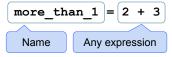
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- Group by some *treatment* and measure some *outcome*
- Simplest setting: a treatment group and a control group
- If the outcome differs between these two groups, that's evidence of an association (or relation)
 - E.g., the top-tier chocolate eaters died of heart disease at a lower rate (12%) than chocolate abstainers (17%)
- If the two groups are similar in all ways but the treatment itself, a difference in the outcome is evidence of causality
- When a group is divided randomly, it's unlikely that there are systematic differences between sub-groups

Operation	Operator	Example	Value
Addition	+	2 + 3	5
Subtraction	-	2 - 3	-1
Multiplication	*	2 * 3	6
Division	1	7/3	2.66667
Remainder	%	7 % 3	1
Exponentiation	**	2 ** 0.5	1.41421



- Statements don't have a value; they perform an action
- An assignment statement changes the meaning of the name to the left of the = symbol
- The name is bound to a value (not an equation)

Growth rate: The rate of increase per unit time

After one time unit, a quantity x growing at rate g will be

$$x * (1 + g)$$

After t time units, a quantity x growing at rate g will be

$$x * (1 + g) ** t$$

• If after and before are measurements of the same quantity taken t time units apart, then the growth rate is

$$(after/before) ** (1/t) - 1$$

A range is an array of consecutive numbers

- np.arange(end):
 - An array of increasing integers from 0 up to end
- np.arange(start, end):
 - An array of increasing integers from start up to end
- np.arange(start, end, step):

A range with step between consecutive values

The range always includes start but excludes end

The **group** method aggregates all rows with the same value for a column into a single row in the result

- First argument: Which column to group by
- Second argument: How to combine values
 - len number of grouped values (default)
 - o sum total of all grouped values
 - list list of all grouped values

The pivot method aggregates by a combination of columns and organizes the result into a grid

- First argument: Which column gives the pivot columns
- Second argument: Which column gives the pivot rows
- Third argument: (Optional) Column of pivot values
- Fourth argument: (Optional) How to combine values

max, min	Maximum or minimum of a sequence
str, float, int	Convert a value to a string, number, or integer
np.prod	Multiply all elements together
sum, np.sum	Add all elements together
all, np.all	Test whether all elements are true values (non-zero numbers are true)
any, np.any	Test whether any elements are true values (non-zero numbers are true)
np.count_nonzero	Count the number of non-zero elements. False is considered zero and True non-zero.
np.diff	Difference between adjacent elements
round, np.round	Round each number to the nearest integer (whole number)
np.cumprod	A cumulative product: for each element, multiply all elements so far
np.cumsum	A cumulative sum: for each element, add all elements so far
np.exp	Exponentiate each element
np.log	Take the natural logarithm of each element
np.abs	Take the absolute value of each element
np.sqrt	Take the square root of each element
np.sort	Sort the elements

- < and > mean what you expect (less than, greater than)
- <= means "less than or equal"; likewise for >=
- == means "equal"; != means "not equal"
- Both numbers and strings can be compared, but a string cannot be compared to a number
- Comparing strings compares their alphabetical order

A table can be created using...

- Table.read table(url) reads an existing table
- Table (labels) is a table with empty columns
- Table () is an empty table with no columns

A table t can be extended using...

- t.with column(label, values)
- t.with columns (labels and values)
- t.with row(row) and t.with rows(rows)
- t.select(columns) keeps only certain columns
- t.drop(columns) keeps all but certain columns
- t.relabeled(a, b) substitutes label a with b
- Each column has a label and an index (starting at 0)
 - The resulting array has one item per row
- t.where (column, value) keeps all rows containing a certain value in a column
- t.where (condition) keeps all rows for which the condition is true, where condition is a boolean array
- t.take(row numbers) keeps the numbered rows
- t.sort(column) sorts the rows in increasing order
- Each row has an index (starting at 0)
 - The resulting row value has one item per column
 - Row items can be selected by column index or label

Tables can generate charts using these methods:

- barh draw a horizontal bar chart
- hist draw a histogram (later)
- scatter draw a scatter diagram (later)

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Types of values: All values in a column should have the same type **and** be comparable to each other in some way

- Categorical Each value is from a fixed inventory
 - May or may not have an ordering
 - Categories are the same or different
 - Allows grouping by value (group, pivot, join)
- Numerical Each value is from a fixed scale
 - Numerical measurements are ordered
 - Allows binning by value (bin, hist)

Binning is counting the number of numerical values that lie within ranges, called bins.

- Bins are defined by their lower bounds (inclusive)
- The upper bound is the lower bound of the next bin 188, 170, 189, 163, 183, 171, 185, 168, 173, ...

