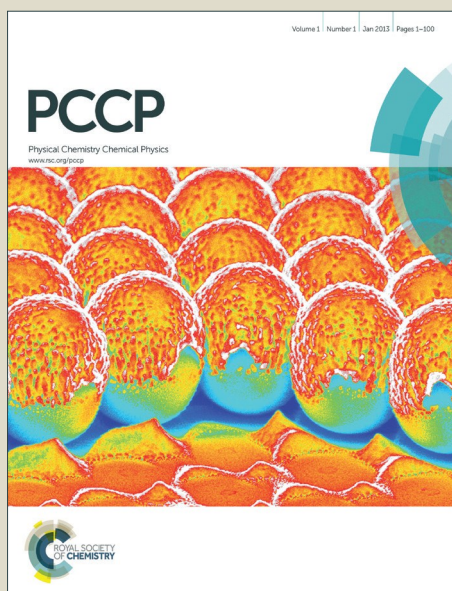


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# Structure and $\text{Li}^+$ ion transport in a mixed carbonate/ $\text{LiPF}_6$ electrolyte near graphite electrode surfaces: a molecular dynamics study

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Electrolyte and electrode materials used in lithium-ion batteries have been studied separately to a great extent, however the structural and dynamical properties of the electrolyte-electrode interface still remain largely unexplored despite its critical role in governing battery performance. Using molecular dynamics simulations, we examine the structural reorganization of solvent molecules (cyclic ethylene carbonate: linear dimethyl carbonate 1:1 molar ratio doped with 1M  $\text{LiPF}_6$ ) in the vicinity of graphite electrodes with varying surface charge densities ( $\sigma$ ). The interfacial structure is found to be sensitive to the molecular geometry and polarity of each solvent molecule as well as the surface structure and charge distribution of the negative electrode. We also evaluated the potential difference across the the electrolyte-electrode interface, which exhibits a nearly linear variation with respect to  $\sigma$  up until the onset of  $\text{Li}^+$  ion accumulation onto the graphite edges from the electrolyte. In addition, well-tempered metadynamics simulations are employed to predict the free-energy barriers to  $\text{Li}^+$  ion transport through the relatively dense interfacial layer, along with analysis of the  $\text{Li}^+$  solvation sheath structure. Quantitative analysis of the molecular arrangements at the electrolyte-electrode interface will help better understand and describe electrolyte decomposition, especially in the early stages of solid-electrolyte-interphase (SEI) formation. Moreover, the computational framework presented in this work offers a means to explore the effects of solvent composition, electrode surface modification, and operating temperature on the interfacial structure and properties, which may further assist in efforts to engineer the electrolyte-electrode interface leading to a SEI layer that optimizes battery performance.

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## I. Introduction

With the global movement towards a CO<sub>2</sub>-free economy and the rapid growth in intermittent renewable energy, energy storage is more important now, than ever. Since their inception, lithium-ion batteries (LIB) have aided the technological revolution of portable electronic devices. A similar long sought-after revolution is anticipated in the automotive industry. Unfortunately, the current LIBs severely limit battery-powered electric vehicles to short-range commuting because of their low energy densities and charge rates. Despite a broad spectrum of work to develop new storage concepts and transition to more sustainable materials, LIBs remain the state-of-the-art in the area of electrochemical energy storage. Gaps between theoretical and actual performance in current LIBs highlight the need for further understanding to improve existing technologies as well as to develop new energy storage concepts.<sup>1–6</sup>

Modern LIBs are typically comprised of transition metal oxide cathodes, graphitic carbon anodes, and electrolytes containing inorganic lithium salts dissolved in small molecule organic solvents. However, typical organic solvents (carbonates, ethers, etc.) and salt anions (PF<sub>6</sub><sup>−</sup>, BF<sub>4</sub><sup>−</sup>, ClO<sub>4</sub><sup>−</sup>, etc.) are not electrochemically stable at the graphite electrode surface and may undergo decomposition to form a passivating layer, typically labeled as the solid-electrolyte interphase (SEI).<sup>7–10</sup> The electrode and electrolyte materials have been studied separately to great extents, but it is at the interfaces where the key electrochemical processes occur which govern battery performance.<sup>2,8,10–28</sup> Therefore, a fundamental (molecular level) understanding of thermodynamics, transport phenomena, and electrochemical reactions at the electrolyte-electrode interface is crucial for the further advancement of battery technologies.

Due to the transient nature of electrochemical processes in LIBs, real-time *in situ*<sup>29</sup> characterization is preferable, especially since an *ex situ postmortem* study may fail to capture

real-time dynamics.<sup>5</sup> Moreover, owing to the size and time scales of the electrolyte-electrode interfacial phenomena, there are only a few experimental techniques able to provide the appropriate resolution. Alternatively, computational studies may allow the system to be observed at (across) spatial (temporal) scales often unavailable in experiments.<sup>30–38</sup>

Molecular modeling techniques have been extensively used to understand the fundamentals of electrochemical and transport processes in LIB systems. First principles methods, usually based on the density functional theory (DFT), are able to provide unprecedented fundamental details on the interfacial structure and dynamics, such as lithium diffusion and intercalation, solvent reorganization and decomposition, and so forth. Although the first-principles approach can effectively describe complex electrochemical processes,<sup>30–35</sup> the high computational cost restricts its application to systems of no more than several hundred atoms with trajectories of tens of picoseconds. Classical force field calculations, on the other hand, lack the chemical nature, but well reproduce many structural and dynamical properties of materials while simulating tens of thousands of atoms over hundreds of nanoseconds. Force field-based molecular dynamics (MD) studies have already been used to explore the nature of bulk electrolytes<sup>36</sup> as well as lithium ion behavior at various interfaces.<sup>37,38</sup> Vatamanu *et al.*<sup>37</sup> examined the effect of electrode potential on the structure of a mixed carbonate/LiPF<sub>6</sub> electrolyte near the basal surface of graphite. While graphite edge-planes have been shown to have several orders of magnitude higher electron transfer rates<sup>39</sup> and are thus expected to dominate the salient reaction chemistries found in LIBs, Jorn *et al.*<sup>38</sup> considered both basal and flat edge-planes but only for a single carbonate electrolyte, and Jow *et al.*<sup>40</sup> reported free energy profiles calculated as a function of Li<sup>+</sup> position in a mixed carbonate/LiPF<sub>6</sub> electrolyte near a uncharged graphite edge-plane.

