

OZONE

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R Markdown

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When you click the **Knit** button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document. You can embed an R code chunk like this:

```
#ozone dataset
library(readr)
onehr <- read_csv("C:/Users/Hafid Pradipta/OneDrive/STAT 520/dataset/Ozone/onehr.csv")
```

```
## Parsed with column specification:
## cols(
##   .default = col_character(),
##   t_pk = col_double(),
##   t_av = col_double(),
##   percp = col_double(),
##   attribute = col_integer()
## )
```

```
## See spec(...) for full column specifications.
```

```
## Warning in rbind(names(probs), probs_f): number of columns of result is not
## a multiple of vector length (arg 1)
```

```
## Warning: 352 parsing failures.
```

```
## row # A tibble: 5 x 5 col      row    col expected actual expected   <int> <chr>    <chr>  <chr> actual
## ... .....
## See problems(...) for more details.
```

```
head(onehr)
```

```
## # A tibble: 6 x 74
##       Date wsr0 wsr1 wsr2 wsr3 wsr4 wsr5 wsr6 wsr7 wsr8 wsr9
##       <chr> <chr> <chr> <chr> <chr> <chr> <chr> <chr> <chr> <chr> <chr>
## 1 1/1/1998  0.8  1.8  2.4  2.1    2  2.1  1.5  1.7  1.9  2.3
## 2 1/2/1998  2.8  3.2  3.3  2.7  3.3  3.2  2.9  2.8  3.1  3.4
## 3 1/3/1998  2.9  2.8  2.6  2.1  2.2  2.5  2.5  2.7  2.2  2.5
## 4 1/4/1998  4.7  3.8  3.7  3.8  2.9  3.1  2.8  2.5  2.4  3.1
## 5 1/5/1998  2.6  2.1  1.6  1.4  0.9  1.5  1.2  1.4  1.3  1.4
## 6 1/6/1998  3.1  3.5  3.3  2.5  1.6  1.7  1.6  1.6  2.3  1.8
## # ... with 63 more variables: wsr10 <chr>, wsr11 <chr>, wsr12 <chr>,
## #   wsr13 <chr>, wsr14 <chr>, wsr15 <chr>, wsr16 <chr>, wsr17 <chr>,
## #   wsr18 <chr>, wsr19 <chr>, wsr20 <chr>, wsr21 <chr>, wsr22 <chr>,
## #   wsr23 <chr>, wsr_pk <chr>, wsr_av <chr>, t0 <chr>, t1 <chr>, t2 <chr>,
## #   t3 <chr>, t4 <chr>, t5 <chr>, t6 <chr>, t7 <chr>, t8 <chr>, t9 <chr>,
## #   t10 <chr>, t11 <chr>, t12 <chr>, t13 <chr>, t14 <chr>, t15 <chr>,
## #   t16 <chr>, t17 <chr>, t18 <chr>, t19 <chr>, t20 <chr>, t21 <chr>,
## #   t22 <chr>, t23 <chr>, t_pk <dbl>, t_av <dbl>, t85 <chr>, rh85 <chr>,
```

```
## #   u85 <chr>, v85 <chr>, ht85 <chr>, t70 <chr>, rh70 <chr>, u70 <chr>,
## #   v70 <chr>, ht70 <chr>, t50 <chr>, rh50 <chr>, u50 <chr>, v50 <chr>,
## #   ht50 <chr>, ki <chr>, tt <chr>, slp <chr>, slp_ <chr>, percp <dbl>,
## #   attribute <int>

### cleaning the data
which(onehr$wsr0=="?")

