Supplementary Material for QFib: Fast and Efficient Brain Tractogram Compression

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1 Detailed tables.

In this section, we add more details on the tables presented in the articles. They are referenced using the same numbers. We added the 1.0 mm stepsize and the 60k streamlines datasets.

Stepsize δ		$0.1 \mathrm{mm}$			$0.2 \mathrm{\ mm}$			0.5 mm		1.0 mm			
Nb. of streamlines	60k	500k	3M	60k	500k	3M	60k	500k	3M	60k	500k	3M	
Size of input file (GB)													
Deterministic	0.46	3.80	22.8	0.23	1.92	11.5	0.10	0.84	5.01	0.06	0.49	2.94	
Probabilistic	0.52	4.36	26.2	0.28	2.35	14.1	0.15	1.26	7.53	0.12	1.03	6.16	
Maximum angle (°)													
Deterministic	7.20	7.20	7.20	14.4	14.4	14.4	36.0	36.0	36.0	72.0	72.0	72.0	
Probabilistic	14.3	14.3	14.4	28.5	28.6	28.8	70.8	71.5	71.6	142	144	144	

Table 1: Size of the files (tck format) and maximum angle of each tractogram.

Stepsiz	$pprox \delta$		$0.1 \mathrm{mm}$	Į.		0.2 mm	Į.		0.5 mm		$1.0~\mathrm{mm}$		
Nb. of stre	amlines	60k	500k	3M	60k	500k	3M	60k	500k	3M	60k	500k	3M
				Maxim	um err	or (×10	^{-2}mm)					
Quantization	Precision		Deterministic										
Fibonacci	8 bits	4.94	4.94	5.30	10.0	10.3	10.6	32.1	33.2	34.1	75.8	81.0	88.0
Fiboliacci	16 bits	0.54	0.50	0.57	0.25	0.28	0.28	0.36	0.39	0.38	1.26	1.39	1.42
Octahedral	8 bits	7.27	7.53	8.03	15.1	16.5	16.5	48.2	46.7	51.0	122	127	129
Octanedrai	16 bits	0.55	0.50	0.56	0.25	0.27	0.29	0.50	0.50	0.52	1.82	1.81	1.91
Quantization	Precision						Proba	bilistic					
Fibonacci	8 bits	2.94	3.04	2.95	5.33	5.86	5.91	18.2	19.7	20.6	39.4	41.8	44.4
Fiboliacci	16 bits	0.12	0.13	0.14	0.13	0.14	0.16	0.66	0.69	0.72	1.90	2.06	2.08
Octahedral	8 bits	4.74	4.79	4.90	8.48	8.55	9.38	29.6	29.8	31.7	63.0	63.6	67.1
Octanedrai	16 bits	0.12	0.13	0.14	0.16	0.17	0.19	0.82	0.87	0.93	2.51	2.66	2.83
				Avera	ge erro	r (×10 ⁻	$^{-3}mm)$						
Quantization	Precision						Detern	$_{ m ninistic}$					
Fibonacci	8 bits	10.4	2.54	0.52	25.7	9.10	2.04	79.5	55.8	9.76	184	153	38.9
1 iboliacci	16 bits	0.23	0.10	0.03	0.26	0.10	0.03	1.09	0.47	0.11	3.99	3.04	0.57
Octahedral	8 bits	14.7	3.12	0.55	37.0	12.4	2.29	116	66.8	18.8	270	216	64.6
Octanediai	16 bits	0.23	0.10	0.03	0.27	0.10	0.03	1.19	0.64	0.15	4.39	3.27	1.01
Quantization	Precision						Proba	bilistic					
Fibonacci	8 bits	11.2	1.35	0.22	21.3	5.01	0.83	57.9	19.2	3.73	112	46.5	8.66
1 iboliacci	16 bits	0.14	0.04	0.01	0.37	0.08	0.01	2.04	0.63	0.16	6.53	2.87	0.48
Octahedral	8 bits	13.4	2.69	0.45	35.0	5.21	1.11	84.4	37.5	6.26	148	68.8	15.3
Octanedral	16 bits	0.16	0.04	0.01	0.43	0.08	0.02	2.31	0.94	0.20	7.28	2.94	0.59

Table 2: Maximum and average errors of our method depending on the dataset, precision in bits and quantization method.

