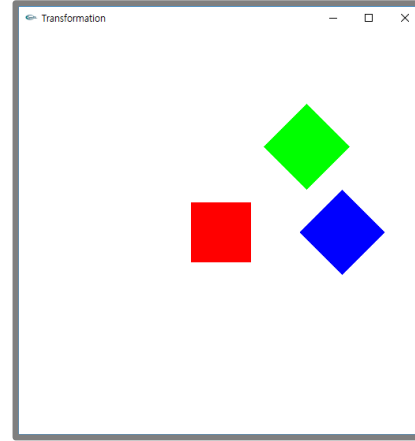


디지털 그래픽스 [6주차]

Geometric Transformation

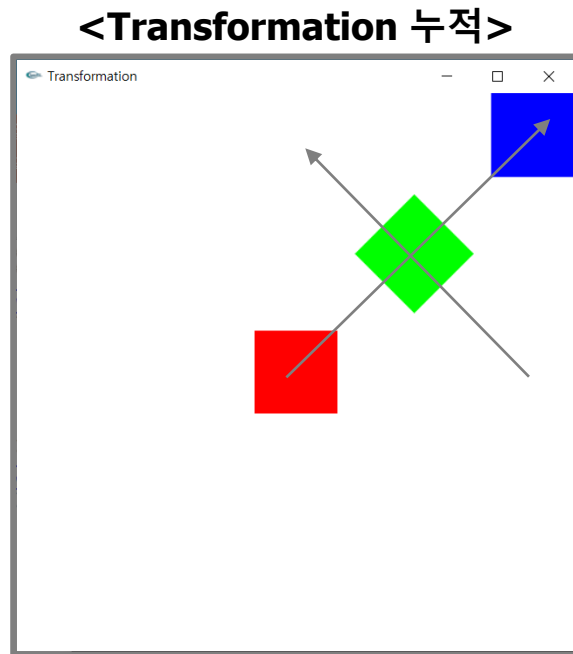


Goals

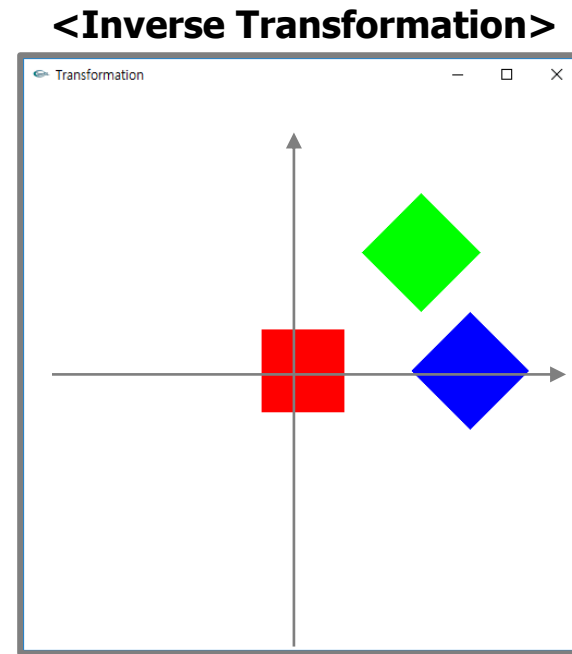
- **Matrix Stack**
- **glPushMatrix & glPopMatrix**
- **Scale Matrix**
- **Transformation by Keyboard**

Transformation의 누적 현상

- Transformation은 누적된다.
 - Inverse Transformation 사용으로 해결



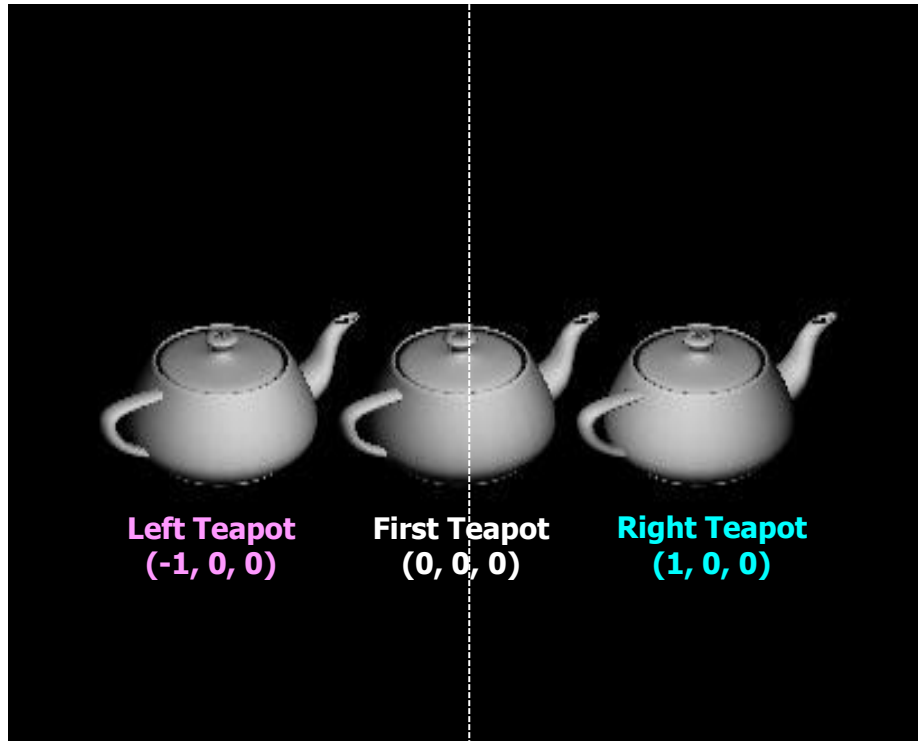
TR RT



TR $T^{-1}R^{-1}$ RT

Transformation의 누적 현상

- Three teapots



```
DrawTeapot();
```

```
glTranslate(1,0,0);
```

```
DrawTeapot();
```

```
glTranslate(-1,0,0);
```

```
DrawTeapot();
```

?

Matrix Multiplication 누적

- 동작 원리
 - **Matrix Stack**
 - Current Matrix: the top of matrix stack
 - 모든 matrix 연산은 current matrix에 누적

DrawTeapot();

glTranslate(1,0,0);

DrawTeapot();

glTranslate(-1,0,0);

DrawTeapot();

current
matrix에
적용

Matrix Stack

T(0,0,0)

current
matrix에
적용

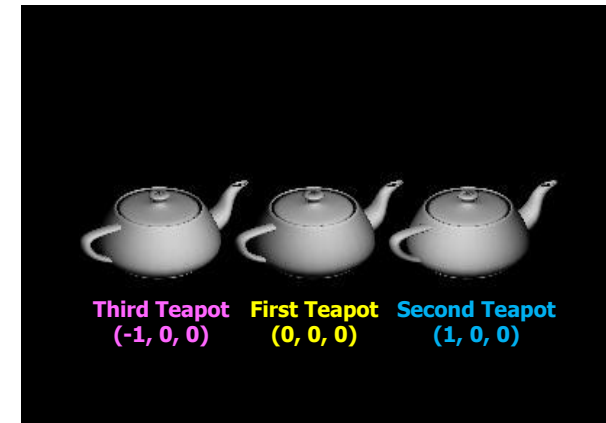
Matrix Stack

T(1,0,0)

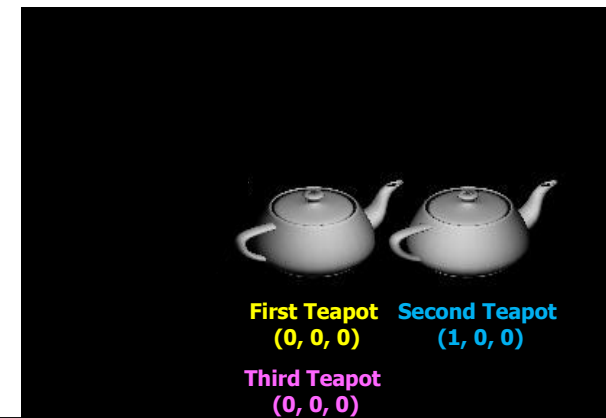
Matrix Stack

T(0,0,0)

matrix stack

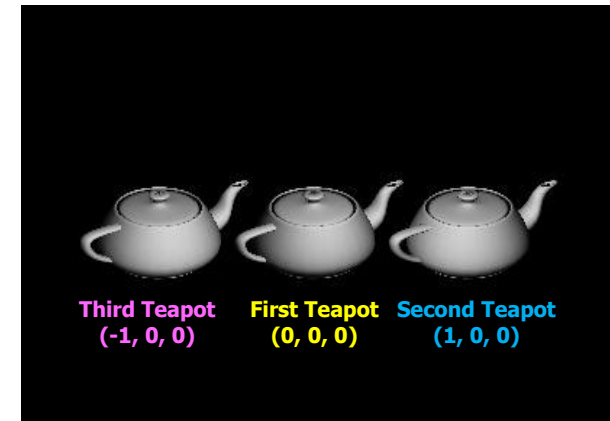
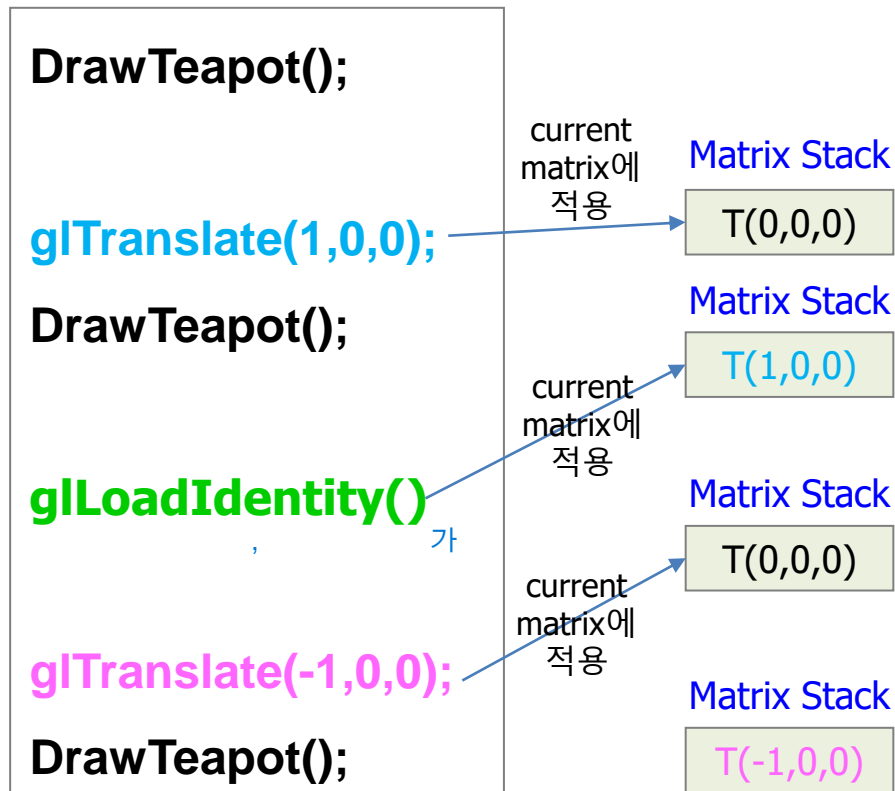