## [1] 270 277 278 279 280 281 282 283 284 285 286 287 288 289
## [15] 290 291 292 293 294 295 296 297 298 299 303 559 627 1307
## [29] 1310 1312 1320 1327 1330 1339 1340 1601 1618 1632 1633 1634 1635 1636
## [43] 1637 1638 1639 1640 1641 1642 1643 1644 1645 1646 1647 1648 1649 1650
## [57] 1651 1652 1653 1654 1655 1656 1657 1658 1659 1660 1661 1662 1663 1664
## [71] 1665 1666 1667 1668 1669 1670 1671 1672 1673 1674 1675 1676 1677 1678
## [85] 1679 1680 1681 1682 1683 1684 1685 1686 1687 1688 1689 1690 1691 1692
## [99] 1693 1694 1695 1696 1697 1698 1699 1700 1701 1702 1703 1704 1705 1706
## [113] 1707 1708 1709 1710 1711 1712 1713 1714 1715 1716 1717 1718 1719 1720
## [127] 1721 1722 1723 1724 1725 1726 1727 1728 1729 1730 1731 1732 1733 1734
## [141] 1735 1736 1737 1738 1739 1740 1741 1742 1743 1744 1745 1746 1747 1748
## [155] 1749 1750 1751 1752 1753 1754 1755 1756 1757 1758 1759 1760 1761 1762
## [169] 1763 1764 1765 1766 1767 1768 1769 1770 1771 1772 1773 1774 1775 1776
## [183] 1777 1778 1779 1780 1781 1782 1783 1784 1785 1786 1787 1788 1789 1790
## [197] 1791 1792 1793 1794 1795 1796 1797 1798 1799 1800 1801 1802 1803 1804
## [211] 1805 1806 1807 1808 1809 1810 1811 1812 1813 1814 1815 1816 1817 1818
## [225] 1819 1820 1821 1822 1823 1824 1825 1826 1836 1837 1838 1839 1840 1841
## [239] 1842 1843 1844 1845 1846 1847 1848 1853 1854 1855 1856 1857 1858 1859
## [253] 1860 1861 1862 1863 1864 1865 1866 1867 1868 1869 1870 1871 1872 1873
## [267] 1874 1875 1876 1877 2017 2128 2130 2131 2132 2133 2134 2135 2136 2137
## [281] 2138 2139 2140 2141 2142 2143 2144 2145 2146 2147 2148 2149 2150 2151
## [295] 2152 2153 2154 2155 2156

onehr[onehr=="?"]<-NA
head(onehr==NA)

##      Date wsr0 wsr1 wsr2 wsr3 wsr4 wsr5 wsr6 wsr7 wsr8 wsr9 wsr10 wsr11
## [1,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [2,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [3,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [4,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [5,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [6,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
##      wsr12 wsr13 wsr14 wsr15 wsr16 wsr17 wsr18 wsr19 wsr20 wsr21 wsr22
## [1,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [2,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [3,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [4,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [5,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [6,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
##      wsr23 wsr_pk wsr_av t0 t1 t2 t3 t4 t5 t6 t7 t8 t9 t10 t11 t12 t13 t14
## [1,]   NA   NA   NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [2,]   NA   NA   NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [3,]   NA   NA   NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [4,]   NA   NA   NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [5,]   NA   NA   NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [6,]   NA   NA   NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
##      t15 t16 t17 t18 t19 t20 t21 t22 t23 t_pk t_av t85 rh85 u85 v85 ht85
```

```
