Contents

			4.2.3 積 (FMT)	13
1	準備	2	4.2.4 逆元 (FMT)	13
	1.1 Caps Lock を Control に変更	2	4.2.5 平方根 (FMT)	
	1.2 init.el	2	4.3 行列	
	1.3 tpl.cpp	2	4.3.1 線形方程式の解 (Givens 消去法)	
	1.4 get input	2	4.4 割り当て問題	
	1.5 alias	2	4.4.1 ハンガリアン法 1	
	1.5 dias	2	4.4.1 ハフカリアン法	:4
2	文字列	2	5 幾何	11
	2.1 マッチング	2	5.1 点	1.4
	2.1.1 複数文字列マッチング (Aho-Corasick 法)	2		
		2		
	2.2 Suffix Array	2		
	2.3 回文長 (Manacher)	3	27077	
2	グラフ	2		
		3		16
	3.1 強連結成分分解	3	5.4.3 点-多角形包含判定 1	16
	3.1.1 関節点	3	5.4.4 凸多角形の共通部分	16
	3.1.2 橋	4	5.4.5 凸多角形の直径 1	17
	3.1.3 強連結成分分解	4	5.4.6 ドロネー三角形分割 (逐次添加法)	17
	3.1.4 無向中国人郵便配達問題	5		
	3.1.5 全点対間最短路 (Johnson)	5	6 データ構造 1	17
	3.1.6 無向グラフの全域最小カット	5	6.1 Union-Find 木	17
	3.2 7 🗆 –	5	6.2 Meldable Heap	18
	3.2.1 最大流	5	6.3 Binary-Indexed-Tree	18
	3.2.2 二部マッチング	6	6.4 Segment Tree	18
	3.2.3 最小費用流	6		12
	3.2.4 Gomory-Hu 木	7	•	
	3.3 木	7		
		7		
	3.3.1 木の直径	7	22-7/10-11-11-11-11-11-11-11-11-11-11-11-11-1	- /
	3.3.2 最小全域木	/		
	3.3.3 最小全域有向木	8	=	
	3.3.4 最小シュタイナー木	8	ALL SOURCE CONTRACTOR	
	3.3.5 木の同型性判定	8	6.10.2 wavelet 行列	14 14 14 15 15 16 16 16 16 17 17 17 17 18 18 18 18 19 21 22 22 22 24 24 24 24 24 25 25
	3.3.6 HL 分解	9		
	3.3.7 重心分解	9		
	3.4 彩色数	10	7.1 ビジュ アライザ 2	24
	3.4.1 包除原理	10		
	3.4.2 極大独立集合	10	5 (crates 3) 5 = 5 7 7 7 (
			8.1 Wrong Answer	
4	数学	11		
	4.1 整数	11	, &	24
	 4.1.1 剰余	11	8.4 出力が壊滅的なとき	25
	4.1.2 剰余積	11	8.5 そもそも解けないとき	25
	4.1.3 離散対数問題		8.6 解法メモ	
	4.1.4 カタラン数			
	4.1.5 乱数 (xor shift)			
	4.1.6 確率的素数判定 (Miller-Rabin 法)			
	4.2 多項式			
	4.2.1 FFT(complex)	12		

1 準備

1.1 Caps Lock を Control に変更

2 つ

1. 変更

```
setxkbmap -option ctrl:nocaps;
```

元に戻す

```
setxkbmap -option;
```

2. 上でダメな場合

```
xmodmap -e 'remove Lock = Caps_Lock';
xmodmap -e 'add Control = Caps_Lock';
xmodmap -e 'keysym Caps_Lock = Control_L';
```

1.2 init.el

linum は emacs24 のみ

```
(keyboard-translate ?\C-h ?\C-?)
(global-linum-mode t)
(setq linum-format "%4d ")
```

1.3 tpl.cpp

```
#include <bits/stdc++.h>
   using namespace std;
   #define rep(i,n) repi(i,0,n)
   #define repi(i,a,b) for(int i=int(a);i<int(b);++i)</pre>
   #define repit(it,u) for(auto it=begin(u);it!=end(u);++it)
   #define all(u) begin(u),end(u)
   #define uniq(u) (u).erase(unique(all(u)),end(u))
   #define 11 long
   #define long int64_t
   #define mp make_pair
   #define pb push_back
   #define eb emplace_back
13
14
   bool input()
15
16
17
       return true;
   }
18
19
   void solve()
20
21
22
23
24
25
   int main()
26
27
       cin.tie(0);
```

```
ios_base::sync_with_stdio(false);

while (input()) solve();
}
```

1.4 get input

```
wget -r http://(url of sample input)
```

1.5 alias

```
alias g++='g++ -g -02 -std=gnu++0x -Wl,-stack_size,64000000';
alias emacs='emacs -nw';
```

2 文字列

2.1 マッチング

2.1.1 複数文字列マッチング (Aho-Corasick 法)

O(N+M)

```
const int C = 128;
   struct pma_node {
        pma_node *next[C]; // use next[0] as failure link
        vector<int> match;
        pma_node() { fill(next, next + C, (pma_node *) NULL); }
        pma_node() { rep(i, C) if (next[i] != NULL) delete next[i]; }
   };
10
   pma_node *construct_pma(const vector<string>& pat) {
        pma_node *const root = new pma_node();
        root->next[0] = root;
13
        // construct trie
14
        rep(i, pat.size()) {
15
            const string& s = pat[i];
            pma_node *now = root;
17
            for (const char c : s) {
                if (now->next[int(c)] == NULL) now->next[int(c)] = new pma_node();
18
                now = now->next[int(c)];
19
20
            now->match.pb(i);
21
22
        // make failure links by BFS
23
24
        queue < pma_node *> q;
25
        repi(i, 1, C) {
            if (root->next[i] == NULL) root->next[i] = root;
26
27
                root->next[i]->next[0] = root;
28
                q.push(root->next[i]);
29
30
31
        while (not q.empty()) {
32
33
            auto now = q.front();
34
            q.pop();
            repi(i, 1, C) if (now->next[i] != NULL) {
35
```

```
36
                auto next = now->next[0];
                while (next->next[i] == NULL) next = next->next[0];
37
                now->next[i]->next[0] = next->next[i];
38
                vector<int> tmp;
39
                set_union(all(now->next[i]->match), all(next->next[i]->match), back_inserter
40
                now->next[i]->match = tmp;
41
                q.push(now->next[i]);
42
43
44
45
       return root;
46
47
48
   void match(pma_node*& now, const string s, vector<int>& ret) {
       for (const char c : s) {
49
50
            while (now->next[int(c)] == NULL) now = now->next[0];
51
            now = now->next[int(c)];
52
            for (const int e : now->match) ret[e] = true;
53
54
```

2.2 Suffix Array

```
find_string(): O(|T|\log|S|)
S 中に T が含まれないなら-1, 含まれるならその先頭.
LCS(): O(|S+T|)
最長共通部分文字列. (先頭. 長さ) を返す.
```

```
// verify
   // sa: http://www.spoj.com/problems/SARRAY/
   // lcp: http://www.spoj.com/problems/SUBLEX/
   int n, k;
   vector<int> rnk, tmp, sa, lcp;
   bool compare_sa(int i, int j) {
     if(rnk[i] != rnk[j]) return rnk[i] < rnk[j];</pre>
       int ri = i + k \leq n ? rnk[i+k] : -1:
       int rj = j + k <= n ? rnk[j+k] : -1;
13
       return ri < rj;
14
15
17
   void construct_sa(const string &s) {
     n = s.size();
18
     rnk.assign(n+1, 0);
     tmp.assign(n+1, 0);
20
     sa.assign(n+1, 0);
2.1
     lcp.assign(n+1, 0);
     for(int i = 0; i \le n; i++) {
23
24
       sa[i] = i;
25
       rnk[i] = i < n ? s[i] : -1;
26
27
     for(k = 1: k \le n: k*=2)
       sort(sa.begin(), sa.end(), compare_sa);
28
       tmp[sa[0]] = 0;
29
       for(int i = 1: i <= n: i++) {
30
          tmp[sa[i]] = tmp[sa[i-1]] + (compare_sa(sa[i-1], sa[i]) ? 1 : 0);
31
32
33
       for(int i = 0; i \le n; i++) {
         rnk[i] = tmp[i];
34
35
```

```
36
37
38
   void construct_lcp(const string &s) {
     for(int i = 0; i <= n; i++) rnk[sa[i]] = i;
     int h = 0:
42
     lcp[0] = 0;
43
      for(int i = 0; i < n; i++) {
44
       int j = sa[rnk[i] - 1];
       if(h > 0) h--;
45
       for(; j + h < n \&\& i + h < n; h++) {
46
47
        if(s[j+h] != s[i+h]) break;
48
49
       lcp[rnk[i] - 1] = h;
50
     }
51
   }
```

2.3 回文長 (Manacher)

O(N)

各文字を中心とした時の回文の長さ. 偶数長の回文はダミーを挟むことで求められている.

```
vector<int> manacher(const string &s) {
    int n = s.size()*2;
    vector<int> rad(n,0);
    for (int i = 0, j = 0, k; i < n; i += k, j = max(j-k, 0)) {
        while (i-j >= 0 && i+j+1 < n && s[(i-j)/2] == s[(i+j+1)/2]) ++j;
        rad[i] = j;
        for (k = 1; i-k >= 0 && rad[i]-k >= 0 && rad[i-k] != rad[i]-k; ++k)
            rad[i+k] = min(rad[i-k], rad[i]-k);
    }
    return rad;
}
```

3 グラフ

```
struct edge {
2
       int to; long w;
        edge(int to, long w) : to(to), w(w) {}
3
   typedef vector<vector<edge> > graph;
   graph rev(const graph& G) {
       const int n = G.size();
        graph ret(n);
       rep(i, n) for (const auto& e : G[i]) {
10
            ret[e.to].eb(i, e.w);
11
12
13
       return ret;
14
```

3.1 強連結成分分解

3.1.1 関節点

O(E)

ある関節点 $\mathbf u$ がグラフを $\mathbf k$ 個に分割するとき art には $\mathbf k$ -1 個の $\mathbf u$ が含まれる. 不要な場合は unique を忘れないこと.

```
typedef vector<vector<int> > graph;
   class articulation {
       const int n;
       graph G;
       int cnt;
       vector<int> num, low, art;
       void dfs(int v) {
            num[v] = low[v] = ++cnt;
10
            for (int nv : G[v]) {
11
                if (num[nv] == 0) {
12
                    dfs(nv);
                    low[v] = min(low[v], low[nv]):
13
                    if ((num[v] == 1 and num[nv] != 2) or
14
                        (num[v] != 1 and low[nv] >= num[v])) {
15
16
                        art[v] = true:
17
                } else {
18
19
                    low[v] = min(low[v], num[nv]);
20
21
22
   public:
23
       articulation(const graph& G): n(G.size()), G(G), cnt(0), num(n), low(n), art(n) {
24
            rep(i, n) if (num[i] == 0) dfs(i);
25
26
27
       vector<int> get() {
            return art;
28
29
   };
30
```

3.1.2 橋

```
O(V+E)
```

```
typedef vector<vector<int> > graph;
2
   class bridge {
       const int n;
       graph G;
       int cnt;
       vector<int> num, low, in;
       stack<int> stk;
       vector<pair<int, int> > brid;
       vector<vector<int> > comp;
11
       void dfs(int v, int p) {
            num[v] = low[v] = ++cnt;
12
13
            stk.push(v), in[v] = true;
            for (const int nv : G[v]) {
14
15
                if (num[nv] == 0) {
16
                    dfs(nv. v):
                    low[v] = min(low[v], low[nv]);
17
18
                } else if (nv != p and in[nv]) {
                    low[v] = min(low[v], num[nv]);
19
                }
20
21
            if (low[v] == num[v]) {
22
                if (p != n) brid.eb(min(v, p), max(v, p));
23
24
                comp.eb();
                int w;
25
                do {
26
```

```
27
                    w = stk.top();
28
                    stk.pop(), in[w] = false;
29
                    comp.back().pb(w);
30
                } while (w != v);
31
           }
32
       }
33
   public:
        bridge(const graph\& G) : n(G.size()), G(G), cnt(0), num(n), low(n), in(n) {
34
35
            rep(i, n) if (num[i] == 0) dfs(i, n);
36
        vector<pair<int, int> > get() {
37
            return brid;
38
39
        vector<vector<int> > components() {
40
41
            return comp;
42
43
   };
```

