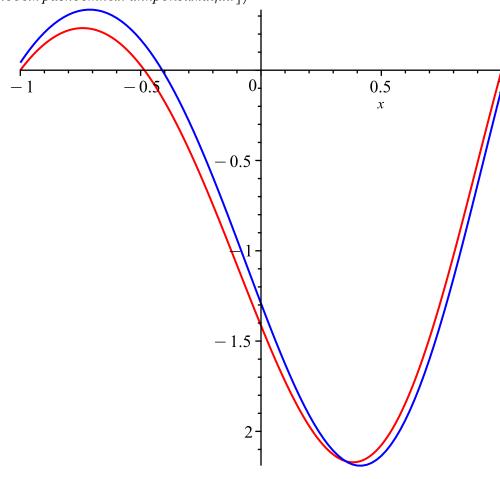
```
#
      local i, n, x arr, x, alpha arr, beta arr;
      n := numelems(a);
      alpha\_arr := Array(\left|-\frac{c[1]}{b[1]}\right|);
     beta\_arr := Array \left( \left\lceil \frac{f[1]}{b[1]} \right\rceil \right);
      f[1] := f[1] - a[1] \cdot L;
      f[n] := f[n] - c[n] \cdot R;
      a[1] := 0;
      c[n] := 0;
      for i from 2 to n do
       \begin{aligned} & \textit{ArrayTools:-Append} \bigg( \textit{alpha\_arr}, -\frac{c[i-1]}{a[i-1] \cdot \textit{alpha\_arr}[i-1] + b[i-1]} \bigg); \\ & \textit{ArrayTools:-Append} \bigg( \textit{beta\_arr}, \frac{f[i-1] - a[i-1] \cdot \textit{beta\_arr}[i-1]}{a[i-1] \cdot \textit{alpha\_arr}[i-1] + b[i-1]} \bigg); \end{aligned}
       end do;
      x \ arr := Array([]);
      for i from 1 to n do
       ArrayTools:-Append(x \ arr, cat(x, i));
      end do;
       x\_arr[n] := \frac{-a[n] \cdot beta\_arr[n] + f[n]}{a[n] \cdot alpha\_arr[n] + b[n]};
      for i from n-1 to 1 by -1 do
        x \ arr[i] := alpha \ arr[i+1] \cdot x \ arr[i+1] + beta \ arr[i+1];
       end do;
      return x arr
      end proc:
                                                                                      y''+p(x)y'+q(x)y=f(x)
 \rightarrow difference method := \mathbf{proc}(p, q, f, h, l, r, L, R)
      local a, b, c, d, i, n, x \ arr, xk
       a := Array([]);
       b := Array([]);
       c := Array([\ ]);
       d := Array([\ ]);
       x\_arr := Array([\ ]);
       n := \operatorname{floor}\left(\frac{r-l}{h}\right);
       xk := l;
       for i from 1 to n + 1 do
       ArrayTools:-Append \left(a, 1 - \frac{p(xk)}{2} \cdot h\right);
      ArrayTools:-Append \left(b, -2 + q(xk) \cdot h^2 - \frac{p(xk)}{2} \cdot h\right);
       ArrayTools:-Append(c, 1);
```

```
ArrayTools:-Append(d, f(xk) \cdot h^2);
      ArrayTools:-Append(x arr, xk);
      xk := xk + h;
      end do:
      return [x\_arr, running(a, b, c, d, L, R)]
     end proc:
 \rightarrow chebyshev\_norm := \mathbf{proc}(x\_arr, y\_arr, func)
      local res, i, temp;
      res := 0;
      for i from 1 to numelems(x \ arr) do
      temp := abs(y\_arr[i] - rhs(evalf(subs(x = x\_arr[i], sol))));
      if temp > res then
      res := temp;
      end if
      end do;
      return res;
      end proc:
 > evklid_norm := proc(x_arr, y_arr, func)
      local res, i;
      res := 0;
      for i from 1 to numelems(x \ arr) do
      res := res + (y\_arr[i] - rhs(evalf(subs(x = x\_arr[i], sol))))^2
      end do;
      return sqrt(res)
end proc:
                                                      #1
 ode := diff(y(x), x$2) + p(x) \cdot diff(y(x), x) + q(x) \cdot y(x) = f(x) 
 ode := \frac{d^2}{dx^2} y(x) + \frac{(1 + \cos(19) x) y(x)}{\sin(19)} = -\frac{1}{\sin(19)} 
                                                                                                           (1)
sol := dsolve(\{y(-1) = 0, y(1) = 0, ode\}):
res := difference\_method(p, q, f, 0.02, -1, 1, 0, 0):
 \rightarrow plot2 := plots:-pointplot([seq([convert(res[1][i], float), convert(res[2][i], float)], i = 1
         ..numelems(res[1]))], connect = true):
```

> plots[display](plot1, plot2, color = [red, blue], legend = [Решение, Методом разностных аппроксимаций])