## [1,] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [2,] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [3,] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [4,] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [5,] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [6,] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
##      t70 rh70 u70 v70 ht70 t50 rh50 u50 v50 ht50 ki tt slp slp_ percp
## [1,] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [2,] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [3,] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [4,] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [5,] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [6,] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
##      attribute
## [1,] NA
## [2,] NA
## [3,] NA
## [4,] NA
## [5,] NA
## [6,] NA
```

```
onehrc<-na.omit(onehr)
sum(length(which(is.na(onehrc))))
```

```
## [1] 0
```

```
library(MVN)
class(onehrc)
```

```
## [1] "tbl_df"      "tbl"          "data.frame"
```

```
onehrc2<-onehrc[,-1]
```

```
lapply(onehrc2,class) #because the missing value is ? therefore R record is as character, we want it as
```

```
## $wsr0
## [1] "character"
##
## $wsr1
## [1] "character"
##
## $wsr2
## [1] "character"
##
## $wsr3
## [1] "character"
##
## $wsr4
## [1] "character"
##
## $wsr5
## [1] "character"
##
## $wsr6
## [1] "character"
##
```

```
## $wsr7
## [1] "character"
##
## $wsr8
## [1] "character"
##
## $wsr9
## [1] "character"
##
## $wsr10
## [1] "character"
##
## $wsr11
## [1] "character"
##
## $wsr12
## [1] "character"
##
## $wsr13
## [1] "character"
##
## $wsr14
## [1] "character"
##
## $wsr15
## [1] "character"
##
## $wsr16
## [1] "character"
##
## $wsr17
## [1] "character"
##
## $wsr18
## [1] "character"
##
## $wsr19
## [1] "character"
##
## $wsr20
## [1] "character"
##
## $wsr21
## [1] "character"
##
## $wsr22
## [1] "character"
##
## $wsr23
## [1] "character"
##
## $wsr_pk
## [1] "character"
##
```

```
## $wsr_av
## [1] "character"
##
## $t0
## [1] "character"
##
## $t1
## [1] "character"
##
## $t2
## [1] "character"
##
## $t3
## [1] "character"
##
## $t4
## [1] "character"
##
## $t5
## [1] "character"
##
## $t6
## [1] "character"
##
## $t7
## [1] "character"
##
## $t8
## [1] "character"
##
## $t9
## [1] "character"
##
## $t10
## [1] "character"
##
## $t11
## [1] "character"
##
## $t12
## [1] "character"
##
## $t13
## [1] "character"
##
## $t14
## [1] "character"
##
## $t15
## [1] "character"
##
## $t16
## [1] "character"
##
```

```
## $t17
## [1] "character"
##
## $t18
## [1] "character"
##
## $t19
## [1] "character"
##
## $t20
## [1] "character"
##
## $t21
## [1] "character"
##
## $t22
## [1] "character"
##
## $t23
## [1] "character"
##
## $t_pk
## [1] "numeric"
##
## $t_av
## [1] "numeric"
##
## $t85
## [1] "character"
##
## $rh85
## [1] "character"
##
## $u85
## [1] "character"
##
## $v85
## [1] "character"
##
## $ht85
## [1] "character"
##
## $t70
## [1] "character"
##
## $rh70
## [1] "character"
##
## $u70
## [1] "character"
##
## $v70
## [1] "character"
##
```