3.1.3 強連結成分分解

O(V + E)

```
typedef vector<vector<int> > graph;
   class scc {
3
        const int n;
        graph G;
6
        int cnt;
        vector<int> num, low, in;
7
        stack<int> stk;
        vector<vector<int> > comp;
10
        void dfs(int v) {
11
            num[v] = low[v] = ++cnt;
            stk.push(v), in[v] = true;
12
13
            for (const int nv : G[v]) {
                if (num[nv] == 0) {
14
                    dfs(nv);
15
16
                    low[v] = min(low[v], low[nv]);
17
                } else if (in[nv]) {
18
                    low[v] = min(low[v], num[nv]);
19
20
            if (low[v] == num[v]) {
21
22
                comp.eb();
23
                int w;
24
                do {
25
                    w = stk.top();
                    stk.pop(), in[w] = false;
26
27
                    comp.back().pb(w);
28
                } while (w != v);
            }
29
30
        }
   public:
31
32
        scc(const graph& G) : n(G.size()), G(G), cnt(0), num(n), low(n), in(n) {
33
            rep(i, n) if (num[i] == 0) dfs(i);
34
35
        vector<vector<int> > components() {
            return comp;
36
37
38
   };
```

3.1.4 無向中国人郵便配達問題

 $O(om \log n + o^2 2^o)$, -O2 で $o \le 18$ 程度が限界

```
long chinesePostman(const graph &g) {
        long total = 0:
2
       vector<int> odds;
       rep(u, g.size()) {
            for(auto &e: q[u]) total += e.w;
            if (g[u].size() % 2) odds.push_back(u);
       }
       total /= 2;
       int n = odds.size(), N = 1 << n;</pre>
       int w[n][n]; // make odd vertices graph
10
       rep(u,n) {
11
            int s = odds[u]; // dijkstra's shortest path
12
13
            vector<int> dist(g.size(), 1e9); dist[s] = 0;
            vector<int> prev(g.size(), -2);
14
            priority_queue<edge> Q;
15
            Q.push( edge(-1, s, 0) );
16
            while (!Q.empty()) {
17
                edge e = Q.top(); Q.pop();
18
                if (prev[e.to] != -2) continue;
19
20
                prev[e.to] = e.src;
                for(auto &f: g[e.to]) {
21
                    if (dist[f->to] > e.w+f->w) {
22
                        dist[f->to] = e.w+f->w;
23
                        Q.push(edge(f->src, f->to, e.w+f->w));
24
25
                }
26
27
            rep(v,n) w[u][v] = dist[odds[v]];
28
29
       long best[N]; // DP for general matching
30
31
       rep(S,N) best[S] = INF;
       best[0] = 0;
32
33
34
       for (int S = 0; S < N; ++S)
            for (int i = 0; i < n; ++i)
35
36
                if (!(S&(1<<i)))
37
                    for (int j = i+1; j < n; ++j)
38
                        if (!(S&(1<<j)))
39
                            best[S|(1<<i)|(1<<j)] = min(best[S|(1<<i)|(1<<j)], best[S]+w[i][
        return total + best[N-1];
40
41
```

3.1.5 全点対間最短路 (Johnson)

 $O(max(VE \log V, V^2))$

```
bool shortest_path(const graph &g, vector<vector<int> > & dist, vector<vector<int> > & prev) {
    int n = g.size();
    vector<int> h(n+1);
    rep(k,n) rep(i,n) for(auto &e: g[i]) {
        if (h[e.to] > h[e.from] + e->w) {
            h[e.to] = h[e.from] + e->w;
            if (k == n-1) return false; // negative cycle
        }
    }
    dist.assign(n, vector<int>(n, 1e9));
    prev.assign(n, vector<int>(n, -2));
    rep(s, n) {
```

```
13
            priority_queue < edge > q;
14
            q.push(edge(s, s, 0));
15
            while (!q.empty()) {
                edge e = q.top(); q.pop();
16
                if (prev[s][e.dst] != -2) continue;
17
                prev[s][e.to] = e.from;
18
                for(auto &f:g[e.to]) {
19
                    if (dist[s][f.to] > e.w + f->w) {
20
21
                         dist[s][f.to] = e.w + f->w;
                         q.push(edge(f-.from, f.to, e.w + f->w));
22
23
                    }
24
25
26
            rep(u, n) dist[s][u] += h[u] - h[s];
27
28
   }
29
   vector<int> build_path(const vector<vector<int> >& prev, int s, int t) {
        vector<int> path;
31
        for (int u = t; u \ge 0; u = prev[s][u])
32
            path.push_back(u);
33
        reverse(begin(path), end(path));
34
35
        return path;
36
```

3.1.6 無向グラフの全域最小カット

 $O(V^3)$

```
int minimum_cut(const graph &g) {
2
        int n = q.size();
        vector< vector<int> > h(n, vector<int>(n)); // make adj. matrix
        rep(u,n) for(auto &e: g[u]) h[e.src][e.dst] += e.weight;
        vector < int > V(n); rep(u, n) V[u] = u;
        int cut = 1e9;
7
        for(int m = n; m > 1; m--) {
            vector<int> ws(m, 0);
            int u, v;
            int w;
12
            rep(k. m) {
                u = v; v = max_element(ws.begin(), ws.end())-ws.begin();
13
14
                w = ws[v]; ws[v] = -1;
                rep(i, m) if (ws[i] \geq 0) ws[i] += h[V[v]][V[i]];
15
16
            rep(i. m) {
17
                h[V[i]][V[u]] += h[V[i]][V[v]];
18
19
                h[V[u]][V[i]] += h[V[v]][V[i]];
20
21
            V.erase(V.begin()+v);
            cut = min(cut. w):
22
23
24
        return cut;
25
```

5

3.2 フロー

3.2.1 最大流

 $O(EV^2)$

```
const int inf = 1e9:
   struct edge {
        int to, cap, rev;
        edge(int to, int cap, int rev) : to(to), cap(cap), rev(rev) {}
5
    typedef vector<vector<edge> > graph;
    void add_edge(graph& G, int from, int to, int cap) {
        G[from].eb(to, cap, G[to].size());
        G[to].eb(from, 0, G[from].size() - 1);
10
   }
11
12
13
   class max_flow {
        const int n;
14
        graph& G;
15
        vector<int> level, iter;
16
17
        void bfs(int s, int t) {
            level.assign(n, -1);
18
            queue<int> q;
19
            level[s] = 0, q.push(s);
20
            while (not q.empty()) {
21
                const int v = q.front();
22
23
                q.pop();
                if (v == t) return;
24
                for (const auto& e : G[v]) {
25
                     if (e.cap > 0 and level[e.to] < 0) {</pre>
26
                         level[e.to] = level[v] + 1;
27
28
                         q.push(e.to);
29
                }
30
31
32
        int dfs(int v, int t, int f) {
33
            if (v == t) return f;
34
            for (int& i = iter[v]; i < (int) G[v].size(); ++i) {</pre>
35
36
                edge& e = G[v][i];
37
                if (e.cap > 0 and level[v] < level[e.to]) {</pre>
38
                     const int d = dfs(e.to, t, min(f, e.cap));
39
                     if (d > 0) {
                         e.cap -= d, G[e.to][e.rev].cap += d;
40
41
                         return d;
42
43
44
45
            return 0;
46
    public:
47
48
        max_flow(graph& G) : n(G.size()), G(G) {}
49
        int calc(int s, int t) {
50
            int ret = 0, d;
51
            while (bfs(s, t), level[t] \geq 0) {
52
                iter.assign(n, 0);
53
                while ((d = dfs(s, t, inf)) > 0) ret += d;
54
55
            return ret;
56
57
   };
```

3.2.2 二部マッチング

```
O(EV)
```

```
int V;
vector<int> G[MAX_V];
```

```
int match[MAX_V];
   bool used[MAX_V];
5
   void add_edge(int u, int v){
7
        G[u].push_back(v);
        G[v].push_back(u);
9
10
11
   bool dfs(int v){
        used[v] = 1;
12
13
        rep(i,G[v].size()){
14
            int u = G[v][i], w = match[u];
            if(w < 0 || !used[w] && dfs(w)){
15
                match[v] = u;
16
17
                match[u] = v;
18
                return 1;
            }
19
20
21
        return 0;
22
23
   int bi_matching(){
24
        int res = 0;
25
26
        memset(match, -1, sizeof(match));
27
        rep(v,V) if(match[v] < 0){
            memset(used, 0, sizeof(used));
28
29
            if(dfs(v)) res++;
       }
30
31
        return res;
32
```

3.2.3 最小費用流

$O(FE \log V)$

```
const int inf = 1e9;
   struct edge {
        int to, cap, cost, rev;
        edge(int to, int cap, int cost, int rev) : to(to), cap(cap), cost(cost), rev(rev) {}
   typedef vector<vector<edge> > graph;
   void add_edge(graph& G, int from, int to, int cap, int cost) {
       G[from].eb(to, cap, cost, G[to].size());
10
        G[to].eb(from, 0, -cost, G[from].size() - 1);
   }
11
12
   int min_cost_flow(graph& G, int s, int t, int f) {
13
        const int n = G.size();
15
        struct state {
16
            int v, d;
17
            state(int v, int d) : v(v), d(d) {}
            bool operator <(const state& t) const { return d > t.d; }
18
19
       };
20
21
        int ret = 0;
22
        vector<int> h(n, 0), dist, prev(n), prev_e(n);
23
        while (f > 0) {
24
            dist.assign(n, inf);
25
            priority_queue<state> q;
26
            dist[s] = 0, q.emplace(s, 0);
27
            while (not q.empty()) {
28
                const int v = q.top().v;
                const int d = q.top().d;
29
30
                q.pop();
```

```
31
                if (dist[v] < d) continue;</pre>
                 rep(i, G[v].size()) {
32
                     const edge& e = G[v][i]:
33
                     if (e.cap > 0 \text{ and } dist[e.to] > dist[v] + e.cost + h[v] - h[e.to]) {
34
35
                         dist[e.to] = dist[v] + e.cost + h[v] - h[e.to];
                         prev[e.to] = v, prev_e[e.to] = i;
36
                         q.emplace(e.to, dist[e.to]);
37
38
39
                }
40
            if (dist[t] == inf) return -1;
41
            rep(i, n) h[i] += dist[i];
42
43
            int d = f:
44
            for (int v = t; v != s; v = prev[v]) {
45
46
                d = min(d, G[prev[v]][prev_e[v]].cap);
47
            f -= d, ret += d * h[t];
48
            for (int v = t; v != s; v = prev[v]) {
49
                edge& e = G[prev[v]][prev_e[v]];
50
                e.cap -= d, G[v][e.rev].cap += d;
51
52
53
54
        return ret;
55
```

3.2.4 Gomory-Hu 木

O(VMAXFLOW)

```
#define RESIDUE(s,t) (capacity[s][t]-flow[s][t])
   graph cutTree(const graph &g) {
       int n = g.size();
       Matrix capacity(n, Array(n)), flow(n, Array(n));
       rep(u,n) for(auto &e: g[u]) capacity[e.from][e.to] += e.w;
       vector<int> p(n), prev;
       vector<int> w(n);
       for (int s = 1; s < n; ++s) {
            int t = p[s]; // max-flow(s, t)
11
            rep(i,n) rep(j,n) flow[i][j] = 0;
12
            int total = 0;
13
            while (1) {
14
                queue<int> Q; Q.push(s);
15
                prev.assign(n, -1); prev[s] = s;
                while (!Q.empty() && prev[t] < 0) {</pre>
17
                    int u = Q.front(); Q.pop();
                    for(auto &e: q[u]) if (prev[e.to] < 0 && RESIDUE(u, e.to) > 0) {
18
                        prev[e.to] = u;
19
                        Q.push(e.to);
20
                    }
21
22
                if (prev[t] < 0) goto esc;</pre>
23
24
                int inc = 1e9;
25
                for (int j = t; prev[j] != j; j = prev[j])
                    inc = min(inc, RESIDUE(prev[j], j));
26
27
                for (int j = t; prev[j] != j; j = prev[j])
                    flow[prev[j]][j] += inc, flow[j][prev[j]] -= inc;
28
29
                total += inc;
30
31
        esc:w[s] = total; // make tree
            rep(u, n) if (u != s \&\& prev[u] != -1 \&\& p[u] == t)
32
33
                p[u] = s;
            if (prev[p[t]] != -1)
34
35
                p[s] = p[t], p[t] = s, w[s] = w[t], w[t] = total;
```

```
36
37
       graph T(n); // (s, p[s]) is a tree edge of weight w[s]
38
       rep(s, n) if (s != p[s]) {
           T[ s ].push_back( Edge(s, p[s], w[s]) );
39
40
           T[p[s]].push_back(Edge(p[s], s, w[s]));
41
42
       return T;
43
44
   // Gomory-Hu tree を用いた最大流 O(n)
   int max_flow(const graph &T, int u, int t, int p = -1, int w = 1e9) {
47
       if (u == t) return w;
       int d = 1e9;
48
49
        for(auto &e: T[u]) if (e.to != p)
           d = min(d, max_flow(T, e.to, t, u, min(w, e.w)));
50
51
52
```

3.3 木

3.3.1 木の直径

ある点(どこでもよい)から一番遠い点 a を求める. 点 a から一番遠い点までの距離がその木の直径になる.

