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1 準備

1.1 init.el

linum は emacs24 のみ

```
; key
(keyboard-translate ?\C-h ?\C-?)
(global-set-key "\M-g" 'goto-line)

; tab
(setq-default indent-tabs-mode nil)
(setq-default tab-width 4)
(setq indent-line-function 'insert-tab)
; line number
(global-linum-mode t)
(setq linum-format "%4d ")
```

1.2 tpl.cpp

```
#include <bits/stdc++.h>
   using namespace std;
   #define rep(i,a) for(int i = 0; i < (a); i++)
   #define repi(i,a,b) for(int i = (a); i < (b); i++)
   #define repd(i,a,b) for(int i = (a); i >= (b); i--)
   #define repit(i,a) for(__typeof((a).begin()) i = (a).begin(); i != (a).end(); i++)
   #define all(u) (u).begin(),(u).end()
   #define rall(u) (u).rbegin(),(u).rend()
   #define UNIQUE(u) (u).erase(unique(all(u)),(u).end())
   #define pb push_back
   #define mp make_pair
   const int INF = 1e9;
   const double EPS = 1e-8:
   const double PI = acos(-1.0);
   typedef long long 11;
   typedef vector<int> vi;
   typedef vector<vi> vvi;
   typedef pair<int,int> pii;
22
   int main(){
23
   }
```

2 文字列

2.1 Aho-Corasick 法

O(N+M)

```
struct PMA{
    PMA* next[256];    //0 is failure link
    vi matched;

PMA(){memset(next, 0, sizeof(next));}

PMA(){rep(i,256) if(next[i]) delete next[i];}

;

vi set_union(const vi &a,const vi &b){
    vi res;
```

```
set_union(all(a), all(b), back_inserter(res));
       return res;
10
11
   }
   // patternからパターンマッチングオートマトンの生成
12
   PMA *buildPMA(vector<string> pattern){
13
       PMA *root = new PMA, *now;
14
       root->next[0] = root;
15
       rep(i, patter.size()){
16
17
            now = root;
            rep(j, pattern[i].size()){
18
                if(now->next[(int)pattern[i][j]] == 0)
19
                    now->next[(int)pattern[i][j]] = new PMA;
20
                now = now->next[(int)pattern[i][j]];
21
22
            now->matched.push_back(i);
23
24
25
       queue < PMA*> que;
26
       repi(i,1,256){
            if(!root->next[i]) root->next[i] = root;
27
28
                root->next[i]->next[0] = root;
29
                que.push(root->next[i]);
30
31
32
33
       while(!que.empty()){
            now = que.front(); que.pop();
34
35
            repi(i,1,256){
                if(now->next[i]){
36
37
                    PMA *next = now->next[0];
38
                    while(!next->next[i]) next = next->next[0];
39
                    now->next[i]->next[0] = next->next[i];
40
                    now->next[i]->matched = set_union(now->next[i]->matched, next->next[i]->
                         matched):
41
                    que.push(now->next[i]);
42
43
44
       return root;
45
46
47
   void match(PMA* &pma, const string s, vi &res){
48
       rep(i,s.size()){
            int c = s[i]:
49
50
            while(!pma->next[c])
               pma = pma -> next[0]:
51
            pma = pma->next[c];
52
53
            rep(j,pma->matched.size())
                res[pma->matched[i]] = 1;
54
55
56
   }
```

グラフ

3.1 強連結成分分解

3.1.1 関節点

O(E)