```

## $ht70
## [1] "character"
##
## $t50
## [1] "character"
##
## $rh50
## [1] "character"
##
## $u50
## [1] "character"
##
## $v50
## [1] "character"
##
## $ht50
## [1] "character"
##
## $ki
## [1] "character"
##
## $tt
## [1] "character"
##
## $slp
## [1] "character"
##
## $slp_
## [1] "character"
##
## $percp
## [1] "numeric"
##
## $attribute
## [1] "integer"

write.table(onehrc2,file="C:/Users/Hafid Pradipta/OneDrive/Documentos/onehrc2.csv",sep=",",qmethod="double",as.is=T)
head(onehrc2)

```

```

## # A tibble: 6 x 73
##   wsr0 wsr1 wsr2 wsr3 wsr4 wsr5 wsr6 wsr7 wsr8 wsr9 wsr10 wsr11
##   <chr> <chr> <chr> <chr> <chr> <chr> <chr> <chr> <chr> <chr> <chr> <chr>
## 1  0.8  1.8  2.4  2.1    2  2.1  1.5  1.7  1.9  2.3  3.7  5.5
## 2  2.8  3.2  3.3  2.7  3.3  3.2  2.9  2.8  3.1  3.4  4.2  4.5
## 3  2.9  2.8  2.6  2.1  2.2  2.5  2.5  2.7  2.2  2.5  3.1    4
## 4  4.7  3.8  3.7  3.8  2.9  3.1  2.8  2.5  2.4  3.1  3.3  3.1
## 5  3.7  3.2  3.8  5.1    6    7  6.3  6.4  6.3  5.4  6.1  6.4
## 6  2.2  2.9  3.4  4.2  4.7  4.7  5.3  4.9  5.2    6  5.9  6.1
## # ... with 61 more variables: wsr12 <chr>, wsr13 <chr>, wsr14 <chr>,
## #   wsr15 <chr>, wsr16 <chr>, wsr17 <chr>, wsr18 <chr>, wsr19 <chr>,
## #   wsr20 <chr>, wsr21 <chr>, wsr22 <chr>, wsr23 <chr>, wsr_pk <chr>,
## #   wsr_av <chr>, t0 <chr>, t1 <chr>, t2 <chr>, t3 <chr>, t4 <chr>,
## #   t5 <chr>, t6 <chr>, t7 <chr>, t8 <chr>, t9 <chr>, t10 <chr>,
## #   t11 <chr>, t12 <chr>, t13 <chr>, t14 <chr>, t15 <chr>, t16 <chr>,
## #   t17 <chr>, t18 <chr>, t19 <chr>, t20 <chr>, t21 <chr>, t22 <chr>,

```

```
## #   t23 <chr>, t_pk <dbl>, t_av <dbl>, t85 <chr>, rh85 <chr>, u85 <chr>,
## #   v85 <chr>, ht85 <chr>, t70 <chr>, rh70 <chr>, u70 <chr>, v70 <chr>,
## #   ht70 <chr>, t50 <chr>, rh50 <chr>, u50 <chr>, v50 <chr>, ht50 <chr>,
## #   ki <chr>, tt <chr>, slp <chr>, slp_ <chr>, percp <dbl>,
## #   attribute <int>
```

only take the average of the temperature and the windspeed

```
library(readr)
onehrc2 <- read_csv("C:/Users/Hafid Pradipta/OneDrive/STAT 520/dataset/Ozone/onehrc2.csv")

## Parsed with column specification:
## cols(
##   .default = col_double()
## )

## See spec(...) for full column specifications.
```

Descriptive statistics

```
colnames(onehrc2)

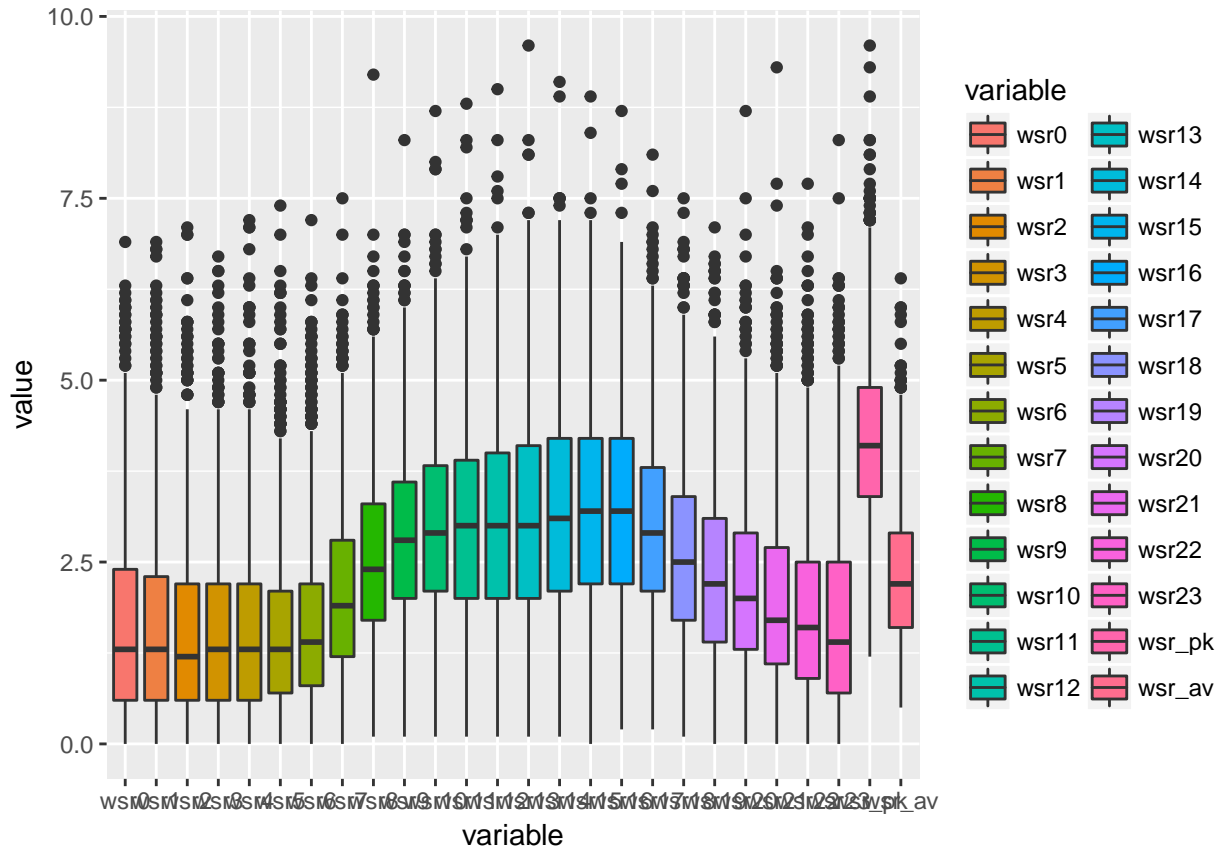
## [1] "wsr0"      "wsr1"      "wsr2"      "wsr3"      "wsr4"
## [6] "wsr5"      "wsr6"      "wsr7"      "wsr8"      "wsr9"
## [11] "wsr10"     "wsr11"     "wsr12"     "wsr13"     "wsr14"
## [16] "wsr15"     "wsr16"     "wsr17"     "wsr18"     "wsr19"
## [21] "wsr20"     "wsr21"     "wsr22"     "wsr23"     "wsr_pk"
## [26] "wsr_av"    "t0"        "t1"        "t2"        "t3"
## [31] "t4"        "t5"        "t6"        "t7"        "t8"
## [36] "t9"        "t10"       "t11"       "t12"       "t13"
## [41] "t14"       "t15"       "t16"       "t17"       "t18"
## [46] "t19"       "t20"       "t21"       "t22"       "t23"
## [51] "t_pk"      "t_av"      "t85"       "rh85"      "u85"
## [56] "v85"       "ht85"      "t70"       "rh70"      "u70"
## [61] "v70"       "ht70"      "t50"       "rh50"      "u50"
## [66] "v50"       "ht50"      "ki"        "tt"        "slp"
## [71] "slp_"     "percp"     "attribute"
```