Expectation



glLoadIdentity()

- OpenGL의 Transformation Matrix 초기화 필요
 - glLoadIdentity()** 함수는 Transformation Matrix 초기화 수행
 - replace the current matrix with the identity matrix



Solar system

- We can draw **blue planets** with `loadIdentity()`

```
DrawCircle();
```

```
glTranslate(0.6,0,0);
```

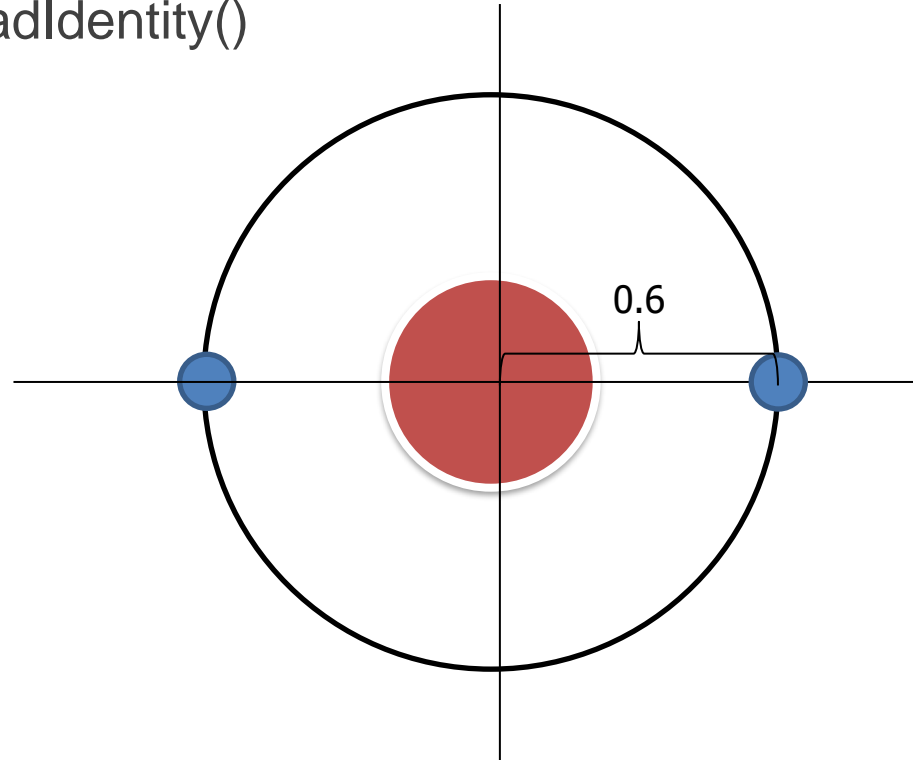
```
DrawCircle();
```

```
glLoadIdentity()
```

```
glTranslate(-0.6,0,0);
```

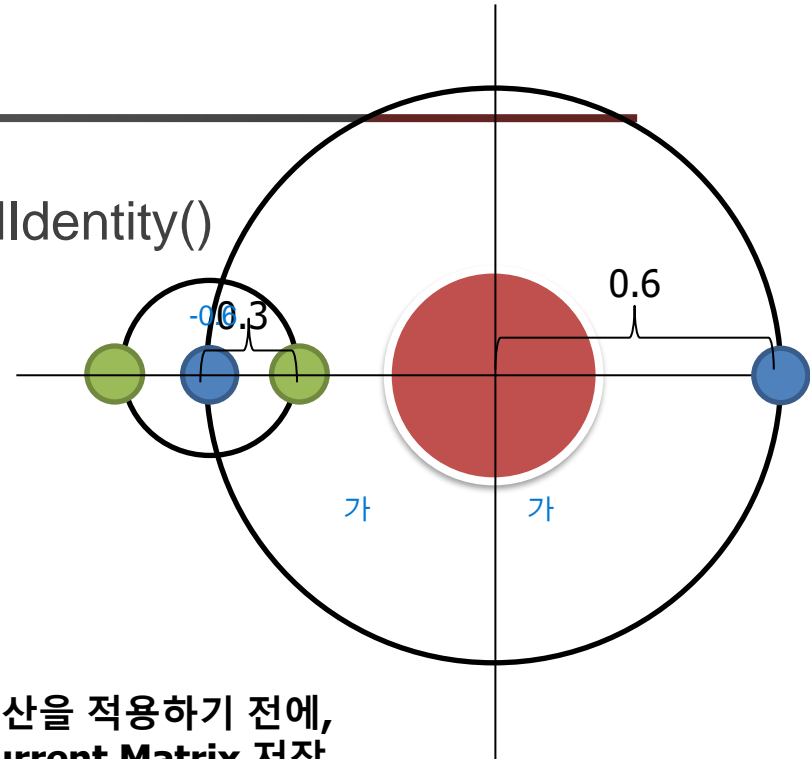
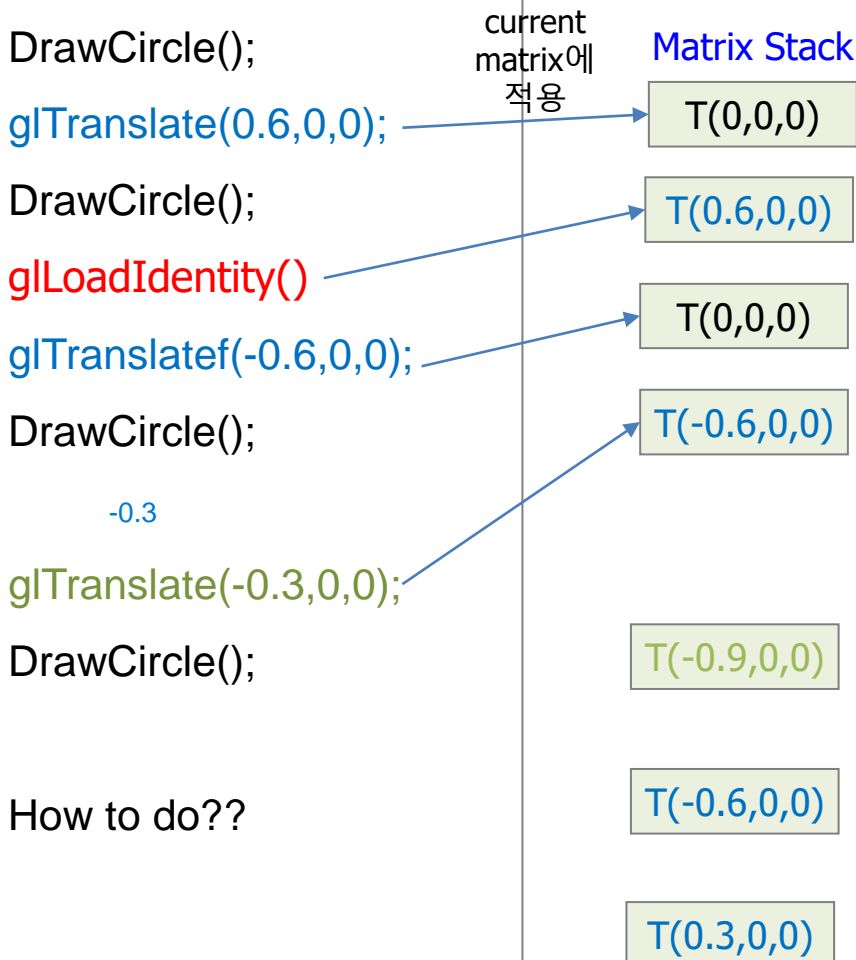
```
DrawCircle();
```

