Towards lifelong mapping in pointclouds

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Abstract

The thesis discuses the application of non parametric Bayesian methods and how such tools can be directed to improve lifelong mapping capabilities of existing methods. A novel method of object clustering and matching is presented and its results are applied to an EKF SLAM algorithm. The strengths, weaknesses as well as future directions that can be taken to improve the method are then presented.

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1. Introduction

Simultaneous localization and mapping is one of the fundamental problems of autonomous systems[1]. In order for a robot to be truly autonomous, it must have the ability to enter an area and infer its structure. To that direction, a lot of effort has been put in algorithms that are able to map static environments. With solutions like EKF-SLAM[2], FastSlam[40] and GraphSLAM[3] robots are now able to efficiently map static environments. The logical extention to methods that can map static environments is methods that remove this restriction. The idea of lifelong robot learning is not new and has been introduced as a general concept to the literature by Sebastian Thrun [5]. Konolige et al.[6] specifically focus on lifelong learning in mapping and the utility such methods would have. In the PhD thesis of Walcott [7] long term mapping is decomposed to 4 basic subproblems:

- Continuously incorporate new information.

- Address the problem of tractability for growing DPG

- Representation of the environment should include the history of the map as changes occur with the passage of time.

- Detect changes and update the map online

The first two problems can be though of as compression problems as the map increases over time whereas the latter ones can be though of as dynamic environment problems. Methods of tackling those problems vary according to what sensors a robot uses to perform the mapping. In this project the focus will be directed in methods that use RGBD devices to perform SLAM like Microsoft's Kinect.

Since its introduction in 2010 Microsoft Kinect[25] has revolutionized RGBD devices with its low price range and high quality sensors. It came as no surprise that research in point clouds, the representation system of Kinect sensor readings, has increased since. Many libraries that enable the user to perform tasks from feature extraction to plane segmentation[12] in pointclouds are currently available. In the field of robotics, many teams are using the Kinect sensors to perform simultaneous localization and mapping[13]. The goal of this thesis is to introduce a novel approach to tackle the compression problem of long term mapping methods that use the Kinect device by using Bayesian non parametric methods.

Dirichlet processes and Dirichlet process mixture models [26] are the cornerstone of Bayesian non parametric statistics. The strength of those models lies in the fact that they allow the model's mixture components to grow as much as needed so as to best fit the data. The dynamic number of components in combination with the highly resilient priors leads to very flexible models that can be used in a very large area of applications from topic modeling[43] to speaker diarization[45].

The main motivation behind this project is to use such methods as a means of compressing the information provided by the environment. In that direction, finding a way to robustly cluster a point cloud into semantically sound "chunks" of structure seems a reasonable starting point. This leads to the direction of object based SLAM, which is a domain where objects are used as reference points to perform the mapping.

In this paper, an EKF SLAM method that takes point clouds as input will be implemented. Its results will then be empirically tested as well as its ability to concretely compress the data a point

cloud. Its strengths and weaknesses will be presented and analysed; furthermore, directions on how the method could be extended to tackle the first two subproblems of Walcott's thesis will be given in the discussion.

The rest of the paper is structured as follows. Section 2 will present relevant literature review, Section 3 will introduce the theories behind the model, Section 4 4 will define the model, Section 5 5 will show experimental results of the method. Finally, Section 6 6 will end up with a discussion on the methods strengths and weaknesses.

2. Literature review

Related research will be focused on 4 general sub fields of related literature.

- Object based SLAM or semantic slam

- Point Cloud Object segmentation

- Non-parametric clustering methods

- The correspondence problem in SLAM

More specifically, object based SLAM is crucial due to the nature of the input the method at hand has. Since point clouds are used as input and from such input object representations must be extracted, methods that use such approaches to perform SLAM are then needed. The second part of the research is focused on point cloud representations. This part of the research is mostly focused on what features or meta-features need to be taken into account so that the reduced representation is solid. The third part of the research is focused on non-parametric Bayesian methods and the clustering tools they provide. Such tools are important as they can be used to provide new approaches to object segmentation within a point cloud. Finally, research is focused on the correspondence problem in SLAM. As one of the fundamental problems that need to be solved in order to have robust SLAM algorithms, it is imperative the correspondence problem be solved efficiently. In that extent and due to the unique representation of our objects, a novel approach that takes elements from other techniques in the correspondence between objects in a SLAM problem is given.