3.3.2 最小全域木

```
struct mst_edge {
        int u, v; long w;
3
        mst\_edge(int u, int v, long w) : u(u), v(v), w(w) {}
        bool operator <(const mst_edge& t) const { return w < t.w; }
4
        bool operator >(const mst_edge& t) const { return w > t.w; }
5
   };
   graph kruskal(const graph& G) {
        const int n = G.size();
10
        vector<mst_edge> E;
        rep(i, n) for (const auto& e : G[i]) {
12
            if (i < e.to) E.eb(i, e.to, e.w);</pre>
13
14
        sort(all(E));
15
        graph T(n):
17
        disjoint_set uf(n);
        for (const auto& e : E) {
18
19
            if (not uf.same(e.u, e.v)) {
20
                T[e.u].eb(e.v, e.w);
                T[e.v].eb(e.u, e.w);
21
22
                uf.merge(e.u, e.v);
23
24
25
        return T:
   }
26
27
   graph prim(const vector<vector<long> >& A, int s = 0) {
28
        const int n = A.size();
29
30
        graph T(n):
31
        vector<int> done(n);
        priority_queue<mst_edge, vector<mst_edge>, greater<mst_edge> > q;
32
33
        q.emplace(-1, s, 0);
34
        while (not q.empty()) {
            const auto e = q.top();
35
```

```
36
            q.pop();
            if (done[e.v]) continue;
37
            done[e.v] = 1:
38
            if (e.u >= 0) {
39
                T[e.u].eb(e.v, e.w);
40
                T[e.v].eb(e.u, e.w);
41
42
            rep(i. n) if (not done[i]) {
43
44
                q.emplace(e.v, i, A[e.v][i]);
45
46
47
        return T;
48
```

3.3.3 最小全域有向木

O(VE)

```
void visit(Graph &h, int v, int s, int r,
               vector<int> &no, vector< vector<int> > &comp,
2
               vector<int> &prev, vector< vector<int> > &next, vector<int> &mcost,
3
               vector<int> &mark, int &cost, bool &found) {
       const int n = h.size();
       if (mark[v]) {
            vector<int> temp = no;
            found = true;
           do {
                cost += mcost[v];
10
                v = prev[v];
11
                if (v != s) {
12
13
                    while (comp[v].size() > 0) {
                        no[comp[v].back()] = s;
14
15
                        comp[s].push_back(comp[v].back());
                        comp[v].pop_back();
16
                    }
17
                }
18
            } while (v != s);
19
            for(auto &j: comp[s]) if (j != r) for(auto &e: h[j])
20
21
                if (no[e.from] != s) e.w -= mcost[temp[i]];
22
23
       mark[v] = true:
       for(auto &i: next[v]) if (no[i] != no[v] && prev[no[i]] == v)
24
            if (!mark[no[i]] || i == s)
25
26
                visit(h, i, s, r, no, comp, prev, next, mcost, mark, cost, found);
27
   int minimum_spanning_arborescence(const graph &g, int r) {
29
       const int n = g.size();
       graph h(n);
30
       rep(u,n) for(auto &e: g[u]) h[e.to].push_back(e);
31
32
       vector<int> no(n);
33
34
       vector < vector < int > > comp(n);
       rep(u, n) comp[u].push_back(no[u] = u);
35
36
37
       for (int cost = 0: :) {
38
            vector<int> prev(n, -1);
39
            vector<int> mcost(n. INF):
40
            rep(j,n) if (j != r) for(auto &e: q[j])
41
                if (no[e.from] != no[i])
42
                    if (e.w < mcost[no[j]])</pre>
43
                        mcost[no[j]] = e.w, prev[no[j]] = no[e.from];
44
45
            vector< vector<int> > next(n);
46
47
            rep(u,n) if (prev[u] >= 0)
```

```
48
                next[prev[u]].push_back(u);
49
50
            bool stop = true:
            vector<int> mark(n);
51
            rep(u,n) if (u != r && !mark[u] && !comp[u].empty()) {
52
53
                bool found = false:
54
                visit(h, u, u, r, no, comp, prev, next, mcost, mark, cost, found);
55
                if (found) stop = false;
56
            if (stop) {
57
                rep(u,n) if (prev[u] >= 0) cost += mcost[u];
58
59
                return cost;
60
61
62
```

3.3.4 最小シュタイナー木

 $O(4^{|T|}V)$

g は無向グラフの隣接行列. T は使いたい頂点の集合.

```
int minimum_steiner_tree(vi &T, vvi &g){
        int n = g.size(), t = T.size();
2
        if(t <= 1) return 0;
        vvi d(g); // all-pair shortest
        rep(k,n)rep(i,n)rep(j,n) //Warshall Floyd
            d[i][j] = min(d[i][j], d[i][k] + d[k][j]);
        int opt[1 << t][n];</pre>
9
        rep(S,1 << t) rep(x,n)
10
            opt[S][x] = INF;
11
12
        rep(p,t) rep(q,n) // trivial case
13
            opt[1 << p][q] = d[T[p]][q];
14
15
        repi(S,1,1<<t){ // DP step
16
            if(!(S & (S-1))) continue;
            rep(p,n) rep(E,S)
17
18
                if((E \mid S) == S)
19
                    opt[S][p] = min(opt[S][p], opt[E][p] + opt[S-E][p]);
20
            rep(p,n) rep(q,n)
21
                opt[S][p] = min(opt[S][p], opt[S][q] + d[p][q]);
22
23
24
        int ans = INF;
25
        rep(S,1 << t) rep(q,n)
26
            ans = min(ans, opt[S][q] + opt[((1 << t) - 1) - S][q]);
27
        return ans;
28
```

3.3.5 木の同型性判定

順序付き O(n)順序なし $O(n \log n)$

```
// ordered
struct node {
    vector<node*> child;
};
bool otreeIsomorphism(node *n, node *m) {
    if (n->child.size() != m->child.size()) return false;
```

```
rep(i, n->child.size())
            if (!otreeIsomorphism(n->child[i], m->child[i])) return false;
       return true:
9
10
11
   // not ordered
12
13
   struct node {
       vector<node *> child;
14
15
       vector<int> code;
16
   };
   void code(node *n) {
17
       int size = 1;
18
       vector< pair<vector<int>, int> > codes;
19
       rep(i, n->child.size()) {
20
            code(n->child[i]);
21
            codes.push_back( make_pair(n->child[i]->code, i) );
22
23
            size += codes[i].first[0];
24
       sort(codes.rbegin(), codes.rend()); // !reverse
25
       n->code.push_back(size);
26
       for (int i = 0; i < n->child.size(); ++i) {
27
            swap(n->child[i], n->child[ codes[i].second ]);
28
            n->code.insert(n->code.end(),
29
                           codes[i].first.begin(), codes[i].first.end());
30
31
32
   bool utreeIsomorphism(node *n, node *m) {
33
       code(n); code(m); return n->code == m->code;
34
35 }
```

3.3.6 HL 分解

```
namespace HLD {
   const int N = 200010;
   vector<vector<int>> chains, childs;
   int V, dep[N], par[N], heavy[N], head[N], chain[N], id[N], size[N], q[N];
   void calc_heavy() {
       int root = -1;
       childs.assign(V, vector < int > ());
       for(int v = 0; v < V; v++) {
10
            size[v] = 0;
            heavy[v] = -1;
11
12
            if(par[v] < 0) root = v;
13
            else childs[par[v]].push_back(v);
14
       int 1 = 0, r = 0;
15
       q[r++] = root;
16
17
       while(1 < r)  {
            int v = q[1++];
18
19
            for(auto &w: childs[v]) {
                if(w == par[v]) continue;
20
21
                dep[w] = dep[v]+1;
22
                q[r++] = w;
23
24
25
       reverse(q,q+V);
       for(int i = 1; i < V; i++) {
26
            int v = q[i], &u = par[v];
27
            size[u] += ++size[v];
28
            if(heavy[u] == -1 or size[v] > size[heavy[u]]) heavy[u] = v;
29
30
       }
31
32 void calc_chain() {
```

```
33
        chains.clear();
34
        int idx = 0;
35
        for (int v = 0; v < V; v++) {
            if(par[v] < 0 or heavy[par[v]] != v) {</pre>
36
37
                 chains.push_back(vector<int>());
38
                for (int w = v; w != -1; w = heavy[w]) {
39
                     chain[w] = idx;
                    head[w] = v;
40
41
                    id[w] = chains.back().size();
                     chains.back().push_back(w);
42
43
44
                idx++;
45
           }
46
        }
47
   void make_par(const vector<vector<int>> &g, int root = 0) {
49
        memset(par,-1,sizeof(par));
        par[root] = 0;
50
        int 1 = 0, r = 0;
51
        q[r++] = root;
52
        while(1 < r)  {
53
54
            int v = q[1++];
55
            for(const int &w: g[v]) if(par[w] < 0) q[r++] = w, par[w] = v;
56
57
        par[root] = -1;
58
59
   void build(const vector<vector<int>> &g, int root = 0) {
        V = g.size();
        make_par(g,root);
62
        calc_heavy();
        calc_chain();
63
64
   int lca(int u, int v) {
        while (chain[u] != chain[v]) {
67
            if (dep[head[u]] > dep[head[v]]) swap(u,v);
68
            v = par[head[v]];
69
70
        return dep[u] < dep[v]? u: v;</pre>
71
72
   }
```

3.3.7 重心分解

```
const int N = 100010;
   int level[N], par[N], done[N];
   vector<int> bfs(int s) {
        vector<int> ret;
        queue < int > que;
        que.push(s), par[s] = -1;
        while (not que.empty()) {
7
            int v = que.front(); que.pop();
            ret.push_back(v);
9
            done[v] = true;
11
            for (int u : G[v]) {
                if (level[u] == 0 and not done[u]) {
12
13
                    que.push(u), par[u] = v;
14
15
           }
16
17
        return ret;
18
19
   int size[N], ch[N];
   void update(int v) {
20
21
        size[v] = 1, ch[v] = 0;
```

```
22
        for (int u : G[v]) {
23
            if (u != par[v] and level[u] == 0) {
24
                size[v] += size[u];
                ch[v] = max(ch[v], size[u]);
25
26
27
        }
28
    void decompomposite() {
29
30
        auto ord = bfs(0);
        rep(i, 26) {
31
            fill_n(done, n, 0);
32
            for (int v : ord) {
33
                if (level[v] == 0 and not done[v]) {
34
                     auto sub = bfs(v):
35
                     reverse(all(sub));
36
                     for (int u : sub) update(u);
37
                     int whole = size[v], petal = ch[v];
38
                     for (bool flag = true; flag; ) {
39
                         flag = false;
40
                         for (int c : G[v]) {
41
                             if (level[c] == 0) {
42
                                 int tmp = max(ch[c], whole - size[c]);
43
                                 if (petal > tmp) {
44
                                      v = c, petal = tmp;
45
46
                                      flag = true;
                                      break;
47
48
49
                             }
                         }
50
51
                     // v is a centroid
52
53
                     level[v] = i + 1;
54
55
56
57
   }
```

3.4 彩色数

3.4.1 包除原理

 $O(2^{V}V)$

```
N[i] := i と隣接する頂点の集合 (i も含む)
   const int MAX V=16:
   const int mod = 10009;
   int N[MAX_V], I[1<<MAX_V], V;</pre>
   inline int mpow(int a, int k){ return k==0? 1: k%2? a*mpow(a,k-1)%mod: mpow(a*a%mod,k
        /2);}
   bool can(int k){
       int res = 0;
       rep(S, 1<<V){
            if(__builtin_popcountl1(S)%2) res -= mpow(I[S], k);
            else res += mpow(I[S],k);
10
11
       return (res%mod+mod)%mod;
12
13
14
   int color_number(){
15
       memset(I, 0, sizeof(I));
16
17
       I[0] = 1;
       repi(S,1,1<<V){
18
            int v = 0:
19
```

```
20
            while(!(S&(1<<v))) v++;
21
           I[S] = I[S-(1 << v)] + I[S&(~N[v])];
22
23
        int lb = 0, ub = V, mid;
        while(ub-lb>1){
24
            mid = (1b+ub)/2;
25
26
            if(can(mid)) ub = mid;
27
            else lb = mid:
28
       }
        return ub;
29
30
```