In this work, we employ classical MD simulations to investigate the structural reorganization of EC:DMC(1:1)/LiPF<sub>6</sub> 1M due to the interaction with edge-plane graphite surfaces, along with the resulting potential difference across the electrolyte-electrode interface as well as Li<sup>+</sup> ion transport through the interfacial layer. We first predict the near-interface EC/DMC/Li<sup>+</sup>/PF<sub>6</sub><sup>-</sup> distributions with varying charge densities on the hydrogen-terminated graphite edges. From the resulting structures, we also estimate the variation of the potential difference across the electrolyte-electrode interface as well as the relation between applied voltage and electrode surface charge density. Then, we evaluate the transport rate of Li<sup>+</sup> by calculating the free-energy penalties associated with its moving to the interface from the bulk region using advanced sampling techniques (metadynamics) to understand how the interfacial structure affects Li<sup>+</sup> ion dynamics. This theoretical study aims at gaining a deeper understanding of the nature of molecular interactions at the interfaces between carbonate-based mixed solvent electrolytes and graphite electrodes, especially the reorganization of solvent molecules due to electrode charging.

Nowadays it is common practice to utilize binary and even ternary mixtures of carbonate solvents to balance lithium salt solubility and viscosity; this provides an additional degree of freedom which has been largely neglected in the study of SEI formation and Li<sup>+</sup> ion transport. Our study clearly demonstrates that the composition and structural ordering of the mixed electrolyte in proximity to the interface are substantially different from those in the bulk. Quantitative prediction of the interfacial structure is essential to better understanding electrolyte decomposition/diffusion processes along with Li<sup>+</sup> ion dynamics near the electrode, especially at the onset of SEI formation that may significantly influence its growth which is known to be kinetically governed. The improved understanding may further assist in efforts to engineer the

electrolyte-electrode interface leading to an SEI which optimizes LIB performance.

## II. Computational methods

### A. Classical molecular dynamics

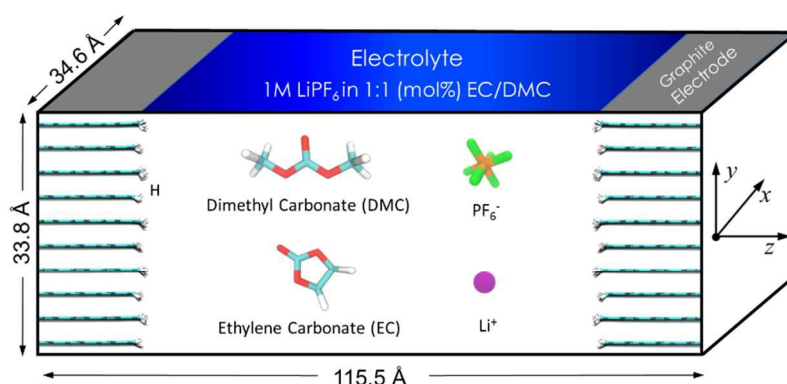


Figure 6. Schematic of the simulation cell. The electrolyte solution contains 1M  $\text{LiPF}_6$  in EC:DMC (= 1:1 molar ratio) and the negative electrode is modelled as a stack of ten graphene nanoribbons with hydrogen-terminated zigzag edges. For EC, DMC, and  $\text{PF}_6^-$ , white, red, blue, orange, and green colors represent H, O, C, P, and F, respectively. Periodic boundary conditions are applied in the  $x$ ,  $y$  and  $z$  directions.

We performed MD simulations with the OPLS-AA force field<sup>41–43</sup> using the GROMACS simulation package (version 4.6.7)<sup>44</sup>. As illustrated in Figure 6, simulations with periodic boundary conditions were conducted using a system representing the half-cell of the anode side in a LIB; the rectangular simulation cell is comprised of a liquid electrolyte (1M  $\text{LiPF}_6$  in EC:DMC (= 1:1 molar ratio)) and a negative electrode (which is modelled as a stack of ten graphene nanoribbons with hydrogen-terminated zigzag edges). The nanoribbon sheets are staggered in an ABAB pattern due to the van der Waals interaction between them, yielding a regular corrugated face. The graphite electrode has 3920 carbon atoms in  $35 \text{ Å} \times 34 \text{ Å} \times 32 \text{ Å}$ ; several C atoms in each sheet were restrained with a harmonic potential to prevent significant slip. The electrolyte side consists of 375 DMC and 375 EC molecules in addition to 57  $\text{PF}_6^-$

anions; the number of  $\text{Li}^+$  cations is varied depending on the amount of excess charge added to the negative electrode; the excess negative charge was assumed to be uniformly distributed throughout the edge C atoms.

A MD timestep of 1 fs was used in all simulations. The short-range interactions were computed with a spherical cutoff of 1.2 nm, while the long-range electrostatics were accounted for using the particle mesh Ewald (PME) summation method. The systems were initially equilibrated in the NPT ensemble<sup>45,46</sup> and then subsequently annealed in the NVT ensemble<sup>47</sup> at 700 K for 1 ns. After the quench for 0.5 ns, the production runs using various algorithms were carried out at 300 K and comprised a total of more than several hundreds of nanoseconds.

## B. Metadynamics

We used well-tempered metadynamics<sup>48,49</sup> to reconstruct the free energy profile associated with  $\text{Li}^+$  ion transport through the interfacial layer. The enhanced sampling is performed by biasing a low-dimensional collective variable (CV) which, in our case, is the position  $z$  from the electrolyte-electrode interface. The metadynamics was performed using the GROMACS simulation package<sup>44</sup> and the PLUMED plugin<sup>50</sup>. The bias is represented by a history-dependent potential constructed as a sum of Gaussian distributions centered along the trajectory in the CV space:

$$V(\vec{s}, t) = \sum_{t'=0, \tau, 2\tau, \dots}^{t' \leq t} W e^{\frac{-V(s(q(t'), t'))}{\Delta T}} \exp\left(-\sum_{i=1}^d \frac{(s_i(q) - s_i(q(t')))^2}{2\sigma_i^2}\right) \quad (1)$$