2.1. Object based SLAM

Object based SLAM or semantic slam methods proposed to the literature focus in domain specific solutions of a particular problem. Salas-Moreno et al [14] define a method of performing object based slam for specific objects. The objects are identified by camera that is on top of the robot. By having a model of pretrained objects SLAM can be performed on environments the robot knows what objects to expect. The disadvantage of that method is that object models have be to be well defined and there is a small number of such objects. Castle et al. use object recognition to perform object based SLAM with the use of a hand-held cameras. Selvatici et al [15] use a similar approach while exploiting structural information such as object height and position within the room. That way a couch that is a large object situated in floor level is easier to be recognized. Choudhary et al. [17] use point clouds and an object database to match objects currently seen with known objects

within their database. They use omnimaper [27] as their mapping method and as a representation a combination of the downsampled voxel grids with additional normal and curvature information. Finally, all their operations are done in the non-planar components of the point cloud. Jensfelt et al [15] present an object based approach to SLAM where the robot can manipulate the objects of the map. They use camera pictures as input and receptive Field Histogram as the method to abstract the camera input and extract features for their object matching algorithm. Their approach is proposed as a solution to a service robot scenario. MonoSLAM [19] introduces a method of performing slam using a monocular camera.

What all the previous methods have in common is that they approach the problem of object based slam as a classification task. Objects need to be semantically understood before they are processed. The approach introduced in this paper considers the environment to be a collection of chunks. So having specific enough environment descriptors should lead to the robot being able to operate in a label free environment. This would remove the need of having to classify objects but would also increase the time it takes to extract features from the environment as features are the base of the unsupervised object discovery. Seongyong Koo et al. [20] introduce a method of unsupervised object individuation from RGB-D image sequences. They cluster their initial cloud into candidate objects using Eucledian clustering and proceed to extract features like the Euclidian distance(L2) and the Kullback-Leibler distance between point cloud objects. They use IMFT to solve their tracking problem.

2.2. Point Cloud Object segmentation

Research towards object segmentation in point clouds is focusing on calculating meta information regarding the points and applying some heuristic function to see if the points could belong in the same segment of the cloud. Trevor et al. [29] take positional information, Euclidean distances and the normal of points to as input to their heuristic and output segments that are part of the same object. PCL library [12] introduces methods like Euclidean clustering and conditional Euclidean clustering that use a number of heuristics that take normal as well as curvature information to extract segments in the point cloud that represent objects. Furthermore, a there is a lot of resarch on segmentation of point clouds in scenes, the emphasis is usually on extracting geometric primitives [30], [31] using cues like normals and curvature. Rabbani et al [23] introduce a new method of object segmentation using KNN as their base algorithm. They also present a very informative literature review along with the strengths and weaknesses of existing methods. Finally Triebel et al. [32] introduce a general clustering framework that does not rely on plane segmentation. Instead of segmenting the plane by using classical approaches like RANSAC or MLASAC they introduce a framework where they make no assumptions regarding plane data.

2.3. Non Parametric Bayesian methods

Bayesian non-parametric methods are the cornerstone of Bayesian statistics. In this project the focus was directed towards the clustering methods that are being introduced by those tools. Radford M. Neal [38] with his paper regarding MCMC methods for Dirichlet process mixture models made the definitive step towards Dirichlet process mixture models(DPMM's) reaching mainstream sucess. Since then, a variety of approaches for inference on such models has been

introduced with Statistical inference and MCMC methods, and Variational inference being two prominent ones. Variational inference for DPMM's was introduced by Jordan et al. [39] and it introduces deterministic tools to perform inference and approximate the posterior distribution and marginals of a dataset. Both methods have strengths and weaknesses and many tools have been established by using the two approaches as their base. Blei et al. [43] introduced LDA as a method to perform topic modelling. Teh et al [41] introduce a hierarchy on the inference process by introducing the Hierarchical Dirichlet process. Particle filter approaches have also been established. Doucet et al. [42] introduce Sequential Monte Carlo as a fast way to approximate inference. Inference on Dirichlet process mixtures is a very active research field and covering it is beyond the scope of this report. In this project SMC samplers where used due to their robustness as well as their inherent extensiveness.