```
#windspeede at given time
```

```
wsx<-onehrc2[,1:26]
datawsx<-melt(wsx)
```

```
## No id variables; using all as measure variables
```

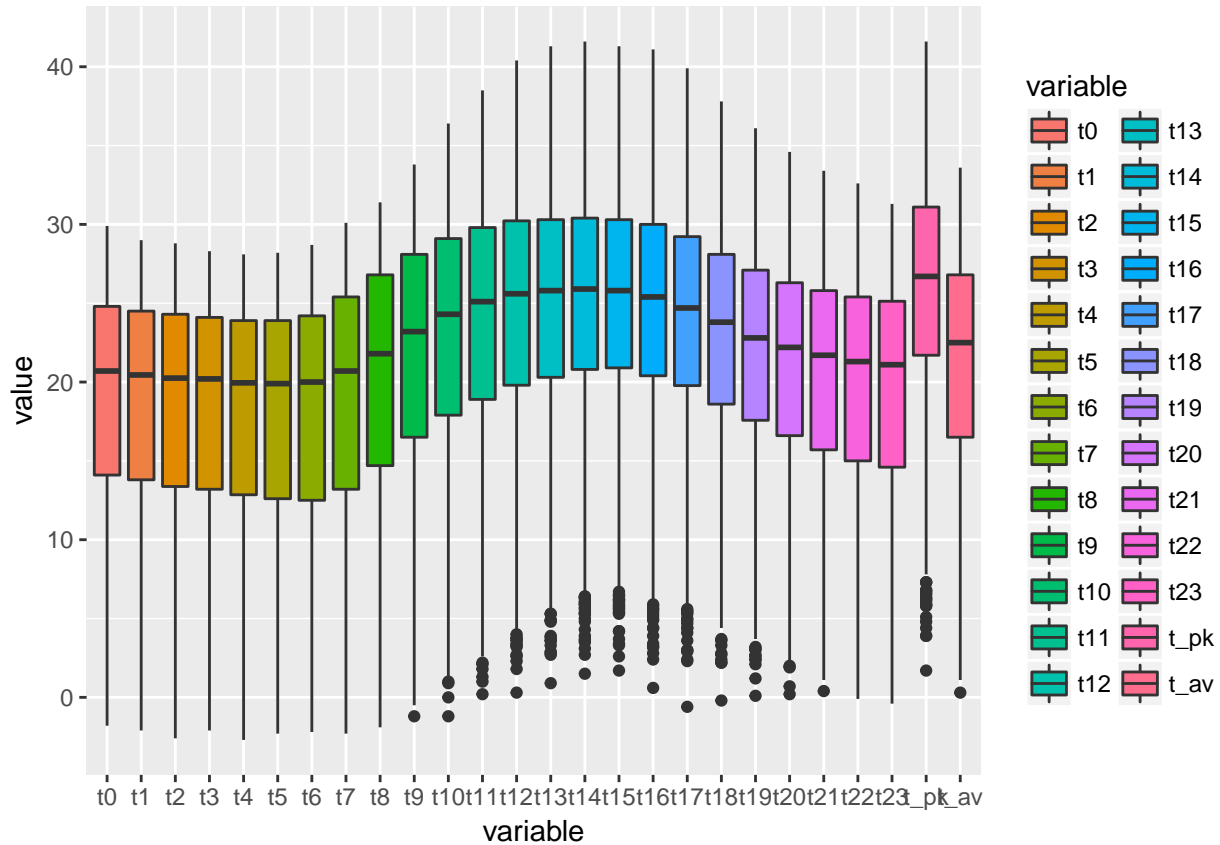
```
ggplot(datawsx,aes(x=variable, y=value, fill=variable)) + geom_boxplot()
```

```
#temperature at given time
tx<-onehrc2[,27:52]
datatx<-melt(tx)
```

```
## No id variables; using all as measure variables
```

```
ggplot(datatx,aes(x=variable, y=value, fill=variable)) + geom_boxplot()
```



```
#grouping
#using average temperature and winspeed
names(onehrc2)

## [1] "wsr0"      "wsr1"      "wsr2"      "wsr3"      "wsr4"
## [6] "wsr5"      "wsr6"      "wsr7"      "wsr8"      "wsr9"
## [11] "wsr10"     "wsr11"     "wsr12"     "wsr13"     "wsr14"
## [16] "wsr15"     "wsr16"     "wsr17"     "wsr18"     "wsr19"
## [21] "wsr20"     "wsr21"     "wsr22"     "wsr23"     "wsr_pk"
## [26] "wsr_av"    "t0"        "t1"        "t2"        "t3"
## [31] "t4"        "t5"        "t6"        "t7"        "t8"
## [36] "t9"        "t10"       "t11"       "t12"       "t13"
## [41] "t14"       "t15"       "t16"       "t17"       "t18"
## [46] "t19"       "t20"       "t21"       "t22"       "t23"
## [51] "t_pk"      "t_av"      "t85"       "rh85"      "u85"
## [56] "v85"       "ht85"      "t70"       "rh70"      "u70"
## [61] "v70"       "ht70"      "t50"       "rh50"      "u50"
## [66] "v50"       "ht50"      "ki"        "tt"        "slp"
## [71] "slp_"      "percp"     "attribute"
```

```
oneav<-onehrc2[,c(25,26,51:73)]
```

```
#check normality of whole dataset
uniNorm(oneav, type="SW")
```

```
## $`Descriptive Statistics`
```

```

##          n      Mean Std.Dev   Median    Min      Max      25th
## wsr_pk    1848      4.177   1.174      4.1    1.2      9.6      3.400
## wsr_av    1848      2.317   0.919      2.2    0.5      6.4      1.600
## t_pk      1848     25.892   6.859     26.7    1.7     41.6     21.700
## t_av      1848     21.164   6.749     22.5    0.3     33.6     16.500
## t85       1848     13.718   4.762     14.4   -4.5     24.5     10.800
## rh85      1848      0.582   0.256      0.6    0.0      1.0      0.400
## u85       1848      1.979   4.518      1.8  -15.8     18.3     -1.100
## v85       1848      1.944   6.094      1.7  -16.1     22.2     -2.200
## ht85      1848    1533.693  35.314    1537.0 1357.0   1642.0   1513.500
## t70       1848      6.077   3.801      6.8   -9.9     16.2      3.700
## rh70      1848      0.402   0.264      0.4    0.0      1.0      0.200
## u70       1848      5.167   6.329      4.8  -14.4     28.2      0.600
## v70       1848      1.012   6.294      0.9  -23.7     25.5     -2.800
## ht70      1848    3148.377  46.645    3156.0 2919.0   3249.0   3121.000
## t50       1848     -10.499   3.805    -10.1  -24.8     -1.7    -13.200
## rh50      1848      0.305   0.248      0.2    0.0      1.0      0.100
## u50       1848      9.820   9.345      9.2  -14.9     41.4      2.700
## v50       1848      0.647   7.354      0.3  -26.0     30.4     -4.000
## ht50      1848    5822.459  75.705    5835.0 5480.0   5965.0   5775.000
## ki        1848     10.690  20.175     14.7  -56.7     42.1     -2.725
## tt        1848     37.698  11.012     41.4  -10.1     59.2     33.000
## slp       1848   10165.446  52.058   10160.0 9995.0  10350.0  10130.000
## slp_      1848     -0.850  34.130      0.0 -135.0    140.0    -20.000
## percp     1848      0.360   1.263      0.0    0.0     20.7      0.000
## attribute 1848      0.031   0.173      0.0    0.0      1.0      0.000
##          75th    Skew Kurtosis
## wsr_pk      4.900  0.537    0.559
## wsr_av      2.900  0.744    0.378
## t_pk       31.100 -0.643    0.009
## t_av       26.800 -0.618   -0.493
## t85        17.400 -0.667    0.092
## rh85        0.800 -0.483   -0.788
## u85         4.800  0.155    0.357
## v85         6.100  0.059   -0.093
## ht85       1557.500 -0.677    1.317
## t70         9.000 -0.753    0.476
## rh70        0.600  0.309   -0.967
## u70         9.800  0.155   -0.310
## v70         4.700  0.052    0.507
## ht70       3181.500 -0.852    1.086
## t50        -7.400 -0.423   -0.467
## rh50        0.500  0.797   -0.295
## u50        16.500  0.165   -0.495
## v50         4.625  0.313    0.695
## ht50       5880.000 -0.831    0.525
## ki         27.825 -0.778   -0.122
## tt         45.200 -1.297    1.423
## slp       10195.000  0.506    0.582
## slp_        15.000  0.297    1.819
## percp        0.100  7.230   76.489
## attribute    0.000  5.423   27.420
##
## $`Shapiro-Wilk's Normality Test`

```

##	Variable	Statistic	p-value	Normality
## 1	wsr_pk	0.9835	0.0000	NO
## 2	wsr_av	0.9600	0.0000	NO
## 3	t_pk	0.9676	0.0000	NO
## 4	t_av	0.9478	0.0000	NO
## 5	t85	0.9658	0.0000	NO
## 6	rh85	0.9375	0.0000	NO
## 7	u85	0.9947	0.0000	NO
## 8	v85	0.9988	0.2081	YES
## 9	ht85	0.9763	0.0000	NO
## 10	t70	0.9621	0.0000	NO
## 11	rh70	0.9458	0.0000	NO
## 12	u70	0.9954	0.0000	NO
## 13	v70	0.9954	0.0000	NO
## 14	ht70	0.9614	0.0000	NO
## 15	t50	0.9751	0.0000	NO
## 16	rh50	0.9018	0.0000	NO
## 17	u50	0.9933	0.0000	NO
## 18	v50	0.9900	0.0000	NO
## 19	ht50	0.9520	0.0000	NO
## 20	ki	0.9314	0.0000	NO
## 21	tt	0.8857	0.0000	NO
## 22	slp	0.9804	0.0000	NO
## 23	slp_	0.9702	0.0000	NO
## 24	percp	0.3099	0.0000	NO
## 25	attribute	0.1621	0.0000	NO

```
normtest<-uniNorm(oneav, type="SW")
normtest
```

