

arrh

```
library(mediation)
```

```
## Warning: package 'mediation' was built under R version 4.2.3
```

```
## Loading required package: MASS
```

```
## Loading required package: Matrix
```

```
## Loading required package: mvtnorm
```

```
## Loading required package: sandwich
```

```
## Warning: package 'sandwich' was built under R version 4.2.3
```

mediation: Causal Mediation Analysis

```
## Version: 4.5.0
```

```
df <- read.csv('C:/Users/lhi30/Haein/2023/YBIGTA/DA/Project/Share/Stat_Analysis/Data_Cleanup/Data_Stat/
head(df)
```

	#	X	kaptCode	Date	electC	electComb	Elec_Con	Elev_Num	Park_Below
##	1	0	A13203302	202210	12384.9951	46682.88	0	0.03685504	0.85012285
##	2	1	A13203303	202210	4845.2439	30853.59	0	0.01941748	0.00000000
##	3	2	A13295201	202210	12872.0258	49366.99	0	0.03870968	0.94193548
##	4	3	A13286107	202210	770.2577	41554.16	0	0.03780069	0.25429553
##	5	4	A13287801	202210	5637.1289	41772.60	0	0.04529617	0.08013937
##	6	5	A13286203	202210	3505.9053	26752.80	1	0.01893939	0.00000000
##			Begin_Date						
##	1		7146						
##	2		12861						
##	3		5532						
##	4		7268						
##	5		9750						
##	6		12392						

```
A = df$Elec_Con
M = df$selectC
Y = df$selectComb
C1 = df$Begin_Date
C2 = df$Elev_Num
C3 = df$Park_Below
```

```
#models
```

```
med = lm(M~A+C1+C2+C3)
```

```
out = lm(Y~A+M+M*A)
```

```
summary(med)
```

```
##
## Call:
## lm(formula = M ~ A + C1 + C2 + C3)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -47715  -5525  -2264   1279   74341
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  7.658e+02  1.484e+03   0.516 0.605820
## A            3.591e+03  6.571e+02   5.465 5.41e-08 ***
## C1           3.065e-01  1.133e-01   2.704 0.006924 **
## C2           7.946e+04  2.141e+04   3.712 0.000213 ***
## C3           7.008e+03  7.731e+02   9.066 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 11250 on 1492 degrees of freedom
## Multiple R-squared:  0.1416, Adjusted R-squared:  0.1393
## F-statistic: 61.55 on 4 and 1492 DF,  p-value: < 2.2e-16
```

```
summary(out)
```

```
##
## Call:
## lm(formula = Y ~ A + M + M * A)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -55932  -6179   1930   8341  148343
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  3.464e+04  7.955e+02  43.545 < 2e-16 ***
## A            7.631e+03  1.438e+03   5.305 1.29e-07 ***
## M            7.835e-01  5.545e-02  14.130 < 2e-16 ***
## A:M          3.684e-01  7.781e-02   4.734 2.41e-06 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 17750 on 1493 degrees of freedom
## Multiple R-squared:  0.3996, Adjusted R-squared:  0.3984
## F-statistic: 331.2 on 3 and 1493 DF,  p-value: < 2.2e-16
```

```

beta0 = coefficients(med)[1]
beta1 = coefficients(med)[2]
theta1 = coefficients(out)[2]
theta2 = coefficients(out)[3]
theta3 = coefficients(out)[4]

```

```

m = 10000
CDE = theta1 + theta3*m
print(CDE)

```

```

##      A
## 11315

```

```

NDE = theta1 + theta3*beta0 + theta3*beta1*0
print(NDE)

```

```

##      A
## 7913.365

```

```

NIE = beta1*theta2 + beta1*theta3*1
print(NIE)

```

```

##      A
## 4136.632

```

```

set.seed(2019122035)
med.out = mediate(med, out, treat = "A", mediator = "M", robustSE = TRUE, sims = 1000)
print(summary(med.out))