2.4. Correspondence

In its general definition, the correspondence problem refers to the problem of ascertaining which parts of one image correspond to which parts of another image, where differences are due to movement of the camera, the elapse of time, and/or movement of objects in the photos. Under the semantic SLAM context, it refers to the problem of identifying objects as objects that have been encountered before during the mapping process. Towards that direction Cree et al. [34] create a histogram of line segments of each landmark and compute their root mean square error. They then proceed to calculate their RGB signature to calculate the distance between different landmarks. Low et al. [35] match Scale Invariant Feature Transform (SIFT) features, an approach which transforms image data into scale-invariant coordinates relative to local features. Lamon et al [36] store a database of fingerprints which indicate the location in the robot's environment. The features are ordered and stored at a database at as they appear in the robot's immediate surroundings. A new fingerprint is computed for each new view and matched against existing ones. Finally, in Seghal et al. [37] an extension of SIFT descriptors to 3D data and point clouds is given.

The approach presented in this paper takes as input features as the mentioned methods do and is similar to [20] as parts of the point cloud are being clustered a mixture of distributions. The features that are used for the cloud representation are an extension of the features presented in [33] with the addition of extra angular information present in the points of the cloud. Since the operations are now done on cluster level, the distances among clusters can be then represented as distances between distributions and there has been extensive search on that field. Distances like Hellinger, KL divergence, Euclidian, Mahalanobis can all be taken into account when performing the object matching. The robustness of the method can also be increased by using tracking methods like IMFT. The novelty lies in its completely probabilistic mechanism as the clustering is done by using SMC to the augmented feature space. Using distributions as a means of representing objects within the point cloud is a form of compression as objects are represented by a distribution which is smaller in size and easier to maintain and expand. Finally, instead of using heuristics, the distribution correspondence is done through a trained random forest model.

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3. Theory background

Relevant theory will be divided into 2 major sections

- Dependent Dirichlet processes

- SLAM

3.1. Dependent dirichlet process mixture models

//This is draft, I had no time to add theory here. I will update this part later. Dirichlet process priors have been widely used in the literature as non parametric Bayesian tools to estimate the number of clusters in the data [46]. Dependent dirichlet processes extend those priors by allowing the clusters in the data to vary with some covariance over time. Dependent Dirichlet processes(DDP) remove the restriction of exchangeable data and introduce dependencies which can be temporal, positional etc. The DDPs are a natural extension of the DP's in domains where data cannot be considered exchangeable. They where introduced by MacEachern [44] and have been widely used since. The main motivation behind using such methods is the immediate extension they provide to dynamic environments.

A DDP also known as Generalized Polya Urn [47] and has the property of randomly deleting partitions of clusters on every iteration. That way, it can cope with the variance of the data. In the current project, the $n_t h$ datapoint at time t, $x_{t,n}$ has an assignment $c_{t,n}$ at cluster $k \in \{1, 2, ..., K\}$. The size of cluster k at time t is defined as s_t^k. The GPU of this model at time t can now be defined as:

Algorithm 1 GPU

1: **procedure** GPU($pointCloud, t$)
2:     **for** $k = 1, ...K_{t-1,N_{t-1}}$ **do**
3:         Draw $\Delta s_{t-1}^k \sim Binom(s_{t-1,N_{t-1}}^k, \rho)$ ▷ Number of elements to delete
4:         Set $s_{t,0}^k = s_{t-1,N_{t-1}}^k - \Delta s_{t-1}^k$
5:     **end for**
6:     **for** $n = 1, ...N_t$ **do**
7:         Draw $c_{t,n} \sim Cat(\frac{s_{t,n-1}^1}{\alpha + \sum_k s_{t,n-1}^k}, \frac{s_{t,n-1}^{K_{t,n-1}}}{\alpha + \sum_k s_{t,n-1}^k}, \frac{\alpha}{\alpha + \sum_k s_{t,n-1}^k})$
8:         If $c_{t,n} \leq K_{t,n-1}$ $set :$ $s_{t,n}^{c_t,n} = s_{t,n-1}^{c_t,n} + 1, K_{t,n} = K_{t,n-1}$
9:         If $c_{t,n} > K_{t,n-1}$ $set :$ $s_{t,n}^{c_t,n} = 1, K_{t,n} = K_{t,n-1} + 1$
10:     **end for**
11: **end procedure**

