

Tutorial 2: PHY101  
(MONSOON 2023)

1. A particle moves along the curve  $x = 2\sin 3t$ ,  $y = 2\cos 3t$ ,  $z = 8t$ , where  $t$  is the time. Find the components of velocity and acceleration of the particle at  $t = \pi/3$  in the direction  $\hat{i} + \hat{j} + \hat{k}$ .
2. Find the unit tangent vector to any point on the curve  $x = 2t^2$ ,  $y = t^2 - 4t$ ,  $z = 3t - 5$ . Determine the unit tangent at  $t = 2$ .
- 3) Find the projection of the vector  $\mathbf{A} = \mathbf{i} - 2\mathbf{j} + \mathbf{k}$  on the vector  $\mathbf{B} = 4\mathbf{i} - 4\mathbf{j} + 7\mathbf{k}$
- 4) Find the area of the triangle having vertices at P(1, 3, 2), Q(2, -1, 1), R(-1, 2, 3).
- 5) Two vectors A and B have equal magnitudes of 10 units. Vector A makes an angle of 30 degrees with the positive x-axis, while vector B makes an angle of 45 degrees with the positive y-axis. Calculate the dot product and cross product of vectors A and B.
- 6) For what value of 'a' are  $\vec{A} = a\hat{i} - 2\hat{j} + \hat{k}$  and  $\vec{B} = 2a\hat{i} + a\hat{j} - 4\hat{k}$  perpendicular?