# Compiler (Optimization)

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References: Dragon book, Alex Aiken compiler course

### Optimization phase

Lexical analyzer

Syntax analyzer

Semantic ånalyzer

Intermediate code generation

Optimization

Code generation

- Most complexity of modern compilers is in optimization (usually the largest phase)
- Optimization on intermediate language:
  - Machine independent
  - Exposes optimization opportunities

### Optimization goals

- Improve a program's resource utilization
  - Execution time (most often)
  - Code size
  - Network messages sent
  - Memory, disk, power, etc
- Optimization should not alter what the program computes

### **Block**

- Basic block: Maximal sequence of instructions with
  - No labels: except at the first instruction
  - No jumps: except in the last instruction
- So:
  - Basic block is a single-entry, single-exit, straightline code segment
  - Can not jump out of a basic block except at end
  - Can not jump into a basic block except at beginning

### Block Example

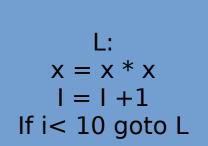
- 1. L:
- 2. t = 2 \* x
- 3. w = t + x w = 3 \* x
- 4. if w>0 goto L'

Can we eliminate 2?

### Control Flow Graph

X = 1Y = 1

- A directed graph with:
  - Basic blocks as nodes
  - An edge from block A to block B if the execution can pass from the last instruction in A to the first instruction in B
- The body of a method can be represented as a control-flow graph
- There is one initial node
  - All return nodes are terminals



### Optimization scope

- Local Optimization (most compilers do)
  - Apply to a basic block in isolation
- Global Optimization (many do)
  - Apply to a control flow graph in isolation (method body)
- Inter-procedural optimization (few do)
  - Apply across method boundries

### Optimization challenges

- In practice often a conscious decision is made not to implement the fanciest optimization known.
- Why?
  - Some are hard to implement
  - Some are costly in compilation time
  - Some have low payoff
  - Many fancy optimizations are all three
- Maximum benefit for minimum cost

# Algebraic simplification

Some statements can be deleted

$$- x = x + 0$$
  
 $- x = x * 1$ 

Some statements can be simplified

```
- x = x * 0 \rightarrow x = 0

- y = y ^ 2 \rightarrow y = y * y

- x = x * 8 \rightarrow x << 3

- x = x * 15 \rightarrow t = x << 4; x = t - x

(if << is faster than * in the target machine)
```

### Constant folding

 Operations on constants can be computed at compile time

$$-X = 2 + 3 \rightarrow X = 5$$

- If 2<0 jump L → can be deleted</li>
- Dangerous constant folding
  - In Cross compilers:
    - Ex: 3.8 + 4.5 = 8.3 or 8.29999

### Unreachable basic blocks

- Code that is unreachable from the initial block
  - Eg: basic blocks that are not target of any jump or fall through from a conditional
- Eliminating these blocks makes program smaller
  - And sometimes faster
    - Due to memory cache effects
    - Increase spatial locality

### Unreachable basic blocks

#define debug 0
 If (debug)

Results of other optimizations

 Each register occurs only once in the left hand side of an assignment

$$-x = z + y$$
  $b = z + y$   
 $-a = x$   $\rightarrow$   $a = b$   
 $-x = 2 * x$   $x = 2 * b$ 

# Common sub expression elimination

#### • If

- basic block is in single assignment form
- a definition x = is the first use of x in a block

#### Then

 when two assignments have the same rhs they compute the same value

$$-X = y + z$$

$$- \dots$$

$$-W = y + z$$

$$\times = y + z$$

$$w = x$$

# Copy propagation

 If w = x appears in a block replace subsequent uses of w with uses of x

$$-x = z + y \qquad b = z + y$$

$$-a = x \qquad \rightarrow \qquad a = b$$

$$-x = 2 * x \qquad x = 2 * b$$

- It is useful for enabling other optimizations
  - Constant folding
  - Dead code elimination

### Example

• 
$$a = 5$$

• 
$$x = 2 * a$$

• 
$$y = x + 6$$

• 
$$t = x * y$$

$$\rightarrow$$

### Dead code elimination

- If
  - w = rhs appears in a basic block and w does not appear anywhere else in the program
- Then
  - statement w = rhs is dead and can be eliminated
- Dead = does not contribute to the program's result

$$-x = z + y$$

$$-a = x$$

$$-x = 2 * x$$

$$b = z + y$$

$$a = b$$

$$x = 2 * b$$

# Consecutive optimization

- Each local optimization does little by itself
  - But performing one optimization enables another
- Optimizing compilers repeat optimizations until no improvement is possible
  - Or stopped at any point to limit compilation time.