0



Solar system

- We **can't** draw **green planets** with `loadIdentity()`



다음 연산을 적용하기 전에,
현재 **current Matrix** 저장

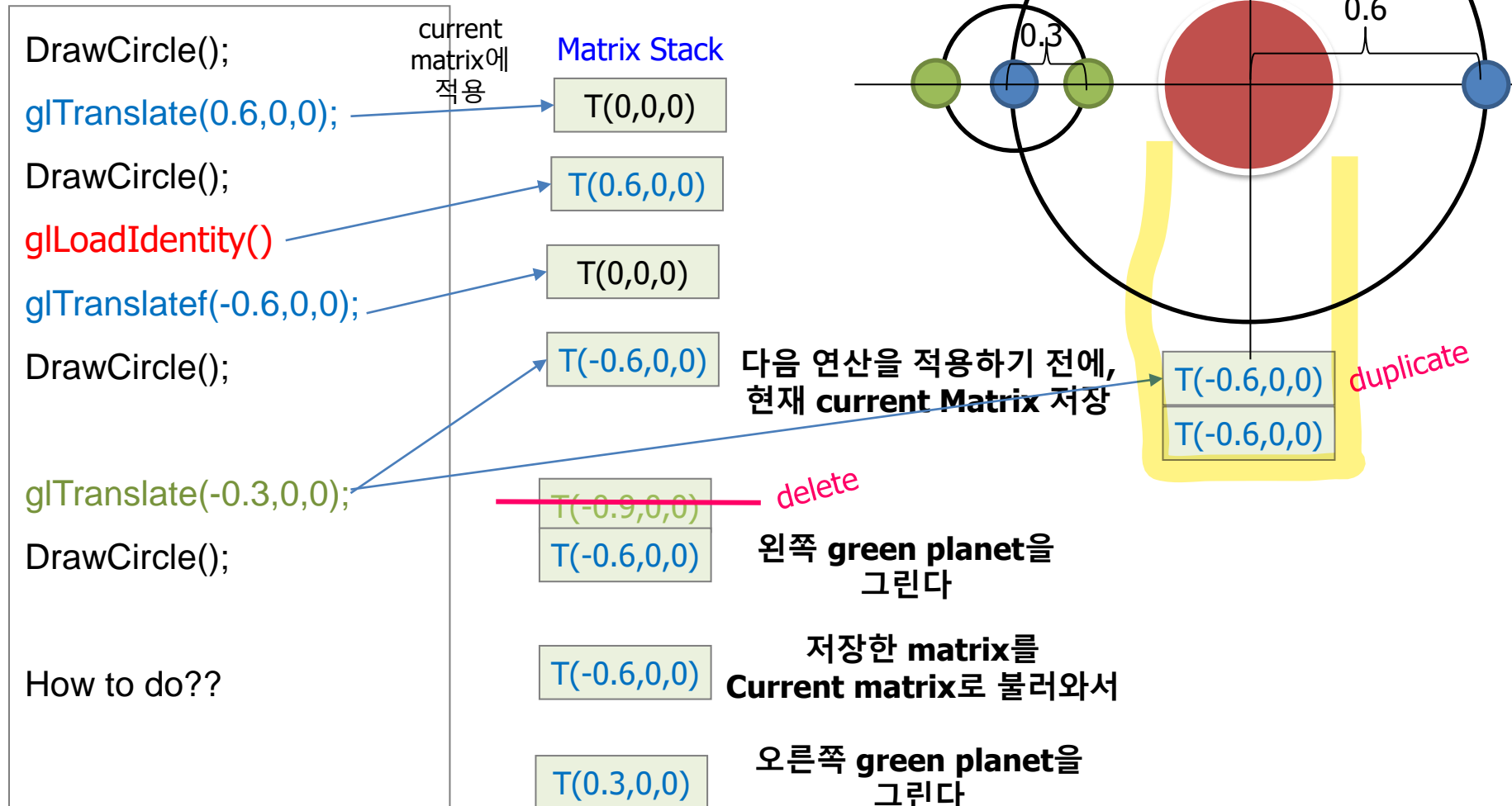
왼쪽 **green planet**을
그린다

저장한 **matrix**를
Current matrix로 불러와서

오른쪽 **green planet**을
그린다

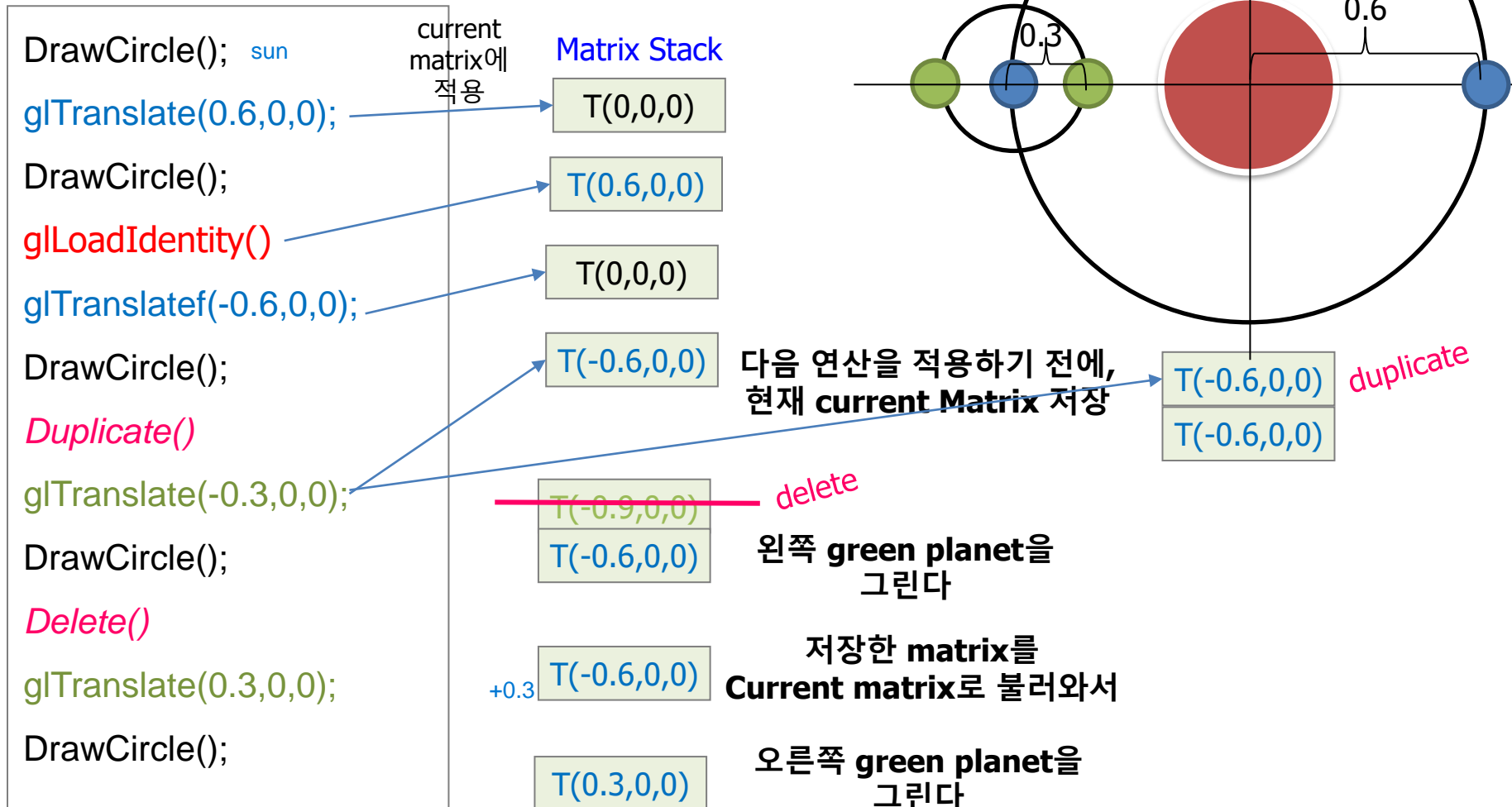
Solar system

- We **can't** draw **green planets** with `loadIdentity()`



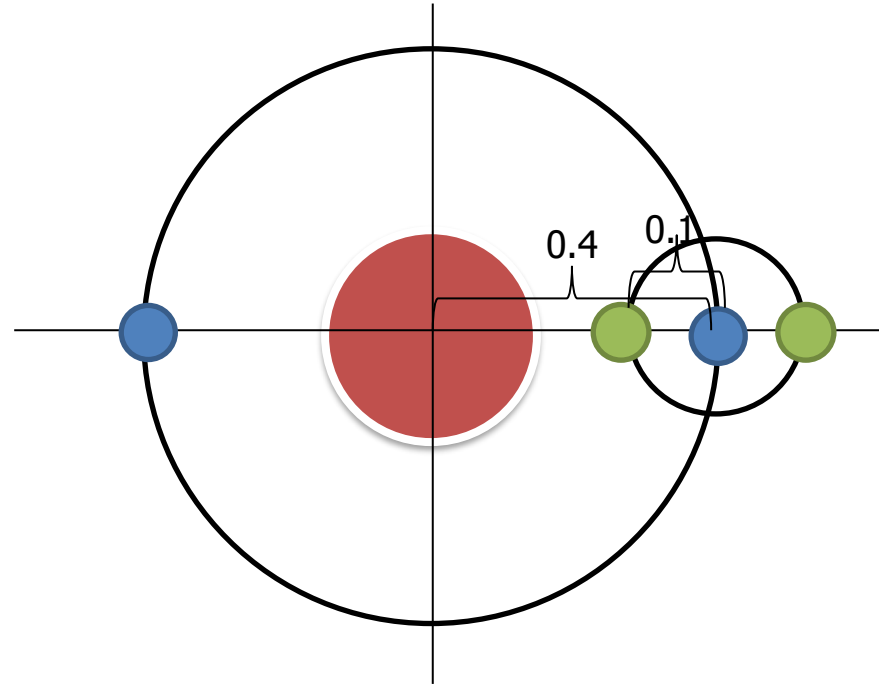
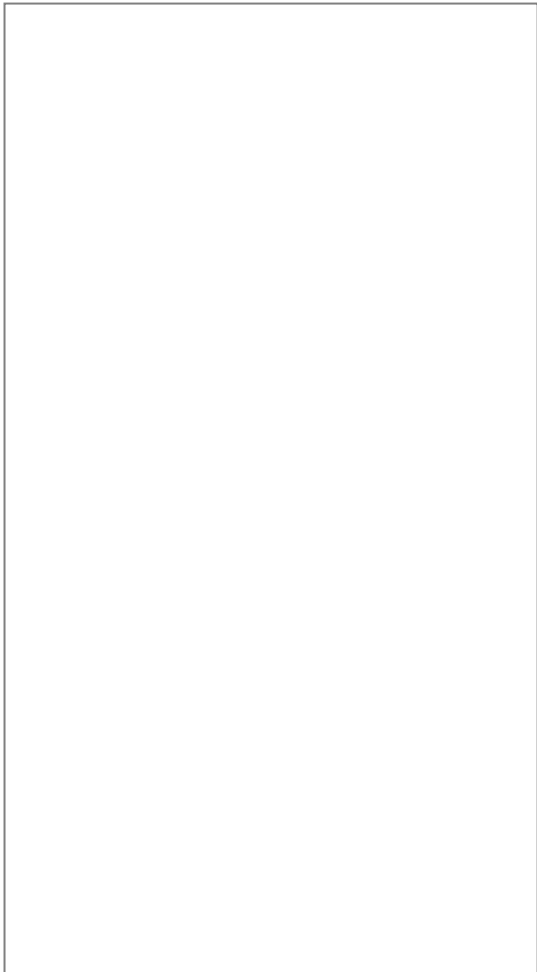
Solar system

- We **can't** draw **green planets** with `loadIdentity()`



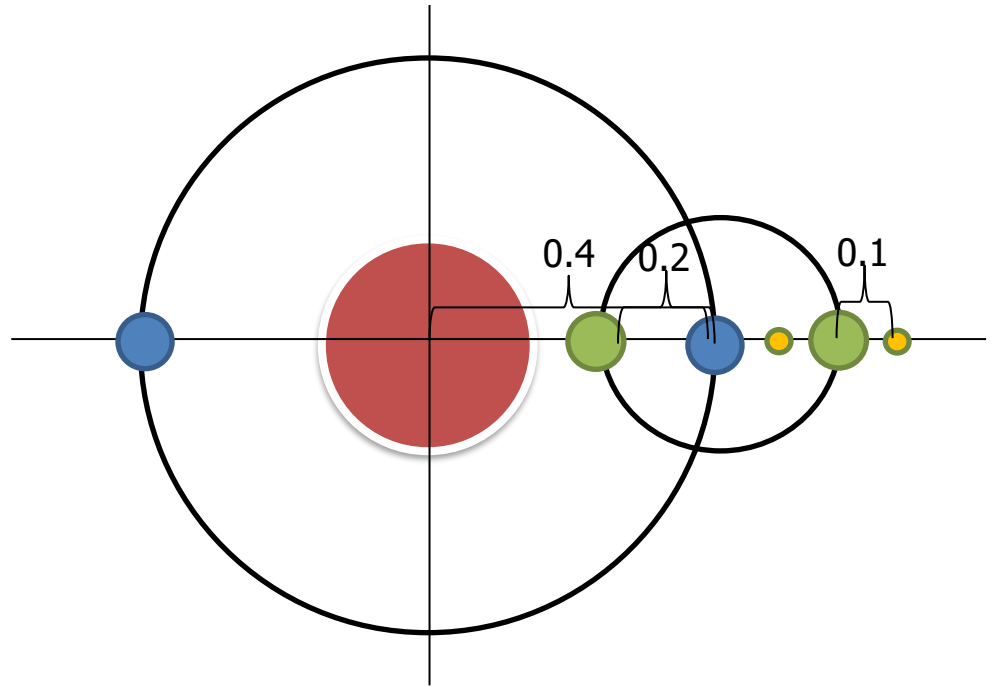
Quiz. duplicate/delete (제출x)

- Red, blue, green planets을 그리는 코드를 작성하세요.