ある関節点 u がグラフを k 個に分割するとき art には k-1 個の u が含まれる. 不要な場合は unique を忘れないこと.

```
ı vi G[MAX], art; // artに関節点のリストが入る
1 int num[MAX], low[MAX], t, V;
3
```

```
4 | void visit(int v, int u){
        low[v] = num[v] = ++t;
        repit(e,G[v]){
6
            int w = *e;
7
            if (num[w] == 0) {
8
                visit(w, v);
9
10
                low[v] = min(low[v], low[w]);
                if ((num[v] == 1 && num[w] != 2) ||
11
12
                    (num[v] != 1 \&\& low[w] >= num[v])) art.pb(v);
13
14
            else low[v] = min(low[v], num[w]);
15
16
   }
17
   void art_point(){
        memset(low, 0, sizeof(low));
18
        memset(num, 0, sizeof(num));
19
20
        art.clear();
        rep(u,V) if (num[u] == 0) {
21
22
            t = 0:
23
            visit(u, -1);
24
25
26
        sort(all(art));
27
        UNIQUE(art);
28
        */
29
   }
```

3.1.2 橋

```
O(V+E)
   vi G[MAX];
   vector<pii> brdg; // brdgに橋のリストが入る
   stack<int> roots, S;
   int num[MAX], inS[MAX], t, V;
   void visit(int v, int u){
       num[v] = ++t;
        S.push(v); inS[v] = 1;
        roots.push(v);
10
        repit(e, G[v]){
11
            int w = *e;
12
            if(!num[w]) visit(w, v);
13
            else if(u != w && inS[w])
14
                while(num[roots.top()] > num[w])
15
                    roots.pop();
16
        if(v == roots.top()){
17
            int tu = u, tv = v;
18
19
            if(tu > tv) swap(tu, tv);
            brdg.pb(pii(tu, tv));
20
21
            while(1){
                int w = S.top(); S.pop();
22
23
                inS[w] = 0;
24
                if(v == w) break:
25
            roots.pop();
27
   }
28
   void bridge(){
30
        memset(num. 0. sizeof(num)):
31
32
        memset(inS, 0, sizeof(inS));
        brdq.clear();
33
34
        while(S.size()) S.pop();
```

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3.1.3 強連結成分分解

```
O(V+E)
   vi G[MAX];
   vvi scc: // ここに強連結成分分解の結果が入る
   stack<int> S;
   int inS[MAX], low[MAX], num[MAX], t, V;
   void visit(int v){
       low[v] = num[v] = ++t;
       S.push(v); inS[v] = 1;
       repit(e,G[v]){
10
           int w = *e;
           if(num[w] == 0){
11
12
               visit(w):
13
               low[v] = min(low[v], low[w]);
14
15
            else if(inS[w]) low[v] = min(low[v], num[w]);
16
17
       if(low[v] == num[v]){
           scc.pb(vi());
18
           while(1){
19
20
               int w = S.top(); S.pop();
               inS[w] = 0;
21
               scc.back().pb(w);
22
               if(v == w) break;
23
24
25
26
27
   void stronglyCC(){
28
       t = 0;
29
       scc.clear();
30
       memset(num, 0, sizeof(num));
31
       memset(low, 0, sizeof(low));
32
33
       memset(inS, 0, sizeof(inS));
       while(S.size()) S.pop();
34
35
       rep(u,V) if(num[u] == 0) visit(u);
36
```

3.2 フロー

3.2.1 最大流

```
o(EV<sup>2</sup>)

struct edge{int to, cap, rev;};

vector<edge> G[MAX];

int level[MAX], itr[MAX];

void add_edge(int from, int to, int cap){
    G[from].push_back((edge){to, cap, int(G[to].size())});
    G[to].push_back((edge){from, 0, int(G[from].size()-1)});
```

```
8 | }
   void bfs(int s, int t){
10
        memset(level, -1, sizeof(level));
11
12
        queue < int > que; que.push(s);
13
        level[s] = 0;
14
        while(!que.empty()){
            int v = que.front(); que.pop();
15
16
            if(v == t) return;
            for(int i = 0; i < G[v].size(); i++){</pre>
17
18
                 edge &e = G[v][i];
19
                 if(e.cap <= 0 or level[e.to] != -1) continue;</pre>
                 que.push(e.to);
20
21
                 level[e.to] = level[v]+1;
22
23
24
25
    int dfs(int v, int t, int f){
26
        if(v == t) return f;
27
        for(int &i = itr[v] ; i < G[v].size(); i++){</pre>
28
29
            edge &e = G[v][i];
            if(level[e.to] <= level[v] or e.cap <= 0) continue;</pre>
30
31
            int d = dfs(e.to, t, min(f, e.cap));
32
            if(d > 0){
33
                 e.cap -= d;
34
                 G[e.to][e.rev].cap += d;
35
                 return d;
36
37
        }
38
        return 0;
39
    int max_flow(int s, int t){
42
        int flow = 0, f;
43
        while(1){
44
            bfs(s, t);
            if(level[t] == -1) return flow;
45
46
            memset(itr, 0, sizeof(itr));
47
            while((f = dfs(s, t, INF)) > 0) flow += f;
48
49
```