The bias potential pushes the system out of local minima and forces it to explore new regions of the phase space. Furthermore, in the long time limit, the bias potential converges to free energy  $-A(\mathbf{s})$  as a function of the CVs:

$$V(\mathbf{s}, t \rightarrow \infty) = -A(\mathbf{s}) + C \quad (2)$$

The metadynamics algorithm is essentially controlled by only four parameters: Gaussian deposition stride  $\tau$ , width  $\sigma_i$ , height  $W(k\tau)$  of the Gaussian, and  $\Delta T$  which controls the rate of Gaussian height decay over the simulation by the well-tempered algorithm.<sup>49</sup>

### III. Results and discussion

#### A. Electrolyte distribution near uncharged electrodes

Figure 1(a) shows the number density ( $\rho_n$ ) profiles with a bin size of 0.15 Å for electrolyte components (based on each molecule's center of mass) along the direction normal to the electrode surface. DMC and EC are found to pack more densely at the interface by approximately 3 and 2 times higher than their bulk values, respectively, which is apparently attributed to the van der Waals (vdW) force at the electrolyte-electrode interface. The preference towards DMC arises from the relatively stronger vdW interactions due to the bulky methyl groups in DMC. The oscillations in  $\rho_n$  appear to dampen after about 2 nm to the bulk-like densities.

The first  $\text{Li}^+$  peak occurs near 0.7 nm where the  $\rho_n$  of both EC and DMC shows a minimum value, while the intensity is noticeably lower than the bulk-like density. This implies that it is relatively difficult for the densely packed carbonate complexes near the electrode to rearrange and solvate  $\text{Li}^+$  ions; note that the first solvation shell of  $\text{Li}^+$  in the bulk phase contains four carbonate molecules and a  $\text{PF}_6^-$  anion, as illustrated in the inset of Figure 1(a). The small but distinct second maximum of the first peak at  $z = 0.55$  nm for both EC and DMC is due to the ordering of these molecules around the  $\text{Li}^+$  concentrated near 0.7 nm. The second peak at  $z = 0.82$  nm is a result of the interplay between the vdW interactions with the first-layer carbonates and the solvation of  $\text{Li}^+$ . Due to their electrostatic attraction,  $\text{PF}_6^-$  organize around the  $\text{Li}^+$



leading to the alternative anion/cation layering, as also commonly seen in ionic liquids<sup>51</sup>, despite the vastly different electrolyte.

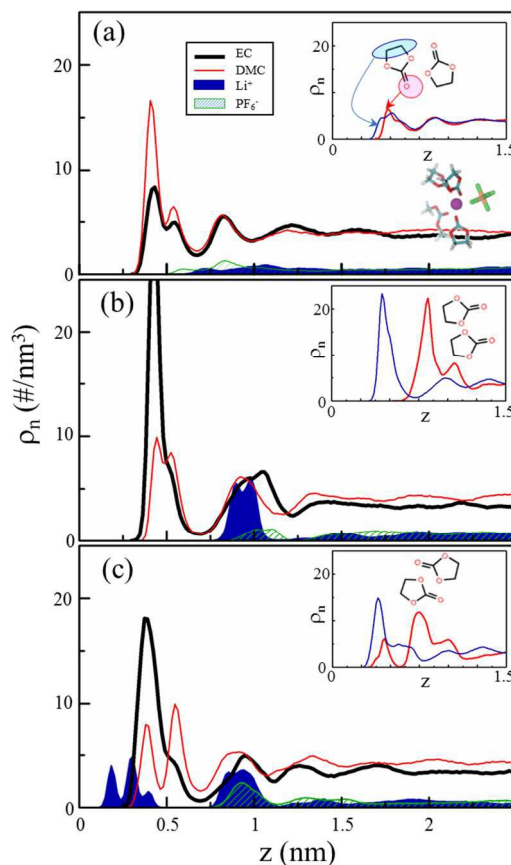


Figure 1. EC, DMC,  $\text{Li}^+$  and  $\text{PF}_6^-$  number density ( $\rho_n$ ) profiles along the  $z$ -direction near graphite electrodes with surface charge densities of (a)  $\sigma = 0 \mu\text{C}/\text{cm}^2$ , (b)  $\sigma = -11.6 \mu\text{C}/\text{cm}^2$ , and (c)  $\sigma = -16.4 \mu\text{C}/\text{cm}^2$ . In each inset, the  $\rho_n$  profiles for the carbonyl oxygen (red line) and ethylene group (blue line) of EC are also presented to demonstrate changes in the molecular orientation, as illustrated by the 2D EC representations. As shown in (a), the first solvation shell of  $\text{Li}^+$  in the bulk-like region commonly consists of four carbonate molecules and one  $\text{PF}_6^-$  anion.

## B. Electrolyte distribution near charged electrodes

To imitate the charge injection in the graphite anode by an applied external voltage, we assigned excess negative charge equally to the electrolyte-adjacent carbon atoms in the electrode; the charge density ( $\sigma$ ) was varied between 0 and  $-16.4 \mu\text{C}/\text{cm}^2$ . Such representation should be

adequate for mimicking the preferential accumulation of excess charges at the metallic graphite edges, as well demonstrated by previous DFT studies<sup>52</sup>. In order to maintain charge neutrality in the model systems considered, additional  $\text{Li}^+$  ions were added to the bulk electrolyte to compensate for the excess negative charge in the electrode.

A charged electrode creates an electric field, which causes the rearrangement of electrolyte components near the electrode to screen the electric field. Figure 1 shows the arrangement of the electrolyte components at  $\sigma = 0 \text{ } \mu\text{C}/\text{cm}^2$  [(a)],  $-11.6 \text{ } \mu\text{C}/\text{cm}^2$  [(b)], and  $-16.4 \text{ } \mu\text{C}/\text{cm}^2$  [(c)]; additional  $\rho_n$  profiles at  $\sigma = -4.1 \text{ } \mu\text{C}/\text{cm}^2$  and  $-8.2 \text{ } \mu\text{C}/\text{cm}^2$  are also presented in the Supporting Information (see Figure S3). At  $\sigma = -11.6 \text{ } \mu\text{C}/\text{cm}^2$  [(b)], the first peaks of both EC and DMC shift towards the electrode, indicating a higher degree of alignment. The first-peak intensity of EC (DMC) at  $z = 0.43 \text{ nm}$  increases (decreases) by four (two) times, in comparison to the charge neutral case. As illustrated in the inset of Figure 1(b), the positively charged ethylene group of EC is aligned towards the negatively charged electrode and its carbonyl group towards the bulk. The relatively smaller vdW volume of EC allows it to pack more densely than DMC in the vicinity of the electrode, thereby more effectively screening the electric field from the charged anode; note also that DMC has its positive charge spread over two terminal methyl groups. The alignment of the carbonyls in EC away from the electrode results in an accumulation of  $\text{Li}^+$  at  $z = 0.9 - 1 \text{ nm}$  of about 10 times the bulk, which in turn attracts  $\text{PF}_6^-$  anions leading to the alternative  $\text{Li}^+/\text{PF}_6^-$  layering.

