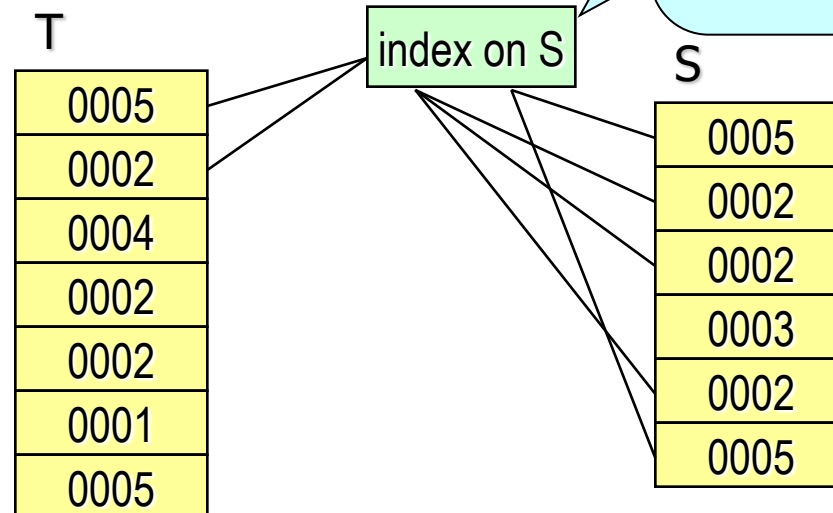
with  $s.sid = ID$

for each such  $s$  in  $S$

output  $\langle t, s \rangle$  to the output

Assume that we have a hash index on  $sid$  for table  $S$

The cost of accessing a hash index is 1.2 pages



Student: 500 pages, 80 tuples/page, 50 bytes/tuple  
Take: 1000 pages, 100 tuples/page, 40 bytes/tuple

- 200 courses in table Take  
- 1, 2, ..., 40 in attribute Age  
of table Student

# Index-Nested Loop Join

Suppose that B = 6 pages

For each tuple  $t$  of  $T$   
     $ID \leftarrow t.sid$   
    use the index to obtain a tuple  $s$  (or tuples) in  $S$   
        with  $s.sid = ID$   
    for each such  $s$  in  $S$   
        output  $\langle t, s \rangle$  to the output

Cost of Reading  $T$  = 1000 pages

The total number of tuples in  $T$  =  $1000 * 100 = 100000$

Cost of Reading  $S$  (with multiple times) =  $100000 * (1.2 + 1) = 220000$  pages

Total Cost =  $1000 + 220000 = 221000$  pages

Why “+1”?



# Outline

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- Block-Nested Loop Join
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- Hash Join



# Hash Join

1. Hash all tuples in T based on sid
2. Hash all tuples in S based on sid
3. For each hash slot,
  1. Join all tuples t from T and all tuples s from S where  $t.sid = s.sid$
  2. Output all these tuples

# Hash Join