# Example

#### Initial code:

$$-a = x^2 \rightarrow x^* x$$

$$- b = 3$$

$$- c = x$$

$$- d = c * c$$

$$- e = b *2$$

$$- f = a + d$$

$$-g = e*f$$

### Example

Initial code:

- 
$$a = x ^2 \rightarrow x^* x$$
  
-  $b = 3$   
-  $c = x$   
-  $d = c^* c \rightarrow x^* x \rightarrow a$   
-  $e = b^* 2 \rightarrow b << 1 \rightarrow 3 << 1 \rightarrow 6$   
-  $f = a + d \rightarrow f = a + a \rightarrow 2^* a$   
-  $g = e^* f \rightarrow g = 6^* f \rightarrow 12^* a$ 

# Peephole optimization

- Optimization applied directly to assembly code
- a sliding window of target instructions (called the peephole) and replacing instruction sequences within the peephole by a shorter or faster sequence, whenever possible.

# Peephole optimization

- Ex1
  - Move \$a, \$b
  - Move \$\$b, \$a
  - If the second line is not the target of a jump
- Ex2
  - Add \$a, \$a i
  - Add \$a, \$a j
- Ex3
  - Addiu \$a, \$b 0 → move \$a, \$b
  - Addiu \$a \$a 0 → eliminated
  - Move \$a \$a → eliminated

Move \$a, \$b

Add \$a, \$a i+j

# Dataflow analysis

 How do we know is it OK to globally propagate constants? Or detect dead code to eliminate

$$X = 3$$
$$B > 0$$

$$Y = z + w$$
  
 $X = 4$ 

$$Y = 0$$

$$A = 2 * \times 3?$$

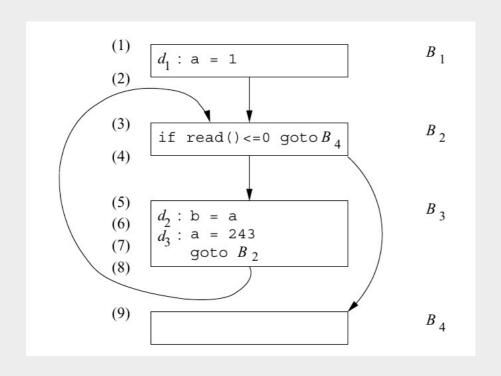
### Dataflow analysis

- Checking the condition requires global dataflow analysis
  - An analysis of entire control-flow graph

### Dataflow analysis

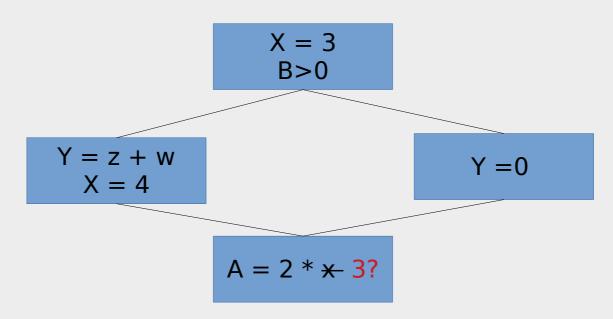
- In general, it is not possible to keep track of all the program states for all possible paths.
- In data-flow analysis, we do not distinguish among the paths taken to reach a program point.
- Moreover, we do not keep track of entire states;
- rather, we abstract out certain details, keeping only the data we need for the purpose of the analysis.

# Data-flow analysis



- To replace a use of x by a constant k we must know:
  - On every path to the use of x, the last assignment to x is x = k

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# Global optimization

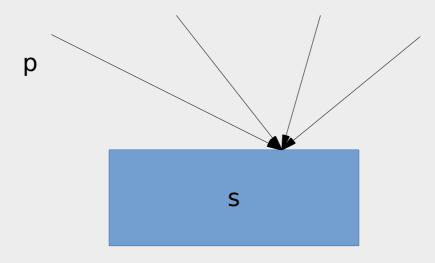
- The optimization depends on knowing a property
   X at a particular point in program execution
- Proving x at any point requires knowledge of the entire program
- Global dataflow analysis is a standard technique for solving problems with these characteristics
- Global constant propagation is one example of an optimization that requires global datafloa analysis

 The analysis of a complicated program can be expressed as a combination of simple rules relating the change in information between adjacent statements

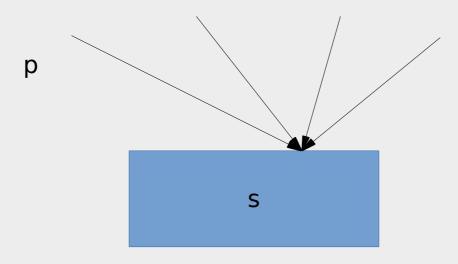
 To make the program precise, we associate one of the following values with x at every program point