3.4.2 極大独立集合

```
typedef vector<vector<int>> graph;
   class maximal_indsets {
        const int n;
        const graph& G;
        vector<vector<int>> ret;
        vector<int> cur, exists, deg, block;
        void erase(int v) {
            if (exists[v]) {
                exists[v] = false;
10
                for (int nv : G[v]) --deg[nv];
            }
11
12
13
        void restore(int v) {
14
            exists[v] = true;
15
            for (int nv : G[v]) ++deg[nv];
16
17
        void select(int v) {
18
            cur.push_back(v);
19
            ++block[v], erase(v);
20
            for (int nv : G[v]) ++block[nv], erase(nv);
21
22
        void unselect(int v) {
23
            cur.pop_back();
24
            --block[v], restore(v);
25
            for (int nv : G[v]) {
                if (--block[nv] == 0) restore(nv);
26
27
28
       }
29
        void dfs() {
30
            int mn = n, v = -1;
31
            rep(u, n) if (exists[u]) {
                if (deg[u] < mn) mn = deg[u], v = u;
32
33
34
            if (v == -1) {
                ret.push_back(cur);
35
           } else {
36
                select(v), dfs(), unselect(v);
37
38
                for (int nv : G[v]) {
39
                    if (exists[nv]) select(nv), dfs(), unselect(nv);
40
           }
41
42
   public:
43
        maximal_indsets(const graph& G): n(G.size()), G(G), exists(n, true), deg(n), block(
            rep(v, n) deg[v] = G[v].size();
45
            dfs():
46
47
        const vector<vector<int>>& get() const { return ret; }
48
   };
49
```

4 数学

4.1 整数

4.1.1 剰余

```
// (x, y) s.t. a x + b y = gcd(a, b)
   long extgcd(long a, long b, long& x, long& y) {
       long g = a; x = 1, y = 0;
       if (b != 0) g = extgcd(b, a % b, y, x), y -= (a / b) * x;
       return q;
    // repi(i, 2, n) mod_inv[i] = mod_inv[m % i] * (m - m / i) % m
   long mod_inv(long a, long m) {
10
       long x, y;
11
       if (extgcd(a, m, x, y) != 1) return 0;
12
       return (x % m + m) % m;
13
14
    // a mod p where n! = a p^e in O(log_p n)
15
   long mod_fact(long n, long p, long& e) {
16
       const int P = 1000010:
17
       static long fact[P] = {1};
18
19
       static bool done = false:
       if (not done) {
20
            repi(i, 1, P) fact[i] = fact[i - 1] * i % p;
21
            done = true:
22
23
       e = 0;
24
       if (n == 0) return 1;
25
26
       long ret = mod_fact(n / p, p, e);
27
       e += n / p;
28
       if (n / p % 2) return ret * (p - fact[n % p]) % p;
       return ret * fact[n % p] % p;
29
30
31
   // nCk mod p
32
   long mod_binom(long n, long k, long p) {
33
       if (k < 0 or n < k) return 0;
34
35
       long e1, e2, e3;
       long a1 = mod_fact(n, p, e1);
36
       long a2 = mod_fact(k, p, e2);
37
       long a3 = mod_fact(n - k, p, e3);
38
39
       if (e1 > e2 + e3) return 0;
       return a1 * mod_inv(a2 * a3 % p, p) % p;
40
41
42
   // a^b mod m
   long mod_pow(long a, long b, long m) {
45
       long ret = 1;
46
       do {
            if (b & 1) ret = ret * a % m;
47
48
            a = a * a % m;
       } while (b >>= 1);
49
50
       return ret;
51
```

4.1.2 剰余積

```
i inline long mod_mul(long a, long b, long m) {
2 long ret = a * b - m * long(roundl((long double)(a) * b / m));
```

```
return ret < 0 ? ret + m : ret;

long mod_powl(long a, long b, long m) {
    long ret = 1;
    do {
        if (b & 1) ret = mod_mul(ret, a, m);
            a = mod_mul(a, a, m);
    } while (b >>= 1);
    return ret;
}
```

4.1.3 離散対数問題

```
long discrete_log(long a, long m) {
       if (a == 0) return -1;
2
       long b = long(sqrt(m)) + 1, t = 1;
       unordered_map<long, long> mem;
       for (int i = 0; i < b; ++i) {
           mem[t] = i;
           t = t * a % m;
           if (t == 1) return i + 1;
9
10
       long u = t:
       for (int i = b; i < m; i += b) {
11
12
           if (mem.find(mod_inverse(u, m)) != mem.end()) {
               return mem[mod_inverse(u, m)] + i;
13
14
           u = u * t % m;
15
17
       return -1;
```

4.1.4 カタラン数

n < 16 程度が限度, n > 1 について以下が成り立つ.

$$C_n = \frac{1}{n+1} {2n \choose n}$$
$$= {2n \choose n} - {2n \choose n-1}$$

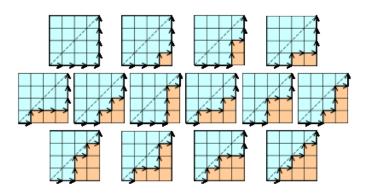
n が十分大きいとき、カタラン数は以下に近似できる.

$$C_n = \frac{4^n}{n^{3/2}\sqrt{\pi}}$$

() を正しく並べる方法, 二分木, 格子状の経路の数え上げ, 平面グラフの交差などに使われる. $C_3=5$



 $C_4 = 14$



4.1.5 乱数 (xor shift)

周期は 2128 - 1

```
unsigned xorshift() {
    static unsigned x = 123456789;
    static unsigned y = 362436069;
    static unsigned z = 521288629;
    static unsigned w = 88675123;
    unsigned t;
    t = x ^cb^86 (x << 11);
    x = y; y = z; z = w;
    return w = (w ^cb^86 (w >> 19)) ^cb^86 (t ^cb^86 (t >> 8));
}
```

4.1.6 確率的素数判定 (Miller-Rabin 法)

 $O(k \log^3 n)$

合成数を素数と判定する確率は最大で 4-k

```
bool suspect(long a, int s, long d, long n) {
       long x = mod_pow(a, d, n); // use mod_powl instead for large n
       if (x == 1) return true;
       for (int r = 0; r < s; ++r) {
           if (x == n - 1) return true;
           x = x * x % n; // use mod_mul instead for large n
       return false;
   // {2.7.61.-1}
                                   is for n < 4759123141 (= 2^32)
   // {2,3,5,7,11,13,17,19,23,-1} is for n < 10^16 (at least)
   bool is_prime(long n) {
12
       if (n <= 1 || (n > 2 && n % 2 == 0)) return false;
13
       int test[] = {2,3,5,7,11,13,17,19,23,-1};
14
       long d = n - 1, s = 0;
15
       while (d \% 2 == 0) ++s, d /= 2;
16
17
       for (int i = 0; test[i] < n && test[i] != -1; ++i)</pre>
           if (!suspect(test[i], s, d, n)) return false;
18
19
       return true:
20
```

4.2 多項式

FFT は基本定数重めなので TLE に注意する.

4.2.1 FFT(complex)

 $O(N \log N)$

複素数を用いた FFT. 変換する vector のサイズは 2 の冪乗にすること.

```
typedef complex < double > cd;
   vector<cd> fft(vector<cd> f. bool inv){
        int n, N = f.size();
        for(n=0;;n++) if(N == (1 << n)) break;
        rep(m,N){
            int m2 = 0;
            rep(i,n) if(m&(1<<i)) m2 |= (1<<(n-1-i));
            if(m < m2) swap(f[m], f[m2]);</pre>
10
11
        for(int t=1;t<N;t*=2){</pre>
            double theta = acos(-1.0) / t;
12
            cd w(cos(theta), sin(theta));
13
            if(inv) w = cd(cos(theta), -sin(theta));
14
15
            for(int i=0;i<N;i+=2*t){</pre>
                 cd power(1.0, 0.0);
16
                 rep(j,t){
17
                     cd tmp1 = f[i+j] + f[i+t+j] * power;
18
                     cd tmp2 = f[i+j] - f[i+t+j] * power;
19
                     f[i+j] = tmp1;
20
21
                     f[i+t+j] = tmp2;
22
                     power = power * w;
23
            }
24
25
        if(inv) rep(i,N) f[i] /= N;
26
        return f:
27
28
```

4.2.2 FFT(modulo)

 $O(N \log N)$

剰余環を用いた FFT(FMT). 変換する vector のサイズは 2 の冪乗にすること. mod は $a*2^e+1$ の形.

```
#include "number_theory.cpp"
   const int mod = 7*17*(1<<23)+1;
   vector<int> fmt(vector<int> f, bool inv){
       int e, N = f.size();
        // assert((N&(N-1))==0 and "f.size() must be power of 2");
       for(e=0;;e++) if(N == (1 << e)) break;
       rep(m.N){
            rep(i,e) if(m&(1<< i)) m2 |= (1<<(e-1-i));
           if(m < m2) swap(f[m], f[m2]);
11
12
        for(int t=1: t<N: t*=2){
13
            int r = pow_mod(3, (mod-1)/(t*2), mod);
14
            if(inv) r = mod inverse(r.mod):
15
16
            for(int i=0; i<N; i+=2*t){
17
                int power = 1;
                rep(j,t){
18
```

```
19
                     int x = f[i+j], y = 1LL*f[i+t+j]*power%mod;
                     f[i+j] = (x+y) \% mod;
20
                     f[i+t+j] = (x-y+mod)%mod;
21
                     power = 1LL*power*r%mod;
22
23
24
25
        if(inv) for(int i=0,ni=mod_inv(N,mod);i<N;i++) f[i] = 1LL*f[i]*ni%mod;</pre>
26
27
        return f;
28
```

4.2.3 積 (FMT)

O(N log N)
poly_mul() が必要.

```
vector<int> poly_mul(vector<int> f, vector<int> g){
   int N = max(f.size(),g.size())*2;
   f.resize(N); g.resize(N);
   f = fmt(f,0); g = fmt(g,0);
   rep(i,N) f[i] = 1LL*f[i]*g[i]%mod;
   f = fmt(f,1);
   return f;
}
```

4.2.4 逆元 (FMT)

 $O(N \log N)$

extgcd(), mod_inverse(), poly_mul(), fmt() が必要.

```
vector<int> poly_inv(const vector<int> &f){
2
       int N = f.size();
       vector<int> r(1,mod_inv(f[0],mod));
       for(int k = 2; k \le N; k \le 1)
           vector<int> nr = poly_mul(poly_mul(r,r), vector<int>(f.begin(),f.begin()+k));
           nr.resize(k):
           rep(i,k/2) {
               nr[i] = (2*r[i]-nr[i]+mod)%mod;
                nr[i+k/2] = (mod-nr[i+k/2])%mod;
10
11
           r = nr;
12
13
       return r;
14
```

4.2.5 平方根 (FMT)

O(NlogN)

extgcd(), mod_inverse(), poly_inv(), poly_mul(), fmt() が必要.

```
const int inv2 = (mod+1)/2;
vector<int> poly_sqrt(const vector<int> &f) {
   int N = f.size();
   vector<int> s(1,1); // s[0] = sqrt(f[0])
   for(int k = 2; k <= N; k <<= 1) {
        s.resize(k);
        vector<int> ns = poly_mul(poly_inv(s), vector<int>(f.begin(),f.begin()+k));
        ns.resize(k);
}
```

4.3 行列

```
typedef double number:
    typedef vector<number> vec;
    typedef vector<vec> mat;
   vec mul(const mat& A, const vec& x) {
        const int n = A.size():
        vec b(n);
        rep(i, n) rep(j, A[0].size()) {
9
           b[i] = A[i][j] * x[j];
10
11
        return b;
12
   }
13
14
   mat mul(const mat& A, const mat& B) {
        const int n = A.size();
15
        const int o = A[0].size();
16
        const int m = B[0].size();
17
        mat C(n, vec(m));
18
19
        rep(i, n) rep(k, o) rep(j, m) {
20
           C[i][j] += A[i][k] * B[k][j];
21
22
        return C;
23
   }
24
25
   mat pow(mat A, long m) {
        const int n = A.size();
26
27
        mat B(n, vec(n));
28
        rep(i, n) B[i][i] = 1;
29
30
            if (m \& 1) B = mul(B, A);
31
            A = mul(A, A);
32
        } while (m >>= 1);
33
        return B:
34
35
   const number eps = 1e-4;
37
   // determinant: 0(n^3)
   number det(mat A) {
        int n = A.size();
40
41
        number D = 1;
42
        rep(i,n){
43
            int pivot = i;
44
            repi(j,i+1,n)
45
                if (abs(A[j][i]) > abs(A[pivot][i])) pivot = j;
46
            swap(A[pivot], A[i]);
47
            D *= A[i][i] * (i != pivot ? -1 : 1);
            if (abs(A[i][i]) < eps) break;</pre>
48
49
            repi(j,i+1,n)
50
                for (int k=n-1; k>=i; --k)
51
                    A[j][k] -= A[i][k] * A[j][i] / A[i][i];
52
53
        return D;
   }
54
55
    // rank; 0(n^3)
   int rank(mat A) {
```

```
int n = A.size(), m = A[0].size(), r = 0;
58
        for(int i = 0; i < m and r < n; i++){
59
            int pivot = r:
60
            repi(j,r+1,n)
61
62
                if (abs(A[j][i]) > abs(A[pivot][i])) pivot = j;
            swap(A[pivot], A[r]);
63
            if (abs(A[r][i]) < eps) continue;</pre>
64
            for (int k=m-1; k>=i; --k)
65
66
                A[r][k] /= A[r][i];
            repi(j,r+1,n) repi(k,i,m)
67
                A[j][k] -= A[r][k] * A[j][i];
68
69
70
        return r;
71
72
```