Quiz1. duplicate/delete (제출o)

- Red, blue, green and yellow planets을 그리는 코드를 작성하세요.



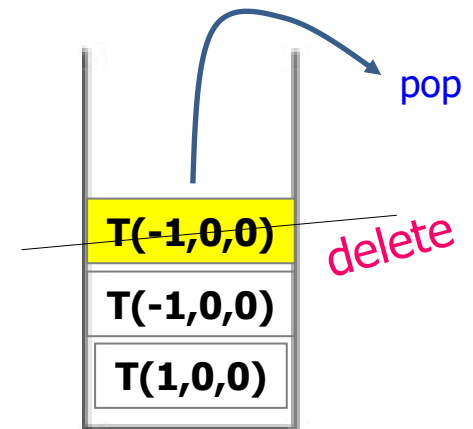
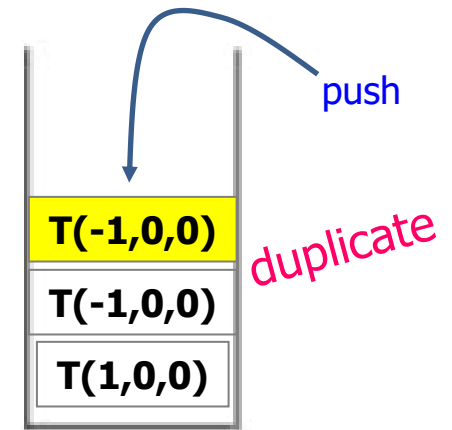
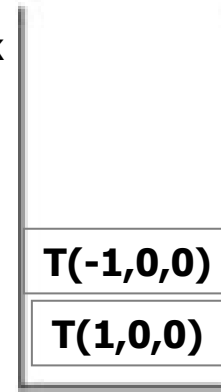
Goals

- **Matrix Stack**
- **glPushMatrix & glPopMatrix**
- **Scale Matrix**
- **Transformation by Keyboard**

glPushMatrix() / glPopMatrix()

Matrix Stack

- **glPushMatrix()** *duplicate*
 - pushes the current matrix stack down by one, **duplicating the current matrix**.
 - after a glPushMatrix call, the matrix on top of the stack is **identical to the one below it**.
- **glPopMatrix()** *delete*
 - **pops the current matrix stack**, replacing the current matrix with the one below it on the stack.



glPushMatrix() / glPopMatrix()

- glLoadIdentity()로 대체 가능

DrawSquare();

T(0,0,0)

glPushMatrix();

T(0,0,0)

T(0,0,0)

glTranslatef(-0.6f, 0.0f, 0.0f);

~~T(-0.6,0,0)~~

DrawSquare();

T(0,0,0)

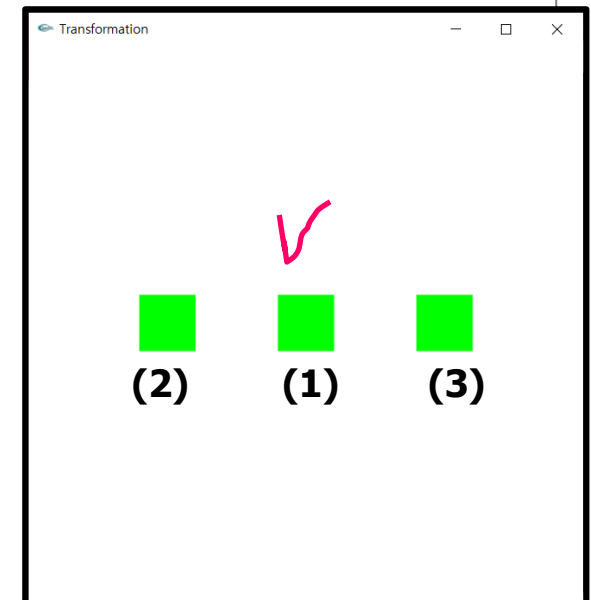
glPopMatrix();

T(0,0,0)

glTranslatef(0.6f, 0.0f, 0.0f);

T(0.6,0,0)

DrawSquare();



glPushMatrix() / glPopMatrix()

- glLoadIdentity()로 해결이 안되는 경우

```
glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT);
```

```
DrawSquare();
```

T(0,0,0)

```
glTranslatef(-0.6f, 0.0f, 0.0f);
```

T(-0.6,0,0)

```
DrawSquare();
```

```
glPushMatrix();
```

```
glTranslatef(-0.3f, 0.0f, 0.0f);
```

```
DrawSquareSmall();
```

```
glPopMatrix();
```

T(-0.6,0,0)

T(-0.6,0,0)

T(-0.9,0,0)

T(-0.6,0,0)

T(-0.6,0,0)

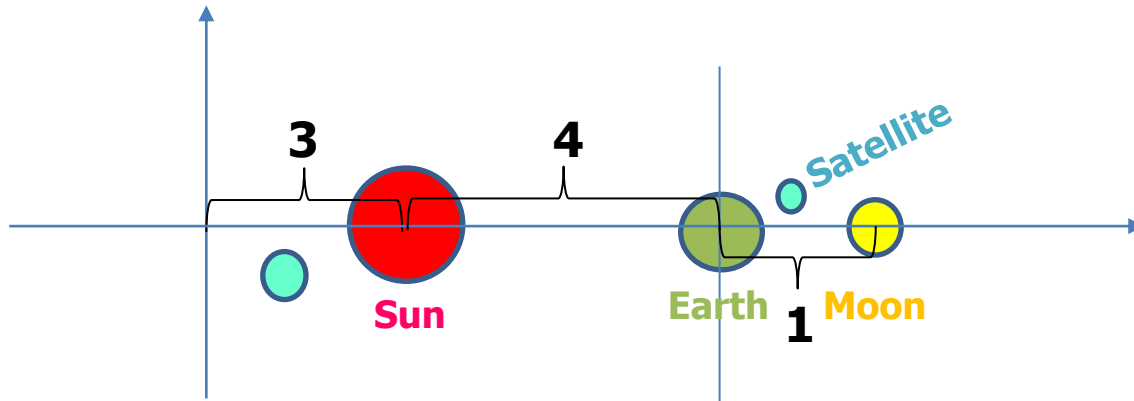
```
glTranslatef(0.3f, 0.0f, 0.0f);
```

T(-0.3,0,0)

```
DrawSquareSmall();
```



Coding Example. Solar System



```
glTranslatef(3.0, 0.0, 0.0);
```

```
drawSun();
```

```
glPushMatrix();
```

```
glTranslatef(4.0, 0.0, 0.0);
```

```
drawEarth();
```

```
glPushMatrix();
```

```
glTranslatef(1.0, 0.0, 0.0);
```

```
drawMoon();
```

```
glPopMatrix();
```

```
glTranslatef(0.5, 0.5, 0.0);
```

```
drawSatelite();
```

```
glPopMatrix();
```

$T(3,0,0)$

$T(3,0,0)$

$T(3,0,0)$

$T(7,0,0)$

$T(3,0,0)$

$T(7,0,0)$

$T(7,0,0)$

$T(3,0,0)$

$T(7,0,0)$

$T(3,0,0)$

~~$T(8,0,0)$~~

$T(7,0,0)$

$T(3,0,0)$

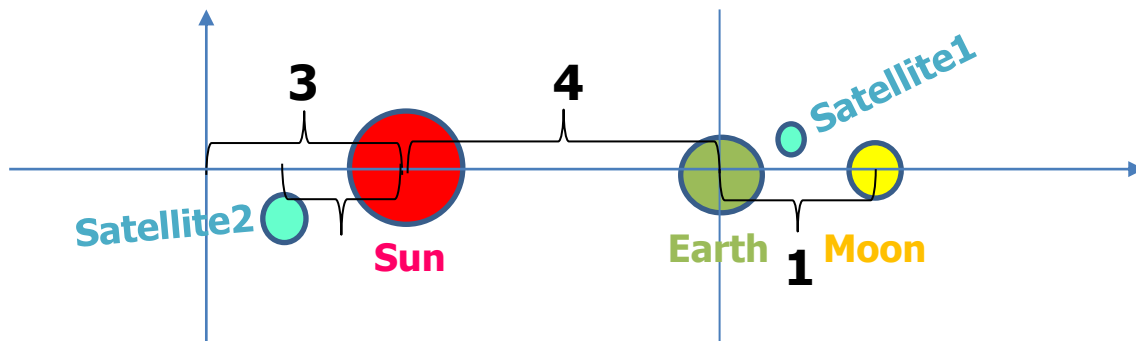
~~$T(7.5,0.5,0)$~~

$T(3,0,0)$

$T(3,0,0)$

Quiz2. Satellite2를 그리는 코드 추가

- Satellite2 는 Sun 에서 왼쪽으로 0.8 아래쪽으로 0.8 떨어져 있다.



```
glTranslatef(3.0, 0.0, 0.0);
```

```
drawSun();
```

```
glPushMatrix();
```

```
glTranslatef(4.0, 0.0, 0.0);
```

```
drawEarth();
```

```
glPushMatrix();
```

```
glTranslatef(1.0, 0.0, 0.0);
```

```
drawMoon();
```

```
glPopMatrix();
```

```
glTranslatef(0.5, 0.5, 0.0);
```

```
drawSatelite();
```

```
glPopMatrix();
```