##	`Descriptive Statistics`						
##	n	Mean	Std.Dev	Median	Min	Max	25th
## wsr_pk	1848	4.177	1.174	4.1	1.2	9.6	3.400
## wsr_av	1848	2.317	0.919	2.2	0.5	6.4	1.600
## t_pk	1848	25.892	6.859	26.7	1.7	41.6	21.700
## t_av	1848	21.164	6.749	22.5	0.3	33.6	16.500
## t85	1848	13.718	4.762	14.4	-4.5	24.5	10.800
## rh85	1848	0.582	0.256	0.6	0.0	1.0	0.400
## u85	1848	1.979	4.518	1.8	-15.8	18.3	-1.100
## v85	1848	1.944	6.094	1.7	-16.1	22.2	-2.200
## ht85	1848	1533.693	35.314	1537.0	1357.0	1642.0	1513.500
## t70	1848	6.077	3.801	6.8	-9.9	16.2	3.700
## rh70	1848	0.402	0.264	0.4	0.0	1.0	0.200
## u70	1848	5.167	6.329	4.8	-14.4	28.2	0.600
## v70	1848	1.012	6.294	0.9	-23.7	25.5	-2.800
## ht70	1848	3148.377	46.645	3156.0	2919.0	3249.0	3121.000
## t50	1848	-10.499	3.805	-10.1	-24.8	-1.7	-13.200
## rh50	1848	0.305	0.248	0.2	0.0	1.0	0.100
## u50	1848	9.820	9.345	9.2	-14.9	41.4	2.700
## v50	1848	0.647	7.354	0.3	-26.0	30.4	-4.000
## ht50	1848	5822.459	75.705	5835.0	5480.0	5965.0	5775.000
## ki	1848	10.690	20.175	14.7	-56.7	42.1	-2.725
## tt	1848	37.698	11.012	41.4	-10.1	59.2	33.000
## slp	1848	10165.446	52.058	10160.0	9995.0	10350.0	10130.000
## slp_	1848	-0.850	34.130	0.0	-135.0	140.0	-20.000

```

## percp      1848      0.360  1.263    0.0    0.0    20.7    0.000
## attribute 1848      0.031  0.173    0.0    0.0     1.0    0.000
##           75th    Skew Kurtosis
## wsr_pk      4.900  0.537    0.559
## wsr_av      2.900  0.744    0.378
## t_pk       31.100 -0.643    0.009
## t_av       26.800 -0.618   -0.493
## t85        17.400 -0.667    0.092
## rh85        0.800 -0.483   -0.788
## u85         4.800  0.155    0.357
## v85         6.100  0.059   -0.093
## ht85       1557.500 -0.677    1.317
## t70         9.000 -0.753    0.476
## rh70        0.600  0.309   -0.967
## u70         9.800  0.155   -0.310
## v70         4.700  0.052    0.507
## ht70       3181.500 -0.852    1.086
## t50        -7.400 -0.423   -0.467
## rh50        0.500  0.797   -0.295
## u50        16.500  0.165   -0.495
## v50         4.625  0.313    0.695
## ht50       5880.000 -0.831    0.525
## ki         27.825 -0.778   -0.122
## tt         45.200 -1.297    1.423
## slp       10195.000  0.506    0.582
## slp_        15.000  0.297    1.819
## percp        0.100  7.230   76.489
## attribute    0.000  5.423   27.420
##
## $`Shapiro-Wilk's Normality Test`
##   Variable Statistic   p-value Normality
## 1  wsr_pk      0.9835    0.0000     NO
## 2  wsr_av      0.9600    0.0000     NO
## 3   t_pk      0.9676    0.0000     NO
## 4   t_av      0.9478    0.0000     NO
## 5    t85      0.9658    0.0000     NO
## 6   rh85      0.9375    0.0000     NO
## 7    u85      0.9947    0.0000     NO
## 8    v85      0.9988    0.2081     YES
## 9   ht85      0.9763    0.0000     NO
## 10   t70      0.9621    0.0000     NO
## 11  rh70      0.9458    0.0000     NO
## 12   u70      0.9954    0.0000     NO
## 13   v70      0.9954    0.0000     NO
## 14  ht70      0.9614    0.0000     NO
## 15   t50      0.9751    0.0000     NO
## 16  rh50      0.9018    0.0000     NO
## 17   u50      0.9933    0.0000     NO
## 18   v50      0.9900    0.0000     NO
## 19  ht50      0.9520    0.0000     NO
## 20   ki      0.9314    0.0000     NO
## 21   tt      0.8857    0.0000     NO
## 22   slp      0.9804    0.0000     NO
## 23  slp_      0.9702    0.0000     NO

```