Step	psize δ 0.1 mm					0.2 mm	l		0.5 mm	l	$1.0~\mathrm{mm}$		
Nb. of st	treamlines	60k	500k	3M	60k	500k	3M	60k	500k	3M	60k	500k	3M
				Compr	ession 1	ratios (i	n perce	ntage)					
Method	Precision		Deterministic										
qfib	8 bits	91.4	91.4	91.4	91.1	91.1	91.1	90.4	90.4	90.4	89.6	89.5	89.5
qiib	16 bits	83.1	83.1	83.1	82.8	82.8	82.8	82.2	82.3	82.2	81.5	81.4	81.4
zfib	same*	78.5	N/A	N/A	78.4	78.4	N/A	96.7	96.6	96.8	96.2	96.3	96.3
2110	0.2 mm	98.1	98.1	98.1	95.9	95.9	96.0	87.5	87.5	87.5	74.2	74.2	N/A
Method	Precision						Proba	bilistic					
qfib	8 bits	91.4	91.4	91.4	91.2	91.2	91.2	90.8	90.8	90.8	90.7	90.7	90.6
qiib	16 bits	83.1	83.1	83.1	82.9	82.9	82.9	82.6	82.6	82.6	82.5	82.4	82.4
zfib	same*	78.1	N/A	N/A	78.0	78.1	N/A	86.8	87.1	N/A	87.4	87.6	88.5
	0.2 mm	96.0	96.0	N/A	88.7	88.7	N/A	69.9	69.9	N/A	67.9	67.9	N/A

same*: same error than qfib when using an 8 bit octahedral quantization (Table.2).

Table 3: Compression ratios of \mathtt{qfib} and \mathtt{zfib} . The N/A values are the ones for which the algorithm was not able to perform the compression and decompression.

Stepsi	ze δ		0.1 mm			0.2 mm			0.5 mm		1.0 mm			
Nb. of stre	eamlines	60k	500k	3M	60k	500k	3M	60k	500k	3M	60k	500k	3M	
Compression time (s)														
	qfib (fibo)	2.94	24.1	144	1.50	12.8	74.8	0.66	5.49	32.0	0.42	3.28	19.04	
Deterministic	qfib (octa)	0.94	7.83	46.5	0.50	3.81	22.6	0.21	1.67	9.76	0.12	0.98	6.00	
	zfib	84.1	702	4243	46.3	387	2284	45.7	387	2373	57.8	475.2	N/A	
	qfib (fibo)	3.40	27.9	167	1.90	15.3	90.6	1.04	8.27	49.7	0.85	6.82	40.6	
Probabilistic	qfib (octa)	1.09	8.61	54.7	0.60	4.86	29.0	0.31	2.53	15.5	0.25	2.05	12.7	
	zfib	104	910	N/A	127	1052	N/A	174	1418	N/A	147	1252	N/A	
				Dece	ompress	ion time	e (s)							
	qfib (fibo)	0.61	4.98	30.1	0.32	2.61	15.4	0.15	1.14	6.79	0.09	0.70	3.97	
Deterministic	qfib (octa)	0.44	3.56	20.7	0.25	1,90	11.3	0.11	0.88	5.30	0.06	0.47	3.09	
	zfib	1.46	12.1	72.7	1.54	12.9	77.1	2.05	17.3	103	2.53	20.9	N/A	
	qfib (fibo)	0.70	5.77	34.9	0.39	3.23	18.9	0.22	1.75	10.3	0.18	1.44	8.37	
Probabilistic	qfib (octa)	0.47	4.08	24.3	0.25	2.24	13.3	0.14	1.29	7.47	0.20	1.06	6.32	
	zfib	3.40	28.5	N/A	5.14	43.0	N/A	7.34	60.8	N/A	6.45	53.6	N/A	

Table 4: Computation times of qfib and zfib. With zfib, we set the maximal error to 0.2 mm. N/A are the values for which the algorithm was not able to perform the full compression and decompression.

Stepsize δ			$0.1~\mathrm{mm}$			$0.2~\mathrm{mm}$			$0.5~\mathrm{mm}$		$1.0 \mathrm{\ mm}$			
Nb. of strea	mlines	60k	500k	3M	60k	500k	3M	60k	500k	3M	60k	500k	3M	
	Average error of FA (in percentage)													
Method	Bits		Deterministic											
qfib	8	0.004	0.004	0.004	0.012	0.008	0.009	0.014	0.023	0.023	0.032	0.040	0.042	
fibonacci	16	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.000	0.000	0.002	0.000	0.001	
qfib	8	0.004	0.006	0.006	0.014	0.012	0.012	0.034	0.033	0.036	0.078	0.069	0.069	
octahedral	16	0.000	0.000	0.000	0.000	0.000	0.000	0.002	0.001	0.000	0.001	0.001	0.000	
zfib	-	2.577	2.506	2.527	2.538	2.572	2.553	2.104	2.200	2.219	1.171	1.211	N/A	
Method	Bits						Proba	bilistic						
qfib	8	0.002	0.002	0.002	0.003	0.004	0.002	0.002	0.003	0.002	0.007	0.005	0.002	
fibonacci	16	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.000	0.000	
qfib	8	0.005	0.003	0.003	0.004	0.005	0.003	0.000	0.004	0.006	0.020	0.006	0.005	
octahedral	16	0.000	0.000	0.000	0.000	0.000	0.000	0.002	0.000	0.000	0.000	0.001	0.000	
zfib	-	0.580	0.575	N/A	0.338	0.347	N/A	0.080	0.077	N/A	0.060	0.068	N/A	