Where Cat is a categorical distribution, Bin is the binomial distribution, α is the DP concentration parameter and ρ is the deletion parameter of the GPU. This Generative Polya Urn distribution also has the shorthand notation GPU(α, ρ)

To define our method, we need to explicitly define the input it will receive. Our data points along with their meta-features that were extracted in the first part of the pipeline. Each point x in

(a) General pipeline
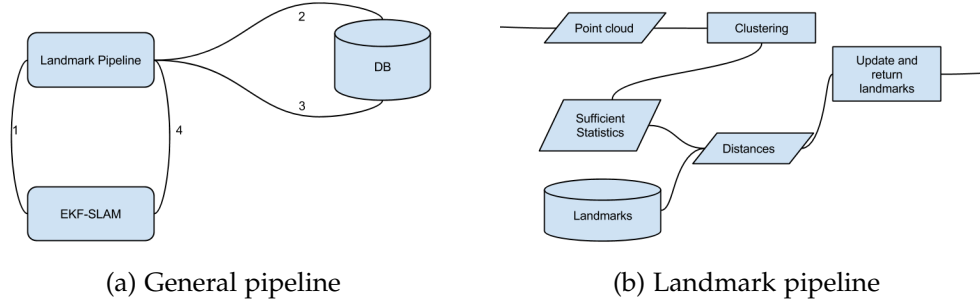
(b) Landmark pipeline

Figure 1: General landmark update pipeline

the input consists of a tuple $x_{t,n} = (x_t^s, x_t^a, x_t^c)$ where superscript s represents spatial information, a angle information, and c colour information. The method those features are extracted is explained in the model definition section of the paper. For the purpose of this project each part of the cloud was represented by vector of length 32.

4. MODEL DEFINITION

A model that takes as input point clouds from a Kinect sensor mounted on a robot and outputs the most probable landmarks given the input and the previous landmarks in now presented. Fig. 1 depicts the general workflow of what happens during the observation step of SLAM. The SLAM node requires landmark information, and the landmark pipeline outputs the most probable landmarks given the current database of landmarks and the current observations. If needed landmarks added to the database and the landmark ids are given to back to the SLAM node.

The model introduces a Pipeline in the layer of landmark detection of the EKF-SLAM algorithm. All the operations from feature extraction to clustering and object matching will be performed at that layer. More specifically the pseudo-code for the method is the following:

This top level description has a lot of implied steps so a line by line description will be provided:

Method input: The method takes as input a point cloud. The post transformation comment has to do with the fact that the cloud expected is the one after all the frame transformations are done in the tf layer of the robot.

Lines 3-4: Feature extraction is done through the pcl [12] library. An initial point cloud reduction is mandatory to increase the speed of the process. A voxel grid is used to reduce the dataset size. A leaf size of 0.04cm produces a good tradeoff between precision and speed. The object representation approach is similar to [17]. Instead of using the CSHOT descriptor, pcl's fpfh [22] is being used. Fast point feature histogram(fpfh) represents an angular signature between a point and its neighbors. In that way we end up with a 23 dimensional angular signature of information between a point and its neighbors. Since the information are given in the form of a histogram, classical statistic solutions regarding the distances between angular signatures can


Algorithm 2 Landmark Layer

1: **procedure** GETLANDMARKIDS(*pointCloud*, *timepoint*, *existingLandmarks*)▷ Post transformation
2:     *initialize*(*landMarkIds*)   ▷ Initialize empty list
3:     *pointCloudReduced* ← *extractMetaFeatures*(*pointCloud*)   ▷ Cloud preprocessing
4:     *features* ← *extractMetaFeatures*(*pointCloudReduced*)
5:     *landmarks* ← *cluster*(*features*)   ▷ Cluster using features
6:     **for** *landmarks* **as** *landmark* **do**
7:         (*probability*, *landId*) ← *getBestLandmarkCorrespondence*(*landmark*, *existingLandmarks*)
8:         **if** *probability* > *threshold* **then**
9:             *addLandmarks*(*landMarkIds*, *landId*)   ▷ Return known landmark
10:         **else**
11:             *newLandID* ← *addLandmarkDB*(*landmarkDB*, *landmark*)   ▷ Add get new id
12:             *addLandmarks*(*newLandID*)   ▷ Add landmark
13:         **end if**
14:     **end for**
15:     **return** *landMarkIds*   ▷ Return added landmark
16: **end procedure**