When  $\sigma = -16.4 \text{ } \mu\text{C}/\text{cm}^2$  [(c)],  $\text{Li}^+$  begin to accumulate at the graphite edges as the EC/DMC solvent molecules are unable to pack densely enough to shield the charged electrode. The  $\rho_n$  profile of  $\text{Li}^+$  exhibits two distinct peaks at  $z = 0.19\text{-}0.4 \text{ nm}$  and  $0.85\text{-}0.95 \text{ nm}$ . The first peak shows three maxima largely due to the corrugation and hydrogen terminations at the graphite

edges (rendering multiple stable sites for  $\text{Li}^+$  depending on its coordination). In this case,  $\text{Li}^+$  cations at the interface tend to be partially solvated by EC (and DMC) carbonyl O ( $z = 0.45$  nm), while the majority of EC molecules still remain perpendicular to the electrode edge with their carbonyl group around  $z = 0.75$  nm. The orientation of EC molecules has been shown to be related to the favorability of their decomposition.<sup>53</sup> As  $\text{Li}^+$  accumulates on the electrode, the  $\rho_n$  of EC (DMC) decreases (increases) in the first layer.

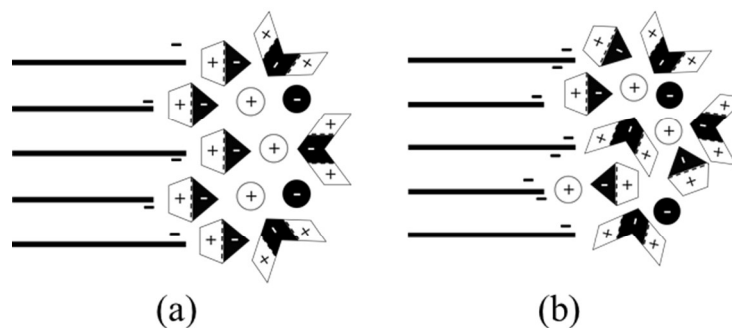


Figure 2. Schematic illustrations of the reorganization of solvent molecules near graphite anodes with (a) moderately and (b) highly charged surfaces. Cyclic ethylene carbonate (EC) and acyclic dimethyl carbonate (DMC) are depicted by a pentagon and a chevron, respectively, while their polarization is indicated by the minus and plus signs. Filled and open circles respectively represent  $\text{PF}_6^-$  anions and  $\text{Li}^+$  cations.

A schematic shown in Figure 2 illustrates the effect of  $\text{Li}^+$  accumulation on the electrolyte packing near the interface. In the case of  $\sigma = -11.6 \mu\text{C}/\text{cm}^2$  [(a)], the first layer mainly consists of EC with carbonyls oriented towards the bulk, leading to the distinct alternating layers of charged groups/ions normal to the electrode. When  $\sigma = -16.4 \mu\text{C}/\text{cm}^2$  [(b)], the presence of  $\text{Li}^+$  at the graphite edges causes a local rearrangement of EC to partially solvate  $\text{Li}^+$ , and thus the layering behavior is suppressed due to the charge variations occurring not only perpendicular, but also parallel to the electrode.

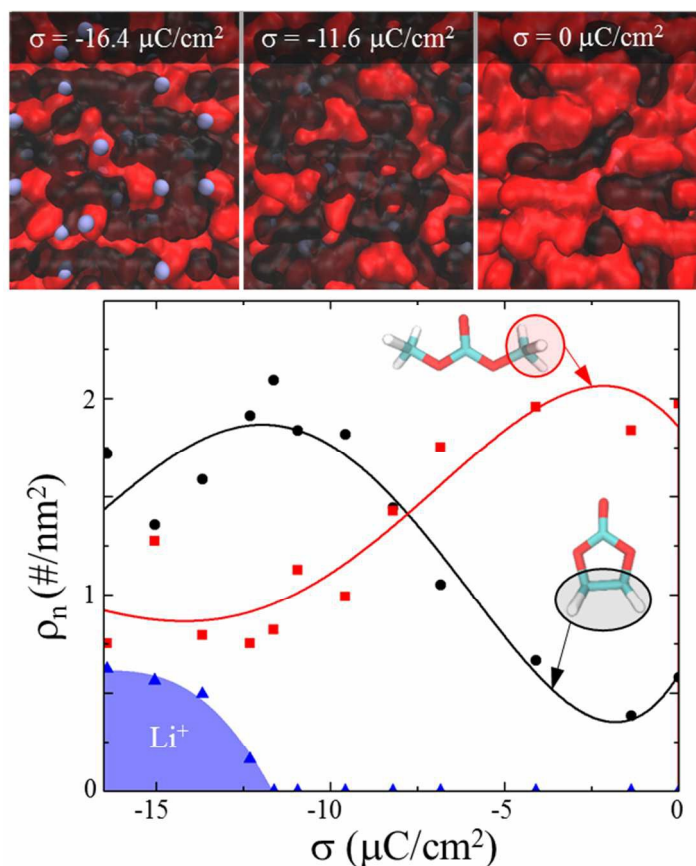


Figure 3. Variations in the number density ( $\rho_n$ ) of  $\text{Li}^+$  and positively charged ethylene/methyl groups (in EC/DMC, as shown by the models) in contact with the electrode at varying surface charge densities ( $\sigma$ ). In upper panels, MD snapshots are also shown to visualize the rearrangement of electrolyte species near the negatively charged electrode surfaces. Red/black isosurfaces represent DMC/EC-enriched regions and small blue balls indicate  $\text{Li}^+$  cations. DMC which is predominant at  $\sigma = 0 \mu\text{C}/\text{cm}^2$  is gradually replaced by EC with increasing  $|\sigma|$ , and eventually  $\text{Li}^+$  begins to accumulate on the electrode surface.