T(3,0,0)

T(3,0,0)

T(3,0,0)

T(7,0,0)

T(3,0,0)

T(7,0,0)

T(7,0,0)

T(3,0,0)

T(7,0,0)

T(3,0,0)

~~T(8,0,0)~~

T(7,0,0)

T(3,0,0)

~~T(7.5,0.5,0)~~

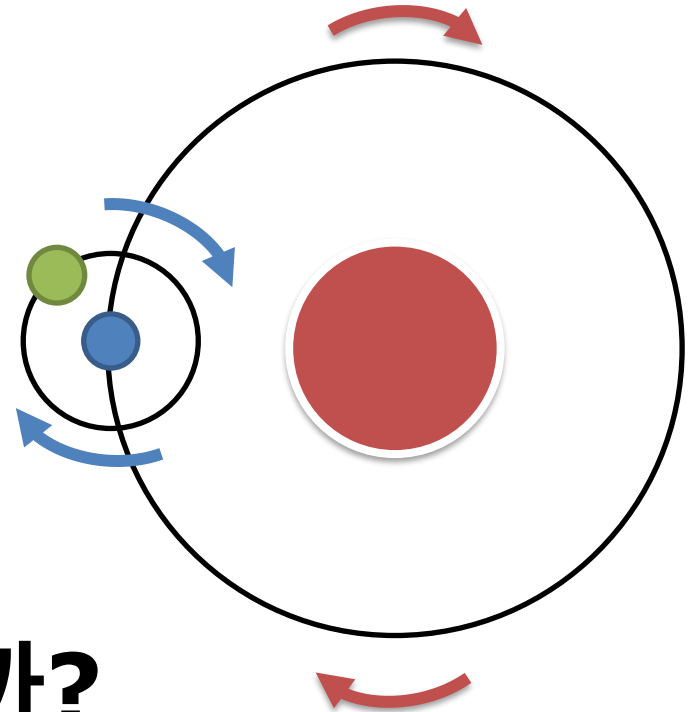
T(3,0,0)

T(3,0,0)

Coding Example. Solar System

각 **Sphere**는 행성을 의미

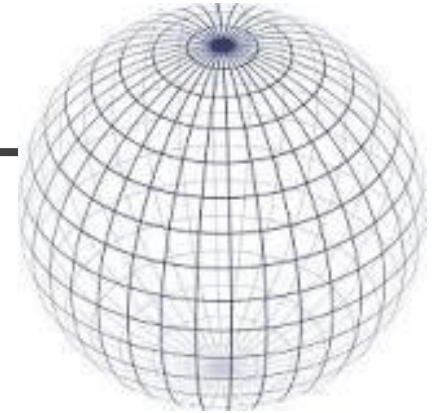
- 각 행성은 공전과 자전을 수행
- 검정색 라인은 비행선이 움직인 궤도
- Red Sun
- Red Sun을 회전하는 Blue Earth
- Blue Earth를 회전하는 green moon



어떻게 구현할 수 있을까?

- glPushMatrix() / glPopMatrix() 이용
- Animation 구현

sphere



Usage

- void `glutSolidSphere`(GLdouble radius, GLint slices, GLint stacks);
- void `glutWireSphere`(GLdouble radius, GLint slices, GLint stacks);

radius

- The radius of the sphere.

slices

- The number of subdivisions around the Z axis (similar to lines of **longitude**).

stacks

- The number of subdivisions along the Z axis (similar to lines of **latitude**).

Description

- Renders a sphere centered at the modeling coordinates origin of the specified radius. The sphere is subdivided around the Z axis into slices and along the Z axis into stacks.

Solar System

```
#include <gl/glut.h>
```

```
GLfloat blueAngle = 0.0f;
```

```
int main(int argc, char** argv)
```

```
{  
    glutInit(&argc, argv);  
  
    glutInitDisplayMode(GLUT_RGBA |  
                        GLUT_DEPTH | GLUT_SINGLE);  
    glutCreateWindow("Transformation");
```

```
    glutDisplayFunc(display);
```

```
    glutIdleFunc(display);
```

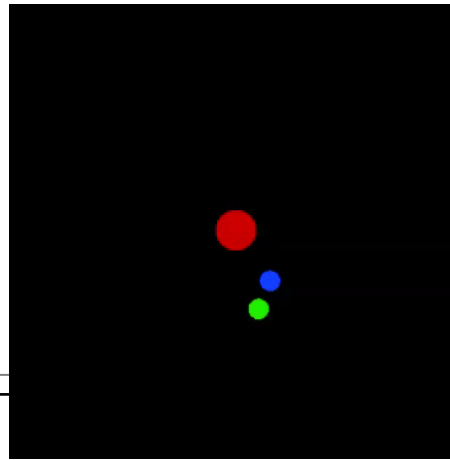
```
    // idle:cpu가 가 .
```

```
    glutMainLoop();
```

```
    return 0;
```

```
}
```

- Red Sun
- Red Sun을 회전하는 blue Earth
- Blue Earth를 회전하는 green moon



```
void display(void)
```

```
{
```

```
    glClear(GL_COLOR_BUFFER_BIT |  
            GL_DEPTH_BUFFER_BIT);  
    glLoadIdentity();
```

```
    glColor3f(1.0f, 0.0f, 0.0f);    // red  
    glutSolidSphere(0.1f, 100, 100);
```

```
    glPushMatrix();
```

```
    glRotatef(blueAngle, 0.0f, 0.0f, 1.0f);
```

```
    glTranslatef(0.6f, 0.0f, 0.0f);
```

```
    glColor3f(0.0f, 0.0f, 1.0f);    // blue
```

```
    glutSolidSphere(0.05f, 100, 100);
```

```
    glPushMatrix();
```

```
    glRotatef(blueAngle, 0.0f, 0.0f, 1.0f);
```

```
    glTranslatef(0.3f, 0.0f, 0.0f);
```

```
    glColor3f(0.0f, 1.0f, 0.0f);    // green
```

```
    glutSolidSphere(0.05f, 100, 100);
```

```
    glPopMatrix();
```

```
    glPopMatrix();
```

```
    blueAngle += 1.0f;
```

```
    glFlush();
```

```
}
```

Solar System

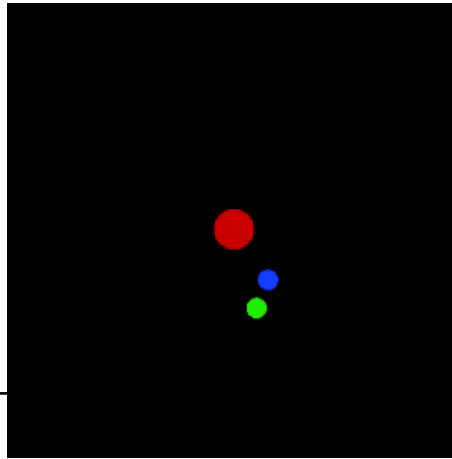
- 이 예제에서 glPushMatrix(), glPopMatrix() 함수를 반드시 사용해야 할까요?

NO!

```
loadidentity, push, pop  
>>
```

```
load          push pop  
>> push, pop
```

```
load          push pop  
>>          transformation
```



```
void display(void)
{
    glClear(GL_COLOR_BUFFER_BIT |
            GL_DEPTH_BUFFER_BIT);
    glLoadIdentity();

    glColor3f(1.0f, 0.0f, 0.0f);    // red
    glutSolidSphere(0.1f, 100, 100);

    glPushMatrix();
    glRotatef(blueAngle, 0.0f, 0.0f, 1.0f);
    glTranslatef(0.6f, 0.0f, 0.0f);
    glColor3f(0.0f, 0.0f, 1.0f);    // blue
    glutSolidSphere(0.05f, 100, 100);

    glPushMatrix();
    glRotatef(blueAngle, 0.0f, 0.0f, 1.0f);
    glTranslatef(0.3f, 0.0f, 0.0f);
    glColor3f(0.0f, 1.0f, 0.0f);    // green
    glutSolidSphere(0.05f, 100, 100);
    glPopMatrix();
    glPopMatrix();

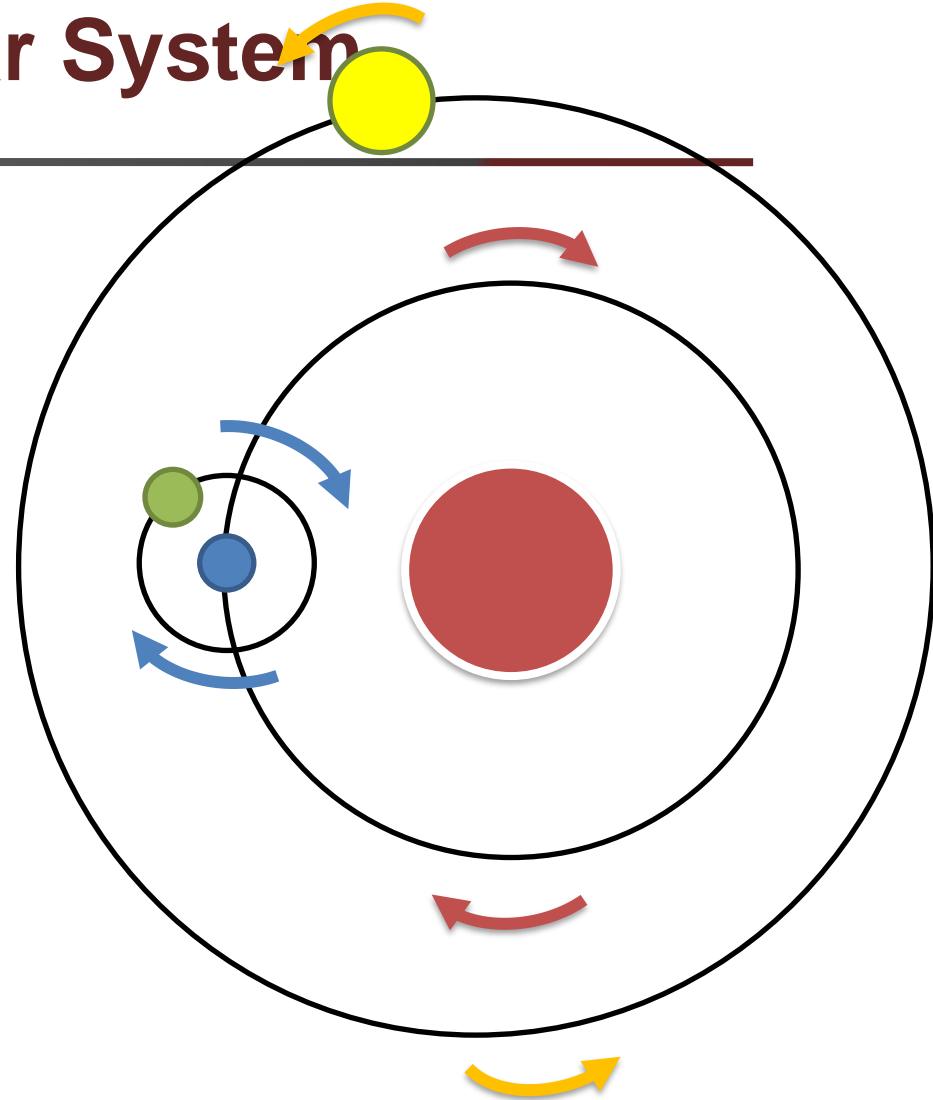
    blueAngle += 1.0f;
    glFlush();
}
```

Coding Example. Solar System

각 **Sphere**는 행성을 의미

- 각 행성은 공전과 자전을 수행
 - 검정색 라인은 비행선이 움직인 궤도
 - Red Sun
 - Red Sun을 회전하는 Blue Earth
 - Blue Earth를 회전하는 green moon
 - Red Sun을 반시계 방향으로 회전하는 Yellow Satellite
- 이 예제에서 `glPushMatrix()`, `glPopMatrix()` 함수를 반드시 사용해야 할까요?

