ICPC Library

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1 Template

```
1 #ifndef TEMPLATE
 2 #define TEMPLATE
 4 // #include <bits/stdc++.h>
 5 using namespace std;
 7 #define SZ(x) (int)(x.size())
 8 #define REP(i, n) for(int i = 0; i < n; i++)</pre>
 9 #define FOR(i, a, b) for(int i = a; i < b; i++)
11 using ll = long long;
12 using ld = long double;
13 using P = pair<int, int>;
14 using vi = vector<int>;
15 using vvi = vector<vi>;
16 using vll = vector<ll>;
17 using vvll = vector<vli>;
18 const double eps = 1e-8;
19 const int MOD = 1000000007;
21 //int main() {
22 // cin.tie(0);
23 // ios::sync_with_stdio(false);
24 // cout << fixed << setprecision(10);
25 //
26 //}
27
28 #endif
```

2 Graph

2.1 Dijkstra

```
1 #include "template.cpp"
 3 template<typename T>
 4 vector<T> dijkstra(const Graph<T> &g, int s) {
      const auto INF = numeric_limits<T>::max();
      vector<T> d(g.size(), INF);
      using Pi = pair<T, int>;
      priority_queue<Pi, vector<Pi>, greater<Pi>> que;
      d[s] = 0;
10
11
      que.emplace(d[s], s);
12
      while (!que.empty()) {
13
          T cost;
14
          int v;
          tie(cost, v) = que.top();
15
16
          que.pop();
          if (d[v] < cost) continue;</pre>
17
18
          for (auto &e : g[v]) {
              auto nxt = cost + e.cost;
19
              if (d[e.to] > nxt) {
20
21
                 d[e.to] = nxt;
22
                 que.emplace(nxt, e.to);
```

```
23 }
24 }
25 }
26 return d;
27 }
```

2.2 Dinic

```
1 #include "template.cpp"
3 template<typename T>
 4 struct Dinic {
     const T INF;
      struct edge {
          int to;
9
          T cap;
10
          int rev;
11
          bool isrev;
12
13
14
      vector<vector<edge>> g;
15
      vector<int> level, iter;
16
17
      Dinic(int V) : INF(numeric_limits<T>::max()), g(V) {}
18
19
      void add_edge(int from, int to, T cap) {
          g[from].push_back({to, cap, (int)g[to].size(), false});
20
21
          g[to].push_back({from, 0, (int)g[from].size()-1, true});
22
23
24
      bool bfs(int s, int t) {
25
          level.assign(g.size(), -1);
26
          queue<int> que;
          level[s] = 0;
27
28
          que.push(s);
29
          while (!que.empty()) {
30
             int v = que.front();
              que.pop();
31
32
             for (auto &e : g[v]) {
33
                 if (e.cap > 0 && level[e.to] == -1) {
34
                     level[e.to] = level[v] + 1;
35
                     que.push(e.to);
36
37
             }
38
39
          return level[t] != -1;
40
41
      T dfs(int v, const int t, T flow) {
42
43
          if (v == t) return flow;
          for (int &i = iter[v]; i < g[v].size(); i++) {</pre>
44
45
              edge &e = g[v][i];
46
              if (e.cap > 0 && level[v] < level[e.to]) {</pre>
47
                 T d = dfs(e.to, t, min(flow, e.cap));
                 if (d > 0) {
48
49
                     e.cap -= d;
50
                     g[e.to][e.rev].cap += d;
51
                     return d;
                 }
52
```

```
53
54
55
         return 0:
56
57
58
     T max_flow(int s, int t) {
59
         T flow = 0;
         while (bfs(s, t)) {
60
61
             iter.assign(g.size(), 0);
62
             T f = 0;
63
             while((f = dfs(s, t, INF)) > 0) flow += f;
64
65
         return flow;
66
67 };
```

