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1 準備

1.1 init.el

linum は emacs24 のみ

```
1 ;key
2 (keyboard-translate ?\C-h ?\C-?)
3 (global-set-key "\M-g" 'goto-line)
4
5 ;tab
6 (setq-default indent-tabs-mode nil)
7 (setq-default tab-width 4)
8 (setq indent-line-function 'insert-tab)
9
10 ;line number
11 (global-linum-mode t)
12 (setq linum-format "%4d ")
```

1.2 tpl.cpp

```
1 #include <bits/stdc++.h>
2 using namespace std;
3
4 #define rep(i,a) for(int i = 0; i < (a); i++)
5 #define repi(i,a,b) for(int i = (a); i < (b); i++)
6 #define repd(i,a,b) for(int i = (a); i >= (b); i--)
7 #define repit(i,a) for(__typeof((a).begin()) i = (a).begin(); i != (a).end(); i++)
8 #define all(u) (u).begin(),(u).end()
9 #define rall(u) (u).rbegin(),(u).rend()
10 #define UNIQUE(u) (u).erase(unique(all(u)),(u).end())
11 #define pb push_back
12 #define mp make_pair
13 const int INF = 1e9;
14 const double EPS = 1e-8;
15 const double PI = acos(-1.0);
16
17 typedef long long ll;
18 typedef vector<int> vi;
19 typedef vector<vi> vvi;
20 typedef pair<int,int> pii;
21
22 int main(){
23 }
```

2 文字列

2.1 Aho-Corasick 法

$O(N + M)$

```
1 struct PMA{
2     PMA* next[256];    //0 is failure link
3     vi matched;
4     PMA(){memset(next, 0, sizeof(next));}
5     ~PMA(){rep(i,256) if(next[i]) delete next[i];}
6 };
7 vi set_union(const vi &a,const vi &b){
8     vi res;
9     set_union(all(a), all(b), back_inserter(res));
```

```

10     return res;
11 }
12 // patternからパターンマッチングオートマトンの生成
13 PMA *buildPMA(vector<string> pattern){
14     PMA *root = new PMA, *now;
15     root->next[0] = root;
16     rep(i, patter.size()){
17         now = root;
18         rep(j, pattern[i].size()){
19             if(now->next[(int)pattern[i][j]] == 0)
20                 now->next[(int)pattern[i][j]] = new PMA;
21             now = now->next[(int)pattern[i][j]];
22         }
23         now->matched.push_back(i);
24     }
25     queue<PMA*> que;
26     repi(i,1,256){
27         if(!root->next[i]) root->next[i] = root;
28         else {
29             root->next[i]->next[0] = root;
30             que.push(root->next[i]);
31         }
32     }
33     while(!que.empty()){
34         now = que.front(); que.pop();
35         repi(i,1,256){
36             if(now->next[i]){
37                 PMA *next = now->next[i];
38                 while(!next->next[i]) next = next->next[0];
39                 now->next[i]->next[0] = next->next[i];
40                 now->next[i]->matched = set_union(now->next[i]->matched, next->next[i]->
41                     matched);
42                 que.push(now->next[i]);
43             }
44         }
45     }
46     return root;
47 }
48 void match(PMA* &pma, const string s, vi &res){
49     rep(i,s.size()){
50         int c = s[i];
51         while(!pma->next[c])
52             pma = pma->next[0];
53         pma = pma->next[c];
54         rep(j,pma->matched.size())
55             res[pma->matched[j]] = 1;
56     }
57 }

```

3 グラフ

3.1 関節点

$O(E)$

ある関節点 u がグラフを k 個に分割するとき art には $k-1$ 個の u が含まれる. 不要な場合は `unique` を忘れないこと.

```

1 vi G[MAX], art; // artに関節点のリストが入る
2 int num[MAX], low[MAX], t, V;
3
4 void visit(int v, int u){
5     low[v] = num[v] = ++t;

```

```

6     repit(e,G[v]){
7         int w = *e;
8         if (num[w] == 0) {
9             visit(w, v);
10            low[v] = min(low[v], low[w]);
11            if ((num[v] == 1 && num[w] != 2) ||
12                (num[v] != 1 && low[w] >= num[v])) art.pb(v);
13        }
14        else low[v] = min(low[v], num[w]);
15    }
16 }
17 void art_point(){
18     memset(low, 0, sizeof(low));
19     memset(num, 0, sizeof(num));
20     art.clear();
21     rep(u,V) if (num[u] == 0) {
22         t = 0;
23         visit(u, -1);
24     }
25     /*
26     sort(all(art));
27     UNIQUE(art);
28     */
29 }