```

```

##
## Causal Mediation Analysis
##
## Quasi-Bayesian Confidence Intervals
##
##              Estimate 95% CI Lower 95% CI Upper p-value
## ACME (control)      2.82e+03  1.62e+03   4158.50 <2e-16 ***
## ACME (treated)      4.06e+03  2.04e+03   6568.56 <2e-16 ***
## ADE (control)       1.18e+04  9.52e+03  13827.51 <2e-16 ***
## ADE (treated)       1.30e+04  1.07e+04  15407.28 <2e-16 ***
## Total Effect        1.58e+04  1.34e+04  18441.79 <2e-16 ***
## Prop. Mediated (control) 1.74e-01  1.11e-01    0.25 <2e-16 ***
## Prop. Mediated (treated) 2.53e-01  1.40e-01    0.38 <2e-16 ***
## ACME (average)      3.44e+03  1.85e+03   5244.91 <2e-16 ***
## ADE (average)       1.24e+04  1.04e+04  14408.73 <2e-16 ***
## Prop. Mediated (average) 2.13e-01  1.33e-01    0.30 <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Sample Size Used: 1497
##
##
## Simulations: 1000

```

```

#C1
med = lm(M~C1+A+C2+C3)
out = lm(Y~C1+M+M*C1)
summary(med)

##
## Call:
## lm(formula = M ~ C1 + A + C2 + C3)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -47715  -5525  -2264   1279   74341
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  7.658e+02  1.484e+03   0.516  0.605820
## C1           3.065e-01  1.133e-01   2.704  0.006924 **
## A           3.591e+03  6.571e+02   5.465  5.41e-08 ***
## C2          7.946e+04  2.141e+04   3.712  0.000213 ***
## C3          7.008e+03  7.731e+02   9.066  < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 11250 on 1492 degrees of freedom
## Multiple R-squared:  0.1416, Adjusted R-squared:  0.1393
## F-statistic: 61.55 on 4 and 1492 DF,  p-value: < 2.2e-16

summary(out)

##
## Call:
## lm(formula = Y ~ C1 + M + M * C1)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -59533  -4870   1513   7893  143798
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  4.306e+04  1.507e+03  28.583  < 2e-16 ***
## C1          -8.595e-01  1.746e-01  -4.922  9.51e-07 ***
## M           1.217e+00  6.825e-02  17.827  < 2e-16 ***
## C1:M        -3.497e-05  8.834e-06  -3.959  7.89e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 18010 on 1493 degrees of freedom
## Multiple R-squared:  0.3818, Adjusted R-squared:  0.3805
## F-statistic: 307.3 on 3 and 1493 DF,  p-value: < 2.2e-16

beta0 = coefficients(med)[1]
beta1 = coefficients(med)[2]