2.3 Hopcroft Karp

```
1 #include "template.cpp"
 3 struct HopcroftKarp {
      vector<vector<int>> g;
      vector<int> d, mch;
      vector<bool> used, vv;
      HopcroftKarp(int n, int m) : g(n), mch(m, -1), used(n) {}
10
       void add_edge(int u, int v) {
          g[u].push_back(v);
11
12
13
14
       void bfs() {
15
          d.assign(g.size(), -1);
16
          queue<int> que;
          for (int i = 0; i < g.size(); i++) {</pre>
17
              if (!used[i]) {
18
19
                  que.emplace(i);
                  \bar{d}[i] = 0;
20
^{21}
22
23
24
          while (!que.empty()) {
^{25}
              int a = que.front();
26
              que.pop();
27
              for (auto &b : g[a]) {
28
                  int c = mch[b];
29
                  if (c >= 0 \&\& d[c] == -1) {
30
                     d[c] = d[a] + 1;
31
                      que.emplace(c);
32
33
34
          }
35
      }
36
37
      bool dfs(int a) {
38
          vv[a] = true;
39
          for (auto &b : g[a]) {
40
              int c = mch[b];
41
              if (c < 0 \mid | (!vv[c] && d[c] == d[a] + 1 && dfs(c))) {
                  mch[b] = a;
```

```
used[a] = true:
44
                 return (true);
45
          }
46
47
          return (false):
48
49
50
      int bipartite_matching() {
51
          int ret = 0;
          while (true) {
52
53
              bfs();
54
              vv.assign(g.size(), false);
55
              int flow = 0;
              for (int i = 0; i < g.size(); i++) {</pre>
56
57
                 if (!used[i] && dfs(i)) ++flow;
58
59
              if (flow == 0) return ret:
60
              ret += flow;
61
62
63 };
```

2.4 Kruskal

```
1 #include "template.cpp"
 3 #include "../structure/union_find.cpp"
 5 template<typename T>
 6 T kruskal(vector<edge<T>> &es, int V) {
      UnionFind uf(V):
      T ret = 0:
      // sort destructively
      sort(es.begin(), es.end(), [](edge<T> &a,edge<T> &b){
12
13
              return a.cost < b.cost;</pre>
14
      for (auto &e : es) {
15
16
          if (!uf.issame(e.src, e.to)) {
17
             ret += e.cost;
18
             uf.merge(e.src, e.to);
19
20
21
      // // sort only the order to check
      // vector<int> ord(es.size());
      // iota(ord.begin(), ord.end(), 0);
      // sort(ord.begin(), ord.end(), [&](int i,int j){
      // return es[i].cost < es[j].cost;</pre>
27
      // });
28
      // for (auto i : ord) {
      // auto &e = es[i]:
      // if (!uf.issame(e.src, e.to)) {
      // ret += e.cost;
      // uf.merge(e.src, e.to);
33
      // }
      // }
34
35
36
      return ret;
```

37 }

2.5 LCA

```
1 #include "../template.cpp"
 3 struct LCA {
      int n, log2_n;
      vector<int> depth;
      vector<vector<int>> par;
      void dfs(const vector<vector<int>>& G, int v, int p, int d) {
          depth[v] = d;
          par[0][v] = p;
10
11
          for (auto to : G[v]) {
12
              if (to != p) dfs(G, to, v, d+1);
13
      }
14
15
      LCA(const vector<vector<int>>& G. int root=0) :
16
          n(G.size()), log2_n(log2(n)), depth(n),
17
18
          par(log2_n+1, vector < int > (n,-1)) {
19
20
              dfs(G, root, -1, 0);
21
22
              for (int k = 0; k < log2_n; ++k) {
23
                 for (int v = 0; v < n; ++v) {
24
                     if (par[k][v] != -1) {
25
                         par[k+1][v] = par[k][par[k][v]];
26
27
28
              }
29
          }
30
31
      int query(int u, int v) {
32
          if (depth[u] > depth[v]) swap(u, v);
33
34
          // align the depth of u and v
35
          for (int k = 0; k <= log2_n; ++k) {</pre>
36
              if ((depth[v] - depth[u]) >> k & 1) {
37
                  v = par[k][v];
38
          }
39
40
          if (u == v) return u;
41
42
          // go back until u and v's parents do not match
          for (int k = log2_n; k >= 0; --k) {
43
              if (par[k][u] != par[k][v]) {
    u = par[k][u];
44
45
                 v = par[k][v];
46
47
48
          return par[0][u];
50
51 };
```