```

3.2 橋

$O(V + E)$

```

1 vi G[MAX];
2 vector<pii> brdg; // brdgに橋のリストが入る
3 stack<int> roots, S;
4 int num[MAX], inS[MAX], t, V;
5
6 void visit(int v, int u){
7     num[v] = ++t;
8     S.push(v); inS[v] = 1;
9     roots.push(v);
10    repit(e, G[v]){
11        int w = *e;
12        if(!num[w]) visit(w, v);
13        else if(u != w && inS[w])
14            while(num[roots.top()] > num[w])
15                roots.pop();
16    }
17    if(v == roots.top()){
18        int tu = u, tv = v;
19        if(tu > tv) swap(tu, tv);
20        brdg.pb(pii(tu, tv));
21        while(1){
22            int w = S.top(); S.pop();
23            inS[w] = 0;
24            if(v == w) break;
25        }
26        roots.pop();
27    }
28 }
29
30 void bridge(){
31     memset(num, 0, sizeof(num));
32     memset(inS, 0, sizeof(inS));
33     brdg.clear();
34     while(S.size()) S.pop();
35     while(roots.size()) roots.pop();
36     t = 0;
37     rep(u,V) if(num[u] == 0){

```

```

38     visit(u,V);
39     brdg.pop_back();
40 }
41 }

```

3.3 強連結成分分解

$O(V + E)$

```

1  vi G[MAX];
2  vvi scc; // ここに強連結成分分解の結果が入る
3  stack<int> S;
4  int inS[MAX], low[MAX], num[MAX], t, V;
5
6  void visit(int v){
7      low[v] = num[v] = ++t;
8      S.push(v); inS[v] = 1;
9      repit(e,G[v]){
10         int w = *e;
11         if(num[w] == 0){
12             visit(w);
13             low[v] = min(low[v], low[w]);
14         }
15         else if(inS[w]) low[v] = min(low[v], num[w]);
16     }
17     if(low[v] == num[v]){
18         scc.pb(vi());
19         while(1){
20             int w = S.top(); S.pop();
21             inS[w] = 0;
22             scc.back().pb(w);
23             if(v == w) break;
24         }
25     }
26 }
27
28 void stronglyCC(){
29     t = 0;
30     scc.clear();
31     memset(num, 0, sizeof(num));
32     memset(low, 0, sizeof(low));
33     memset(inS, 0, sizeof(inS));
34     while(S.size()) S.pop();
35     rep(u,V) if(num[u] == 0) visit(u);
36 }

```

3.4 最大流

$O(EV^2)$

```

1  struct edge{int to, cap, rev;};
2  vector<edge> G[MAX];
3  int level[MAX], itr[MAX];
4
5  void add_edge(int from, int to, int cap){
6      G[from].push_back((edge){to, cap, int(G[to].size())});
7      G[to].push_back((edge){from, 0, int(G[from].size()-1)});
8  }
9
10 void bfs(int s, int t){
11     memset(level, -1, sizeof(level));
12     queue<int> que; que.push(s);
13     level[s] = 0;
14     while(!que.empty()){
15         int v = que.front(); que.pop();

```

```

16         if(v == t) return;
17         for(int i = 0; i < G[v].size(); i++){
18             edge &e = G[v][i];
19             if(e.cap <= 0 or level[e.to] != -1) continue;
20             que.push(e.to);
21             level[e.to] = level[v]+1;
22         }
23     }
24 }
25
26 int dfs(int v, int t, int f){
27     if(v == t) return f;
28     for(int &i = itr[v]; i < G[v].size(); i++){
29         edge &e = G[v][i];
30         if(level[e.to] <= level[v] or e.cap <= 0) continue;
31         int d = dfs(e.to, t, min(f, e.cap));
32         if(d > 0){
33             e.cap -= d;
34             G[e.to][e.rev].cap += d;
35             return d;
36         }
37     }
38     return 0;
39 }
40
41 int max_flow(int s, int t){
42     int flow = 0, f;
43     while(1){
44         bfs(s, t);
45         if(level[t] == -1) return flow;
46         memset(itr, 0, sizeof(itr));
47         while((f = dfs(s, t, INF)) > 0) flow += f;
48     }
49 }