12 if (s[q] < 0)13 for (p = j; p >= 0; j = p)y[j] = k = t[j], p = x[k], x[k] = j;14 15 16 $if (x[i] < 0) {$ int d = inf: 17 $rep(k,q+1) \ rep(j,n) \ if \ (t[j] < 0) \ d = min(d, fx[s[k]] + fy[j] - a[s[k]][j]);$ 18 19 rep(j,n) fy[j] += (t[j] < 0 ? 0 : d);20 rep(k,q+1) fx[s[k]] -= d;21 } else i++; 22 23 int ret = 0; 24 rep(i,n) ret += a[i][x[i]]; return ret; 25 26

4.3.1 線形方程式の解 (Givens 消去法)

```
O(N^3)
```

```
// Givens elimination: 0(n^3)
   typedef double number:
   typedef vector<vector<number> > matrix;
   inline double my_hypot(double x, double y) { return sqrt(x * x + y * y); }
   inline void givens_rotate(number& x, number& y, number c, number s) {
       number u = c * x + s * y, v = -s * x + c * y;
       x = u, y = v;
10
   vector<number> givens(matrix A, vector<number> b) {
11
       const int n = b.size():
12
       rep(i, n) repi(j, i + 1, n) {
13
            const number r = my_hypot(A[i][i], A[j][i]);
14
            const number c = A[i][i] / r, s = A[j][i] / r;
15
            givens_rotate(b[i], b[j], c, s);
16
17
           repi(k, i, n) givens_rotate(A[i][k], A[j][k], c, s);
18
       for (int i = n - 1; i >= 0; --i) {
19
           repi(j, i + 1, n) b[i] -= A[i][j] * b[j];
20
           b[i] /= A[i][i];
21
22
23
       return b;
24
```

4.4 割り当て問題

4.4.1 ハンガリアン法

```
O(N^2)
```

```
int hungarian(const vector<vector<int>> &a) {
   int n = a.size(), p, q;
   vector<int> fx(n, inf), fy(n, 0), x(n, -1), y(n, -1);
   rep(i,n) rep(j,n) fx[i] = max(fx[i], a[i][j]);

for (int i = 0; i < n; ) {
    vector<int> t(n, -1), s(n+1, i);
   for (p = q = 0; p <= q && x[i] < 0; ++p)
   for (int k = s[p], j = 0; j < n && x[i] < 0; ++j)
    if (fx[k] + fy[j] == a[k][j] && t[j] < 0) {
        s[++q] = y[j], t[j] = k;
}</pre>
```

5 幾何

```
// constants and eps-considered operators
const double eps = le-8; // choose carefully!
const double pi = acos(-1.0);

inline bool lt(double a, double b) { return a < b - eps; }
inline bool gt(double a, double b) { return lt(b, a); }
inline bool le(double a, double b) { return !lt(b, a); }
inline bool ge(double a, double b) { return !lt(a, b); }
inline bool ne(double a, double b) { return lt(a, b) or lt(b, a); }
inline bool eq(double a, double b) { return lt(a, b) or lt(b, a); }
```

5.1 点

```
typedef complex<double> point;
   inline double dot (point a, point b) { return real(conj(a) * b); }
   inline double cross(point a, point b) { return imag(conj(a) * b); }
3
4
    * Here is what ccw(a, b, c) returns:
              1
        2 la 0 bl -2
10
       _____
              - 1
12
    * Note: we can implement intersect PS(p, s) as !ccw(s.a, s.b, p).
13
14
15
   int ccw(point a, point b, point c) {
       b -= a, c -= a;
       if (cross(b, c) > eps) return +1;
17
       if (cross(b, c) < eps) return -1;
18
                                return +2; // c -- a -- b
19
       if (dot(b, c) < eps)</pre>
       if (lt(norm(b), norm(c))) return -2; // a -- b -- c
20
21
       return 0;
22
```

5.2 直線と線分

```
struct line {
       point a. b:
       line(point a, point b) : a(a), b(b) {}
   bool intersectLS(const line& 1, const line& s) {
       return ccw(1.a, 1.b, s.a) * ccw(1.a, 1.b, s.b) <= 0;
   bool intersectSS(const line& s. const line& t) {
       return intersectLS(s. t) and intersectLS(t. s):
10
11
   bool intersectLL(const line& l. const line& m) {
12
13
       return ne(cross(l.b - l.a, m.b - m.a), 0.0) // not parallel
           or eg(cross(l.b - l.a, m.a - l.a), 0.0); // overlap
14
15
   point crosspointLL(const line& 1, const line& m) {
16
17
       double A = cross(1.b - 1.a, m.b - m.a);
       double B = cross(l.b - l.a. m.a - l.a):
18
       if (eq(A, 0.0) \text{ and } eq(B, 0.0)) return m.a; // overlap
19
                                                   // not parallel
20
       assert(ne(A, 0.0));
       return m.a - B / A * (m.b - m.a);
21
22
23
   point proj(const line& l, point p) {
       double t = dot(1.b - 1.a, p - 1.a) / norm(1.b - 1.a);
24
       return 1.a + t * (1.b - 1.a);
25
26
   point reflection(const line& 1, point p) { return 2.0 * proj(1, p) - p; }
27
28
   double distanceLP(const line& 1, point p) { return abs(proj(1, p) - p); }
   double distanceLL(const line& 1, const line& m) {
30
       return intersectLL(1, m) ? 0.0 : distanceLP(1, m.a);
31
32
   double distanceLS(const line& 1, const line& s) {
33
       return intersectLS(1, s) ? 0.0 : min(distanceLP(1, s.a), distanceLP(1, s.b));
34
35
   double distancePS(point p, const line& s) {
36
37
       point h = proj(s, p);
       return ccw(s.a, s.b, h)? min(abs(s.a - p), abs(s.b - p)): abs(h - p);
38
39
   double distanceSS(const line& s, const line& t) {
40
       if (intersectSS(s, t)) return 0.0;
41
       return min(min(distancePS(s.a, t), distancePS(s.b, t)),
42
                   min(distancePS(t.a, s), distancePS(t.b, s)));
43
44
```

5.3 円

```
struct circle {
       point o; double r;
       circle(point o, double r) : o(o), r(r) {}
   };
   bool intersectCL(const circle& c. const line& 1) {
       return le(norm(proj(1, c.o) - c.o), c.r * c.r);
   int intersectCS(const circle& c, const line& s) {
       if (not intersectCL(c, s)) return 0;
10
       double a = abs(s.a - c.o):
11
       double b = abs(s.b - c.o);
12
       if (lt(a, c,r) and lt(b, c,r)) return 0:
13
       if (lt(a, c.r) or lt(b, c.r)) return 1;
14
       return ccw(s.a, s.b, proj(s, c.o)) ? 0 : 2;
15
16 }
```

```
17
   bool intersectCC(const circle& c, const circle& d) {
18
        double dist = abs(d.o - c.o);
19
        return le(abs(c.r - d.r), dist) and le(dist, c.r + d.r):
20
   line crosspointCL(const circle& c, const line& l) {
21
22
        point h = proi(1, c.o):
23
        double a = sqrt(c.r * c.r - norm(h - c.o));
24
        point d = a * (1.b - 1.a) / abs(1.b - 1.a);
25
       return line(h - d, h + d);
26
   line crosspointCC(const circle& c, const circle& d) {
27
        double dist = abs(d.o - c.o), th = arg(d.o - c.o);
        double ph = acos((c.r * c.r + dist * dist - d.r * d.r) / (2.0 * c.r * dist));
29
        return line(c.o + polar(c.r, th - ph), c.o + polar(c.r, th + ph));
30
31
32
33
   line tangent(const circle& c, double th) {
       point h = c.o + polar(c.r, th);
35
        point d = polar(c.r, th) * point(0, 1);
       return line(h - d, h + d);
36
37
   vector<line> common_tangents(const circle& c, const circle& d) {
38
        vector<line> ret;
39
        double dist = abs(d.o - c.o), th = arg(d.o - c.o);
40
41
        if (abs(c.r - d.r) < dist) { // outer}
            double ph = acos((c.r - d.r) / dist);
42
43
            ret.pb(tangent(c, th - ph));
44
            ret.pb(tangent(c, th + ph));
45
        if (abs(c.r + d.r) < dist) { // inner}
46
            double ph = acos((c.r + d.r) / dist);
47
48
            ret.pb(tangent(c, th - ph));
49
            ret.pb(tangent(c, th + ph));
       return ret:
   pair<circle, circle> tangent_circles(const line& 1, const line& m, double r) {
        double th = arg(m.b - m.a) - arg(1.b - 1.a);
        double ph = (arg(m.b - m.a) + arg(1.b - 1.a)) / 2.0;
        point p = crosspointLL(1, m);
        point d = polar(r / sin(th / 2.0), ph);
        return mp(circle(p - d, r), circle(p + d, r));
58
   line bisector(point a. point b):
60
   circle circum_circle(point a, point b, point c) {
        point o = crosspointLL(bisector(a, b), bisector(a, c));
        return circle(o, abs(a - o));
63
64
```

5.4 多角形

```
typedef vector<point> polygon;

double area(const polygon& g) {
    double ret = 0.0;
    int j = g.size() - 1;
    rep(i, g.size()) {
        ret += cross(g[j], g[i]), j = i;
    }
    return ret / 2.0;
}

point centroid(const polygon& g) {
    if (g.size() == 1) return g[0];
    if (g.size() == 2) return (g[0] + g[1]) / 2.0;
```

```
point ret = 0.0;
14
       int j = g.size() - 1;
15
       rep(i, g.size()) {
16
            ret += cross(g[j], g[i]) * (g[j] + g[i]), j = i;
17
18
       return ret / area(g) / 6.0;
19
20
21
   line bisector(point a, point b) {
22
       point m = (a + b) / 2.0;
       return line(m, m + (b - a) * point(0, 1));
23
24
   polygon convex_cut(const polygon& g, const line& l) {
25
26
       polygon ret;
27
       int j = g.size() - 1;
28
       rep(i, g.size()) {
29
            if (ccw(l.a, l.b, g[j]) != -1) ret.pb(g[j]);
            if (intersectLS(1, line(g[j], g[i]))) ret.pb(crosspointLL(1, line(g[j], g[i])));
30
31
32
33
       return ret;
34
   polygon voronoi_cell(polygon g, const vector<point>& v, int k) {
35
36
       rep(i, v.size()) if (i != k) {
37
            g = convex_cut(g, bisector(v[i], v[k]));
38
39
        return g;
40
```

5.4.1 凸包

```
namespace std {
        bool operator <(const point& a, const point& b) {
            return ne(real(a), real(b)) ? lt(real(a), real(b)) : lt(imag(a), imag(b));
       }
5
   polvgon convex hull(vector<point> v) {
       const int n = v.size();
        sort(all(v));
10
        polygon ret(2 * n);
        int k = 0;
11
        for (int i = 0; i < n; ret[k++] = v[i++]) {
12
13
            while (k \ge 2 \text{ and } ccw(ret[k - 2], ret[k - 1], v[i]) \le 0) --k;
14
15
        for (int i = n - 2, t = k + 1; i >= 0; ret[k++] = v[i--]) {
            while (k \ge t \text{ and } ccw(ret[k - 2], ret[k - 1], v[i]) \le 0) --k;
16
17
        ret.resize(k - 1):
18
        return ret;
19
20
   }
```

5.4.2 最近点対

だいたい $O(n \log n)$, 最悪縦 1 列に並んでる場合 $O(n^2)$

```
pair<point, point> closest_pair(vector<point> p) {
   int n = p.size(), s = 0, t = 1, m = 2, S[n];
   S[0] = 0, S[1] = 1;
   sort(all(p)); // "p < q" <=> "p.x < q.x"
   double d = norm(p[s]-p[t]);
   for (int i = 2; i < n; S[m++] = i++) rep(j, m) {</pre>
```

```
if (norm(p[S[j]]-p[i])<d) d = norm(p[s = S[j]]-p[t = i]);

if (real(p[S[j]]) < real(p[i]) - d) S[j--] = S[--m];

}
return make_pair(p[s], p[t]);
}</pre>
```