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be taken into account. In our solution EMD,Hellinger,and KL divergence are being computed in the pipeline. Color information is being encoded with an approach similar to [33]. The colour spectrum is discretized and what is extracted is the count of different colour signatures between a point and its k nearest neighbors. Finally positional information is also given as input to the algorithm. The pipeline is presented in figure Fig. 2. What the algorithm outputs is then a vector of $\mathbf{x} = (x_s, x_c, x_a)$ where s represents a 3x1 vector of space information, c a 27x1 vector of colour information and a angular information whose dimensionality depends on the distances computed(in our case 3x1). It must be noted that pcl offers a multi threading operation on the point feature histogram extraction. This feature is important since it greatly reduces(6-8 times) the speed of an operation applied on every point of the cloud and that makes the histogram extraction significantly faster.

Figure 2: Point cloud modification pipeline.
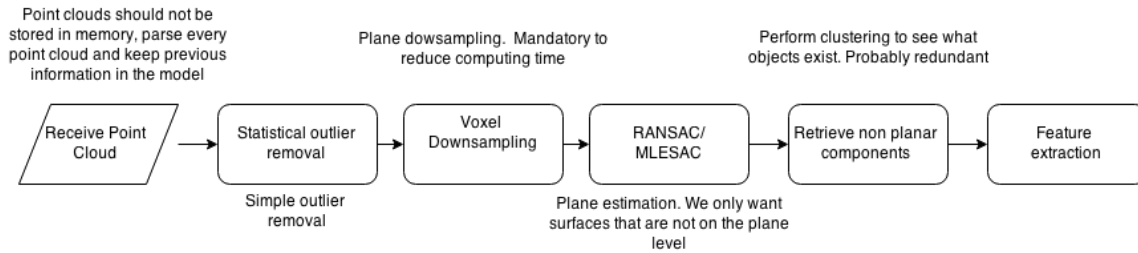
Lines 5: The clustering takes place in this line. The input of the method is the feature

vector for every data point which is calculated in the previous steps. An SMC sampler is used as was presented in the theory section. The data are modeled as following a distribution $G_0(\theta_k) = Normal(x_n^s|\mu, \Sigma) * Mult(x_n^c|\delta) * Exp(x_n^a|\lambda)$ Where Normal is a 3 dimensional Gaussian distribution with mean μ and covariance Σ, Mult is a multinomial with probability vector δ_t and Exp is an exponential with rate λ. The exponential distribution was chosen to model angular information after empiric evaluation showed that it would be a good fit for the angle signature distribution of the data. A typical angle signature distribution is shown in. 3. For this graph data points from various point clouds where taken and passed through the pipeline analysed in lines 3-4. The data were then plotted, and the figure shows what the aggregated angle distribution between neighbor datapoints is. Since there is a clear exponential trend, the exponential distribution was chosen to model it. A gamma distribution is also a nice fit for the data, but due to time constrains, only one modeling distribution was explored.
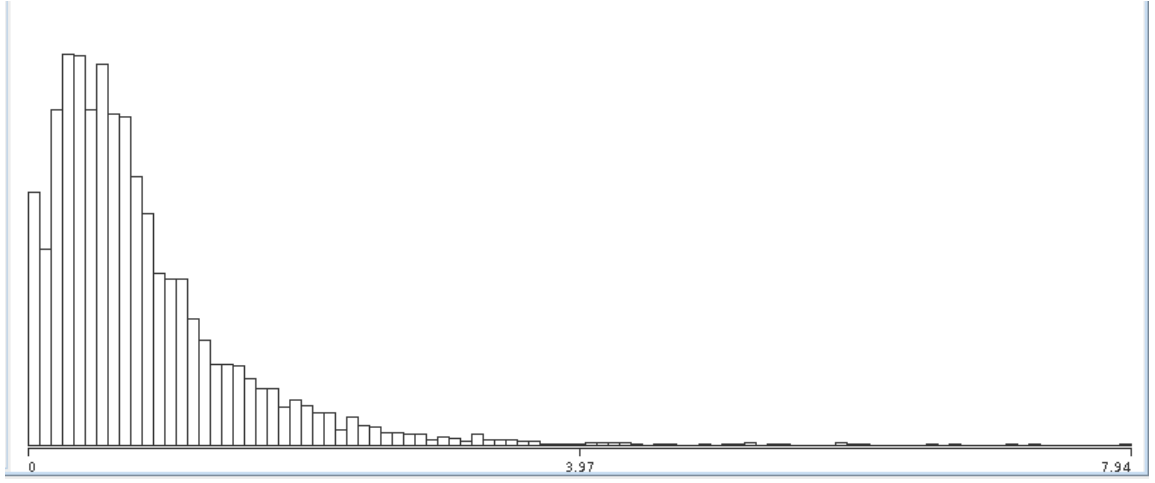