2.6 Lowlink

```
1 #include "./template.cpp"
 3 template<typename T>
 4 struct LowLink {
      const int inf = 1000000000;
      int sz;
      std::vector<int> pre, low;
      std::vector<bool> sel;
      std::vector<std::pair<int, int>> bridge;
10
      std::vector<int> articulation;
11
12
      LowLink(const Graph<T> &g) {
13
          sz = g.size();
14
          pre.resize(sz, inf);
15
          low.resize(sz. inf):
16
          sel.resize(sz, false);
17
          int cnt = 0:
18
          dfs(g, 0, -1, cnt);
19
20
21
      void dfs(const Graph<T> &g, int now, int prev, int &cnt) {
22
          if(pre[now] != inf) {
23
             low[prev] = min(low[prev], pre[now]);
24
             return:
25
          }
26
          pre[now] = cnt;
27
          low[now] = cnt;
28
          cnt++;
29
          for(int i=0;i<(int)(g[now].size());++i) {</pre>
30
              int nxt = g[now][i].to;
31
              //if g is an undirected graph
32
              if(nxt == prev) continue;
33
              dfs(g, nxt, now, cnt);
34
          if(prev != -1) low[prev] = min(low[prev], low[now]);
35
          if(prev != -1 && pre[prev] < low[now]) {</pre>
36
              bridge.emplace_back(make_pair(prev, now));
37
38
      }
39
40
41
      void get_articulation(const Graph<T> &g, int now, int prev) {
42
          sel[now] = true;
43
          int art = 0;
44
          for(int i=0;i<(int)(g[now].size());++i) {</pre>
45
             int nxt = g[now][i].to;
              //cout << now << ":" << nxt << endl;
46
              if(sel[nxt]) continue;
47
             // if g is an undirected graph
48
49
              if(nxt == prev) continue;
              if(now == 0 || pre[now] <= low[nxt]) art++;</pre>
50
             get_articulation(g, nxt, now);
51
52
53
          if((now == 0 \&\& art >= 2) || (now != 0 \&\& art >= 1)) {}
54
              articulation.push_back(now);
55
56
57 };
```

2.7 Maximum Clique

```
1 #include "template.cpp"
 3 int maximum_clique(const vector<vector<bool>>& G) {
       // G: 隣接行列, 無向グラフ
       int n = G.size();
       vector<int> deg(n);
       int M = 0:
       for (int i = 0; i < n; ++i) {</pre>
          for (int j = i+1; j < n; ++j) {
10
              ++deg[i], ++deg[j], ++M;
11
12
       vector<vector<bool>> g = G;
13
14
       vector<bool> used(n);
15
16
       int \lim = \operatorname{sqrt}(2*M), ret = 0;
17
18
      for (int t = 0; t < n; ++t) {</pre>
19
          int u = -1:
          for (int i = 0; i < n; ++i) {</pre>
20
              if (!used[i] && deg[i] < lim) {</pre>
21
22
                  u = i;
23
                  used[u] = true;
^{24}
                  break;
25
26
27
28
          vector<int> neighbor;
29
          if (u != -1) neighbor.push_back(u);
          for (int v = 0; v < n; ++v) if (!used[v]) {</pre>
30
31
               if (u == -1 || g[u][v]) {
32
                  neighbor.push_back(v);
33
34
35
          int sz = neighbor.size();
36
37
          vector<int> bit(sz):
          for(int i = 0; i < sz; i++) {</pre>
38
39
               for(int j = i+1; j < sz; j++) {</pre>
40
                  if(!g[neighbor[i]][neighbor[j]]) {
                      bit[i] |= 1 << j;
41
42
                      bit[j] |= 1 << i;
43
              }
44
          }
45
46
          vector<int> dp(1<<sz);</pre>
47
          dp[0] = 1:
48
          for (int s = 1; s < 1<<sz; ++s) {
49
              int i = __builtin_ffs(s) - 1;
50
51
52
              if (dp[s] = dp[s & ~(1<<i)] && (bit[i] & s) == 0) {</pre>
53
                  ret = max(ret, __builtin_popcount(s));
54
55
          }
56
57
          if (u == -1) break:
58
59
          for (auto v : neighbor) {
60
               --deg[v]. --deg[u]:
               g[u][v] = g[v][u] = false;
61
62
```

```
63 }
64
65 return ret;
66 }
```