```

```
theta1 = coefficients(out)[2]
theta2 = coefficients(out)[3]
theta3 = coefficients(out)[4]
```

```
m = 10000
CDE = theta1 + theta3*m
print(CDE)
```

```
##          C1
## -1.20919
```

```
NDE = theta1 + theta3*beta0 + theta3*beta1*0
print(NDE)
```

```
##          C1
## -0.8862587
```

```
NIE = beta1*theta2 + beta1*theta3*1
print(NIE)
```

```
##          C1
## 0.3728298
```

```
set.seed(2019122035)
med.out = mediate(med, out, treat = "C1", mediator = "M", robustSE = TRUE, sims = 1000)
print(summary(med.out))
```

```
##
## Causal Mediation Analysis
##
## Quasi-Bayesian Confidence Intervals
##
##              Estimate 95% CI Lower 95% CI Upper p-value
## ACME (control)      0.37904   -0.00316      0.86  0.056 .
## ACME (treated)      0.37903   -0.00316      0.86  0.056 .
## ADE (control)      -1.20426   -1.51233     -0.89 <2e-16 ***
## ADE (treated)      -1.20427   -1.51233     -0.89 <2e-16 ***
## Total Effect       -0.82523   -1.36529     -0.10  0.030 *
## Prop. Mediated (control) -0.38910   -3.79169      0.06  0.086 .
## Prop. Mediated (treated) -0.38909   -3.79162      0.06  0.086 .
## ACME (average)      0.37903   -0.00316      0.86  0.056 .
## ADE (average)      -1.20427   -1.51233     -0.89 <2e-16 ***
## Prop. Mediated (average) -0.38910   -3.79166      0.06  0.086 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Sample Size Used: 1497
##
##
## Simulations: 1000
```

```
#C2
```

```
med = lm(M~C2+A+C1+C3)
```

```
out = lm(Y~C2+M+M*C2)
```

```
summary(med)
```

```
##
```

```
## Call:
```

```
## lm(formula = M ~ C2 + A + C1 + C3)
```

```
##
```

```
## Residuals:
```

```
##      Min       1Q   Median       3Q      Max  
## -47715  -5525  -2264   1279   74341
```

```
##
```

```
## Coefficients:
```

```
##              Estimate Std. Error t value Pr(>|t|)  
## (Intercept) 7.658e+02  1.484e+03   0.516 0.605820  
## C2          7.946e+04  2.141e+04   3.712 0.000213 ***  
## A           3.591e+03  6.571e+02   5.465 5.41e-08 ***  
## C1           3.065e-01  1.133e-01   2.704 0.006924 **  
## C3           7.008e+03  7.731e+02   9.066 < 2e-16 ***
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
```

```
## Residual standard error: 11250 on 1492 degrees of freedom
```

```
## Multiple R-squared:  0.1416, Adjusted R-squared:  0.1393
```

```
## F-statistic: 61.55 on 4 and 1492 DF,  p-value: < 2.2e-16
```

```
summary(out)
```

```
##
```

```
## Call:
```

```
## lm(formula = Y ~ C2 + M + M * C2)
```

```
##
```

```
## Residuals:
```

```
##      Min       1Q   Median       3Q      Max  
## -80639  -6298    813   7718  112843
```

```
##
```

```
## Coefficients:
```

```
##              Estimate Std. Error t value Pr(>|t|)  
## (Intercept) 2.608e+04  1.273e+03  20.490 < 2e-16 ***  
## C2          3.640e+05  3.765e+04   9.669 < 2e-16 ***  
## M           7.936e-01  5.816e-02  13.645 < 2e-16 ***  
## C2:M         4.752e+00  1.138e+00   4.177 3.13e-05 ***
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
```

```
## Residual standard error: 17570 on 1493 degrees of freedom
```

```
## Multiple R-squared:  0.4114, Adjusted R-squared:  0.4102
```

```
## F-statistic: 347.8 on 3 and 1493 DF,  p-value: < 2.2e-16
```

```
beta0 = coefficients(med)[1]
```

```
beta1 = coefficients(med)[2]
```

```
theta1 = coefficients(out)[2]
theta2 = coefficients(out)[3]
theta3 = coefficients(out)[4]
```

```
m = 10000
CDE = theta1 + theta3*m
print(CDE)
```

```
##          C2
## 411549.8
```

```
NDE = theta1 + theta3*beta0 + theta3*beta1*0
print(NDE)
```

```
##          C2
## 367664.1
```

```
NIE = beta1*theta2 + beta1*theta3*1
print(NIE)
```

```
##          C2
## 440684.1
```

```
set.seed(2019122035)
med.out = mediate(med, out, treat = "C2", mediator = "M", robustSE = TRUE, sims = 1000)
print(summary(med.out))
```

```
##
## Causal Mediation Analysis
##
## Quasi-Bayesian Confidence Intervals
##
##              Estimate 95% CI Lower 95% CI Upper p-value
## ACME (control)      6.64e+04  -1.06e+04  2.01e+05  0.12
## ACME (treated)      3.24e+05  -2.47e+06  3.30e+06  0.80
## ADE (control)       4.14e+05   3.06e+05  5.12e+05  <2e-16 ***
## ADE (treated)       6.71e+05  -2.22e+06  3.65e+06  0.54
## Total Effect        7.38e+05  -2.04e+06  3.68e+06  0.51
## Prop. Mediated (control) 1.89e-02  -7.69e-01  7.30e-01  0.63
## Prop. Mediated (treated) 7.31e-01  -3.58e+00  4.38e+00  0.29
## ACME (average)      1.95e+05  -1.15e+06  1.65e+06  0.75
## ADE (average)       5.42e+05  -9.08e+05  2.03e+06  0.37
## Prop. Mediated (average) 3.75e-01  -1.29e+00  1.81e+00  0.24
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Sample Size Used: 1497
##
##
## Simulations: 1000
```