YES!



은하계를 여행하는 비행선

```
void display(void)
```

```
{
```

```
    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT);  
    glLoadIdentity();
```

```
    glColor3f(1.0f, 0.0f, 0.0f);          // red  
    glutSolidSphere(0.1f, 100, 100);
```

```
    glPushMatrix();
```

```
    glRotatef(blueAngle, 0.0f, 0.0f, 1.0f);
```

```
    glTranslatef(0.6f, 0.0f, 0.0f);
```

```
    glColor3f(0.0f, 0.0f, 1.0f);          // blue
```

```
    glutSolidSphere(0.05f, 100, 100);
```

```
    glPushMatrix();
```

```
    glRotatef(blueAngle, 0.0f, 0.0f, 1.0f);
```

```
    glTranslatef(0.3f, 0.0f, 0.0f);
```

```
    glColor3f(0.0f, 1.0f, 0.0f);          // green
```

```
    glutSolidSphere(0.05f, 100, 100);
```

```
    glPopMatrix();
```

```
    glPopMatrix();
```

```
    glRotatef(1-blueAngle, 0.0f, 0.0f, 1.0f);
```

```
    glTranslatef(0.8f, 0.0f, 0.0f);
```

```
    glColor3f(1.0f, 1.0f, 0.0f);          // yellow
```

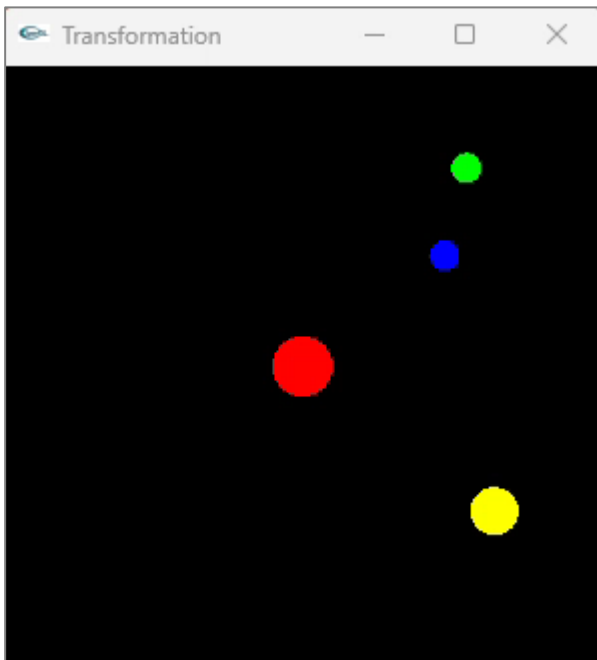
```
    glutSolidSphere(0.08f, 100, 100);
```

```
    blueAngle += 1.0f;
```

```
    if (blueAngle == 360) blueAngle = 0;
```

```
    glFlush();
```

```
}
```

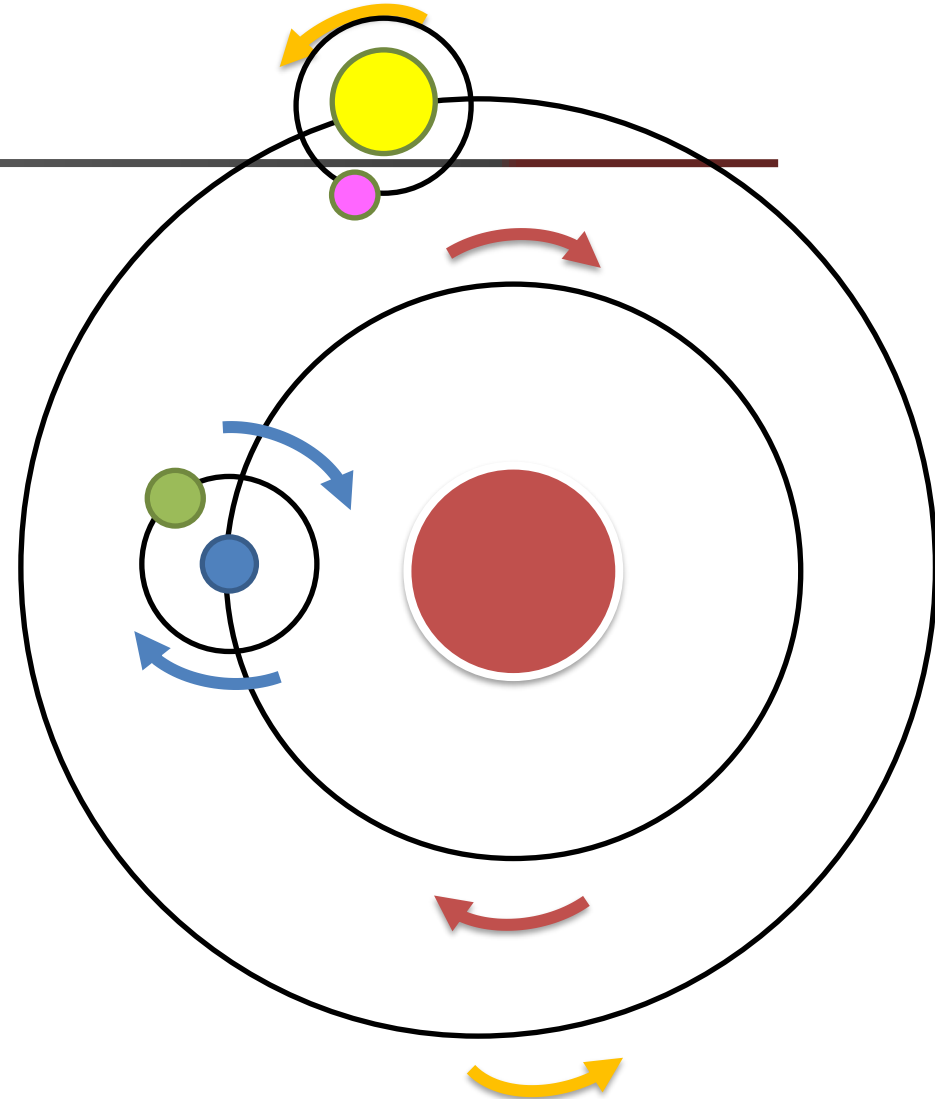


Quiz2. Solar System

이전 슬라이드에 있는 코드에 **pink satellite**의 회전을 추가하세요.

각 **Sphere**는 행성을 의미

- 각 행성은 공전과 자전을 수행
 - 검정색 라인은 비행선이 움직인 궤도
- Red Sun
 - Red Sun을 회전하는 Blue Earth
 - Blue Earth를 회전하는 green moon
 - Red Sun을 반시계 방향으로 회전하는 Yellow Satellite
 - Yellow satellite를 회전하는 pink satellite



* 방향을 표기하지 않으면, default 시계 방향 회전

Quiz3. Solar System

이전 슬라이드에 있는 코드에 **pink satellite**를 추가하세요.

회전 없이

태양, 지구, 달, 위성을 고정 위치에 그리세요

```
void display(void)
{
    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT);
    glLoadIdentity();

    glColor3f(1.0f, 0.0f, 0.0f); // red
    glutSolidSphere(0.1f, 100, 100);

    glPushMatrix();
    glRotatef(blueAngle, 0.0f, 0.0f, 1.0f);
    glTranslatef(0.6f, 0.0f, 0.0f);
    glColor3f(0.0f, 0.0f, 1.0f); // blue
    glutSolidSphere(0.05f, 100, 100);

    glPushMatrix();
    glRotatef(blueAngle, 0.0f, 0.0f, 1.0f);
    glTranslatef(0.3f, 0.0f, 0.0f);
    glColor3f(0.0f, 1.0f, 0.0f); // green
    glutSolidSphere(0.05f, 100, 100);

    glPopMatrix();
    glPopMatrix();
    glRotatef(1-blueAngle, 0.0f, 0.0f, 1.0f);
    glTranslatef(0.8f, 0.0f, 0.0f);
    glColor3f(1.0f, 1.0f, 0.0f); // yellow
    glutSolidSphere(0.08f, 100, 100);

    blueAngle += 1.0f;
    if (blueAngle == 360) blueAngle = 0;
    glFlush();
}
```

과제 1. Matrix Stack

- 아래 애니메이션을 구현하세요. (포탈 <강의자료>에 동영상 파일 첨부)
- 기존 코드
 - Red Sun
 - Red Sun을 회전하는 Blue Earth
 - Blue Earth를 회전하는 green moon
- 신규 코드 작성
 - Red Sun을 회전하는 Yellow satellite
 - Yellow satellite를 회전하는 pink satellite
 - Blue Earth를 회전하는 또 다른 black satellite
 - Green Moon을 회전하는 sky satellite