Figure 3: Exponential trend in KL distances.

Lines 6-12: The correspondence of the previous landmarks to current ones happens in theses lines. Since the landmarks are distributions, statistical distances can be taken to perform the matching. The distances are then discretized and are being given as input to the getBestLandmarkCorrespondence. The getBestLandmarkCorrespondence function is a random forest implementation. An offline model has been trained to recognize correlation between those distances and landmark detection. This approach is similar to [20]. It must be noted that the method depends on the training to be general enough so a good initial data set is mandatory. The random forest outputs the probability of a landmark having been encountered before; if the probability is high enough, it is being added to the landmarks list to be send for update in the EKF, otherwise a new landmark is added and its ID is then updated to the list.

Lines 15: The algorithm returns the list of the most probable landmarks the robot encounters in this current time.

The EKF SLAM works with no adjustments made to the package but the landmarks which are now distributions of data.

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5. RESULTS

The results of the pipeline as well as the results of its performance in SLAM methods will be discussed.

The main purpose of the pipeline of Fig. 2 is to decrease the size of a point cloud so that operations on the reduced dataset are feasible. A point cloud instance as taken raw from the kinect sensor approximately 240.000 points and matrix operations at such large matrices are non feasible. The main target of the pipeline is to reduce the size of the data to a more manageable scale. The initial dense point cloud is shown in Fig. 4.
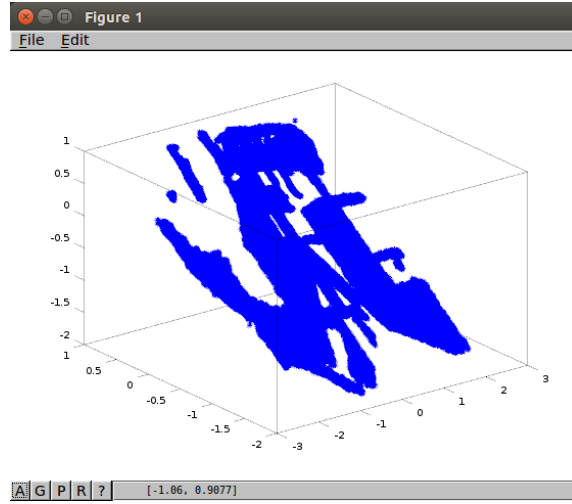

Figure 4: Exponential trend in KL distances.

The cloud is too dense to be correctly displayed in the plot. The planar components of the plane also dominate the cloud and its hard to operate on them. An image with a high amount of planar components is typical when data are acquired from a turtlebot with the camera being situated near the ground. In order to perform the clustering operations, the cloud needs to be downsampled. The process followed is the one described in the method definition and the results are shown in Fig 5. The operation used is a pipeline voxel downsampling, statistical outlier removal and plane estimation via RANSAC is typical in the literature /refobjectDisc.

The cloud is stripped of its planar components with the remaining structure having minimal to no loss of structural information. The cloud is now ready to be used as input for the sampler which will take the features calculated in the pipeline to cluster the cloud into segments of structure. The whole takes a medium amount of time and depending on the parameter tweaking it can