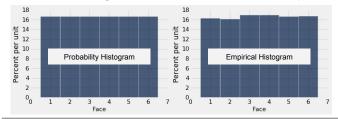


A histogram has two defining properties:

- The bins are contiguous (though some might be empty) and are drawn to scale
- The area of each bar is proportional to the number of entries in the bin

A histogram drawn *on the density scale* has total area 1 Vertical axis units: Proportion / Unit on the horizontal axis Height of a bar: (proportion of entries in bin) / (width of bin)

- A histogram of proportions of all possible outcomes of a known random process is called a probability histogram
- A histogram is a summary visualization of a distribution
- A histogram of proportions of actual outcomes generated by sampling is called an *empirical histogram*
- When a histogram is created from data, it is empirical

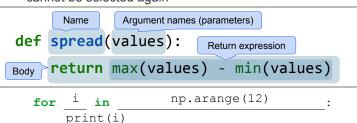


Sampling from a population means selecting a subset

Probability sample: Use a random procedure for which you *know in advance* the chance that each subset of the population will enter the sample (called the *distribution*) *Uniform random sample* example: choose each movie at random with equal chance

Each item has equal chance of being drawn

- With replacement: Items can be drawn more than once, and no draw affects the chance of any other draw
- Without replacement: Once an item is selected, it cannot be selected again



The body is executed **for** every item in a sequence The body of the statement can have multiple lines The body should do something: print, assign, hist, etc. Law of averages: If a chance experiment is repeated independently under identical conditions, in the long run:

The proportion of times that an event occurs gets closer and closer to the theoretical probability of the event

Biased estimate: On average across all possible samples, the estimate is either too high or too low.

- Bias creates a systematic error in one direction.
- Good estimates typically have low bias.
- The value of an estimate varies across samples.
- High variability makes it hard to estimate accurately.
- Good estimates typically have low variability.

Mean (or average): Balance point of the histogram

- **Not** the "half-way point" of the data; the mean is not the median unless the histogram is symmetric
- If the histogram is skewed, then the mean is pulled away from the median in the direction of the tail

Standard deviation (SD)=rootmeansquare ofdeviations fromaverage54321

Measures roughly how far off the values are from average

"average ± z SDs"

- z measures "how many SDs above average"
- If z is negative, the value is below average
- z is called standard units
- Almost all standard units are in the range (-5, 5)
- Convert a value to standard units: z = (value average) / SD

Percent in Range	All Distributions	Normal Distribution	
average ± 1 SD	at least 0%	about 68%	
average ± 2 SDs	at least 75%	about 95%	
average ± 3 SDs	at least 88.888%	about 99.73%	

Correlation Coefficient (r) =

average	product	x in	and	y in
of	of	standard units		standard units

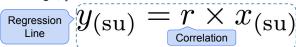
Measures how clustered the scatter is around a straight line

- -1 ≤ *r* ≤ 1
- r = ± 1 if the scatter is a perfect straight line
- r is a pure number, with no units
- r is not affected by changing units of measurement
- r is not affected by switching the horizontal and vertical axes

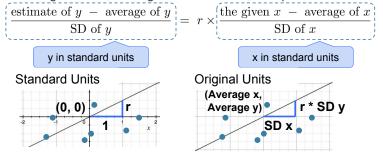
Regression to the mean: a statement about x and y pairs

- Measured in standard units
- Describing the deviation of x from 0 (the average of x's)
- And the deviation of y from 0 (the average of y's)

