

# 1. Arrays

- **Description:** Collection of elements identified by index.
- **Operations:**
  - Access: `array[i]`
  - Insertion: Add at the end or specific index.
  - Deletion: Remove from the end or specific index.
  - Traversal: Loop through elements.
- **Time Complexities:**
  - Access:  $O(1)$
  - Insertion:  $O(1)$  (end),  $O(n)$  (middle)
  - Deletion:  $O(1)$  (end),  $O(n)$  (middle)
  - Search:  $O(n)$
- **Applications:** Lookup tables, matrices, database indexing.

# 2. Linked Lists

- **Description:** Sequence of nodes, each containing data and a reference to the next node.
- **Types:** Singly, Doubly, Circular.
- **Operations:**
  - Insertion: Add node at the beginning, end, or middle.
  - Deletion: Remove node from beginning, end, or middle.
  - Traversal: Loop through nodes.
- **Time Complexities:**
  - Access:  $O(n)$
  - Insertion:  $O(1)$  (beginning),  $O(n)$  (end or middle)
  - Deletion:  $O(1)$  (beginning),  $O(n)$  (end or middle)
  - Search:  $O(n)$
- **Applications:** Implementing stacks and queues, adjacency lists in graphs.

# 3. Stacks

- **Description:** Collection of elements with Last-In-First-Out (LIFO) access.
- **Operations:**
  - Push: Add element to the top.
  - Pop: Remove element from the top.
  - Peek: Access top element.
- **Time Complexities:**
  - Push:  $O(1)$
  - Pop:  $O(1)$

- Peek:  $O(1)$
- **Applications:** Function call management, undo mechanisms, syntax parsing.

## 4. Queues

- **Description:** Collection of elements with First-In-First-Out (FIFO) access.
- **Types:** Simple, Circular, Priority.
- **Operations:**
  - Enqueue: Add element to the rear.
  - Dequeue: Remove element from the front.
  - Front: Access front element.
- **Time Complexities:**
  - Enqueue:  $O(1)$
  - Dequeue:  $O(1)$
  - Front:  $O(1)$
- **Applications:** Scheduling tasks, resource management, buffering.

## 5. Trees

- **Description:** Hierarchical structure with nodes connected by edges.
- **Types:** Binary Tree, Binary Search Tree (BST), AVL Tree, Red-Black Tree, Heap, Trie.
- **Operations:**
  - Insertion: Add a node.
  - Deletion: Remove a node.
  - Traversal: In-order, Pre-order, Post-order.
  - Search: Find a node.
- **Time Complexities:**
  - Insertion:  $O(\log n)$  for balanced trees,  $O(n)$  for unbalanced.
  - Deletion:  $O(\log n)$  for balanced trees,  $O(n)$  for unbalanced.
  - Search:  $O(\log n)$  for balanced trees,  $O(n)$  for unbalanced.
  - Traversal:  $O(n)$
- **Applications:** Hierarchical data representation, databases (B-trees), memory management (heaps).

## 6. Graphs

- **Description:** Set of vertices connected by edges.
- **Types:** Directed, Undirected, Weighted, Unweighted.
- **Representations:** Adjacency Matrix, Adjacency List.
- **Operations:**
  - Traversal: Depth-First Search (DFS), Breadth-First Search (BFS).

- Shortest Path: Dijkstra's, Bellman-Ford, Floyd-Warshall.
- Minimum Spanning Tree: Kruskal's, Prim's.
- **Time Complexities:**
  - Traversal:  $O(V + E)$
  - Shortest Path:  $O(E + V \log V)$  for Dijkstra's,  $O(V^3)$  for Floyd-Warshall.
  - MST:  $O(E \log V)$  for Kruskal's and Prim's.
- **Applications:** Network routing, social networks, dependency resolution.

## 7. Hashing

- **Description:** Technique to map keys to array indices using hash functions.
- **Collision Resolution:** Chaining, Open Addressing.
- **Operations:**
  - Insertion: Add key-value pair.
  - Deletion: Remove key-value pair.
  - Search: Find value by key.
- **Time Complexities:**
  - Insertion:  $O(1)$
  - Deletion:  $O(1)$
  - Search:  $O(1)$
- **Applications:** Implementing dictionaries, caches, database indexing.

## 8. Heaps

- **Description:** Complete binary tree used for priority queues.
- **Types:** Min-Heap, Max-Heap.
- **Operations:**
  - Insertion: Add an element.
  - Deletion: Remove root element.
  - Peek: Access root element.
- **Time Complexities:**
  - Insertion:  $O(\log n)$
  - Deletion:  $O(\log n)$
  - Peek:  $O(1)$
- **Applications:** Priority queues, graph algorithms (Dijkstra's, Prim's).

## Summary Table

Data Structure	Access	Search	Insertion	Deletion	Applications
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<b>Array</b>	$O(1)$	$O(n)$	$O(1)/O(n)$	$O(1)/O(n)$	Matrices, lookup tables
<b>Linked List</b>	$O(n)$	$O(n)$	$O(1)$	$O(1)$	Implementing stacks/queues, graphs
<b>Stack</b>	$O(n)$	$O(n)$	$O(1)$	$O(1)$	Function calls, undo mechanisms
<b>Queue</b>	$O(n)$	$O(n)$	$O(1)$	$O(1)$	Scheduling, buffering
<b>Binary Tree</b>	$O(\log n)$	$O(\log n)$	$O(\log n)$	$O(\log n)$	Hierarchical data, databases
<b>BST</b>	$O(\log n)$	$O(\log n)$	$O(\log n)$	$O(\log n)$	Searching, sorting
<b>Heap</b>	$O(n)$	$O(n)$	$O(\log n)$	$O(\log n)$	Priority queues, sorting
<b>Hash Table</b>	$O(1)$	$O(1)$	$O(1)$	$O(1)$	Dictionaries, caching
<b>Graph</b>	$O(V+E)$	$O(V+E)$	$O(V+E)$	$O(V+E)$	Network routing, dependencies

## Additional Notes

- **Time Complexity Notation:**  $O(1)$  is constant,  $O(n)$  is linear,  $O(\log n)$  is logarithmic,  $O(V + E)$  is for graph traversals where V is vertices and E is edges.
- **Balanced vs. Unbalanced Trees:** Balanced trees maintain  $O(\log n)$  operations, unbalanced can degrade to  $O(n)$ .
- **Choosing the Right Structure:** Depends on specific needs like speed, memory usage, and type of operations frequently performed.