## **Contents**

1	準備 1.1 1.2	init.el         1           tpl.cpp         1
2	文字 2.1	P列 1 Aho-Corasick 法
3	グラ	
	3.1	<u> </u>
		3.1.1 関節点
		3.1.2 橋
		3.1.3 強連結成分分解
	3.2	70
		3.2.1 最大流
		3.2.2 二部マッチング
		3.2.3 最小費用流
	3.3	最小シュタイナー木

## 1 準備

## 1.1 init.el

linum は emacs24 のみ

```
; key
(keyboard-translate ?\C-h ?\C-?)
(global-set-key "\M-g" 'goto-line)

; tab
(setq-default indent-tabs-mode nil)
(setq-default tab-width 4)
(setq indent-line-function 'insert-tab)
; line number
(global-linum-mode t)
(setq linum-format "%4d ")
```

## 1.2 tpl.cpp

```
#include <bits/stdc++.h>
using namespace std;
#define rep(i,a) for(int i = 0; i < (a); i++)
#define repi(i,a,b) for(int i = (a); i < (b); i++)
#define repd(i,a,b) for(int i = (a); i >= (b); i--)
#define repit(i,a) for(__typeof((a).begin()) i = (a).begin(); i != (a).end(); i++)
#define all(u) (u).begin(),(u).end()
#define rall(u) (u).rbegin(),(u).rend()
#define UNIQUE(u) (u).erase(unique(all(u)),(u).end())
#define pb push_back
#define mp make_pair
const int INF = 1e9;
const double EPS = 1e-8;
const double PI = acos(-1.0);
typedef long long 11;
typedef vector<int> vi;
typedef vector<vi> vvi;
typedef pair<int,int> pii;
int main(){
}
```

# 2 文字列

## 2.1 Aho-Corasick 法

O(N+M)

```
struct PMA{
    PMA* next[256];    //0 is failure link
    vi matched;

PMA(){memset(next, 0, sizeof(next));}

PMA(){rep(i,256) if(next[i]) delete next[i];}

;

vi set_union(const vi &a,const vi &b){
    vi res;
    set_union(all(a), all(b), back_inserter(res));
    return res;
```

```
11 | }
12
    // patternからパターンマッチングオートマトンの生成
13
   PMA *buildPMA(vector<string> pattern){
       PMA *root = new PMA, *now;
14
15
       root->next[0] = root;
       rep(i, patter.size()){
16
            now = root;
17
            rep(j, pattern[i].size()){
18
                if(now->next[(int)pattern[i][j]] == 0)
19
                    now->next[(int)pattern[i][j]] = new PMA;
20
21
                now = now->next[(int)pattern[i][j]];
22
23
            now->matched.push_back(i);
24
25
       queue<PMA*> que;
26
       repi(i,1,256){
27
            if(!root->next[i]) root->next[i] = root;
28
                root->next[i]->next[0] = root;
29
                que.push(root->next[i]);
30
31
32
       while(!que.empty()){
33
            now = que.front(); que.pop();
34
35
            repi(i,1,256){
                if(now->next[i]){
36
37
                    PMA *next = now->next[0];
                    while(!next->next[i]) next = next->next[0];
38
39
                    now->next[i]->next[0] = next->next[i];
40
                    now->next[i]->matched = set_union(now->next[i]->matched, next->next[i]->
                         matched);
41
                    que.push(now->next[i]);
42
43
44
45
       return root;
46
   void match(PMA* &pma, const string s, vi &res){
47
48
       rep(i,s.size()){
49
            int c = s[i]:
50
            while(!pma->next[c])
               pma = pma -> next[0];
51
52
            pma = pma->next[c];
            rep(j,pma->matched.size())
53
                res[pma->matched[j]] = 1;
54
55
56
```

# 3 グラフ

## 3.1 強連結成分分解

#### 3.1.1 関節点

O(E)

ある関節点 u がグラフを k 個に分割するとき art には k-1 個の u が含まれる. 不要な場合は unique を忘れないこと.

```
vi G[MAX], art; // artに関節点のリストが入る
int num[MAX], low[MAX], t, V;

void visit(int v, int u){
    low[v] = num[v] = ++t;
    repit(e,G[v]){
```

```
int w = *e;
            if (num[w] == 0) {
8
                visit(w, v);
9
                low[v] = min(low[v], low[w]);
10
11
                if ((num[v] == 1 && num[w] != 2) ||
                    (num[v] != 1 \&\& low[w] >= num[v])) art.pb(v);
12
13
            else low[v] = min(low[v], num[w]);
14
15
16
   }
   void art_point(){
17
       memset(low, 0, sizeof(low));
       memset(num, 0, sizeof(num));
19
       art.clear();
20
       rep(u, V) if (num[u] == 0) {
21
22
            t = 0;
23
            visit(u, -1);
24
25
26
       sort(all(art));
27
       UNIQUE(art);
        */
28
29
   }
```