3.2.2 二部マッチング

O(EV)

```
vector<int> G[MAX_V];
   int match[MAX_V];
   bool used[MAX_V];
   void add_edge(int u, int v){
        G[u].push_back(v);
        G[v].push_back(u);
10
   bool dfs(int v){
11
12
        used[v] = 1;
13
        rep(i,G[v].size()){
14
            int u = G[v][i], w = match[u];
            if(w < 0 || !used[w] && dfs(w)){</pre>
15
16
                match[v] = u;
17
                match[u] = v;
18
                return 1;
```

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```
19
20
21
        return 0:
22
23
   int bi_matching(){
24
25
       int res = 0;
26
        memset(match, -1, sizeof(match));
27
        rep(v,V) if(match[v] < 0)
            memset(used, 0, sizeof(used));
28
29
            if(dfs(v)) res++;
30
31
        return res;
32
   }
```

3.2.3 最小費用流

$O(FE \log V)$

```
struct edge{ int to, cap, cost, rev;};
2
3
   int V;
   vector<edge> G[MAX_V];
   int h[MAX_V];
   int dist[MAX_V];
   int prevv[MAX_V], preve[MAX_V];
   void add_edge(int from, int to, int cap, int cost){
       G[from].push_back((edge){to, cap, cost, int(G[to].size())});
10
       G[to].push_back((edge){from, 0, -cost, int(G[from].size() - 1)});
11
12
13
14
   int min_cost_flow(int s, int t, int f){
       int res = 0;
15
       fill(h, h + V, 0);
16
17
       while(f > 0){
            priority_queue<pii, vector<pii>, greater<pii> > que;
18
19
            fill(dist, dist + V, inf);
20
            dist[s] = 0;
21
            que.push(pii(0, s));
22
            while(!que.empty()){
23
                pii p = que.top(); que.pop();
24
                int v = p.second;
25
                if(dist[v] < p.first) continue;</pre>
26
                rep(i,G[v].size()){
                    edge &e = G[v][i];
28
                    if(e.cap > 0 \& dist[e.to] > dist[v] + e.cost + h[v] - h[e.to]){
                        dist[e.to] = dist[v] + e.cost + h[v] - h[e.to];
29
                        prevv[e.to] = v;
                        preve[e.to] = i;
31
                        que.push(pii(dist[e.to], e.to));
32
33
                    }
               }
34
35
36
            if(dist[t] == inf) return -1:
            rep(v,V) h[v] += dist[v];
37
38
            int d = f:
            for(int v = t; v != s; v = prevv[v])
39
40
                d = min(d, G[prevv[v]][preve[v]].cap);
41
            f -= d:
            res += d * h[t];
42
            for(int v = t: v != s: v = prevv[v]){
43
44
                edge &e = G[prevv[v]][preve[v]];
45
                e.cap -= d;
                G[v][e.rev].cap += d;
```

3.3 木

3.3.1 木の直径

ある点(どこでもよい)から一番遠い点 a を求める. 点 a から一番遠い点までの距離がその木の直径になる.

3.3.2 最小シュタイナー木

 $O(4^{|T|}V)$

g は無向グラフの隣接行列. T は使いたい頂点の集合.