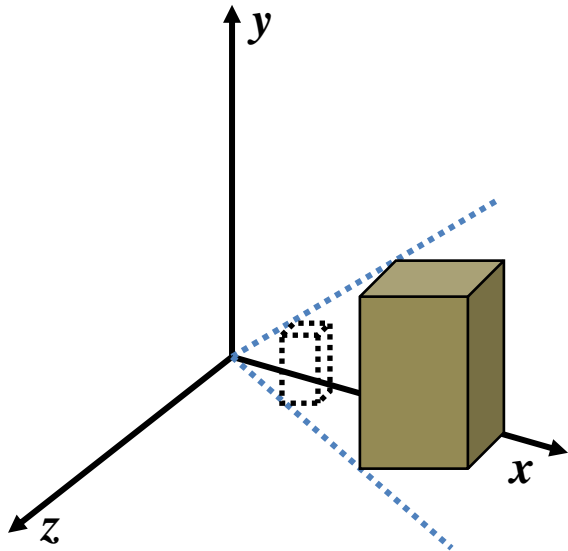
Goals

- **Matrix Stack**
- **glPushMatrix & glPopMatrix**
- **Scale Matrix**
- **Transformation by Keyboard**

3D Scale Matrix

- **glScalef(x, y, z)**
- **Not just for a size**
 - Also for a position, which is a distance from the origin

$$x' = x \cdot s_x, \quad y' = y \cdot s_y, \quad z' = z \cdot s_z$$



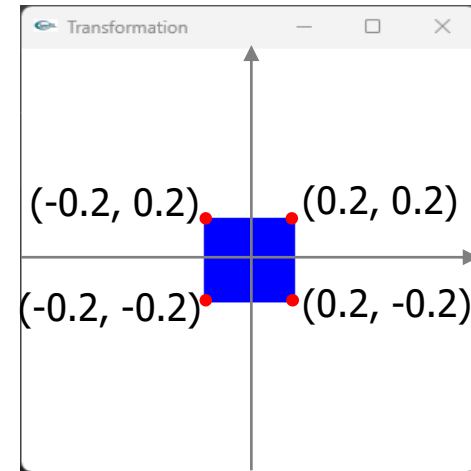
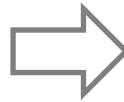
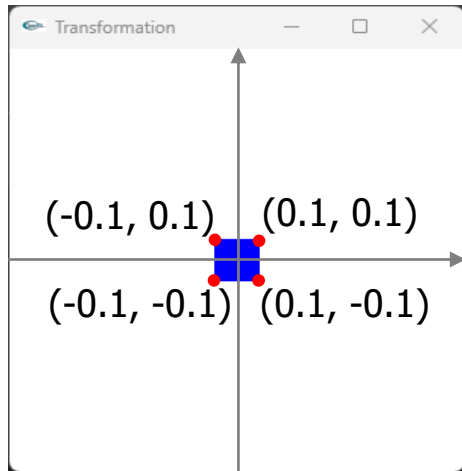
$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} s_x & 0 & 0 & 0 \\ 0 & s_y & 0 & 0 \\ 0 & 0 & s_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

$$\mathbf{x}' = \mathbf{S}_x * \mathbf{x} + 0 * \mathbf{y} + 0 * \mathbf{z} + 0 * \mathbf{1}$$
$$\mathbf{x}' = \mathbf{S}_x * \mathbf{x}$$

Scaling

물체의 중심이 원점에 있을 때 scaling

- `glScalef(2.0, 2.0, 0.0)`
- `glutSolidCube(0.2)`

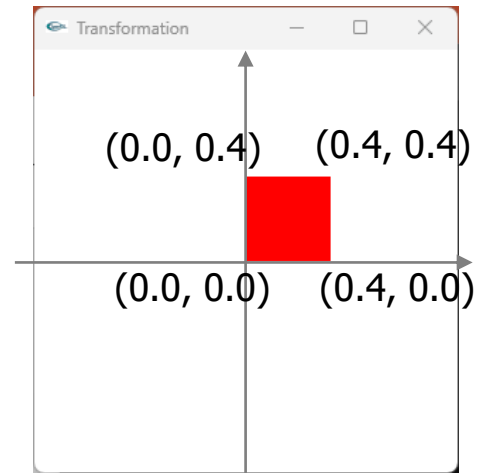
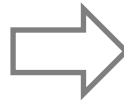
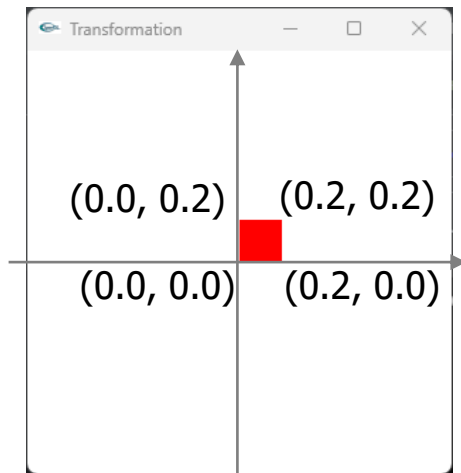


Scaling

물체의 vertex가 원점에 있을 때, scaling

`glScalef(2.0, 2.0, 0.0)`

- `glTranslatef(0.1, 0.1, 0.0)`
- `glutSolidCube(0.2)`

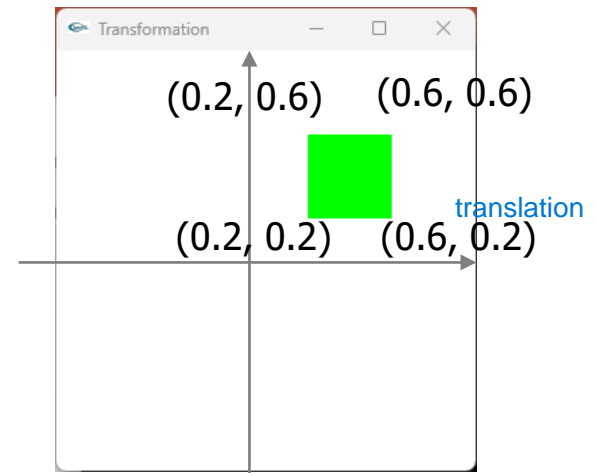
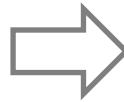
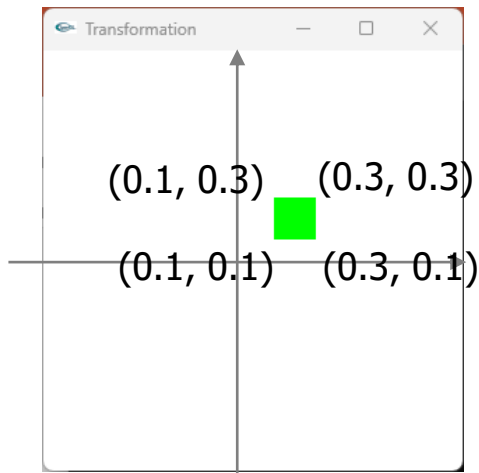


Scaling

물체가 원점에 있지 않을 때, scaling

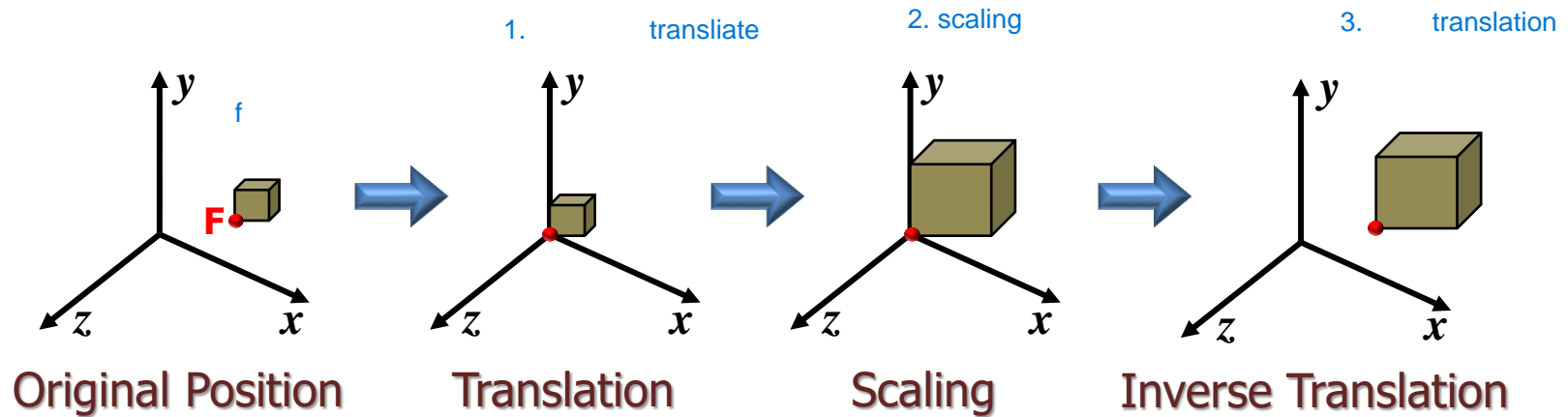
`glScalef(2.0, 2.0, 0.0)`

- `glTranslatef(0.2, 0.2, 0.0)`
- `glutSolidCube(0.2)`



scaling
.

Fixed-point Scaling



$$T(x_f, y_f, z_f) S(s_x, s_y, s_z) T(-x_f, -y_f, -z_f) = \begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & x_f \\ 0 & 1 & 0 & y_f \\ 0 & 0 & 1 & z_f \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} s_x & 0 & 0 & 0 \\ 0 & s_y & 0 & 0 \\ 0 & 0 & s_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & -x_f \\ 0 & 1 & 0 & -y_f \\ 0 & 0 & 1 & -z_f \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

translate scaling minus translate

Goals

- **Matrix Stack**
- **glPushMatrix & glPopMatrix**
- **Scale Matrix**
- **Transformation by Keyboard**

키보드 제어

!

event driven

- **glutKeyboardFunc(..)**

- sets the keyboard callback for the current window.

- **Usage**

<키보드 콜백 함수>를 등록하는 함수

- **void glutKeyboardFunc(void (*func)(unsigned char key,
int x,
int y));** 키보드 콜백함수명
<키보드 콜백 함수>의 매개변수 3개

- func : The new keyboard callback function.

