

Let us define an optimal solution  $O = \{L_{x1}, L_{x2}, L_{x3}, \dots, L_{xn}\}$  and our greedy algorithm solution  $G = \{L_{y1}, L_{y2}, L_{y3}, \dots, L_{ym}\}$ . Assuming that these two solutions are not the same, this means that there are elements in  $O$  that might not be in  $G$ , or elements in  $G$  that might not be in  $O$  and hence the orders of  $O$  and  $G$  might be different or there are elements in  $G$  in a different order than  $O$ . We can **exchange** the elements between the sets to make them similar to each other. If for example, the optimal algorithm stopped at a stop for 20 mins, we'd see my greedy algorithm stopping for 4 mins at 5 different stops. Both algorithms will give a total time of 20 mins and hence can be considered optimal for the first case. The second case is not possible as different orderings can not take place because  $O$  and  $G$  can't go in a reverse order. Hence we can conclude that  $G$  is also the optimal algorithm.