5.4.3 点-多角形包含判定

O(n)

```
enum { OUT, ON, IN };
int contains(const polygon& P, const point& p) {
    bool in = false;
    for (int i = 0; i < (int)P.size(); ++i) {
        point a = P[i] - p, b = P[(i+1)%P.size()] - p;
        if (imag(a) > imag(b)) swap(a, b);
        if (imag(a) <= 0 && 0 < imag(b) && cross(a, b) < 0) in = !in;
        if (cross(a, b) == 0 && dot(a, b) <= 0) return ON;
    }
    return in ? IN : OUT;
}</pre>
```

5.4.4 凸多角形の共通部分

O(n+m)

```
bool intersect_1pt(const point& a, const point& b,
2
                       const point& c, const point& d, point &r) {
        number D = cross(b - a, d - c);
        if (eq(D,0)) return false;
        number t = cross(c - a, d - c) / D;
       number s = -cross(a - c, b - a) / D;
7
        r = a + t * (b - a);
        return ge(t, 0) && le(t, 1) && ge(s, 0) && le(s, 1);
9
   polygon convex_intersect(const polygon &P, const polygon &Q) {
        const int n = P.size(), m = Q.size();
        int a = 0. b = 0. aa = 0. ba = 0:
13
        enum { Pin, Qin, Unknown } in = Unknown;
14
        polygon R;
15
16
            int a1 = (a+n-1) % n, b1 = (b+m-1) % m;
17
            number C = cross(P[a] - P[a1], Q[b] - Q[b1]);
18
            number A = cross(P[a1] - Q[b], P[a] - Q[b]);
            number B = cross(Q[b1] - P[a], Q[b] - P[a]);
19
20
21
            if (intersect_1pt(P[a1], P[a], Q[b1], Q[b], r)) {
                if (in == Unknown) aa = ba = 0;
22
23
                R.push_back( r );
                in = B > 0 ? Pin : A > 0 ? Qin : in;
24
25
26
            if (C == 0 \&\& B == 0 \&\& A == 0) {
27
                if (in == Pin) { b = (b + 1) \% m; ++ba; }
28
                               \{ a = (a + 1) \% m: ++aa: \}
29
           } else if (C >= 0) {
30
                if (A > 0) { if (in == Pin) R.push_back(P[a]); a = (a+1)%n; ++aa; }
31
                           { if (in == Qin) R.push_back(Q[b]); b = (b+1)\%m; ++ba; }
32
           } else {
                if (B > 0) { if (in == Qin) R.push_back(Q[b]); b = (b+1)%m; ++ba; }
33
34
                           { if (in == Pin) R.push_back(P[a]); a = (a+1)%n; ++aa; }
35
        } while ( (aa < n || ba < m) && aa < 2*n && ba < 2*m );
36
```

5.4.5 凸多角形の直径

O(n)

```
inline double diff(const vector<point> &P, const int &i) { return (P[(i+1)%P.size()] - P
   number convex_diameter(const polygon &pt) {
        const int n = pt.size();
       int is = 0, js = 0;
       for (int i = 1; i < n; ++i) {
            if (imag(pt[i]) > imag(pt[is])) is = i;
            if (imag(pt[i]) < imag(pt[js])) js = i;</pre>
       number maxd = norm(pt[is]-pt[js]);
11
       int i, maxi, j, maxj;
       i = maxi = is;
12
13
       j = maxj = js;
14
            if (cross(diff(pt,i), diff(pt,j)) >= 0) j = (j+1) % n;
15
16
            else i = (i+1) \% n;
17
            if (norm(pt[i]-pt[j]) > maxd) {
18
                maxd = norm(pt[i]-pt[j]);
19
                maxi = i; maxj = j;
20
21
       } while (i != is || j != js);
22
        return maxd; /* farthest pair is (maxi, maxj). */
23
```

5.4.6 ドロネー三角形分割(逐次添加法)

 $O(n^2)$

```
bool incircle(point a, point b, point c, point p) {
       a -= p; b -= p; c -= p;
       return norm(a) * cross(b, c)
            + norm(b) * cross(c, a)
             + norm(c) * cross(a, b) >= 0;
       // < : inside, = cocircular, > outside
   #define SET_TRIANGLE(i, j, r) \
       E[i].insert(j); em[i][j] = r; \
       E[j].insert(r); em[j][r] = i; \
10
       E[r].insert(i); em[r][i] = j; \
11
12
       S.push(pair<int,int>(i, j));
   #define REMOVE_EDGE(i, j) \
13
14
       E[i].erase(j); em[i][j] = -1; 
15
       E[j].erase(i); em[j][i] = -1;
   #define DECOMPOSE_ON(i,j,k,r) { \
16
17
            int m = em[j][i]; REMOVE_EDGE(j,i); \
18
            SET_TRIANGLE(i,m,r); SET_TRIANGLE(m,j,r); \
19
            SET_TRIANGLE(j,k,r); SET_TRIANGLE(k,i,r); }
20
   #define DECOMPOSE_IN(i,j,k,r) { \
           SET_TRIANGLE(i,j,r); SET_TRIANGLE(j,k,r); \
21
22
           SET_TRIANGLE(k,i,r); }
```

```
23 | #define FLIP_EDGE(i,j) { \
24
            int k = em[j][i]; REMOVE_EDGE(i,j); \
25
            SET_TRIANGLE(i,k,r); SET_TRIANGLE(k,j,r); }
   #define IS_LEGAL(i, j) \
26
        (em[i][j] < 0 || em[j][i] < 0 || 
27
         !incircle(P[i],P[j],P[em[i][j]],P[em[j][i]]))
28
    double Delaunay(vector<point> P) {
29
        const int n = P.size():
30
31
        P.push_back( point(-inf,-inf) );
        P.push_back( point(+inf,-inf) );
32
33
        P.push_back( point( 0 ,+inf) );
        int em[n+3][n+3]; memset(em, -1, sizeof(em));
34
35
        set < int > E[n+3];
        stack< pair<int,int> > S;
36
        SET_TRIANGLE(n+0, n+1, n+2);
37
38
        for (int r = 0; r < n; ++r) {
39
            int i = n, j = n+1, k;
40
            while (1) {
41
                k = em[i][j];
42
                         (ccw(P[i], P[em[i][j]], P[r]) == +1) j = k;
43
                else if (ccw(P[j], P[em[i][j]], P[r]) == -1) i = k;
44
                else break;
45
46
            if
                     (ccw(P[i], P[j], P[r]) != +1) \{ DECOMPOSE_ON(i,j,k,r); \}
47
            else if (ccw(P[j], P[k], P[r]) != +1) \{ DECOMPOSE_ON(j,k,i,r); \}
48
            else if (ccw(P[k], P[i], P[r]) != +1) \{ DECOMPOSE_ON(k,i,j,r); \}
49
                                                    { DECOMPOSE_IN(i,j,k,r); }
            while (!S.empty()) {
50
51
                int u = S.top().first, v = S.top().second; S.pop();
52
                if (!IS_LEGAL(u, v)) FLIP_EDGE(u, v);
            }
53
54
55
        double minarg = 1e5;
        for (int a = 0; a < n; ++a) {
57
            for(auto &b: E[a]) {
58
                int c = em[a][b];
                if (b < n \&\& c < n) {
59
                    point p = P[a] - P[b], q = P[c] - P[b];
                    minarg = min(minarg, acos(dot(p,q)/abs(p)/abs(q)));
62
63
            }
64
65
        return minarg;
66
```

6 データ構造

6.1 Union-Find 木

```
class disjoint_set {
2
       vector<int> p;
   public:
3
        disjoint_set(int n) : p(n, -1) {}
        int root(int i) { return p[i] >= 0 ? p[i] = root(p[i]) : i; }
        bool same(int i, int j) { return root(i) == root(j); }
        int size(int i) { return -p[root(i)]; }
       void merge(int i, int j) {
           i = root(i), j = root(j);
10
           if (i == j) return;
           if (p[i] > p[j]) swap(i, j);
11
12
           p[i] += p[j], p[j] = i;
13
   };
14
```

6.2 Meldable Heap

```
template <class T>
    class meldable_heap {
        struct node {
            node *1 = NULL, *r = NULL;
            T val:
            node(const T& val) : val(val) {}
            ~node() { delete 1, delete r; }
        };
        node *meld(node *a, node *b) {
            if (!a) return b;
10
            if (!b) return a;
11
            if (a->val > b->val) swap(a, b);
12
13
            a \rightarrow r = meld(a \rightarrow r, b);
            swap(a->1, a->r);
14
15
            return a;
16
17
        node *root = NULL;
        meldable_heap(node *root) : root(root) {}
18
    public:
19
        meldable_heap() {}
20
21
        bool empty() const { return !root; }
22
        const T& top() const { return root->val; }
        void meld(const meldable_heap<T>&& t) { root = meld(root, t.root); }
23
        void push(const T& val) { root = meld(root, new node(val)); }
24
        void pop() {
25
26
            node *t = root;
            root = meld(t->1, t->r);
27
28
            t.l = t.r = NULL;
29
            delete t:
30
31
   };
```

6.3 Binary-Indexed-Tree

0-indexed

```
template < class T> struct bit {
        int n;
        vector<T> dat;
        bit(int n) : n(n) { dat.assign(n,0); }
        // sum [0,i)
       T sum(int i){
            int ret = 0;
            for(--i; i \ge 0; i = (i&(i+1))-1) ret += bit[i];
10
            return ret:
11
12
        // sum [i,j)
        T sum(int i, int j){ return sum(j) - sum(i);}
13
        // add x to i
14
        void add(int i, T x){ for(; i < n; i|=i+1) bit[i] += x;}</pre>
15
16
   };
```

6.4 Segment Tree

区間 add と RMO ができる.

```
template < class T > struct segtree {
int N;
```

```
vector<T> dat, sum;
        segtree(int n) {
            N = 1:
            while (N < n) N <<= 1;
7
            dat.assign(2*N-1,0);
            sum.assign(2*N-1,0);
        void add(int a, int b, T x) { add(a,b,x,0,0,N);}
10
11
        T add(int a, int b, T x, int k, int l, int r) {
            if(b <= l or r <= a) return dat[k];</pre>
12
            if(a \le 1 \text{ and } r \le b) {
13
14
                 sum[k] += x;
                 return dat[k] += x;
15
16
            int m = (1+r)/2;
17
            return dat[k] = min(add(a,b,x,2*k+1,1,m),add(a,b,x,2*k+2,m,r))+sum[k];
18
19
20
        T minimum(int a, int b) { return minimum(a,b,0,0,N);}
        T minimum(int a, int b, int k, int l, int r) {
21
22
            if(b <= 1 or r <= a) return 1e9;
            if(a <= 1 and r <= b) return dat[k];</pre>
23
24
            int m = (1+r)/2;
            return min(minimum(a,b,2*k+1,1,m),minimum(a,b,2*k+2,m,r))+sum[k];
25
26
27
   };
```

6.5 Sparse table

```
const int N = 200010;
   const int K = 18;
   int st[K][N];
   void construct(int *a, int n) {
       copy_n(a, n, st[0]);
       repi(k, 1, K) {
           for (int i = 0; i+(1 << k) <= n; ++i) {
                st[k][i] = min(st[k-1][i], st[k-1][i+(1<<(k-1))]);
10
11
12
   int query(int a, int b) {
       int k = 31-__builtin_clz(b-a);
14
        return min(st[k][a], st[k][b-(1<<k)]);</pre>
15
```

6.6 RBST

```
struct node {
         long val, sum;
         size_t size = 1;
        node *left = NULL, *right = NULL;
        node(long val) : val(val). sum(val) {}
         ~node() { delete left, delete right; }
   inline long sum(node *u) { return u ? u->sum : 0; }
    inline size_t size(node *u) { return u ? u->size : 0; }
   inline node *pull(node *u) {
        u \rightarrow sum = u \rightarrow val + sum(u \rightarrow left) + sum(u \rightarrow right);
        u \rightarrow size = 1 + size(u \rightarrow left) + size(u \rightarrow right):
12
13
        return u:
14
node *merge(node *u, node *v) {
```

18

```
if (!u) return v;
16
       if (!v) return u;
17
       if (rand() * long(size(u) + size(v)) < long(size(u)) * RAND_MAX) {</pre>
18
            u->right = merge(u->right, v);
19
20
            return pull(u);
21
       } else {
22
            v \rightarrow left = merge(u, v \rightarrow left);
23
            return pull(v):
24
25
   pair<node*,node*> split(node *u, size_t k) {
26
       if (!u or k == 0) return {NULL, u};
27
       if (k == size(u)) return {u, NULL};
28
       if (size(u->left) >= k) {
29
            auto p = split(u->left, k);
30
            u->left = p.second;
31
            return {p.first, pull(u)};
32
33
       } else {
            auto p = split(u->right, k - size(u->left) - 1);
34
35
            u->right = p.first;
            return {pull(u), p.second};
36
37
38
   template <class ForwardIterator>
39
40
   node *construct_from(ForwardIterator first, ForwardIterator last) {
       if (first == last) return NULL;
41
       auto mid = next(first, (last - first) / 2);
42
       node *u = new node(*mid);
43
       u->left = construct_from(first, mid);
44
45
       u->right = construct_from(next(mid), last);
       return pull(u);
46
47 }
```