2.8 Primal Dual

```
1 #include "template.cpp"
 3 template<typename flow_t, typename cost_t>
 4 struct PrimalDual {
     const cost t INF:
      struct edge {
         int to:
9
         flow_t cap;
10
          cost_t cost;
11
         int rev;
12
13
      vector<vector<edge>> g;
14
      vector<cost_t> h, d;
15
      vector<int> prevv, preve;
16
      PrimalDual(int V) : g(V), INF(numeric_limits< cost_t >::max()) {}
17
18
19
      void add_edge(int from, int to, flow_t cap, cost_t cost) {
20
          g[from].push_back({to, cap, cost, (int)g[to].size()});
          g[to].push_back({from, 0, -cost, (int)g[from].size()-1});
21
22
23
24
      cost_t min_cost_flow(int s, int t, flow_t f) {
25
         int V = (int)g.size();
26
          cost_t ret = 0;
27
         using Pi = pair<cost_t, int>;
          priority_queue<Pi, vector<Pi>, greater<Pi>> que;
28
29
          h.assign(V, 0);
30
         preve.assign(V, -1);
31
         prevv.assign(V, -1);
32
33
          while (f > 0) {
34
             d.assign(V, INF);
35
             que.emplace(0, s);
36
             d[s] = 0;
37
             while (!que.empty()) {
                 Pi p = que.top(); que.pop();
38
                 if (d[p.second] < p.first) continue;</pre>
39
                 for (int i = 0; i < g[p.second].size(); i++) {</pre>
40
                     edge &e = g[p.second][i];
41
                     cost_t nextCost = d[p.second] + e.cost +
42
                        h[p.second] - h[e.to];
43
                     if (e.cap > 0 && d[e.to] > nextCost) {
44
                        d[e.to] = nextCost;
45
46
                        prevv[e.to] = p.second, preve[e.to] = i;
47
                        que.emplace(d[e.to], e.to);
48
49
                }
50
51
             if (d[t] == INF) return -1;
             for (int v = 0; v < V; v++) h[v] += d[v];
52
             flow_t addflow = f;
```

```
for (int v = t; v != s; v = prevv[v]) {
54
55
                 addflow = min(addflow, g[prevv[v]][preve[v]].cap);
56
57
             f -= addflow;
58
             ret += addflow * h[t]:
59
             for (int v = t; v != s; v = prevv[v]) {
60
                 edge &e = g[prevv[v]][preve[v]];
61
                 e.cap -= addflow;
62
                 g[v][e.rev].cap += addflow;
63
64
         }
65
         return ret;
66
67 };
```