Value	interpretation
1	This statement never executes
С	x = constant c
Т	x is not a constant

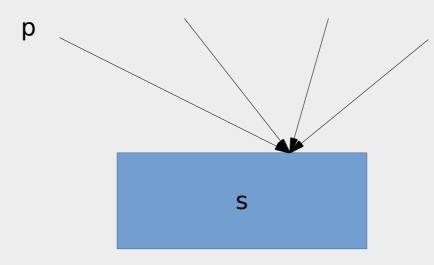
- For each statement s, we compute information about the value of x immediately before and after s
  - C(x, s, in) = value of x before s
  - -C(x, s, out) = value of x after s
- In the following rules, let statement s
  have immediate predecessor
  statements p<sub>1</sub>, ..., p<sub>n</sub>



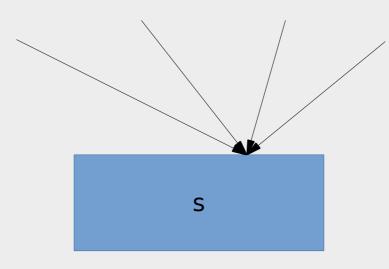
If  $C(P_i, x, out) = T$ , for any i, then C(s, x, in) = T



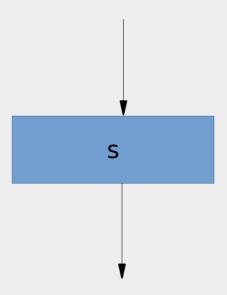
If  $C(P_i, x, out) = c \& c(P_j, x, out) = d \& d <> c$ then C(s, x, in) = T



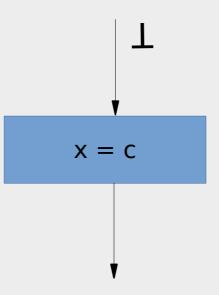
If C(P<sub>i</sub>, x, out) = c or ⊥ for all I, then C(s, x, in) = c



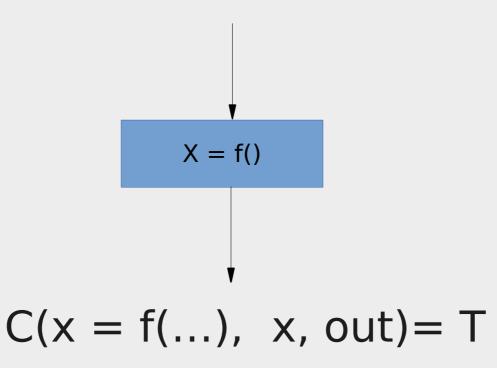
If  $C(P_i, x, out) = \bot$  for all i, then  $C(s, x, in) = \bot$ 

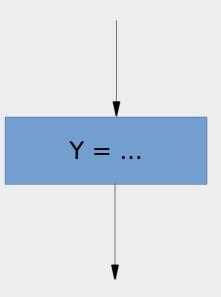


 $C(s, x, out) = \bot$ , if  $C(s, x, in) = \bot$ 



C(x = c, x, out) = c if c is a constant

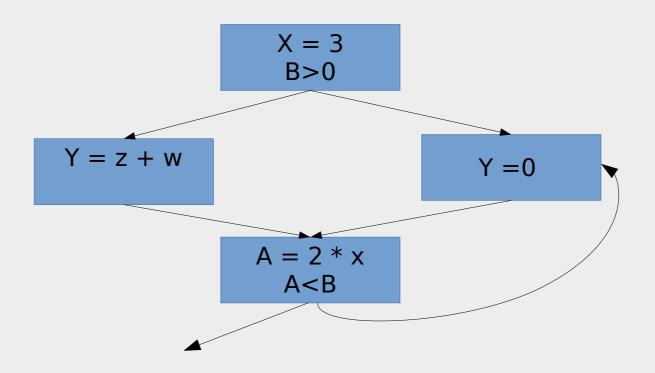




$$C(y = ..., x, out) = C(y = ..., x, in) if x <> y$$

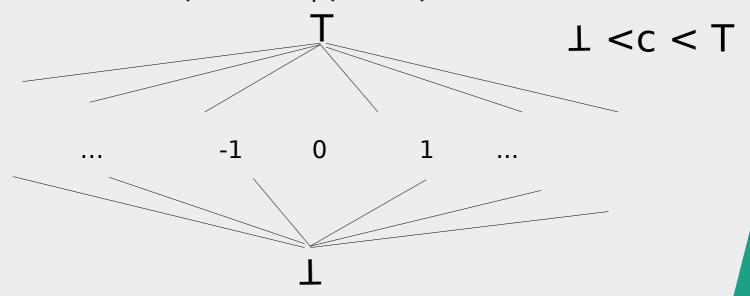
- For every entry s to the program, set
   c(s, x, in) = T
- Set C(s, x, in) = C(s, x, out) = 1
   everywhere else
- Repeat until all points satisfy 1-8:
  - Pick s not satisfying 1-8 and update using the appropriate rule