6.7 永続 RBST

```
template <class T, size_t N>
   struct mempool {
       static T buf[N], *head;
       static size_t cnt() { return head - buf; }
       static void clear() { head = buf: }
       void *operator new(size_t _ __attribute__((unused))) { return head++; }
       void operator delete(void *_ __attribute__((unused))) {}
   template <class T, size_t N> T mempool<T, N>::buf[N];
   template <class T, size_t N> T *mempool<T, N>::head = mempool<T, N>::buf;
11
   struct node;
12
13 | long sum(node *u);
   size_t size(node *u);
   struct node : mempool<node, M> {
15
       const long val = 0, sum = 0, lazy = 0;
16
       const size_t size = 1;
17
       node *const left = NULL, *const right = NULL;
18
19
       node(long val) : val(val), sum(val) {}
20
21
       node(long val. long lazv. node *left. node *right)
22
            : val(val),
             sum(val + ::sum(left) + ::sum(right)),
23
24
             lazv(lazv).
             size(1 + ::size(left) + ::size(right)),
25
26
             left(left).
27
             right(right) {}
28 };
29 | inline long sum(node *u) { return u ? u->sum + u->lazy * u->size : 0; }
```

```
30 | inline size_t size(node *u) { return u ? u->size : 0; }
   inline node *add(node *u, long x) { return u ? new node(u->val, u->lazy + x, u->left, u
        ->right) : NULL: }
   node *merge(node *u, node *v) {
32
       if (!u) return v;
33
34
        if (!v) return u:
35
        if (rand() * long(size(u) + size(v)) < long(size(u)) * RAND_MAX) {</pre>
            return new node(u->val + u->lazy, 0, add(u->left, u->lazy), merge(add(u->right,
36
                u \rightarrow lazy), v));
       } else {
37
            return new node(v->val + v->lazy, 0, merge(u, add(v->left, v->lazy)), add(v->
38
                right, v->lazy));
39
40
   }
   pair<node *, node *> split(node *u, size_t k) {
41
       if (!u or k == 0) return {NULL, u};
43
        if (k == size(u)) return {u, NULL};
        if (size(u->left) >= k) {
44
            auto p = split(add(u->left, u->lazy), k);
45
            return {p.first, new node(u->val + u->lazy, 0, p.second, add(u->right, u->lazy
46
       } else {
47
            auto p = split(add(u->right, u->lazy), k - size(u->left) - 1);
48
            return {new node(u->val + u->lazy, 0, add(u->left, u->lazy), p.first), p.second
49
50
51
   }
   template <class OutputIterator>
   OutputIterator dump(OutputIterator it, const node *u, long lazy = 0) {
54
        if (!u) return it;
55
        lazy += u->lazy;
56
        it = dump(it, u->left, lazy);
57
        *it++ = u->val + lazy;
58
        return dump(it, u->right, lazy);
59
   template <class ForwardIterator>
   node *construct_from(ForwardIterator first, ForwardIterator last) {
        if (first == last) return NULL;
        auto mid = next(first, (last - first) / 2);
64
        return new node(*mid, 0, construct_from(first, mid), construct_from(next(mid), last
65
```

6.8 赤黒木

```
template < class T> class rbtree {
        enum COL { BLACK, RED,};
        struct node {
           T val, lazy, min_val;
            int color, rnk, size;
            node *left, *right;
            // if !left then this node is leaf
            node(T v) : val(v), min_val(v), color(BLACK), rnk(0), size(1) {
10
                lazy = 0;
11
                left = right = NULL:
12
            node(node *1, node *r, int c) : color(c) {
13
14
                lazv = 0:
                left = 1;
15
                right = r:
16
17
                update();
18
19
            void update() {
```

```
20
                 eval();
                 if(left) {
21
                      rnk = max(left->rnk+(left->color==BLACK).
22
                                 right -> rnk + (right -> color == BLACK));
23
24
                      size = left->size+right->size;
                      left->eval(); right->eval();
25
                      min_val = min(left->min_val, right->min_val);
26
27
                 }
28
             void eval() {
29
                 min_val += lazy;
30
                 if(!left) val += lazy;
31
32
                 else {
                      left->lazy += lazy;
33
                      right->lazy += lazy;
34
35
                 lazy = 0;
36
37
        };
38
39
        node *new_node(T v) { return new node(v);}
40
        node *new_node(node *1, node *r, int c) { return new node(1,r,c);}
41
        node *rotate(node *v, int d) {
42
             node *w = d? v->right: v->left;
43
44
             if(d) {
                 v->right = w->left;
45
46
                 w \rightarrow left = v;
                 v->right->update();
47
48
49
             else {
                 v \rightarrow left = w \rightarrow right;
50
51
                 w->right = v;
52
                 v->left->update();
53
54
             v->update(): w->update():
55
             v \rightarrow color = RED:
             w->color = BLACK;
56
57
             return w:
58
59
        node *merge_sub(node *u, node *v) {
60
             u->eval(); v->eval();
             if(u->rnk < v->rnk) {
61
                 node *w = merge_sub(u,v->left);
62
                 v \rightarrow left = w:
63
64
65
                 if(v->color == BLACK and w->color == RED and w->left->color == RED) {
                      if(v->right->color == BLACK) return rotate(v,0);
66
67
                      else {
68
                          v \rightarrow color = RED:
                          v->left->color = v->right->color = BLACK;
69
70
                          return v;
71
                      }
                 }
72
73
                 else return v:
74
75
             else if(u->rnk > v->rnk) {
76
                 node *w = merge_sub(u->right,v);
                 u \rightarrow right = w;
77
78
                 u->update();
                 if(u->color == BLACK and w->color == RED and w->right->color == RED) {
79
                      if(u->left->color == BLACK) return rotate(u,1);
80
81
                      else {
                          u \rightarrow color = RED:
82
                          u->left->color = u->right->color = BLACK;
83
                          return u:
84
85
                 }
86
```

```
87
                 else return u;
88
89
             else return new node(u.v.RED):
90
91
        node *insert(node *v, int k) {
             auto p = split(root,k);
92
93
             return root = merge(merge(p.first,v),p.second);
94
95
        void add(node *v, int res, T val) {
             if(res < 1) return;</pre>
96
97
             v->eval();
             if(v->size == res) {
98
99
                 v->lazy += val;
100
                 return:
101
             add(v->left, min(v->left->size, res), val);
102
             add(v->right, res-v->left->size, val);
103
             v->update();
104
105
        T get(node *v, int k) {
106
             v->eval();
107
             if(!v->left) return v->val;
108
             if(v->left->size > k) return get(v->left, k);
109
             return get(v->right, k-v->left->size);
110
111
        T minimum(node *v, int 1, int r) {
112
             if(r-1 < 1) return inf;</pre>
113
             v->eval();
114
             if(v->size == r-1) return v->min_val;
115
116
             return min(minimum(v->left, 1, min(r, v->left->size)),
                        minimum(v->right, l-min(l, v->left->size), r-v->left->size));
117
118
119
        T inf:
    public:
120
121
122
        node *root:
123
124
             inf = (((1LL << (sizeof(T)*8-2))-1) << 1)+1;
125
             root = NULL;
126
127
         void clear() { delete root; root = NULL;}
        node *build(const vector<T> &vs) {
128
129
             if(!vs.size()) return root = NULL;
130
             if((int)vs.size() == 1) return root = new node(vs[0]):
131
             int m = vs.size()/2;
132
             return root = merge(build(vector<T>(begin(vs),begin(vs)+m)),
                                  build(vector<T>(begin(vs)+m,end(vs))));
133
134
135
         int size() { return root? root->size: 0:}
         node *push_back(T val) { return root = merge(root,new_node(val));}
136
137
        node *push_front(T val) { return root = merge(new_node(val),root);}
        node *merge(node *u, node *v) {
138
139
             if(!u) return v;
             if(!v) return u:
140
141
             u = merge_sub(u,v);
142
             u \rightarrow color = BLACK;
143
             return u:
144
        pair<node*, node*> split(node *v, int k) {
145
146
             if(!k) return pair<node*,node*>(NULL,v);
             if(k == v->size) return pair<node*, node*>(v, NULL);
147
148
             v->eval():
             if(k < v->left->size) {
149
150
                 auto p = split(v->left,k);
151
                 return pair<node*,node*>(p.first,merge(p.second,v->right));
152
             else if(k > v->left->size) {
153
```

20

```
auto p = split(v->right,k-v->left->size);
154
                return pair<node*,node*>(merge(v->left,p.first),p.second);
155
156
            else return pair<node*,node*>(v->left,v->right);
157
        }
158
159
        node *insert(int k, T val) { return insert(new_node(val),k);}
160
        node *erase(int k) {
161
            auto p = split(root,k+1);
162
            return root = merge(split(p.first,k).first, p.second);
163
164
        void add(int 1, int r, T val) { add(root, r, val); add(root, 1, -val);}
165
        T get(int k) { return get(root, k);}
166
        T minimum(int 1, int r) { return minimum(root, 1, r);}
167
        T operator[](const int &i) { return get(i);}
168
169
   };
```

6.9 永続赤黒木

```
//const int MAX = 15000000, BOUND = 14000000;
   template < class T> class prbtree {
   public:
3
        enum COL { BLACK, RED,};
       struct node {
           T val;
            int color;
            int rnk, size;
            node *left, *right;
10
11
            node(){}
            node(T v) : val(v), color(BLACK), rnk(0), size(1) {
12
13
                left = right = NULL;
14
            node(node *1, node *r, int c) : color(c) {
15
                left = 1;
16
17
                right = r;
18
                rnk = max((1? 1->rnk+(1->color==BLACK): 0),
19
                          (r? r->rnk+(r->color==BLACK): 0));
20
                size = !1 and !r? 1: !1? r->size: !r? r->size: 1->size+r->size;
21
       };
22
23
24
       node *root:
25
       //
                  node nodes[MAX]:
26
       //
                  int called:
27
       prbtree() {
28
            root = NULL:
29
            // called = 0;
30
       }
31
32
       prbtree(T val) {
33
34
            root = new_node(val);
35
            // called = 0:
36
37
       // node *new_node(T v) { return &(nodes[called++] = node(v));}
38
       // node *new_node(node *1, node *r, int c) { return &(nodes[called++] = node(1,r,c)
39
40
       node *new_node(T v) { return new node(v);}
       node *new node(node *1. node *r. int c) { return new node(1.r.c):}
41
42
       node *merge_sub(node *u, node *v) {
43
            if(u->rnk < v->rnk) {
44
```

```
node *w = merge_sub(u,v->left);
        if(v->color == BLACK and w->color == RED and w->left->color == RED){
            if(v->right->color == BLACK) return new node(w->left.new node(w->right.
                 v->right, RED), BLACK);
            else return new_node(new_node(w->left,w->right,BLACK),new_node(v->right
                 ->left,v->right->right,BLACK),RED);
        else return new node(w.v->right.v->color):
    else if(u->rnk > v->rnk) {
        node *w = merge_sub(u->right,v);
        if(u->color == BLACK and w->color == RED and w->right->color == RED){
            if(u->left->color == BLACK) return new_node(new_node(u->left,w->left,
                 RED).w->right.BLACK):
            else return new_node(new_node(u->left->left,u->left->right,BLACK),
                 new_node(w->left,w->right,BLACK),RED);
        else return new_node(u->left,w,u->color);
    else return new_node(u,v,RED);
}
node *merge(node *u, node *v) {
    if(!u) return v;
    if(!v) return u;
    u = merge_sub(u,v);
    if(u->color == RED) return new_node(u->left,u->right,BLACK);
    return u;
pair<node*, node*> split(node *v, int k) {
    if(!k) return pair<node*,node*>(NULL,v);
    if(k == v->size) return pair<node*, node*>(v, NULL);
    if(k < v->left->size) {
        auto p = split(v->left.k):
        return pair<node*,node*>(p.first,merge(p.second,v->right));
    else if(k > v->left->size) {
        auto p = split(v->right,k-v->left->size);
        return pair<node*,node*>(merge(v->left,p.first),p.second);
    else return pair<node*,node*>(v->left,v->right);
node *build(const vector<T> &vs) {
    if(!vs.size()) return NULL;
    if((int)vs.size() == 1) return new_node(vs[0]);
    int m = vs.size()/2;
    return merge(build(vector<T>(begin(vs),begin(vs)+m)), build(vector<T>(begin(vs)+
         m, end(vs)));
int size() { return root->size;}
void get(vector<T> &vs) { get(root,vs);}
void get(node *v, vector<T> &vs) {
    if(!v->left and !v->right) vs.push_back(v->val);
    else {
        if(v->left) get(v->left,vs);
        if(v->right) get(v->right, vs);
}
node *push_back(T val) {
    node *v = new node(val):
    return root = merge(root, v);
```