```

3.5 二部マッチング

$O(EV)$

```

1  int V;
2  vector<int> G[MAX_V];
3  int match[MAX_V];
4  bool used[MAX_V];
5
6  void add_edge(int u, int v){
7      G[u].push_back(v);
8      G[v].push_back(u);
9  }
10
11 bool dfs(int v){
12     used[v] = 1;
13     rep(i,G[v].size()){
14         int u = G[v][i], w = match[u];
15         if(w < 0 || !used[w] && dfs(w)){
16             match[v] = u;
17             match[u] = v;
18             return 1;
19         }
20     }
21     return 0;
22 }
23
24 int bi_matching(){
25     int res = 0;
26     memset(match, -1, sizeof(match));
27     rep(v,V) if(match[v] < 0){

```

```

28     memset(used, 0, sizeof(used));
29     if(dfs(v)) res++;
30 }
31 return res;
32 }

```

3.6 最小費用流

$O(FE \log V)$

```

1 struct edge{ int to, cap, cost, rev;};
2
3 int V;
4 vector<edge> G[MAX_V];
5 int h[MAX_V];
6 int dist[MAX_V];
7 int prevv[MAX_V], preve[MAX_V];
8
9 void add_edge(int from, int to, int cap, int cost){
10     G[from].push_back((edge){to, cap, cost, int(G[to].size())});
11     G[to].push_back((edge){from, 0, -cost, int(G[from].size() - 1)});
12 }
13
14 int min_cost_flow(int s, int t, int f){
15     int res = 0;
16     fill(h, h + V, 0);
17     while(f > 0){
18         priority_queue<pii, vector<pii>, greater<pii> > que;
19         fill(dist, dist + V, inf);
20         dist[s] = 0;
21         que.push(pii(0, s));
22         while(!que.empty()){
23             pii p = que.top(); que.pop();
24             int v = p.second;
25             if(dist[v] < p.first) continue;
26             rep(i, G[v].size()){
27                 edge &e = G[v][i];
28                 if(e.cap > 0 && dist[e.to] > dist[v] + e.cost + h[v] - h[e.to]){
29                     dist[e.to] = dist[v] + e.cost + h[v] - h[e.to];
30                     prevv[e.to] = v;
31                     preve[e.to] = i;
32                     que.push(pii(dist[e.to], e.to));
33                 }
34             }
35         }
36         if(dist[t] == inf) return -1;
37         rep(v, V) h[v] += dist[v];
38         int d = f;
39         for(int v = t; v != s; v = prevv[v])
40             d = min(d, G[prevv[v]][preve[v]].cap);
41         f -= d;
42         res += d * h[t];
43         for(int v = t; v != s; v = prevv[v]){
44             edge &e = G[prevv[v]][preve[v]];
45             e.cap -= d;
46             G[v][e.rev].cap += d;
47         }
48     }
49     return res;
50 }

```

3.7 最小シュタイナー木

$O(4^{|T|}V)$

g は無向グラフの隣接行列. T は使いたい頂点の集合.

```

1 int minimum_steiner_tree(vi &T, vvi &g){
2     int n = g.size(), t = T.size();
3     if(t <= 1) return 0;
4     vvi d(g); // all-pair shortest
5     rep(k,n)rep(i,n)rep(j,n) //Warshall Floyd
6         d[i][j] = min(d[i][j], d[i][k] + d[k][j]);
7
8     int opt[1 << t][n];
9     rep(S, 1<<t) rep(x,n)
10         opt[S][x] = INF;
11
12     rep(p,t) rep(q,n) // trivial case
13         opt[1 << p][q] = d[T[p]][q];
14
15     repi(S, 1, 1<<t){ // DP step
16         if(!(S & (S-1))) continue;
17         rep(p,n) rep(E,S)
18             if((E | S) == S)
19                 opt[S][p] = min(opt[S][p], opt[E][p] + opt[S-E][p]);
20         rep(p,n) rep(q,n)
21             opt[S][p] = min(opt[S][p], opt[S][q] + d[p][q]);
22     }
23
24     int ans = INF;
25     rep(S, 1<<t) rep(q,n)
26         ans = min(ans, opt[S][q] + opt[(((1<<t)-1)-S)][q]);
27     return ans;
28 }

```