2.9 SCC

```
1 #include "template.cpp"
 3 template<typename T>
 4 struct SCC {
      int sz, cnt, num;
      vi post, comp;
      vector<pair<int, int>> vp;
      vector<bool> sel;
 9
      Graph<T> revg;
10
11
      SCC(const Graph<T> &g) {
12
          sz = g.size();
13
          cnt = 0;
14
          num = 0:
          post.resize(sz, -1);
15
16
          comp.resize(sz, -1);
17
          sel.resize(sz, false);
18
          revg.resize(sz);
      }
19
20
21
      void build(const Graph<T> &g) {
22
          for(int i=0;i<sz;++i) {</pre>
23
              if(sel[i]) continue;
24
              sel[i] = true;
25
              dfs1(g, i);
26
          }
27
28
          rev(g, revg);
29
30
          for(int i=0;i<sz;++i) {</pre>
31
              vp.emplace_back(make_pair(post[i], i));
32
33
          sort(vp.begin(), vp.end());
34
          reverse(vp.begin(), vp.end());
35
          sel.clear();
36
          sel.resize(sz, false);
37
          for(int i=0;i<sz;++i) {</pre>
38
              if(sel[vp[i].second]) continue;
39
              sel[vp[i].second] = true;
40
              comp[vp[i].second] = num;
41
              dfs2(revg, vp[i].second);
42
              num++;
43
```

```
44
45
46
      vi get_comp() {return comp;}
47
48
      Graph<T> build_graph(const Graph<T> &g) {
49
          build(g);
50
          vector<set<int>> s(sz);
51
          Graph<T> res(sz);
52
          for(int i=0;i<sz;++i) {</pre>
              for(int j=0;j<(int)(g[i].size());++j) {</pre>
53
54
                 s[comp[i]].insert(comp[g[i][j].to]);
55
56
          }
57
          for(int i=0;i<sz;++i) {</pre>
58
              for(auto j: s[i]) {
59
                 if(i != j) res[i].push_back(edge<int>(i, j, 1));
60
          }
61
62
          return res;
63
64
65
      void dfs1(const Graph<T> &g, int now) {
66
          for(int i=0;i<(int)(g[now].size());++i) {</pre>
67
              int nxt = g[now][i].to;
68
              if(sel[nxt]) continue:
69
              sel[nxt] = true;
70
              dfs1(g, nxt);
71
72
          post[now] = cnt;
73
          cnt++;
74
75
76
      void rev(const Graph<T> &g, Graph<T> &revg) {
77
          for(int i=0;i<sz;++i) {</pre>
78
              for(int j=0;j<(int)(g[i].size());++j) {</pre>
79
                  revg[g[i][j].to].push_back({
80
                         g[i][j].to, g[i][j].src, g[i][j].cost});
81
82
          }
      }
83
84
85
      void dfs2(const Graph<T> &revg, int now) {
          for(int i=0;i<(int)(revg[now].size());++i) {</pre>
86
87
              int nxt = revg[now][i].to;
88
              if(sel[nxt]) continue;
89
              sel[nxt] = true;
90
              comp[nxt] = num;
              dfs2(revg, nxt);
91
92
93
94 };
```

2.10 Topological Sort

```
1 #include "template.cpp"
2
3 void topological_sort(const vector<vector<int>>& G, vector<int>& ord)
4 {
5    int n = G.size();
6    vector<int> num(n, 0);
```

```
ord.assign(n, 0);
      for (int i = 0; i < n; ++i) {</pre>
          for (auto u : G[i]) {
10
              ++num[u];
11
      }
12
13
      stack<int> st;
      for(int i = 0; i < n; ++i) {</pre>
14
          if (num[i] == 0) {
15
16
              st.push(i);
17
     }
18
19
      for (int k = 0; !st.empty(); ++k) {
20
         int i = st.top(); st.pop();
21
          ord[k] = i;
          for (auto u : G[i]) {
22
23
              if (--num[u] == 0) {
24
                 st.push(u);
25
26
          }
27
      }
28 }
```