FCCPC Library 21

45

46

47

48

49

50

51

52

53

54

55

56

57 58

59 60

61 62

63

64

65

66

67

68

69

70

71

72

73

74

75

76

77

78

79

80

81

82

83

84

85

87

88

89

90

91

92

93

94

95

96

97

98

99

100

101

102

103

104

105

106

```
107
        // insert leaf at k
108
        node *insert(int k. T val) {
109
            return insert(new_node(val), k);
110
111
112
        // insert tree v at k
113
        node *insert(node *v. int k) {
114
            auto p = split(root,k);
115
            return root = merge(merge(p.first,v),p.second);
116
        }
117
118
119
        // copy [1,r)
        node *copy(int 1, int r) {
120
            return split(split(root, 1).second, r-1).first;
121
122
        // copy and insert [1,r) at k
123
        node *copy_paste(int 1, int r, int k) {
124
            return insert(copy(1,r),k);
125
126
127 };
```

6.10 wavelet 行列

N := 列の長さ M := 最大値

6.10.1 完備辞書

function	計算量
count	<i>O</i> (1)
select	$O(\log N)$

```
template<int N> class FID {
       static const int bucket = 512, block = 16;
       static char popcount[];
       int n, B[N/bucket+10];
       unsigned short bs[N/block+10], b[N/block+10];
   public:
       FID(int n, bool s[]) : n(n) {
            if(!popcount[1]) for (int i = 0; i < (1 < block); i++) popcount[i] =
10
                 __builtin_popcount(i);
11
            bs[0] = B[0] = b[0] = 0;
12
13
            for (int i = 0; i < n; i++) {
14
                if(i%block == 0) {
                    bs[i/block+1] = 0;
15
                    if(i%bucket == 0) {
16
                        B[i/bucket+1] = B[i/bucket];
17
                        b[i/block+1] = b[i/block] = 0;
18
19
20
                    else b[i/block+1] = b[i/block];
21
22
                bs[i/block] |= short(s[i])<<(i%block);</pre>
                b[i/block+1] += s[i];
23
                B[i/bucket+1] += s[i];
24
```

```
25
26
            if(n\%bucket == 0) b[n/block] = 0;
27
        }
28
29
        // number of val in [0,r), O(1)
        int count(bool val, int r) { return val? B[r/bucket]+b[r/block]+popcount[bs[r/block
30
             ]&((1<<(r%block))-1)]: r-count(1,r); }
        // number of val in [1,r), 0(1)
31
32
        int count(bool val, int 1, int r) { return count(val,r)-count(val,1); }
        // position of ith in val, 0-indexed, 0(log n)
33
        int select(bool val, int i) {
34
35
            if(i < 0 or count(val,n) <= i) return -1;</pre>
36
            i++;
37
            int 1b = 0, ub = n, md;
            while(ub-lb>1) {
38
                md = (1b+ub) >> 1;
39
40
                if(count(val,md) >= i) ub = md;
                else lb = md;
41
           }
42
            return ub-1;
43
44
        int select(bool val, int i, int 1) { return select(val,i+count(val,1)); }
45
        bool operator[](int i) { return bs[i/block]>>(i%block)&1; }
46
47
   template<int N> char FID<N>::popcount[1<<FID<N>::block];
```

6.10.2 wavelet 行列

function	計算量	FID::count	FID::select
count	$O(\log M)$	О	
select	$O(\log N \log M)$	О	О
get	$O(\log M)$	0	
maximum	$O(\log M)$ or $O(k \log M)$	0	
kth_number	$O(\log M)$	0	
freq	$O(\log M)$	0	
freq_list	$O(k \log M)$	0	
get_rect	$O(k \log N \log M)$	О	О

```
template < class T, int N, int D> class wavelet {
2
        int n, zs[D];
        FID<N> dat[D];
3
        void max_dfs(int d, int l, int r, int &k, T val, vector<T> &vs) {
            if(1 >= r or !k) return;
            if(d == D) {
                 while (1++ < r \text{ and } k > 0) vs.push_back(val), k--;
10
            int lc = dat[d].count(1,1), rc = dat[d].count(1,r);
11
12
            // if min. change this order
            \max_{dfs(d+1, lc+zs[d], rc+zs[d], k, lULL << (D-d-1)|val,vs);
13
14
            max_dfs(d+1, l-lc, r-rc, k, val, vs);
15
16
        T max dfs(int d. int l. int r. T val. T a. T b) {
17
18
            if(r-1 \le 0 \text{ or val} \ge b) \text{ return } -1:
19
            if(d == D) return val>=a? val: -1;
            int lc = dat[d].count(1,1), rc = dat[d].count(1,r);
20
```

```
21
            T ret = \max_{dfs(d+1, lc+zs[d], rc+zs[d], lULL << (D-d-1)|val, a, b);
22
            if("ret) return ret:
23
             return max dfs(d+1, l-lc, r-rc, val, a, b):
        }
24
25
26
        int freq_dfs(int d, int l, int r, T val, T a, T b) {
27
             if(1 == r) return 0;
28
            if(d == D) return (a <= val and val < b)? r-1: 0:
29
            T \text{ nv} = 1ULL << (D-d-1) | val, nnv = ((1ULL << (D-d-1)) -1) | nv;
            if(nnv < a or b <= val) return 0;</pre>
30
            if(a <= val and nnv < b) return r-1;</pre>
31
             int lc = dat[d].count(1,1), rc = dat[d].count(1,r);
32
             return freq_dfs(d+1,1-lc,r-rc,val,a,b)+
33
                    freq_dfs(d+1,lc+zs[d],rc+zs[d],nv,a,b);
34
        }
35
36
37
        void list_dfs(int d, int l, int r, T val, T a, T b, vector<pair<T,int>> &vs) {
             if(val >= b or r-l <= 0) return;
38
            if(d == D) {
39
                 if(a <= val) vs.push_back(make_pair(val,r-1));</pre>
40
41
                 return:
42
            T \ nv = val | (1LL << (D-d-1)), \ nnv = nv | (((1LL << (D-d-1))-1));
43
            if(nnv < a) return:</pre>
44
45
             int lc = dat[d].count(1,1), rc = dat[d].count(1,r);
            list_dfs(d+1,1-lc,r-rc,val,a,b,vs);
46
             list_dfs(d+1,lc+zs[d],rc+zs[d],nv,a,b,vs);
47
48
49
    public:
50
        wavelet(int n, T seq[]) : n(n) {
            T f[N], l[N], r[N];
51
52
            bool b[N];
53
            memcpy(f, seq, sizeof(T)*n);
             for (int d = 0; d < D; d++) {
54
55
                 int 1h = 0, rh = 0;
56
                 for (int i = 0; i < n; i++) {
                     bool k = (f[i] >> (D-d-1))&1;
57
58
                     if(k) r[rh++] = f[i];
59
                     else l[lh++] = f[i];
60
                     b[i] = k;
61
                 dat[d] = FID < N > (n,b);
62
                 zs[d] = lh;
                 swap(1.f):
64
                 memcpy(f+lh, r, rh*sizeof(T));
65
66
67
        }
68
69
        T get(int i) {
            T ret = 0;
70
71
             bool b;
             for (int d = 0; d < D; d++) {
72
73
                ret <<= 1;
                 b = dat[d][i]:
74
75
                 ret |= b:
76
                 i = dat[d].count(b,i)+b*zs[d];
77
78
            return ret;
79
80
        T operator[](int i) { return get(i); }
81
        int count(T val, int l, int r) {
82
             for (int d = 0: d < D: d++) {
83
84
                 bool b = (val >> (D-d-1))&1;
85
                 1 = dat[d].count(b.1)+b*zs[d]:
                 r = dat[d].count(b,r)+b*zs[d];
86
87
```

```
88
             return r-1;
89
90
         int count(T val. int r) { return count(val.0.r): }
91
92
         int select(T val, int k) {
93
             int ls[D], rs[D], l = 0, r = n:
             for (int d = 0; d < D; d++) {
94
95
                 ls[d] = 1; rs[d] = r;
96
                 bool b = val >> (D-d-1)&1:
97
                 1 = dat[d].count(b,1)+b*zs[d];
                  r = dat[d].count(b,r)+b*zs[d];
98
99
             for (int d = D-1; d >= 0; d--) {
100
                  bool b = val >> (D-d-1)&1:
101
                  k = dat[d].select(b,k,ls[d]);
102
                 if(k >= rs[d] \text{ or } k < 0) \text{ return } -1;
103
                 k -= ls[d];
104
105
             }
106
             return k:
107
         int select(T val, int k, int l) { return select(val,k+count(val,l)); }
108
109
         vector<T> maximum(int 1, int r, int k) {
110
             if (r-1 < k) k = r-1;
111
112
             if(k < 0) return {};
             vector<T> ret;
113
             max_dfs(0,1,r,k,0,ret);
114
             return ret;
115
116
117
         T maximum(int 1, int r, T a, T b) { return max_dfs(0,1,r,0,a,b); }
118
119
120
         // k is 0-indexed
         T kth_number(int 1, int r, int k) {
121
122
             if(r-1 \le k \text{ or } k < 0) \text{ return } -1:
123
             T ret = 0:
124
             for (int d = 0; d < D; d++) {
                  int lc = dat[d].count(1,1), rc = dat[d].count(1,r);
125
126
                  if(rc-lc > k) {
127
                      1 = 1c + zs[d];
128
                      r = rc + zs[d];
                      ret |= 1ULL << (D-d-1);
129
130
                  else {
131
                      k -= rc-lc;
132
133
                     1 -= lc:
134
                      r -= rc;
135
136
             }
137
             return ret;
        }
138
139
140
         vector<pair<T,int>> freq_list(int 1, int r, T a, T b) {
             vector<pair<T.int>> ret:
141
142
             list_dfs(0,1,r,0,a,b,ret);
143
             return ret:
144
        }
145
         vector<pair<int,T>> get_rect(int 1, int r, T a, T b) {
146
147
             vector<pair<T,int>> res = freq_list(l,r,a,b);
148
             vector<pair<int,T>> ret;
149
             for(auto &e: res)
150
                  for (int i = 0: i < e.second: i++)
151
                      ret.push_back(make_pair(select(e.first,i,l), e.first));
152
             return ret:
153
         // number of elements in [1,r) in [a,b), O(D)
154
```

```
int freq(int 1, int r, T a, T b) { return freq_dfs(0,1,r,0,a,b); }
int freq(int 1, int r, T a, T b) { return freq_dfs(0,1,r,0,a,b); }
int freq(int 1, int r, T a, T b) { return freq_dfs(0,1,r,0,a,b); }
```

7 その他

7.1 ビジュアライザ

8 Verdict 別チェックリスト

8.1 Wrong Answer

- コーナーケースはないか?
- 解なしの扱いは正しいか?
 - 処理を抜けているかにも注意
- 初期化したか? またそれは適切か?
 - とくに複数テストケースのとき
- タイプミスはないか?
- 出力形式は正しいか?
- 入力を破壊して,出力に影響していないか?
- オーバーフローの危険性はないか?
 - **-** 1 << n にも注意
- 計算誤差は許容範囲内か?
 - inf,eps がらみの演算は危険! 原則として大小比較でしか使わない
- 使っていない変数はないか?
 - 始点 s など
- DP の更新順は正しいか?

8.2 Time Limit Exceeded

- 計算量は許容範囲内か?
 - テストケースの数にも注意
- 入力はボトルネックにならないか?
- メモ化を忘れていないか?
- 無限ループの危険性はないか?
- ボトルネックを定数倍高速化できないか?
 - int < long long ≪ double</pre>

8.3 Runtime Error/Segmentation Fault

- 配列やコンテナのサイズは適切か?
- 負の添字にアクセスしていないか?
- ◆ 入力は正しく受け取れているか?
 - getline の前に cin.ignore()
- スタックオーバーフローの危険性はないか?
 - 再帰が深くなることはないか?
 - 訪問済みフラグを立て忘れていないか?

8.4 出力が壊滅的なとき

- return を忘れていないか?
- 1-origin を直し忘れていないか?
- 添字に間違いはないか?
- 変数名は衝突していないか?
- 演算子の優先順位に間違いはないか?
 - (1 << n) 1, (x & y) == z

8.5 そもそも解けないとき

- 題意把握に間違いはないか?
- 制約条件を見逃していないか?

8.6 解法メモ

辞書順最小の解 解の存在判定

集合の 2-分割 最小カット

重複が k 個以下の区間 k-最小費用流

高速化 Segment Tree · Doubling · Monge 性

その他 とりあえずソート・逆から解く・LP 定式化