Table 5: Comparison of zfib and qfib for FA computation. We compute the average error in FA computation using a Bresenham-like integration [?].

Stepsiz	$pprox \delta$		$0.1 \mathrm{mm}$	l		0.2 mm			0.5 mm			1.0 mm		
Nb. of stre	amlines	60k	500k	3M	60k	500k	3M	60k	500k	3M	60k	500k	3M	
			Maxi	mum e	rror (ab	solute	value ×	(10^{-2})						
Quantization	Precision		Deterministic											
Fibonacci	8 bits	3.07	3.91	3.93	8.23	7.92	8.32	19.5	22.6	22.9	37.9	49.1	51.4	
Fiboliacci	16 bits	0.23	0.29	0.29	0.11	0.16	0.15	0.18	0.19	0.23	0.59	0.76	0.74	
Octahedral	8 bits	4.52	5.89	6.23	12.6	12.0	12.4	31.7	32.7	32.5	54.0	60.5	67.2	
Octanedrai	16 bits	0.23	0.30	0.29	0.11	0.15	0.15	0.20	0.25	0.28	0.75	0.83	0.91	
Quantization	Precision						Proba	bilistic						
Fibonacci	8 bits	1.99	2.43	2.25	3.69	3.66	3.93	9.10	11.1	12.4	19.4	23.3	25.9	
Fiboliacci	16 bits	0.07	0.09	0.09	0.07	0.09	0.09	0.35	0.44	0.48	0.91	1.23	1.32	
Octahedral	8 bits	3.09	3.48	3.85	5.53	5.61	6.39	14.4	17.6	17.8	26.7	31.3	36.5	
Octanedrai	16 bits	0.07	0.09	0.09	0.08	0.10	0.10	0.39	0.48	0.57	1.21	1.42	1.60	
			Ave	rage err	or (abs	olute va	alue $\times 10^{-3}$)							
Quantization	Precision						Detern	ninistic						
Fibonacci	8 bits	0.46	0.45	0.37	0.99	0.99	0.88	2.72	2.69	2.61	6.08	6.10	6.05	
1 iboliacci	16 bits	0.01	0.01	0.01	0.01	0.01	0.01	0.04	0.04	0.03	0.13	0.13	0.13	
Octahedral	8 bits	0.69	0.67	0.53	1.46	1.45	1.31	3.99	3.95	3.83	8.92	8.95	8.84	
Octanedrai	16 bits	0.01	0.01	0.01	0.01	0.01	0.01	0.04	0.04	0.04	0.14	0.14	0.14	
Quantization	Precision						Proba	bilistic						
Fibonacci	8 bits	0.44	0.44	0.35	0.70	0.70	0.63	1.85	1.87	1.78	3.65	3.64	3.49	
1 iboliacci	16 bits	0.01	0.01	0.00	0.01	0.01	0.01	0.07	0.07	0.06	0.21	0.21	0.20	
Octahedral	8 bits	0.70	0.69	0.54	1.12	1.12	0.99	2.74	2.77	2.63	4.85	4.83	4.64	
Octanedral	16 bits	0.01	0.01	0.01	0.01	0.01	0.01	0.08	0.08	0.07	0.24	0.24	0.23	

 $\begin{tabular}{ll} Table 6: Errors of FA computation between original streamlines and the compressed and decompressed ones using {\tt qfib}. \end{tabular}$

Stepsize δ	0.1 mm			$0.2~\mathrm{mm}$				0.5 mm		$1.0 \mathrm{\ mm}$		
Nb. of streamlines	60k	500k	3M	60k	500k	3M	60k	500k	3M	60k	500k	3M
Compression time (s)												
Deterministic	3.42	29.1	166	1.79	14.3	88.3	0.81	6.82	40.8	0.52	4.25	25.8
Probabilistic	3.95	33.0	192	2.16	17.9	103	1.18	9.99	57.9	1.00	8.14	47.0

 $\label{thm:compression} \mbox{Table 7: Compression times of our out-of-core algorithm ($\tt qfib$) with an 8 bits octahedral quantization. }$