This analysis shows that the electric field created by the electrode's excess charge is shielded by the positively charged ethylene (and methyl) groups of EC (and DMC) and  $\text{Li}^+$  cations, depending on its magnitude. To demonstrate their relative contributions, the integrated  $\rho_n$  of the EC ethylene group, DMC methyl group, and  $\text{Li}^+$  in the vicinity of the electrode are plotted as a function of  $\sigma$  (see Figure 3). At neutral or slightly charged electrodes, DMC methyl groups exceed EC ethylene groups, but as the amount of the excess charge increases the latter

become more populated than the former. A similar trend was shown by Vatamanu *et al.*<sup>37</sup> near graphite basal surfaces where the EC concentration was shown to monotonically increase with increasingly negative potentials. However, beyond the maximum packing density of EC at the edge-plane,  $\text{Li}^+$  begins to accumulate while the  $\rho_n$  of EC ethylene (DMC methyl) groups decreases (increases). This finding may serve as a useful benchmark for comparison of structural evolution of electrolytes at the electrode vicinity during the charging process. Understanding the molecular structure of the electrolyte-electrode interface for different electrolyte compositions under various operating conditions can also lend towards a greater understanding of the formation and growth of SEI, particularly during early stages.

### C. Variation in potential difference across the electrolyte-electrode interface

From the interfacial structures described in the previous section, we estimated the variation of the potential drop ( $\phi$ ) from the metallic electrode to the bulk electrolyte with varying  $\sigma$  until the onset of  $\text{Li}^+$  ion accumulation on the electrode surface. We obtained  $\phi$  by solving Poisson's equation in one dimension ( $\nabla^2\phi = -\rho/\epsilon_0$ ) with boundary conditions of  $\phi = 0$  V and  $\nabla\phi = 0$  in the bulk region of the electrolyte, where  $\epsilon_0$  is the vacuum permittivity and  $\rho$  is the charge density (which is given by weighting the  $\rho_n$  for each atom by its charge value and summing them together). For a reference point, we considered the potential of zero charge (PZC,  $\phi_Z$ ) which is known to be approximately 3 V vs.  $\text{Li}^+/\text{Li(s)}$  (or 0 V vs. standard hydrogen potential)<sup>54,55</sup>. The PZC is due to a charge imbalance arising from the vdW interactions between the graphite edges and electrolyte molecules. From our classical MD simulations, the predicted  $\phi_Z$  is about -0.10 V as a result of the excess of positive methyl and ethylene groups at the interface. A similar  $\phi_Z$  value ( $\approx$  -0.14 V) was predicted for a flat graphite edge-plane against 1M  $\text{LiPF}_6$  in pure EC.<sup>38</sup>

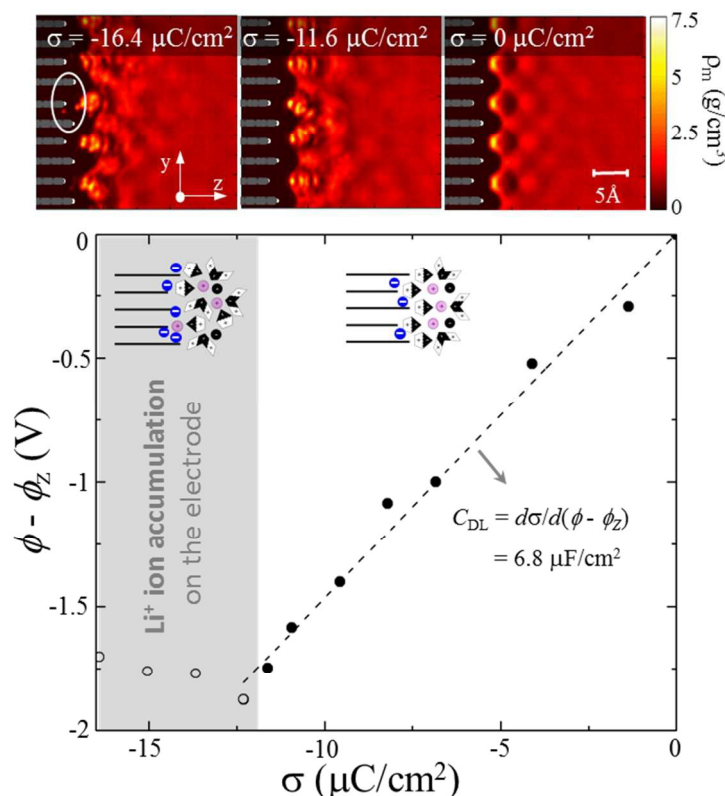


Figure 4. Variations in the potential drop ( $\phi - \phi_z$ ) across the electrolyte-electrode interface as a function of electrode surface charge density ( $\sigma$ ). In upper panels, mass density ( $\rho_m$ ) maps are also shown to visualize perturbations in the spatial distributions of the electrolyte components due to irregular electrode surfaces with rough edges and  $\text{Li}^+$  ions accumulated at the graphite edges; the perturbation becomes stronger as the electrode surface is more negatively charged. The inset illustrations show the accumulation of  $\text{Li}^+$  ions at the corrugated edges when  $\sigma > -12 \mu\text{C}/\text{cm}^2$ , which leads to compensation of excess negative charges on the electrode.

As shown in Figure 4, the predicted potential difference ( $|\phi - \phi_z|$ ) monotonically increases with  $\sigma$  up until  $\sigma \approx -12 \mu\text{C}/\text{cm}^2$  (where  $\text{Li}^+$  ions begin to precipitate on the electrode surface). Although the data are somewhat scattered, the  $(\phi - \phi_z)$  vs.  $\sigma$  plot appears to be nearly linear. From the linear plot, the differential capacitance of the electrical double layer formed at the interface is approximated to be  $C_{\text{DL}} = 6.8 \mu\text{F}/\text{cm}^2 [= d\sigma/d(|\phi - \phi_z|)]$ , in comparison to the 4-5  $\mu\text{F}/\text{cm}^2$  reported for a similar electrolyte at a graphite basal surface<sup>37</sup>. Beyond  $\sigma = -12 \mu\text{C}/\text{cm}^2$ , there is no significant variation in  $\phi - \phi_z$  since the additional excess of negative charge on the

electrode can be compensated by the positive charge of adsorbed  $\text{Li}^+$  ions at the corrugated edges, as illustrated in the inset.