2.11 Warshall Floyd

```
1 #include "template.cpp"
 3 template<typename T>
 4 void warshall_floyd(vector<vector<T>> &g) {
      const auto INF = numeric_limits<T>::max();
      int n = g.size();
      for(int k = 0; k < n; k++) {
          for(int i = 0; i < n; i++) {</pre>
9
              for(int j = 0; j < n; j++) {
10
                 if(g[i][k] == INF | | g[k][j] == INF) continue;
11
                 g[i][j] = min(g[i][j], g[i][k] + g[k][j]);
12
13
14
15 }
```

3 Number

3.1 Mod

```
1 #include "../template.cpp"
2
3 ll powm(ll a, ll n, ll m) {
4     ll ret = 1;
5     while (n > 0) {
6         if (n & 1) (ret *= a) %= m;
7         (a *= a) %= m;
8         n >>= 1;
```

```
9 }
10 return ret;
11 }
12 
13 11 invm(11 a, 11 m) {
14 return powm(a, m-2, m);
15 }
```

3.2 ExtendedGCD

3.3 Combination

```
1 #include "mod.cpp"
3 vector<11> fact;
4 void init_fact(int n, ll m) {
      fact.assign(n+1, 1);
      for (int i = 2; i \le n; ++i) {
          (fact[i] = fact[i-1] * i) %= m;
9 }
11 // require init_fact(GREATER THAN OR EQUAL TO n, m)
12 11 C(11 n, 11 r, 11 m) {
     return (fact[n] * invm((fact[r] * fact[n-r]) % m, m)) % m;
14 }
15
16 // Stirling number
17 // Stirling(n, k) := the number of cases
18 // to split n balls(distinguished)
19 // into k boxes(not distinguished)
20 // s.t. each box contains at least one ball.
21 //
22 // require init_fact(GREATER THAN OR EQUAL TO k, m)
23 ll Stirling(ll n, ll k, ll m) {
     ll ret = 0;
      for (11 1 = 0; 1 <= k; ++1) {
         ll tmp = (C(k, 1, m) * powm((k-1) % m, n, m)) % m;
26
         if (1 & 1) tmp = (-tmp + m) % m;
28
          (ret += tmp) ^{1} = m;
      return (ret *= invm(fact[k], m)) %= m;
31 }
32
```

```
33 // Bell number
34 // Bell(n, k) := the number of cases
35 // to split n balls(distinguished)
36 // into k boxes(not distinguished)
38 // require init_fact(GREATER THAN OR EQUAL TO k, m)
39 ll Bell(ll n, ll k, ll m) {
     ll ret = 0:
      for (11 1 = 0; 1 <= k; ++1) {
41
          (ret += Stirling(n, 1, m)) %= m;
42
43
44
      return ret;
45 }
46
47 // Partition function
48 // Partition[k][n] := the number of cases
49 // to split n balls(not distinguished)
50 // into k boxes(not distinguished)
51 vector<vector<ll>>> Part;
52 void init_partition(ll k, ll n, ll m) {
      Part.assign(k+1, vector<ll>(n+1, 0));
      Part[0][0] = 1;
55
      for (int i = 1; i <= k; ++i) {</pre>
         for (int j = 0; j <= n; ++j) {
57
             if (i-i >= 0) {
                 Part[i][j] = (Part[i-1][j] + Part[i][j-i]) % m;
58
59
             } else {
                 Part[i][j] = Part[i-1][j];
60
61
         }
62
     }
63
64 }
```

4.2 Z Algorithm

```
1 #include "../template.cpp"
3 // GET A[i]: the longest common prefix size of S and S[i:n-1]
4 template<typename S>
5 void z_algorithm(const S& s, vector<int>& A) {
      int n = s.size();
      A.resize(n);
      A[0] = n;
      int i = 1, j = 0;
      while (i < n) {
          while (i+j < n \&\& s[j] == s[i+j]) ++j;
12
          if (j == 0) { ++i; continue; }
13
14
          while (i+k < n \&\& k+A[k] < j) \{ A[i+k] = A[k]; ++k; \}
15
16
          i += k; j -= k;
17
18 }
```