# Why we need ⊥?



# ordering

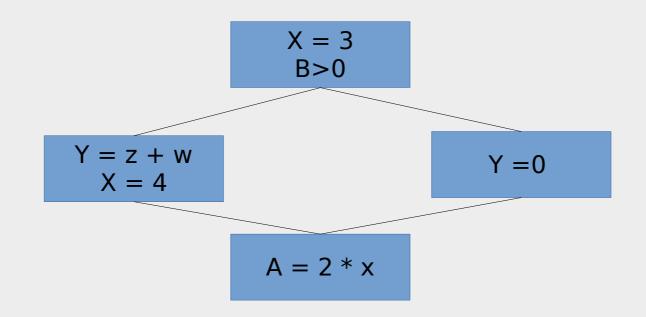
- T is the greatest value,  $\bot$  is the least
  - All constants are in between and incomparable
- Let lub be the least-upper bound in this ordering
- Rules 1-4 can be written using lub:
  - C(s,x,in)=lub{C(p,x,out) | p is a predecessor of s }



# ordering

- Simply saying "repeat until nothing changess" doesn't guarantee that eventually nothing changes
- The use of lub explains why the algorithm terminates
  - Values start as  $\perp$  and only increase
  - L Can change to a constant, and a constant to T
  - Thus, C(s, x, \_) can change at most twice
- Thus the constant propagation algorithm is linear in program size

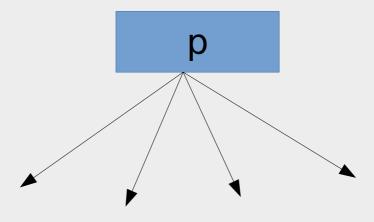
 Once constants have been globally propagated, we would like to eliminate dead code



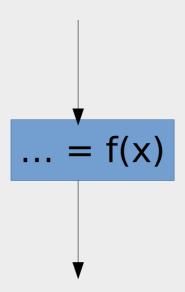
- The first value of x is dead (never used)
- The second value of x is live (may be used)
- X = 3 X = 4 Y = x

- Liveness is an important concept
- A variable x is live at statement s if
  - There exists a statement s' that uses x
  - There is a path from s to s'
  - That path has no intervening assignment to x

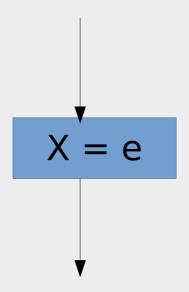
- We can express liveness in terms of information transferred between adjacent statements, just as in copy propagation
- Liveness is simpler that constant propagation it is a boolean property



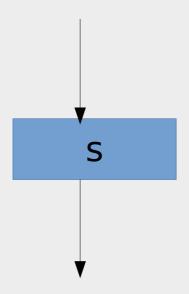
 $L(p, x, out) = V \{ L(s,x, in) | s a successor of p \}$ 



 L(s, x, in) = true if s refers to x on the rhs

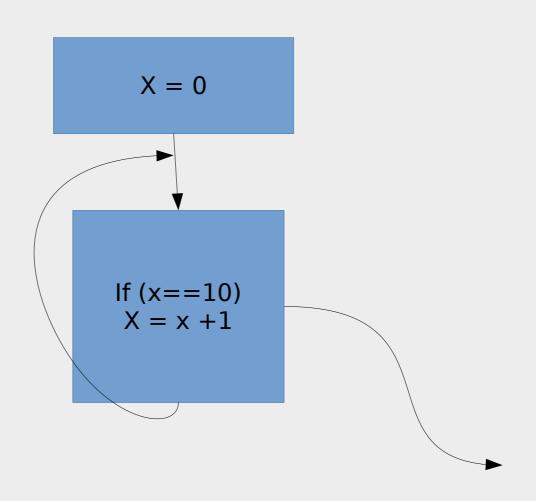


 L(x = e, x, in) = false if e does not refer to x



 L(s, x, in) = L(s, x, out) if s does not refer to x

- Let all L(...) = false initially
- Repeat until all statements s satisfy rules 1-4
  - Pick s where one of 1-4 does not hold and update using the appropriate rule



- A value can change from false to true, but not the other way around
- Each value can change only once, so termination is guaranteed
- Once the analysis is computed, it is simple to eliminate dead code