Now we should point out that this analysis is based on the assumption that no redox reactions would occur at the electrolyte-electrode interface, like non-Faradaic supercapacitors. However, electrolytes containing EC and  $\text{Li}^+/\text{PF}_6^-$  salts have been reported to undergo decomposition around 0.8 V *vs.*  $\text{Li}^+/\text{Li(s)}$ , depending on electrolyte composition<sup>56</sup>; very recently, it was also reported that the reduction of EC:DMC/ $\text{LiPF}_6$  could occur as high as 1.7 V *vs.*  $\text{Li}^+/\text{Li(s)}$ , which was suggested to be related to anion decomposition<sup>57</sup>. For the system considered here, we could approximate the applied voltage (with respect to the potential of the bulk electrolyte) in terms of  $(\phi - \phi_Z)$  and the electrode potential ( $\phi_E$ ), i.e.,  $\phi_a = (\phi - \phi_Z) + \phi_E$ .<sup>51,52,58,59</sup> From our previous work<sup>52</sup>,  $\phi_E$  is approximated to be -0.45 (0.55) V when  $\sigma \approx -12$  (16)  $\mu\text{C}/\text{cm}^2$  at the H-terminated graphene edges. Taking  $\phi_E = -0.45$  V and  $(\phi - \phi_Z) = -1.75$  V (from Figure 4), the applied voltage is roughly -2.2 V (or 0.8 V *vs.*  $\text{Li}^+/\text{Li(s)}$ ) when  $\sigma \approx -12$   $\mu\text{C}/\text{cm}^2$ . This implies that  $\phi_a$  may begin to fall within 0.7-0.9 V *vs.*  $\text{Li}^+/\text{Li(s)}$  (as previously measured for the EC reduction potential on graphite electrodes) when  $\sigma$  reaches above -10  $\mu\text{C}/\text{cm}^2$ . Although there is room for improvement in prediction of the potential values, especially considering charge polarization at the interface<sup>59</sup>, at least we can expect that there would be no significant decomposition of solvent molecules while the graphite electrode is charged up until  $\sigma \approx -10$   $\mu\text{C}/\text{cm}^2$ . Beyond this, perhaps solvent molecules at the interface might undergo decomposition during the first charge cycle. However, this process may not occur instantaneously across the entire electrode surface as it becomes negatively charged, depending on the arrangements of solvent molecules. This implies a value to quantifying the structure of the electrolyte at the interface over a range of applied voltages where the reduction reactions would occur.



Additionally, our study shows that the relation between  $\phi_a$  and  $\sigma$  as well as critical  $\sigma$  (or  $\phi - \phi_Z$ ) for interfacial  $\text{Li}^+$  precipitation can be strongly influenced by electrolyte composition and temperature (which directly affect solvation of  $\text{Li}^+$  ions), along with electrode surface properties. This analysis also highlights the importance of the interfacial structure in characterizing ion mobility, which may be crucial to understanding SEI formation and charge rate.

#### D. Effect of interfacial structure on $\text{Li}^+$ ion transport

As discussed in the previous section, a  $\text{Li}^+$  cation is solvated by a combination of EC, DMC, and  $\text{PF}_6^-$ . The composition and structure of the  $\text{Li}^+$  solvation sheath may vary depending on the solvent composition as well as the relative strength of intermolecular interactions between  $\text{Li}^+$ -solvent and solvent-solvent. In the bulk electrolyte, the solvated  $\text{Li}^+$  may undergo thermally activated random-walk migration, which can be quantified by computing the mean-square displacement or the velocity autocorrelation function of the moving  $\text{Li}^+$ . The mean-field approach is adequate in describing diffusion when the system is relatively uniform. As demonstrated earlier, however, the electrolyte composition is not spatially uniform and its structure becomes even solid-like near the electrode surface. Hence, other techniques may be required in order to characterize  $\text{Li}^+$  solvation and transport properties in the electrolyte-electrode interface region.

The transport rate of  $\text{Li}^+$  through the interfacial layer is related to the free-energy penalties associated with its moving from the bulk region. We calculated the relative free energy ( $\Delta A$ ) profiles for a  $\text{Li}^+$  ion travelling from the bulk electrolyte to the electrode surface using well-tempered metadynamics simulations. As presented in Figure 5, three different charge states of the electrode were considered to examine the effect of the interfacial structure on  $\text{Li}^+$  transport;  $\sigma$



$= 0 \mu\text{C}/\text{cm}^2$  [(a)],  $-11.6 \mu\text{C}/\text{cm}^2$  [(b)], and  $-16.4 \mu\text{C}/\text{cm}^2$  [(c)]. For each system, the result was obtained from a 70 ns simulation conducted with an initial Gaussian height of 10 kJ/mol, Gaussian  $\sigma$  of 0.05 nm,  $\Delta T = 7200\text{K}$ , and with Gaussians deposited every 100 fs.