4 String

4.1 Rolling Hash

```
1 #include "../template.cpp"
 3 struct RollingHash {
      const int base = 9973;
      const int mod[2] = {999999937, 1000000007};
      vector<int> s;
       vector<11> hash[2], pow[2];
      RollingHash(const vector<int> &cs) : s(cs) {
9
10
          int n = s.size();
          for (int id = 0; id < 2; ++id) {
   hash[id].assign(n+1, 0);</pre>
11
12
13
              pow[id].assign(n+1, 1);
              for (int i = 0; i < n; ++i) {
14
                  hash[id][i+1] = (hash[id][i] * base + s[i]) % mod[id];
15
16
                  pow[id][i+1] = pow[id][i] * base % mod[id];
17
          }
18
19
      }
20
21
      // get hash of s[l:r)
```

5 Structure

5.1 Segment Tree

```
1 #include "../template.cpp"
 3 template<typename M>
 4 struct SegmentTree {
      int sz;
      vector<M> data;
      const M e = numeric_limits<M>::max();
      const function<M(M.M)> f = [](M a.M b){ return min(a.b): }:
11
      SegmentTree(int n) {
12
13
          while (sz < n) sz <<= 1;
14
15
          data.assign(2*sz, e);
16
17
18
      void update(int k, const M &x) {
19
         k += sz:
20
         data[k] = x;
21
          while (k >>= 1) {
```

```
data[k] = f(data[2*k], data[2*k+1]);
22
23
     }
24
25
26
      M query(int a, int b, int k, int l, int r) {
          if (r <= a || b <= 1) {
27
28
             return e;
29
         } else if (a <= 1 && r <= b) {</pre>
30
             return data[k];
31
         } else {
32
             return f(query(a,b,2*k, 1,(1+r)/2),
33
                      query(a,b,2*k+1,(1+r)/2,r));
34
     }
35
36
37
      M query(int a, int b) {
38
         // return f[a,b)
39
         return query(a, b, 1, 0, sz);
40
41
42
      M operator[](int k) {
43
         return data[k + sz];
44
45 };
```

5.2 Lazy Segment Tree

```
1 #include "../template.cpp"
 3 template<typename M, typename OM = M>
 4 struct LazySegmentTree {
       int sz;
       vector<M> data;
       vector<OM> lazy;
       // RangeSumRangeAdd
       const function<M(M,M)> f = [](M a,M b){ return a+b; };
const function<M(M,OM,int)> g = [](M a,OM b,int 1){ return a+b*1; };
const function<OM(OM,OM)> h = [](OM a,OM b){ return a+b; };
10
11
12
13
       const M e = 0;
       const OM oe = 0;
14
15
       LazySegmentTree(int n) {
16
17
           sz = 1;
18
           while (sz < n) sz <<= 1;
19
           data.assign(2*sz, e);
20
           lazy.assign(2*sz, oe);
21
22
23
       void propagate(int k, int len) {
24
           if (lazy[k] == oe) return;
25
           if (k < sz) {
                lazy[2*k] = h(lazy[2*k], lazy[k]);
26
27
                lazy[2*k+1] = h(lazy[2*k+1], lazy[k]);
28
29
           data[k] = g(data[k], lazy[k], len);
30
           lazy[k] = oe;
31
32
       M update(int a, int b, const OM &x, int k, int l, int r) {
```

```
propagate(k, r - 1);
34
35
          if (r <= a || b <= 1) {
36
             return data[k]:
37
          } else if (a <= l && r <= b) {</pre>
38
             lazy[k] = h(lazy[k], x);
39
             propagate(k, r - 1);
40
              return data[k];
          } else {
41
42
             return data[k] = f(
43
                 update(a, b, x, 2*k, 1, (1+r)/2),
                 update(a, b, x, 2*k+1, (1+r)/2, r));
44
45
      }
46
47
48
      void update(int a, int b, const OM &x) {
49
          // update [a, b) with x.
50
          update(a, b, x, 1, 0, sz);
51
52
53
      M query(int a, int b, int k, int l, int r) {
          propagate(k, r - 1);
54
55
          if (r <= a || b <= 1) {
56
             return e:
57
          } else if (a <= 1 && r <= b) {</pre>
             return data[k]:
59
          } else {
60
61
                 query(a, b, 2*k, 1, (1+r)/2),
62
                 query(a, b, 2*k+1, (1+r)/2, r));
63
64
65
66
      M query(int a, int b) {
67
          // return f[a, b).
68
          return query(a, b, 1, 0, sz);
69
70 };
```