• Решение - Методом разностных аппроксимаций

#2

> chebyshev_norm(res[1], evalf(res[2]), sol)

(2)

$$p(x) := x$$
:

$$q(x) := x$$

>
$$p(x) := x :$$

> $q(x) := x :$
> $f(x) := x^2 :$
> $l := 0 :$
> $r := 1 :$
> $L := 1 :$
> $k := 0.1 :$

$$l := 0$$

$$r := 1$$
:

$$L := 1:$$

$$R := 1$$
:

$$h := 0.1$$
:

>
$$ode := diff(y(x), x\$2) + p(x) \cdot diff(y(x), x) + q(x) \cdot y(x) = f(x)$$

$$ode := \frac{d^2}{dx^2} y(x) + x \left(\frac{d}{dx} y(x)\right) + x y(x) = x^2$$
(3)

 $\gt{sol} := dsolve(\{y(l) = L, y(r) = R, ode\})$

$$sol := y(x) = \frac{e^{\frac{x(-2+x)}{2}} \left(2 e^{\frac{1}{2}} \operatorname{erfi}\left(\frac{\sqrt{2}}{2}\right) - \operatorname{erfi}(\sqrt{2})\right) e^{\frac{1}{2}}}{\operatorname{erfi}\left(\frac{\sqrt{2}}{2}\right) - \operatorname{erfi}(\sqrt{2})}$$

$$+ \frac{1e^{\frac{x^{2}-2}{2}} \operatorname{erf}\left(\frac{1}{2}\sqrt{2}(-2+x)\right) \left(-1+2 e^{\frac{1}{2}}\right) e^{\frac{1}{2}}}{-\operatorname{erfi}\left(\sqrt{2}\right)} + x-1$$

$$-\operatorname{erfi}\left(\frac{\sqrt{2}}{2}\right) + \operatorname{erfi}(\sqrt{2})$$

$$> plot1 := plot(rhs(sol), x-1..r) :$$

$$> res := difference method(p, q, f, h, l, r, L, R) :$$

$$> plot2 := plots:-pointplot([seq([convert(res[1]|i|, float), convert(res[2]|i|, float)], i=1$$
...numelens(res[1])); connect—true) :
$$> plots[display[[float, plot2, color=[red, blue], legend=[Peuuenue, Memodosi pariocimiosis amiposicus a$$

```
q(x) := -1.5 x:
 ode := \frac{d^2}{dx^2} y(x) + 2 \frac{d}{dx} y(x) - 1.5 x y(x) = \frac{2}{x}
                                                                                            (6)
 \gt{sol} := dsolve(\{y(l) = L, y(r) = R, ode\}):
 \triangleright plot1 := plot(rhs(sol), x = l..r):
 [ > res := difference\_method(p, q, f, h, l, r, L, R) :
 > plot2 := plots:-pointplot([seq([convert(res[1][i], float), convert(res[2][i], float)], i = 1
        ..numelems(res[1]))], connect = true):
 > plots[display](plot1, plot2, color = [red, blue], legend = [Решение,
        Методом разностных аппроксимаций])
              107
                               1.5
                                           2
                                                    2.5
                                                                3
                                                                          3.5
                                                 х
                         Решение -
                                        - Методом разностных аппроксимаций
    chebyshev norm(res[1], res[2], sol)
```

```
7.500465420
                                                                                                                                  (7)
#4
h := 0.000001:
 > ode := diff(y(x), x$2) + q(x) \cdot y(x) = f(x)
                                 ode := \frac{d^2}{dx^2} y(x) - 8 y(x) = 20 x (1.5 - 0.5 x^2)
                                                                                                                                  (8)
sol := dsolve(\{y(l) = L, y(r) = R, ode\})

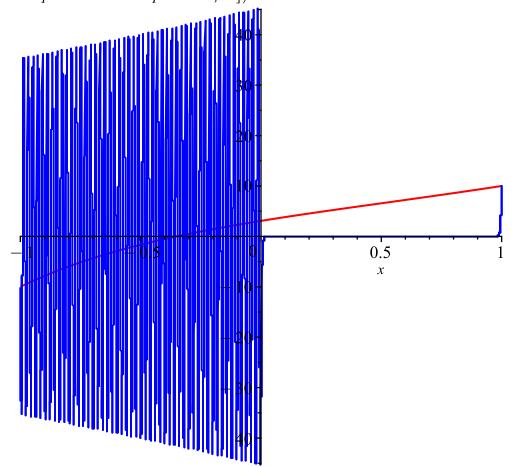
sol := y(x) = \frac{e^{2\sqrt{2}x} (38 - 357 e^{2\sqrt{2}}) e^{-4\sqrt{2}}}{16 e^{4\sqrt{2}} - 16} - \frac{e^{-2\sqrt{2}x} e^{6\sqrt{2}} (38 e^{2\sqrt{2}} - 357)}{16 e^{4\sqrt{2}} - 16} + \frac{5x^3}{4}
                                                                                                                                  (9)

ightharpoonup res := difference method(p, q, f, h, l, r, L, R):
  \rightarrow plot2 := plots:-pointplot(\lceil seq(\lceil convert(res\lceil 1 \rceil \lceil i \rceil, float), convert(res\lceil 2 \rceil \lceil i \rceil, float) \rceil, i = 1
           ..numelems(res[1])), connect = true):
  > plots[display](plot1, plot2, color = [red, blue], legend = [Решение,
            Методом разностных аппроксимаций])
```

```
3-
                2-
                                                                                            3
                               2.2
                                              2.4
                                                             2.6
                                                                            2.8
                            Решение
                                              • Методом разностных аппроксимаций
  > chebyshev_norm(res[1], res[2], sol)
                                                                                                       (10)
                                              7.178039157
ode := \frac{\mathrm{d}^2}{\mathrm{d}x^2} y(x) + \frac{\mathrm{d}}{\mathrm{d}x} y(x) - y(x) = 0
                                                                                                       (11)
 sol := dsolve(\{y(l) = L, y(r) = R, ode\}):
    plot1 := plot(rhs(sol), x = l..r) :

res := difference\_method(p, q, f, h, l, r, L, R) :
```