- **Coding example**

void

```
void keyboard(unsigned char key, int x, int y)
{
}
}
```

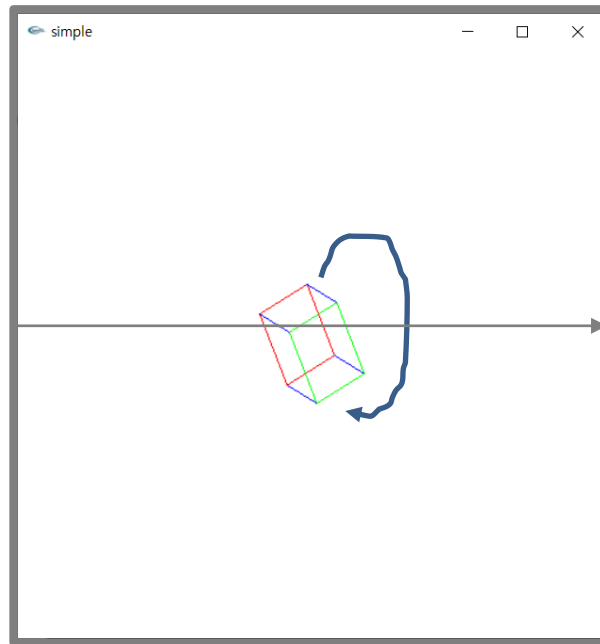
keyboard

```
glutKeyboardFunc( keyboard );
```

Transformation by Keyboard

- Coding example

- drawBox()
 - cube 그리기
- display()
 - 기본 변환
 - drawBox()
- xyzRotate()
 - x축 기준 회전
 - `glRotatef()`
- keyboard()
 - 키보드 처리 `rotate`
 - `glutPostRedisplay()`
- `main()`
 - `display` 콜백함수 등록
 - `keyboard` 콜백함수 등록



키보드 x 누르면 x축 기준 회전

키보드 y 누르면 y축 기준 회전

키보드 z 누르면 z축 기준 회전

키보드 s 누르면 확대

키보드 a 누르면 축소

키보드 t 누르면 오른쪽으로 이동

키보드 r 누르면 왼쪽으로 이동

Transformation by Keyboard

```
#include <iostream>
#include <gl/glut.h>
#include <math.h> //sin(),cos()
using namespace std;
```

```
#define PI 3.141592
```

```
void drawBox()
```

```
{
```

```
    // Red rectangle
```

```
    glColor3f(1.0, 0.0, 0.0);
    glBegin(GL_LINE_LOOP);
    glVertex3f(-1.0, -1.0, -1.0);
    glVertex3f( 1.0, -1.0, -1.0);
    glVertex3f( 1.0,  1.0, -1.0);
    glVertex3f(-1.0,  1.0, -1.0);
    glEnd();
```

```
    // Green rectangle
```

```
    glColor3f(0.0, 1.0, 0.0);
    glBegin(GL_LINE_LOOP);
    glVertex3f(-1.0, -1.0, 1.0);
    glVertex3f( 1.0, -1.0, 1.0);
    glVertex3f( 1.0,  1.0, 1.0);
    glVertex3f(-1.0,  1.0, 1.0);
    glEnd();
```

```
    // Blue lines
```

```
    glColor3f(0.0, 0.0, 1.0);
    glBegin(GL_LINES);
    glVertex3f(-1.0, -1.0, -1.0);
    glVertex3f(-1.0, -1.0,  1.0);
    glVertex3f( 1.0, -1.0, -1.0);
    glVertex3f( 1.0, -1.0,  1.0);
    glVertex3f( 1.0,  1.0, -1.0);
    glVertex3f( 1.0,  1.0,  1.0);
    glVertex3f(-1.0,  1.0, -1.0);
    glVertex3f(-1.0,  1.0,  1.0);
    glEnd();
```

```
}
```

```
void display(void)
```

```
{
```

```
    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT);
```

```
    //glLoadIdentity();
```

```
    glPushMatrix();
```

```
    glRotatef(45.0, 1.0, 1.0, 1.0);
```

```
    glScalef(0.1, 0.2, 0.1);
```

```
    drawBox();
```

```
    glPopMatrix();
```

```
    glFlush();
```

```
}
```

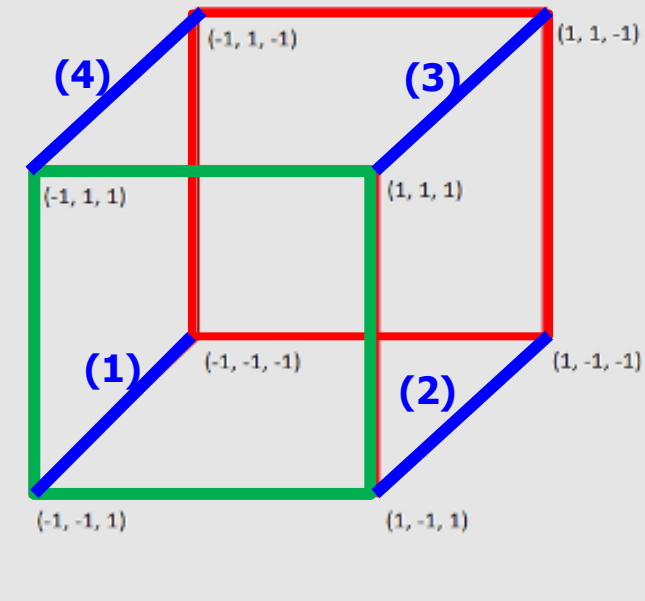
push, pop

// initial setup: no accumulation

// rotation w.r.t $v=(1,1,1)$ 2.45
/ 1,1,1

o o

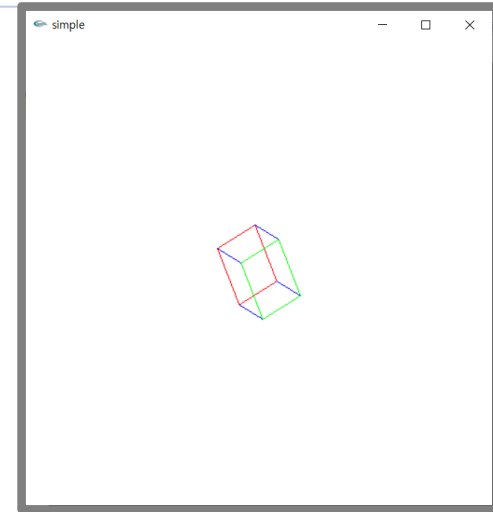
1,2



Transformation by Keyboard

```
void xyzRotate(char mode)
{
    switch (mode) {
        case 'x': glRotatef(PI, 1, 0, 0); break;
        case 'y': glRotatef(PI, 0, 1, 0); break;
        case 'z': glRotatef(PI, 0, 0, 1); break;
        default: break;
    }
}

void keyboard(unsigned char key, int x, int y)
{
    switch (key)
    {
        case 'x': xyzRotate('x'); x rotate . x pi glutPostRedisplay(); break;
        case 'y': xyzRotate('y'); glutPostRedisplay(); break;
        case 'z': xyzRotate('z'); glutPostRedisplay(); break;
        default: break;
    }
}
```



```
x      가?
>> L L display event가      . (
      .>> glutPostRedisplay
```

glutPostRedisplay()

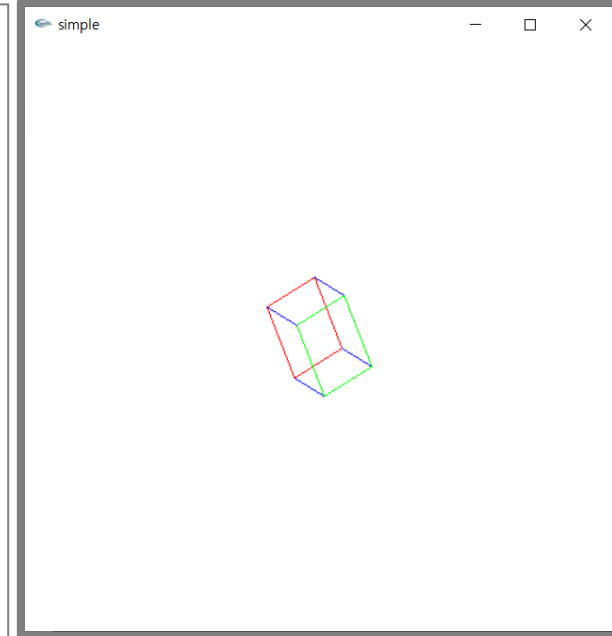
- display event 발생
- display 콜백함수를 의도적으로 호출

Transformation by Keyboard

```
int main(int argc, char** argv)
{
    glutInit(&argc, argv);
    glutInitDisplayMode(GLUT_RGBA | GLUT_DEPTH | GLUT_SINGLE);
    glutCreateWindow("Transformation");

    // Set Background Color
    glClearColor(1.0, 1.0, 1.0, 0.0);
    glutDisplayFunc(display); << , ( )
    glutKeyboardFunc(keyboard);
    glutMainLoop();

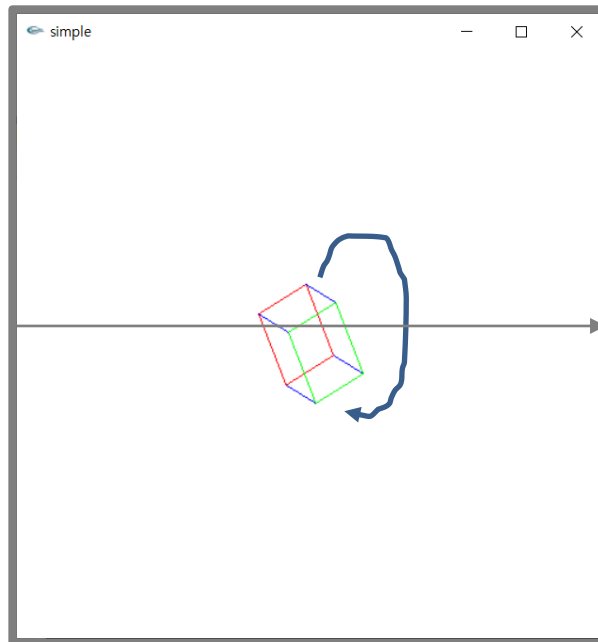
    return 0; >> idle cpu idlefunc display 가 .
}
```



과제 2. Transformation by Keyboard

- 주어진 코드에 **그린색 기능**을 추가하세요.

- drawBox()
 - cube 그리기
- display()
 - 기본 변환
 - drawBox()
- xyzRotate()
 - x축 기준 회전
 - glRotatef()
- keyboard()
 - 키보드 처리
 - glutPostRedisplay()
- main()
 - display 콜백함수 등록
 - keyboard 콜백함수 등록



키보드 x 누르면 x축 기준 회전

키보드 y 누르면 y축 기준 회전

키보드 z 누르면 z축 기준 회전

키보드 s 누르면 확대

키보드 a 누르면 축소

키보드 t 누르면 오른쪽으로 이동

키보드 r 누르면 왼쪽으로 이동

Thank you !