```
int minimum_steiner_tree(vi &T, vvi &g){
        int n = g.size(), t = T.size();
        if(t <= 1) return 0;
        vvi d(g); // all-pair shortest
        rep(k,n)rep(i,n)rep(j,n) //Warshall Floyd
            d[i][j] = min(d[i][j], d[i][k] + d[k][j]);
        int opt[1 << t][n];</pre>
        rep(S,1<<t) rep(x,n)
10
            opt[S][x] = INF;
11
12
        rep(p,t) rep(q,n) // trivial case
13
            opt[1 << p][q] = d[T[p]][q];
14
15
        repi(S,1,1<<t){ // DP step
            if(!(S & (S-1))) continue;
16
            rep(p,n) rep(E,S)
17
18
                if((E \mid S) == S)
19
                    opt[S][p] = min(opt[S][p], opt[E][p] + opt[S-E][p]);
20
            rep(p,n) rep(q,n)
21
                opt[S][p] = min(opt[S][p], opt[S][q] + d[p][q]);
22
23
24
        int ans = INF;
        rep(S,1 << t) rep(q,n)
25
            ans = min(ans, opt[S][q] + opt[((1 << t) - 1) - S][q]);
26
27
        return ans;
28
```

4 数学

4.1 行列

C++11 だと array という名前では衝突するので arr にしている.

```
typedef double number;
typedef vector<number> arr;
typedef vector<arr> mat;
```

4.1.1 单位行列

```
O(N)

mat identity(int n) {
    mat A(n, arr(n));
    rep(i,n) A[i][i] = 1;
    return A;
}
```

4.1.2 積

arr*arr	mat*arr	mat*mat
O(N)	$O(N^2)$	$O(N^3)$

```
number inner_product(const arr &a, const arr &b) {
       number ans = 0;
       rep(i,a.size()) ans += a[i] * b[i];
       return ans;
   arr mul(const mat &A, const arr &x) {
       arr y(A.size());
       rep(i,A.size()) rep(j,A[0].size())
10
           y[i] = A[i][j] * x[j];
       return y;
11
12
13
   mat mul(mat &A, mat &B) {
14
       mat C(A.size(), arr(B[0].size()));
15
       rep(i,C.size()) rep(j,C[i].size()) rep(k,A[i].size())
16
17
           C[i][j] += A[i][k] * B[k][j];
18
       return C;
   }
19
```

4.1.3 累乗

 $O(N^3 \log e)$ 単位行列と積 (mat*mat) が必要.

```
mat pow(mat &A, int e) {
    return e == 0 ? identity(A.size()) :
    e % 2 == 0 ? pow(mul(A, A), e/2) : mul(A, pow(A, e-1));
}
mat pow(mat &A, int e) {
    return e == 0 ? identity(A.size()) :
    e % 2 == 0 ? pow(mul(A, A), e/2) : mul(A, pow(A, e-1));
}
```

4.1.4 線形方程式の解 (Givens 消去法)

 $O(N^3)$

```
#define mkrot(x,y,c,s) {double r = sqrt(x*x+y*y); c = x/r; s = y/r;}
#define rot(x,y,c,s) {double u = c*x+s*y; double v = -s*x+c*y; x = u; y = v;}
arr givens(mat A, arr b){
   int n = b.size();
   rep(i,n) repi(j,i+1,n){
        double c, s;
```

```
mkrot(A[i][i], A[j][i], c, s);
            rot(b[i], b[j], c, s);
            repi(k,i,n) rot(A[i][k],A[j][k],c,s);
9
10
11
       repd(i,n-1,0){
12
            repi(j,i+1,n)
13
               b[i] -= A[i][j] * b[j];
14
           b[i] /= A[i][i];
15
       }
        return b;
16
17
```

4.1.5 トレース

O(N)

```
number trace(const mat &A) {
    number ans = 0;
    rep(i,A.size()) ans += A[i][i];
    return ans;
}
```

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