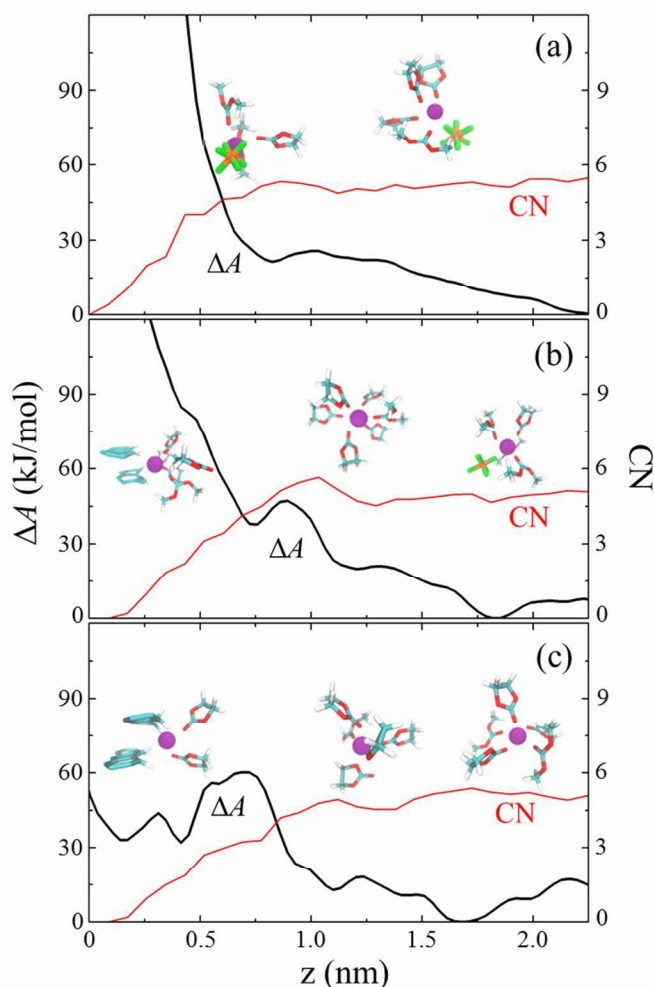


Figure 5. Variations in the relative free energy ( $\Delta A$ ) (left axis) and the Li<sup>+</sup> coordination number (CN) (right axis) along the z-direction near graphite electrodes with surface charge densities of (a)  $\sigma = 0 \mu\text{C}/\text{cm}^2$ , (b)  $\sigma = -11.6 \mu\text{C}/\text{cm}^2$ , and (c)  $\sigma = -16.4 \mu\text{C}/\text{cm}^2$ . Selected screenshots of the Li<sup>+</sup> solvation sheath are also shown to visualize changes in the interaction between Li<sup>+</sup> and neighboring solvent molecules as it moves towards the interface from the bulk-like region.

### 1. Near Uncharged Electrodes.

When  $\sigma = 0 \mu\text{C}/\text{cm}^2$  [(a)], as Li<sup>+</sup> moves towards the interface from the bulk-like region, the  $\Delta A$  gradually increases to a maximum around  $z = 1 \text{ nm}$  followed by a slight minimum around  $z =$

0.8 nm, and then there is a rapid increase in  $\Delta A$ . The energy penalties can be associated with rearrangement of solvent molecules and partial desolvation of  $\text{Li}^+$ . In the region from  $z = 2.25$  nm to 1 nm, the predicted  $\text{Li}^+$  coordination number (CN) is nearly unchanged, suggesting that the  $\text{Li}^+$  may remain fully solvated while diffusing through the electrolyte layer. This also implies that at least part of the primary solvation sheath would move with the  $\text{Li}^+$ , rather than a passing of the  $\text{Li}^+$  over the EC/DMC carbonyls via a ratchet mechanism (which would be well represented by oscillations in the CN as the  $\text{Li}^+$  passes through transition states). We attribute the gradual increase of  $\Delta A$  to the increasing energy cost for rearrangements of the  $\text{Li}^+$  solvation sheath and its surrounding molecules as the electrolyte becomes more ordered with decreasing  $z$ ; recall that the layered structure induced by the electrolyte-electrode interaction extends up to  $z \approx 2.5$  nm, as shown in Figure 1.

It is also interesting to note that the maximum (minimum) of  $\Delta A$  at  $z \approx 1$  nm (0.8 nm) corresponds to a minimum (maximum) in  $\rho_n$  for EC/DMC (see Figure 1). In addition, the relatively high concentration of  $\text{PF}_6^-$  anions at  $z \approx 0.8$  nm may contribute to lowering  $\Delta A$  by interacting with the  $\text{Li}^+$  cation. Below  $z = 0.8$  nm, the sharp increase in  $\Delta A$  is largely attributed to the  $\text{Li}^+$  desolvation as evidenced by the decrease in CN (Figure 5). In the densely packed solid-like layer, the  $\text{Li}^+$  may travel as a partially-solvated ion as solvent molecules are unable to rearrange to fully solvate it, bearing a high energy penalty. Here, we could not exclude the possibility that the non-polarizable force fields employed may lead to overestimation of  $\Delta A$ . Nonetheless, our analysis at least suggests that, in the absence of favorable electrostatic interactions with the electrode, the  $\text{Li}^+$  is highly unlikely to diffuse through the densely packed interfacial layer.

## 2. Near Charged Electrodes.

For both  $\sigma = -11.6 \mu\text{C}/\text{cm}^2$  [(b)] and  $-16.4 \mu\text{C}/\text{cm}^2$  [(c)] cases, the CN of  $\text{Li}^+$  changes minimally as  $\text{Li}^+$  moves up to  $z \approx 1 \text{ nm}$  from the bulk-like region, implying that the  $\text{Li}^+$  can undergo migration while remaining fully solvated. However, unlike the uncharged case [(a)], the  $\Delta A$  profile exhibits fluctuations along the  $z$  direction rather than monotonic increases; the fluctuations appear to become stronger in case (c) compared to case (b). We attribute the  $\Delta A$  fluctuations largely to perturbations in the spatial distributions of the electrolyte constituents, as demonstrated in the 2D density maps (Upper panels in Figure. 4).

In case (b), the pronounced maximum of  $\Delta A$  around  $z = 0.9 \text{ nm}$  appears related to the increased  $\rho_n$  of EC/DMC/ $\text{PF}_6^-$  between  $z = 0.8 \text{ nm}$  and  $1.1 \text{ nm}$ , which may in turn allow  $\text{Li}^+$  ions to accumulate in the region while solvating them more tightly as indicated by the increased  $\rho_n$  and CN of  $\text{Li}^+$ . Therefore, we can expect that  $\text{Li}^+$  ionic transport through the tightly packed region will be significantly impeded. Due to a similar reason, the  $\Delta A$  profile tends to exhibit a shoulder around  $z = 1 \text{ nm}$  in case (c).

Below  $z = 0.8 \text{ nm}$ , for both cases (b) and (c), the CN of  $\text{Li}^+$  is found to monotonically decrease with decreasing  $z$ . This indicates that in the densely packed solid-like layer the  $\text{Li}^+$  may travel as a partially-solvated ion as solvent molecules are unable to rearrange to fully solvate it, bearing a high energy penalty. In contrast to case (a), the rather disordered interface layer may help stabilize the  $\text{Li}^+$  to a certain degree while it becomes more solid-like with increasing the electrode's charge density ( $\sigma$ ); the perturbation effect is likely to be stronger in case (c), relative to case (b), due to the irregularly distributed  $\text{Li}^+$  ions at the electrode surface as evidenced by the comparison between corresponding density maps. In case (c), such perturbations in the first electrolyte layer also likely allow for favorable electrostatic interactions with the negatively

charged electrode, thereby stabilizing the partially desolvated  $\text{Li}^+$  and thus substantially reduce the energy cost  $\Delta A$  from 85 kJ/mol to 60 kJ/mol. It would be interesting to note that the predicted  $\text{Li}^+$  transport barriers are comparable with 50-80 kJ/mol (depending on electrolyte composition) as reported by previous experimental and theoretical studies<sup>13-15,40</sup>, despite different interfacial and operating conditions.