On average, y deviates from 0 less than x deviates from 0



In original units, the regression line has this equation:



```
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census = Table.read_table(census_url)
                  # Returns a tuple of labels
Census.labels
Census.num_columns # Returns an integer number of columns
Census.num_rows # Returns an integer number of rows
census.row(5)
                   # Returns a row, which has items
                  # Returns a column, which is an array
census.column(2)
census.row(0).item(2) == census.column(2).item(0)
# Filtering on one or more conditions
census.where('AGE', 40)
census.where(census.column(2) < 40)</pre>
census.where(np.logical_or(census.column('AGE') == 18,
                           census.column('AGE') == 19))
census.where(np.logical_and(census.column('AGE') >= 18,
                            census.column('AGE') <= 19))</pre>
def age_group(age):
   if age < 2:
        return 'Baby'
   elif age < 13:
        return 'Child'
    elif age < 20:
        return 'Teen'
    else:
        return 'Adult'
population = census.with_columns([
    'Age Group', census.apply(age_group, 'AGE'),
    'Male/Female', census.column('SEX'),
    'Population', census.column('2014')])
population.group('Age Group')
# Creates a table with labels: Age Group | count
sums = population.select([0, 2]).group('Age Group', sum)
# Creates a table with labels: Age Group | Population sum
population.pivot('Age Group', 'Male/Female')
# Counts Labeled: Male/Female | Adult | Baby | Child | Teen
population.join('Age Group', sums)
# Adds a column for the Population sum of each age group
top = Table.read_table('top_movies.csv')
top.take([3, 18, 100])
top.take(np.arange(0, top.num_rows, 40))
np.random.randint(3, 8) # select randomly from 3, 4, 5, 6, 7
start = np.random.randint(0, 10)
top.take(np.arange(start, top.num_rows, 10))
die = Table().with_column('Face', [1, 2, 3, 4, 5, 6])
dice_bins = np.arange(0.5, 7, 1)
die.hist(bins=dice_bins)
die.sample(10, with_replacement=True)
for i in np.arange(5):
    print(i)
# Generating a table of dice rolls
def roll_once(n):
    return np.random.randint(1, n+1)
rolls = Table(['First roll', 'Second roll'])
for i in np.arange(1000):
    row = [roll_once(6), roll_once(6)]
    rolls.append(row)
rolls.hist(bins=dice_bins)
```

```
np.average, np.mean Average of values
                       Standard deviation of values
np.std
                       Variance of values (standard deviaion squared)
np.var
Table.append
                       Append a row or all rows of a table.
Table.append column
                       Appends a column to the table.
Table.apply
                       Returns an array where a function is applied to
                       each item in a column.
                       Group values by bin and compute counts per
Table.bin
                       bin by column.
Table.column
                       Return the values of a column as an array.
Table.drop
                       Return a table with only columns other than
                       selected label or labels.
                       Group rows by unique values in a column;
Table.group
                       count or aggregate other values.
                       Generate a table with the columns of self and
Table.join
                       other, containing rows for all values of a
                       column that appear in both tables.
Table.pivot
                       Group rows by unique values in two columns:
                       count or aggregate values from a third column.
Table.relabel
                       Change the label of a column
Table.relabeled
                       Return a new table with a label changed.
Table.sample
                       Returns a new table where k rows are
                       randomly sampled from the original table.
                       Return a table with only the selected columns.
Table.select
Table.sort
                       Return a table of rows sorted according to the
                       values in a column.
Table.take
                       Return a table of the rows taken by index.
Table.where
                       Return a table of the rows for which the column
                       matches a value or is a non-zero value.
                       Return a table with an additional or replaced
Table.with column
                       column or columns.
Table.with_columns
                       Return a table with an additional row or rows.
Table.with row
Table.with_rows
annual_growth_rate = 0.035
ten_year_growth_rate = (1 + annual_growth_rate) ** 10 - 1
ten_year_growth_rate # evaluates to: 0.410598760621121
baseline_high = 14.48
highs = np.array([baseline_high - 0.880, baseline_high - 0.093,
                  baseline high + 0.105, baseline high + 0.684])
highs # evaluates to: array([ 13.6 , 14.387, 14.585, 15.164])
(9/5) * highs + 32 # array([ 56.48 , 57.89, 58.253 , 59.295])
def percent(x):
    if x < 1e-8:
        return 0.0
    elif x < 0.00005:
        return 100 * x
        return round(100 * x, 2)
percent(1/6) # returns 16.67
percent(1/6000) # returns 0.02
percent(1/60000) # returns 0.00166666666666668
percent(1/6000000000) # returns 0.0
Table(['Odd', 'Even']).with_row([3, 4])
Table(['Odd', 'Even']).with_rows([[3, 4], [5, 6], [7, 8]])
Table().with_column('Odd', [3, 5, 7])
Table().with_columns(['Odd', [3, 5, 7], 'Even', [4, 6, 8]])
```

```
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def standard_units(any_numbers):
    return (any_numbers - np.mean(any_numbers))/np.std(any_numbers)
def correlation(t, x, y):
    return np.mean(standard units(t.column(x))*standard units(t.column(y)))
def slope(table, x, y):
    r = correlation(table, x, y)
    return r * np.std(table.column(y))/np.std(table.column(x))
def intercept(table, x, y):
    a = slope(table, x, y)
    return np.mean(table.column(y)) - a * np.mean(table.column(x))
def fit(table, x, y):
    a = slope(table, x, y)
    b = intercept(table, x, y)
    return a * table.column(x) + b
# Regression effect
heights = Table.read_table('heights.csv')
six_foot_fathers = heights.where(np.round(heights.column('father')) == 72)
six_foot_fathers.hist('son', bins=np.arange(55.5, 80, 1))
np.count_nonzero(six_foot_fathers.column('son') < 72) / six_foot_fathers.num_rows</pre>
np.mean(six_foot_fathers.column('son'))
# Graph of averages
fathers = heights.column('father')
sons = heights.column('son')
heights_su = Table().with_columns([
        'father (su)', standard_units(fathers),
        'son (su)', standard_units(sons)])
rounded = heights_su.with_column('father (su)', np.round(father_su))
rounded.join('father (su)', rounded.group(0, np.average)).scatter(0, s=80)
# Regression model
def signal_and_noise(x, r):
   return r * x + np.random.normal() * (1-r**2)**0.5
def regression model(r, sample size):
   pairs = Table(['x', 'y'])
   for i in np.arange(sample_size):
       x = np.random.normal()
       y = signal and noise(x, r)
       pairs.append([x, y])
   return pairs
regression_model(1/2, 1000).scatter('x', 'y')
def compare(true_r, sample_size):
   pairs = regression_model(true_r, sample_size)
   estimated_r = correlation(pairs, 'x', 'y')
   pairs.scatter('x', 'y', fit_line=True, s=10)
   plt.plot([-3, 3], [-3 * true_r, 3 * true_r], color='g', lw=4)
   print("The true r is ", true_r, " and the estimated r is ", estimated_r)
compare(0.5, 1000) # Compare true line to regression line
```