- plots[display](plot1, plot2, color = [red, blue], legend = [Решение,
 Методом разностных аппроксимаций])



—— Решение —— Методом разностных аппроксимаций

> chebyshev_norm(res[1], res[2], sol)

 $oldsymbol{o}$ ode := $diff(y(x), x$2) + 123456 \cdot x \cdot y(x) = 9999999$

$$ode := \frac{d^2}{dx^2} y(x) + 123456 x y(x) = 9999999$$
 (13)

 $f := dsolve(\{y(-1) = -1, y(1) = 1, ode\})$

$$f := y(x) = \left(333333 \pi 1929^{2/3} \text{ AiryBi}(-4 1929^{1/3}) \text{ (AiryBi}(4 1929^{1/3}) \text{ AiryAi}(\right)$$

$$-4 1929^{1/3} x) - \text{AiryAi}(4 1929^{1/3}) \text{ AiryBi}(-4 1929^{1/3} x)) \left(\int_{-1}^{1} \text{AiryAi}(\right)$$

$$-4 1929^{1/3} z1) dz1 - 333333 \text{ AiryBi}(-4 1929^{1/3} x) \pi 1929^{2/3} \text{ (AiryAi}(\right)$$

$$-4 1929^{1/3}) \text{ AiryBi}(4 1929^{1/3}) - \text{AiryBi}(-4 1929^{1/3}) \text{ AiryAi}(4 1929^{1/3})) \left(\right)$$

 $\int_{-1}^{x} \operatorname{AiryAi}(-4 \, 1929^{1/3} \, _zI) \, d_zI) - 333333 \, \pi \, 1929^{2/3} \, \operatorname{AiryAi}($ $-4 \, 1929^{1/3}) \, \left(\operatorname{AiryBi}(4 \, 1929^{1/3}) \, \operatorname{AiryAi}(-4 \, 1929^{1/3} \, x) - \operatorname{AiryAi}(4 \, 1929^{1/3}) \, \operatorname{AiryBi}($ $-4 \, 1929^{1/3} \, x) \right) \, \left(\int_{-1}^{1} \operatorname{AiryBi}(-4 \, 1929^{1/3} \, _zI) \, d_zI \right) + 333333 \, \operatorname{AiryAi}($ $-4 \, 1929^{1/3} \, x) \, \pi \, 1929^{2/3} \, \left(\operatorname{AiryAi}(-4 \, 1929^{1/3}) \, \operatorname{AiryBi}(4 \, 1929^{1/3}) - \operatorname{AiryBi}($ $-4 \, 1929^{1/3}) \, \operatorname{AiryAi}(4 \, 1929^{1/3}) \right) \, \left(\int_{-1}^{x} \operatorname{AiryBi}(-4 \, 1929^{1/3} \, _zI) \, d_zI \right) + \left(2572 \, \operatorname{AiryBi}($ $-4 \, 1929^{1/3}) \, + 2572 \, \operatorname{AiryBi}(4 \, 1929^{1/3}) \right) \, \operatorname{AiryAi}(-4 \, 1929^{1/3} \, x) - 2572 \, \operatorname{AiryBi}($ $-4 \, 1929^{1/3} \, x) \, \left(\operatorname{AiryAi}(4 \, 1929^{1/3}) + \operatorname{AiryAi}(-4 \, 1929^{1/3}) \right) \right) \, \left(2572 \, \operatorname{AiryAi}($ $-4 \, 1929^{1/3}) \, \operatorname{AiryBi}(4 \, 1929^{1/3}) - 2572 \, \operatorname{AiryBi}(-4 \, 1929^{1/3}) \, \operatorname{AiryAi}(4 \, 1929^{1/3}) \right)$