The sampler as was described in the theory section takes as input the modified cloud and outputs clusters of the structure. Its results are shown in figure 6. The environment is captured as a sequence of clusters. It can be seen that the chair that is situated in the center of the cloud has a number of clusters assigned to it. This behavior of the cluster is expected as a lot of point clouds are part of the chair and the horizontal as well and the vertical components have different angular signatures. It is not possible to create a general framework that takes into account all the
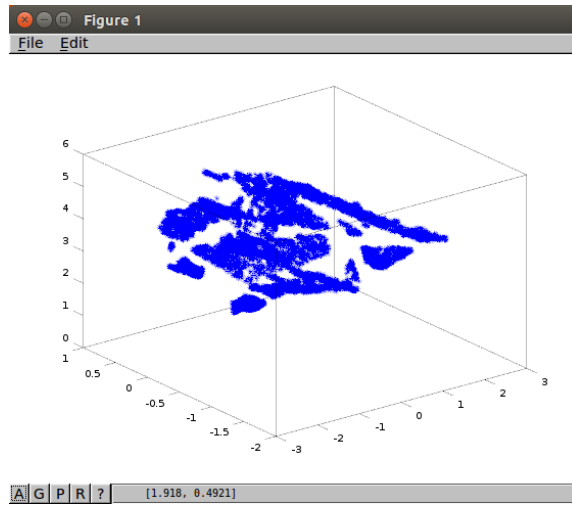
Figure 5: Point cloud post pipeline modifications.

different angle and point signatures between objects. The decision of how the clusters represent a structure should then be taken in a decision layer on top of that cluster. The random forest is build to classify objects by taking as input the output of the sampler.
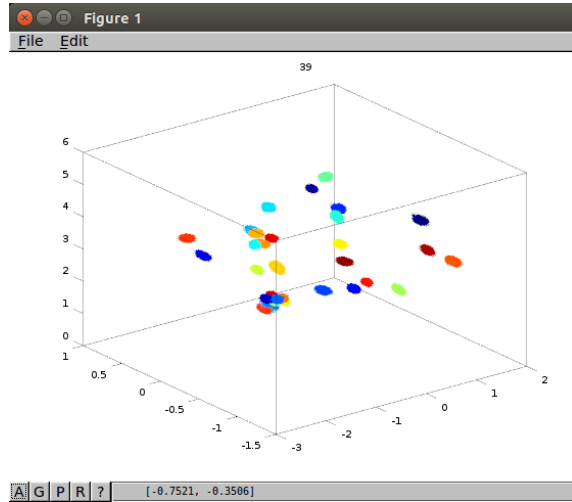

Figure 6: Point cloud post pipeline modifications.

The random forest takes as input the distributions as given by the cluster and outputs the probability that each one represents an element the algorithm has previously already in the database. Only elements past a threshold will be considered as landmarks already encountered and otherwise the new distributions are added to the database. The features taken by the algorithm

are the distances between each distribution and each landmark already stored in the database. More specifically, for the Gaussian parts of the distribution Wasserstein and Kullback Leibler divergence are used to measure the distance between them. For the exponential part, squared Hellinger and Kullback-Leibler being used, and for the categorical EMD, KL divergence and Hellinger distance. All distribution distances are given in the appendix. The final result is a 7 feature vector that will be used to classify if it's a distance signature that classifies a landmark or not. The training set is supplied beforehand to the algorithm. The results of the algorithm are shown in Fig. 7
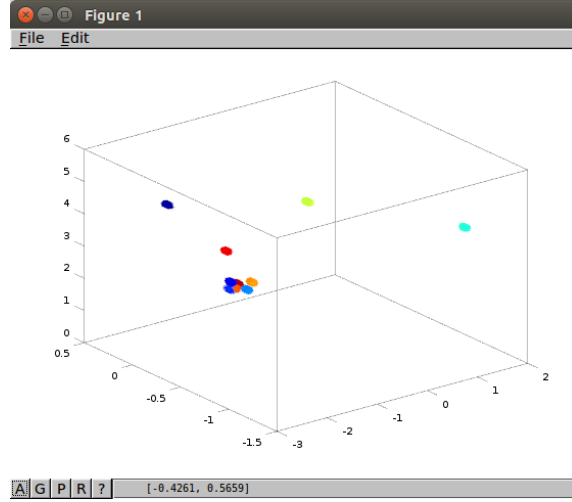

Figure 7: Point cloud post pipeline modifications.

6.   Conclusion and future work

A novel method for SLAM by using compressed representations of objects in a point cloud is introduced. Its strengths and weaknesses are presented. Future work could include:

- Improved tracking by using IMRF

- Extend to dynamic environments

- Extend the representation used

7.   Discussion

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