Example of backpropagation

$$\frac{\text{Hidden}}{h_1 = \phi(z_1)} = \frac{w_1 x_1 + w_2 x_2 + b_1}{1 + e^{-k_1}}$$

$$b_2 = \phi(\overline{z_2}) = \frac{1}{1 + e^{-b_2}}$$

Qutput:
$$z_3 = w_5h_1 + w_bh_2 + b_2$$

$$0_1 = \phi(z_2)$$

$$z_4 = w_7h_1 + w_8h_3 + b_3$$

$$0_2 = \phi(z_4)$$

$$\exists (w) = \frac{1}{2} (y_1 - 0_1) + (y_2 - 0_2)$$

$$w = (w, ---, w_8, b_1, b_2)$$

1) Consider first the weights of links connecting the hidden and the out put layer, e.g. Ws.

$$\frac{\partial W_5}{\partial W_5} = \frac{\partial Z_3}{\partial Q_1} \frac{\partial Z_3}{\partial Z_3} \frac{\partial W_5}{\partial W_5}$$

$$\frac{\partial \mathcal{J}}{\partial \mathcal{O}} = -\left(\mathcal{J}, -\mathcal{O}, \right)$$

$$\frac{\partial O_1}{\partial z_3} = \phi(z_3) = \phi(z_3)(1 - \phi(z_3))$$

$$= O_1(1 - O_1)$$

$$\frac{\partial h^2}{\partial s^3} = h'$$

hence

$$\frac{\partial \Xi}{\partial W_{5}} = -\left(Y_{1} - \theta_{1}\right) \theta_{1} \left(1 - \theta_{1}\right) h_{1}$$

Hence,
$$W_5 = W_5 - 1$$
 ∂W_5 update

$$\frac{\partial A}{\partial w} = \frac{\partial A}{\partial w} \frac{\partial w}{\partial w}$$

$$\frac{\partial \mathbf{S}^{\prime}}{\partial \mu^{\prime}} = \mu^{\prime} \left(1 - \mu^{\prime} \right)$$

and
$$\frac{\partial O_1}{\partial k_1} = O_1(1-9_1) W_5$$

$$\frac{\partial O_2}{\partial k_1} = O_2(1-0_2) W_7$$

hence we can wride:

$$\frac{\partial \Xi}{\partial W_{1}} = \frac{\partial L_{1}}{\partial L_{1}} \times L_{1} + \frac{\partial L_{2}}{\partial W_{1}} = \frac{\partial L_{1}}{\partial L_{1}} \times L_{2} + \frac{\partial L_{2}}{\partial W_{1}} = \frac{\partial L_{1}}{\partial L_{1}} \times L_{2} + \frac{\partial L_{2}}{\partial W_{1}} = \frac{\partial L_{1}}{\partial L_{1}} \times L_{2} + \frac{\partial L_{2}}{\partial W_{1}} \times L_{2} + \frac{\partial L_{2}}$$

and the can also be done for the other weights we , by and wy.