#C3

```
med = lm(M~C3+A+C1+C2)
out = lm(Y~C3+M+M*C3)
summary(med)
```

```
##
## Call:
## lm(formula = M ~ C3 + A + C1 + C2)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -47715  -5525  -2264   1279   74341
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  7.658e+02  1.484e+03   0.516 0.605820
## C3           7.008e+03  7.731e+02   9.066 < 2e-16 ***
## A            3.591e+03  6.571e+02   5.465 5.41e-08 ***
## C1            3.065e-01  1.133e-01   2.704 0.006924 **
## C2           7.946e+04  2.141e+04   3.712 0.000213 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 11250 on 1492 degrees of freedom
## Multiple R-squared:  0.1416, Adjusted R-squared:  0.1393
## F-statistic: 61.55 on 4 and 1492 DF,  p-value: < 2.2e-16
```

```
summary(out)
```

```
##
## Call:
## lm(formula = Y ~ C3 + M + M * C3)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -55576  -5580    963   7699 103894
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  2.811e+04  8.181e+02  34.356 <2e-16 ***
## C3           1.469e+04  8.703e+02  16.884 <2e-16 ***
## M            4.017e-01  4.669e-02   8.604 <2e-16 ***
## C3:M          3.270e-01  2.981e-02  10.969 <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14670 on 1493 degrees of freedom
## Multiple R-squared:  0.5898, Adjusted R-squared:  0.589
## F-statistic: 715.7 on 3 and 1493 DF,  p-value: < 2.2e-16
```



```

beta0 = coefficients(med)[1]
beta1 = coefficients(med)[2]
theta1 = coefficients(out)[2]
theta2 = coefficients(out)[3]
theta3 = coefficients(out)[4]

```

```

m = 10000
CDE = theta1 + theta3*m
CDE

```

```

##          C3
## 17964.35

```

```

NDE = theta1 + theta3*beta0 + theta3*beta1*0
NDE

```

```

##          C3
## 14944.85

```

```

NIE = beta1*theta2 + beta1*theta3*1
NIE

```

```

##          C3
## 5107.385

```

```

set.seed(2019122035)
med.out = mediate(med, out, treat = "C3", mediator = "M", robustSE = TRUE, sims = 1000)
summary(med.out)

```

```

##
## Causal Mediation Analysis
##
## Quasi-Bayesian Confidence Intervals
##
##              Estimate 95% CI Lower 95% CI Upper p-value
## ACME (control)      2.83e+03    1.54e+03    4360.86 <2e-16 ***
## ACME (treated)      5.12e+03    3.24e+03    7027.69 <2e-16 ***
## ADE (control)       1.69e+04    1.51e+04    18803.15 <2e-16 ***
## ADE (treated)       1.92e+04    1.74e+04    21001.48 <2e-16 ***
## Total Effect        2.20e+04    1.99e+04    24116.66 <2e-16 ***
## Prop. Mediated (control) 1.26e-01    7.10e-02     0.19 <2e-16 ***
## Prop. Mediated (treated) 2.30e-01    1.56e-01     0.31 <2e-16 ***
## ACME (average)      3.97e+03    2.42e+03    5686.30 <2e-16 ***
## ADE (average)       1.81e+04    1.63e+04    19862.40 <2e-16 ***
## Prop. Mediated (average) 1.78e-01    1.16e-01     0.24 <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Sample Size Used: 1497
##
##
## Simulations: 1000

```