#### IV. Conclusions

Molecular dynamics (MD) simulations were used to investigate changes in the distribution of a mixed solvent electrolyte (1M  $\text{LiPF}_6$  in ethylene carbonate (EC):dimethyl carbonate (DMC) (= 1:1 molar ratio)) in the vicinity of graphite electrodes with varying surface charge densities ( $\sigma$ ). From the interfacial structures, we estimated the variation of the potential difference across the electrolyte-electrode interface with respect to  $\sigma$ , along with the relation between applied voltage and  $\sigma$ . In addition, we evaluated  $\text{Li}^+$  ion solvation and transport in the ordered and densely-packed interfacial layer by carefully analyzing the solvation sheath structure of  $\text{Li}^+$  (such as its coordination number, CN) as well as the free-energy penalties ( $\Delta A$ ) associated with its moving to the interface from the bulk-like region using advanced sampling techniques (well-tempered metadynamics). The goals of this work were to gain a deeper understanding of the interfacial interactions at the molecular level between mixed carbonate-based electrolytes and graphite electrodes, and to provide some intuition to help better understand the fundamental processes involved in SEI formation along with  $\text{Li}^+$  ion dynamics at the electrolyte-electrode interface.

Our main findings are summarized below.

- DMC and EC pack densely near the uncharged electrode by approximately 3 and 2 times higher than their bulk values due to the van der Waals (vdW) interaction with the electrode. The preference towards DMC is largely attributed to its bulky methyl groups. After about  $z = 2$  nm from the electrolyte-electrode interface, the electrolyte tends to become bulk-like.
- When the electrode is negatively charged, cyclic EC is found to become more populated than linear DMC. We attribute this to the relatively smaller size of EC that allows it to pack more densely, which along with its larger polarity leads to more effective screening of the electric field from the charged electrode.
- Beyond a critical  $\sigma$  ( $\approx -12 \mu\text{C}/\text{cm}^2$ ), we find that  $\text{Li}^+$  ions tend to accumulate at the graphite edges as the EC/DMC molecules are unable to pack densely enough to shield the charged electrode.
- The predicted potential drop ( $\phi$ ) from the graphite electrode to the bulk electrolyte exhibits a nearly linear variation with respect to  $\sigma$  until the onset of  $\text{Li}^+$  precipitation at the interface, after which there is no significant variation in  $\phi$  because of the compensation of the additional excess of negative charge on the electrode by the adsorbed  $\text{Li}^+$  ions. A brief discussion of how  $\sigma$  is related to the applied voltage is also provided.
- The predicted  $\Delta A$  gradually increases as  $\text{Li}^+$  moves from the bulk-like region to about  $z = 1$  nm from the electrode surface, while its CN changes marginally. This suggests that the  $\text{Li}^+$  may remain fully solvated while diffusing through the electrolyte layer. The increasing energy cost results from rearrangements of the  $\text{Li}^+$  solvation sheath and its surrounding molecules as the electrolyte becomes more ordered with decreasing  $z$ .
- For  $z < 1$  nm, as evidenced by its decreasing CN, the  $\text{Li}^+$  may travel as a partially-solvated ion through the densely packed solid-like layer (where solvent molecules are unable to

rearrange to fully solvate it). Therefore, the  $\Delta A$  sharply increases as the CN of  $\text{Li}^+$  continues to decrease unless the electrode charges are sufficient enough to stabilize the partially-desolvated  $\text{Li}^+$  ion through favorable electrostatic interactions. Beyond the critical  $\sigma$  ( $\approx -12 \mu\text{C}/\text{cm}^2$ ),  $\Delta A$  is predicted to be substantially reduced due to the electrostatic interaction with the negatively charged electrode; in turn this allows the  $\text{Li}^+$  to diffuse through the densely packed electrolyte layer followed by its accumulation on the electrode.

- Our analysis shows that the spatial distributions of ions and solvent molecules in the interfacial layer can be substantially perturbed by irregular electrode surfaces with rough edges,  $\text{Li}^+$  ions accumulated at the graphite edges, and/or various functional groups. Such perturbation tends to favorably influence  $\text{Li}^+$  ion transport through the electrolyte-electrode interface.

In this work, we only focused on the reorganization of solvent molecules (EC and DMC), without considering their decomposition, in the vicinity of the negative electrode at varying applied voltages, including where they may begin to decompose via reduction. Quantitative analysis of the molecular arrangements at the electrolyte-electrode interface helps to better describe electrolyte decomposition/diffusion processes, especially in the initial stages of SEI formation. A better description of the onset of SEI formation is particularly important as it may significantly influence the growth and structure of SEI layers which are known to be kinetically governed to a large extent.

This study suggests that the interfacial structure can be significantly altered by not only electrolyte composition but also electrode surface modification and operating conditions, warranting further investigations. Such improved mechanistic understanding of the effects of solvent mixture, electrode surface, and operating temperature on the interfacial properties will further assist in efforts to engineer the electrolyte-electrode interface leading to an SEI which

optimizes LIB performance. This work also shows the value of metadynamics as an effective means for evaluating  $\text{Li}^+$  ion transport near electrolyte-electrode interfaces. The computational framework presented herein offers a means to explore the interfacial structure and properties for various electrode/electrolyte and operating conditions.

### Supporting Information

Electronic supplementary information (ESI) available: Additional available information includes the predicted structural and transport properties of the electrolyte considered (1M  $\text{LiPF}_6$  in EC:DMC) for validation of the classical force fields employed in this work, in addition to one-dimensional charge density profiles used to estimate the potential difference across the electrolyte-electrode interface as well as the number density profiles for EC, DMC,  $\text{Li}^+$  and  $\text{PF}_6^-$  along the perpendicular direction of the electrode surface at electrode surface charge densities of  $\sigma = -4.1 \mu\text{C}/\text{cm}^2$  and  $-8.2 \mu\text{C}/\text{cm}^2$ .

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Table of Contents