#### 3.1.2 橋

O(V + E)

```
vi G[MAX];
   vector<pii> brdg; // brdgに橋のリストが入る
   stack<int> roots, S;
   int num[MAX], inS[MAX], t, V;
   void visit(int v, int u){
       num[v] = ++t;
       S.push(v); inS[v] = 1;
       roots.push(v);
10
       repit(e, G[v]){
11
           int w = *e;
           if(!num[w]) visit(w, v);
12
13
           else if(u != w && inS[w])
                while(num[roots.top()] > num[w])
14
15
                    roots.pop();
17
       if(v == roots.top()){
18
           int tu = u, tv = v;
19
           if(tu > tv) swap(tu, tv);
           brdq.pb(pii(tu, tv));
20
           while(1){
                int w = S.top(); S.pop();
22
                inS[w] = 0;
23
24
                if(v == w) break;
25
26
           roots.pop();
27
       }
   }
28
   void bridge(){
30
       memset(num, 0, sizeof(num));
31
       memset(inS, 0, sizeof(inS));
32
33
       brdq.clear();
       while(S.size()) S.pop():
34
35
       while(roots.size()) roots.pop();
       t = 0:
36
37
       rep(u, V) if(num[u] == 0){
```

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## 3.1.3 強連結成分分解

```
O(V+E)
   vi G[MAX];
   vvi scc; // ここに強連結成分分解の結果が入る
   stack<int> S:
   int inS[MAX], low[MAX], num[MAX], t, V;
   void visit(int v){
       low[v] = num[v] = ++t;
       S.push(v); inS[v] = 1;
       repit(e,G[v]){
           int w = *e;
10
           if(num[w] == 0){
11
12
               visit(w);
13
                low[v] = min(low[v], low[w]);
14
           else if(inS[w]) low[v] = min(low[v], num[w]);
15
16
       if(low[v] == num[v]){
17
18
           scc.pb(vi());
           while(1){
19
               int w = S.top(); S.pop();
20
                inS[w] = 0;
21
                scc.back().pb(w);
22
23
                if(v == w) break;
24
25
26
27
28
   void stronglyCC(){
29
       t = 0;
30
       scc.clear();
       memset(num, 0, sizeof(num));
31
32
       memset(low, 0, sizeof(low));
33
       memset(inS, 0, sizeof(inS));
34
       while(S.size()) S.pop();
35
       rep(u, V) if(num[u] == 0) visit(u);
36
   }
```

## 3.2 フロー

## 3.2.1 最大流

```
struct edge{int to, cap, rev;};
vector<edge> G[MAX];
int level[MAX], itr[MAX];

void add_edge(int from, int to, int cap){
    G[from].push_back((edge){to, cap, int(G[to].size())});
    G[to].push_back((edge){from, 0, int(G[from].size()-1)});
}

void bfs(int s, int t){
    memset(level, -1, sizeof(level));
```

```
12
        queue<int> que; que.push(s);
13
        level[s] = 0;
        while(!que.empty()){
14
            int v = que.front(); que.pop();
15
16
            if(v == t) return;
            for(int i = 0; i < G[v].size(); i++){</pre>
17
                edge &e = G[v][i];
18
                if(e.cap <= 0 or level[e.to] != -1) continue;</pre>
19
20
                que.push(e.to);
                level[e.to] = level[v]+1;
21
22
23
24
25
   int dfs(int v, int t, int f){
26
        if(v == t) return f;
27
28
        for(int &i = itr[v] ; i < G[v].size(); i++){</pre>
29
            edge &e = G[v][i];
            if(level[e.to] <= level[v] or e.cap <= 0) continue;</pre>
30
31
            int d = dfs(e.to, t, min(f, e.cap));
            if(d > 0){
32
                e.cap -= d;
33
                G[e.to][e.rev].cap += d;
34
35
                return d;
36
            }
       }
38
        return 0;
39
   int max_flow(int s, int t){
42
       int flow = 0, f;
43
        while(1){
44
            bfs(s, t);
            if(level[t] == -1) return flow;
45
            memset(itr, 0, sizeof(itr));
            while ((f = dfs(s, t, INF)) > 0) flow += f;
48
   }
```