5.3 Union Find

```
1 #include "../template.cpp"
3 struct UnionFind
4 {
      vector<int> par, sz;
      UnionFind(int n) : par(n), sz(n, 1) {
          for (int i = 0; i < n; ++i) par[i] = i;</pre>
8
9
      int root(int x) {
10
          if (par[x] == x) return x;
         return par[x] = root(par[x]);
11
12
13
      void merge(int x, int y) {
         x = root(x);
14
15
         y = root(y);
         if (x == y) return;
16
         if (sz[x] < sz[y]) swap(x, y);
17
         par[y] = x;
18
19
         sz[x] += sz[y];
          sz[v] = 0;
```

```
21    }
22    bool issame(int x, int y) {
23        return root(x) == root(y);
24    }
25    int size(int x) {
26        return sz[root(x)];
27    }
28 };
```

5.4 Weighted Union Find

```
1 #include "../template.cpp"
 3 template<typename A>
 4 struct WeightedUnionFind
      vector<int> par, sz;
      vector<A> data; // data[x]: diff from root to x
      WeightedUnionFind(int n, A e=0) :
          par(n), sz(n, 1), data(n, e) {
          for (int i = 0; i < n; ++i) par[i] = i;</pre>
10
11
12
      int root(int x) {
13
          if (par[x] == x) return x;
14
15
         int r = root(par[x]);
         data[x] += data[par[x]];
16
17
         return par[x] = r;
18
19
      A weight(int x) {
20
21
         root(x);
22
         return data[x];
23
24
25
      A diff(int x, int y) {
          // diff from x to y
26
27
         return data[y] - data[x];
28
29
30
      void merge(int x, int y, A w) {
          // merge so that "diff from x to y" will be w.
31
32
         w += weight(x); w -= weight(y);
33
         x = root(x); y = root(y);
34
         if (x == y) return;
         if (sz[x] < sz[y]) swap(x, y), w = -w;
35
36
         par[y] = x;
         sz[x] += sz[y];
37
38
         sz[y] = 0;
39
         data[y] = w;
     }
40
41
      bool issame(int x, int y) {
43
         return root(x) == root(y);
44
45 };
```

6 Vimrc

```
1 syntax enable
2 set number
3 set autoindent
4 set expandtab
5 set tabstop=4
6 set shiftwidth=4
```

7 Emacs

```
1 (package-initialize)
 3 (setq inhibit-startup-message t)
 5 (setq make-backup-files nil)
 7 (setq delete-auto-save-files t)
9 (setq-default tab-width 4 indent-tabs-mode nil)
11 (setq eol-mnemonic-dos "(CRLF)")
12 (setq eol-mnemonic-mac "(CR)")
13 (setq eol-mnemonic-unix "(LF)")
15 (tool-bar-mode -1)
16 (menu-bar-mode -1)
18 (column-number-mode t)
19 (global-linum-mode t)
20 (blink-cursor-mode t)
21 (show-paren-mode 1)
22 (setq mouse-wheel-scroll-amount '(1 ((shift) . 5)))
23 (load-theme 'monokai t)
```