#### 3.2.2 二部マッチング

O(EV)

```
int V:
   vector<int> G[MAX_V];
   int match[MAX_V];
   bool used[MAX_V];
   void add_edge(int u, int v){
       G[u].push_back(v);
       G[v].push_back(u);
8
9
10
11
   bool dfs(int v){
12
       used[v] = 1:
       rep(i,G[v].size()){
13
14
           int u = G[v][i], w = match[u];
           if(w < 0 || !used[w] && dfs(w)){
15
                match[v] = u;
16
                match[u] = v;
17
18
                return 1;
           }
19
20
       }
       return 0;
21
22
```

```
23
24
   int bi_matching(){
25
       int res = 0:
26
       memset(match, -1, sizeof(match));
       rep(v,V) if(match[v] < 0)
27
            memset(used, 0, sizeof(used));
28
            if(dfs(v)) res++;
29
       }
30
31
       return res;
32
```

## 3.2.3 最小費用流

```
O(FE \log V)
   struct edge{ int to, cap, cost, rev;};
   int V;
   vector<edge> G[MAX_V];
   int h[MAX_V];
   int dist[MAX_V];
   int prevv[MAX_V], preve[MAX_V];
   void add_edge(int from, int to, int cap, int cost){
10
       G[from].push_back((edge){to, cap, cost, int(G[to].size())});
       G[to].push_back((edge){from, 0, -cost, int(G[from].size() - 1)});
11
12
13
   int min_cost_flow(int s, int t, int f){
14
15
       int res = 0;
        fill(h, h + V, 0);
16
17
       while(f > 0){
            priority_queue<pii, vector<pii>, greater<pii> > que;
18
19
            fill(dist, dist + V, inf);
            dist[s] = 0:
20
            que.push(pii(0, s));
21
22
            while(!que.emptv()){
23
                pii p = que.top(); que.pop();
                int v = p.second;
24
                if(dist[v] < p.first) continue;</pre>
25
                rep(i,G[v].size()){
26
                    edge &e = G[v][i]:
27
                    if(e.cap > 0 \& dist[e.to] > dist[v] + e.cost + h[v] - h[e.to]){
28
                        dist[e.to] = dist[v] + e.cost + h[v] - h[e.to];
29
30
                        prevv[e.to] = v;
31
                        preve[e.to] = i:
                        que.push(pii(dist[e.to], e.to));
32
33
                }
34
35
            if(dist[t] == inf) return -1:
36
            rep(v,V) h[v] += dist[v];
37
38
            int d = f:
39
            for(int v = t; v != s; v = prevv[v])
                d = min(d, G[prevv[v]][preve[v]].cap);
40
            f -= d:
41
            res += d * h[t];
42
            for(int v = t; v != s; v = prevv[v]){
43
                edge &e = G[prevv[v]][preve[v]];
44
                e.cap -= d;
45
                G[v][e.rev].cap += d;
46
47
48
       return res;
49
50
```

## 3.3 最小シュタイナー木

 $O(4^{|T|}V)$ g は無向グラフの隣接行列. T は使いたい頂点の集合.

```
int minimum_steiner_tree(vi &T, vvi &g){
       int n = g.size(), t = T.size();
       if(t <= 1) return 0;
       vvi d(g); // all-pair shortest
       rep(k,n)rep(i,n)rep(j,n) //Warshall Floyd
            d[i][j] = min(d[i][j], d[i][k] + d[k][j]);
       int opt[1 << t][n];</pre>
       rep(S,1 << t) rep(x,n)
            opt[S][x] = INF;
10
11
12
        rep(p,t) rep(q,n) // trivial case
13
            opt[1 << p][q] = d[T[p]][q];
14
15
       repi(S,1,1<<t){ // DP step
            if(!(S & (S-1))) continue;
17
            rep(p,n) rep(E,S)
18
                if((E \mid S) == S)
                    opt[S][p] = min(opt[S][p], opt[E][p] + opt[S-E][p]);
19
20
            rep(p,n) rep(q,n)
21
                opt[S][p] = min(opt[S][p], opt[S][q] + d[p][q]);
22
23
       int ans = INF;
24
25
       rep(S,1 << t) rep(q,n)
            ans = min(ans, opt[S][q] + opt[((1<<t)-1)-S][q]);
26
27
28
```

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