```
## 24 percp      0.3099    0.0000    NO
## 25 attribute  0.1621    0.0000    NO
```

```
#visualizatoion of normality dataset
```

```
name<-colnames(oneav)
```

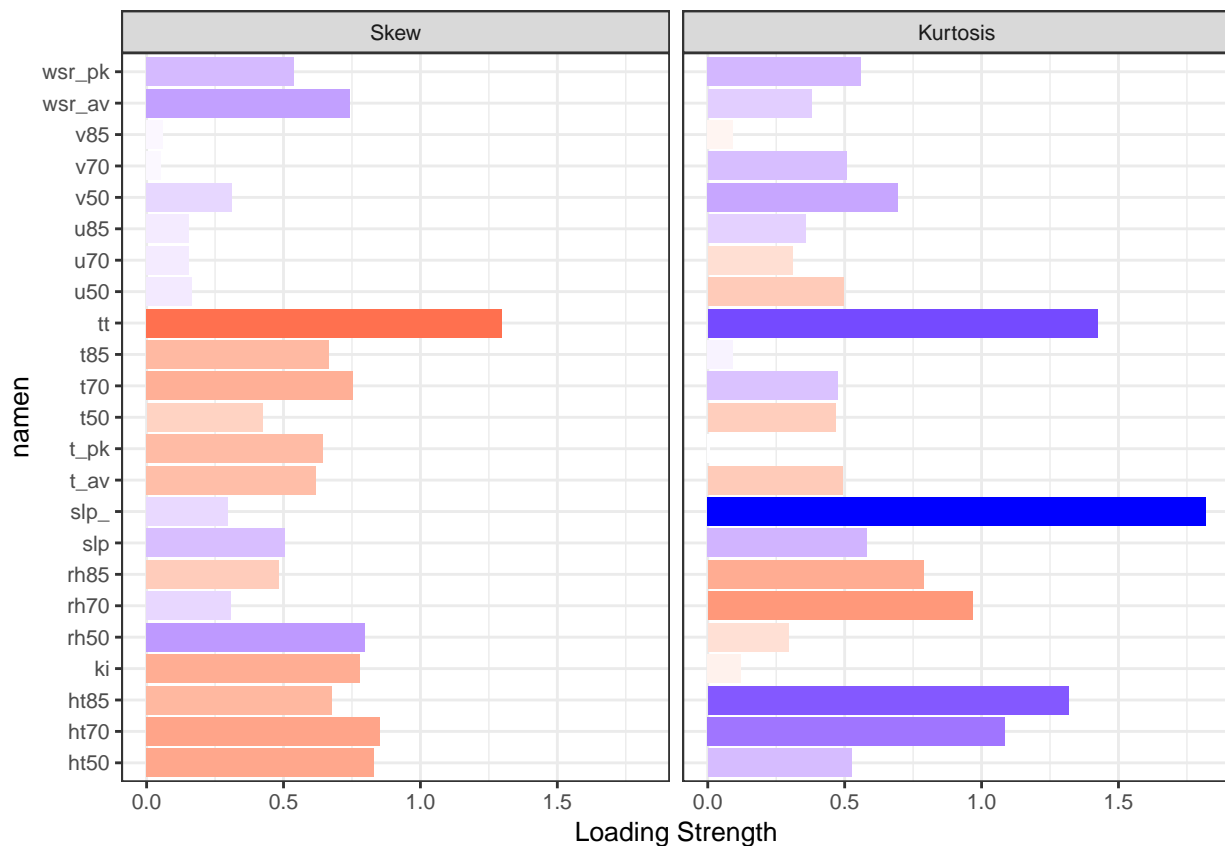
```
namen<-colnames(oneav[1:23])
```

```
normplot<-normtest$`Descriptive Statistics`[1:23,9:10]
```

```
datanorm<-data.frame(namen,normplot)
```

```
loadings.1 <- melt(datanorm, id="namen",
                  measure=c("Skew", "Kurtosis"),
                  variable.name="Factor", value.name="Loading")
```

```
ggplot(loadings.1, aes(namen, abs>Loading), fill=Loading)) +
  facet_wrap(~ Factor, nrow=1) + #place the factors in separate facets
  geom_bar(stat="identity") + #make the bars
  coord_flip() + #flip the axes so the test names can be horizontal
  #define the fill color gradient: blue=positive, red=negative
  scale_fill_gradient2(name = "Loading",
                      high = "blue", mid = "white", low = "red",
                      midpoint=0, guide=F) +
  ylab("Loading Strength") + #improve y-axis label
  theme_bw(base_size=10) #use a black-and-white theme with set font size
```



```
colnames(oneav)
```

```
## [1] "wsr_pk" "wsr_av" "t_pk" "t_av" "t85"
## [6] "rh85" "u85" "v85" "ht85" "t70"
## [11] "rh70" "u70" "v70" "ht70" "t50"
```

```
## [16] "rh50"      "u50"      "v50"      "ht50"     "ki"
## [21] "tt"        "slp"      "slp_"     "percp"    "attribute"

#windspeedrate
wsr<-oneav[,1:2]
datawsr<- melt(wsr)

## No id variables; using all as measure variables
#ggplot(datawsr,aes(x=variable, y=value, fill=variable)) + geom_boxplot()

#temperature
tempav<-oneav[,3:4]
datatempav<- melt(tempav)

## No id variables; using all as measure variables
#ggplot(datatempav,aes(x=variable, y=value, fill=variable)) + geom_boxplot()

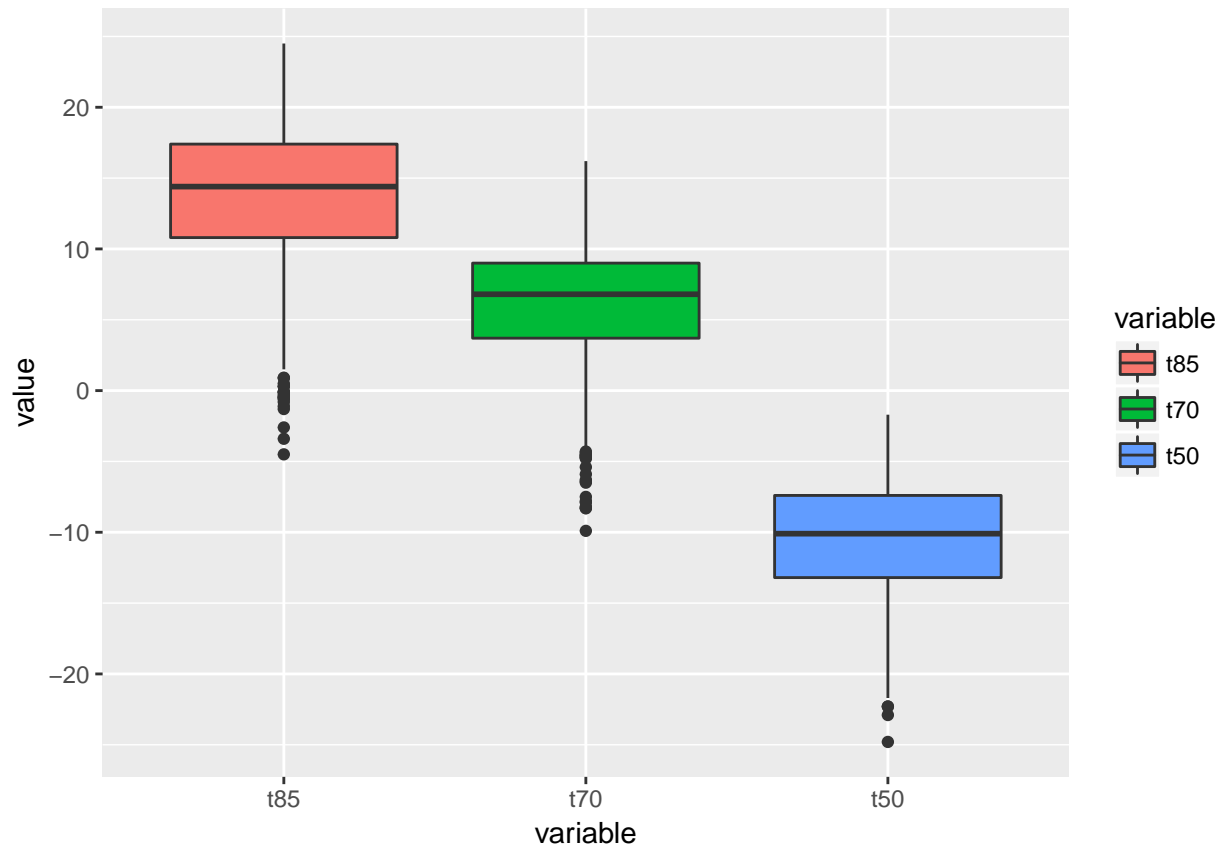
#various variable at 85hpa(1500m)
x85<-oneav[,5:9]

#various variable at 70hpa(3100m)
x70<-oneav[,10:14]

#various variable at 50hpa(5500m)
x50<-oneav[,15:19]

#temperature at various level
temp<-oneav[,c(5,10,15)]
datatemp<- melt(temp)

## No id variables; using all as measure variables
ggplot(datatemp,aes(x=variable, y=value, fill=variable)) + geom_boxplot()
```



```
#skew to the right, transformation for lambda<1
```

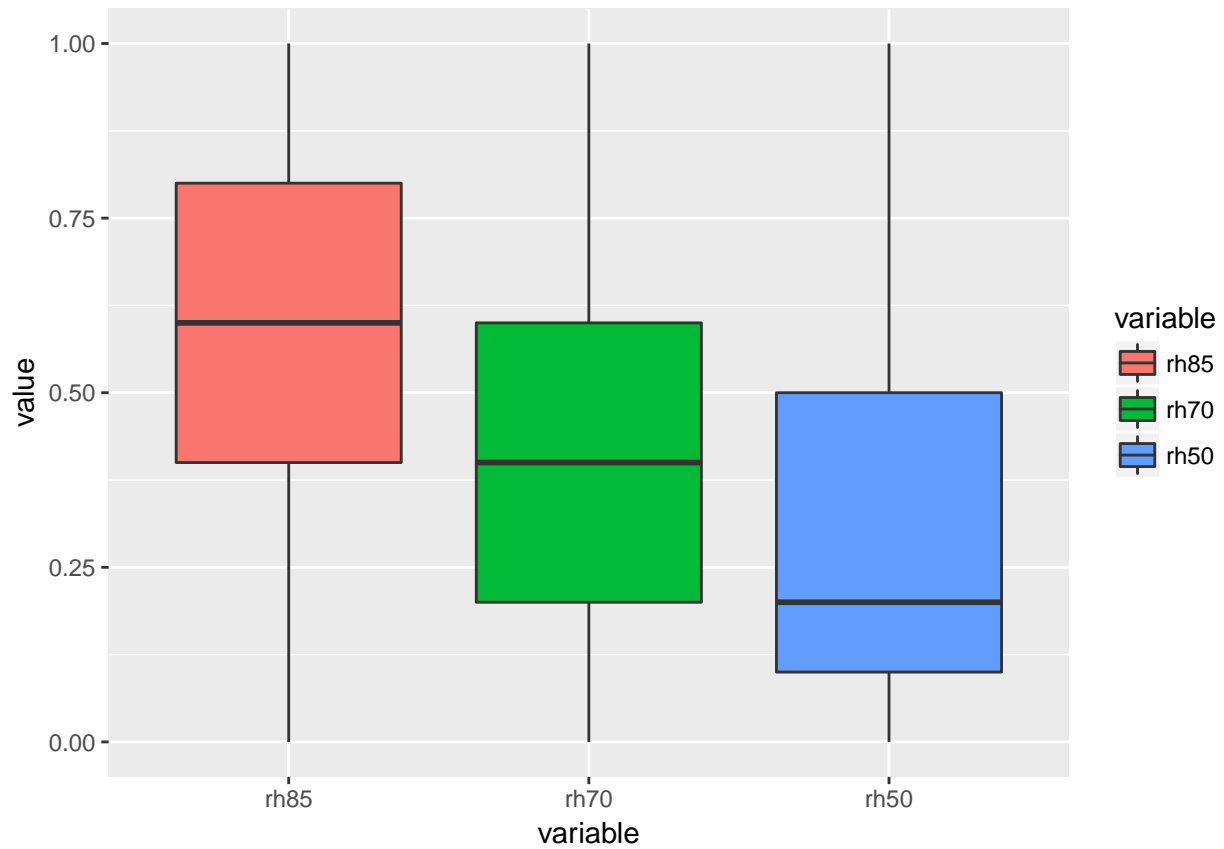
```
#relative humidity
```

```
rhum<-oneav[,c(6,11,16)]
```

```
datarhum<- melt(rhum)
```

```
## No id variables; using all as measure variables
```

```
ggplot(datarhum,aes(x=variable, y=value, fill=variable)) + geom_boxplot()
```

```
#skewed to the right
```

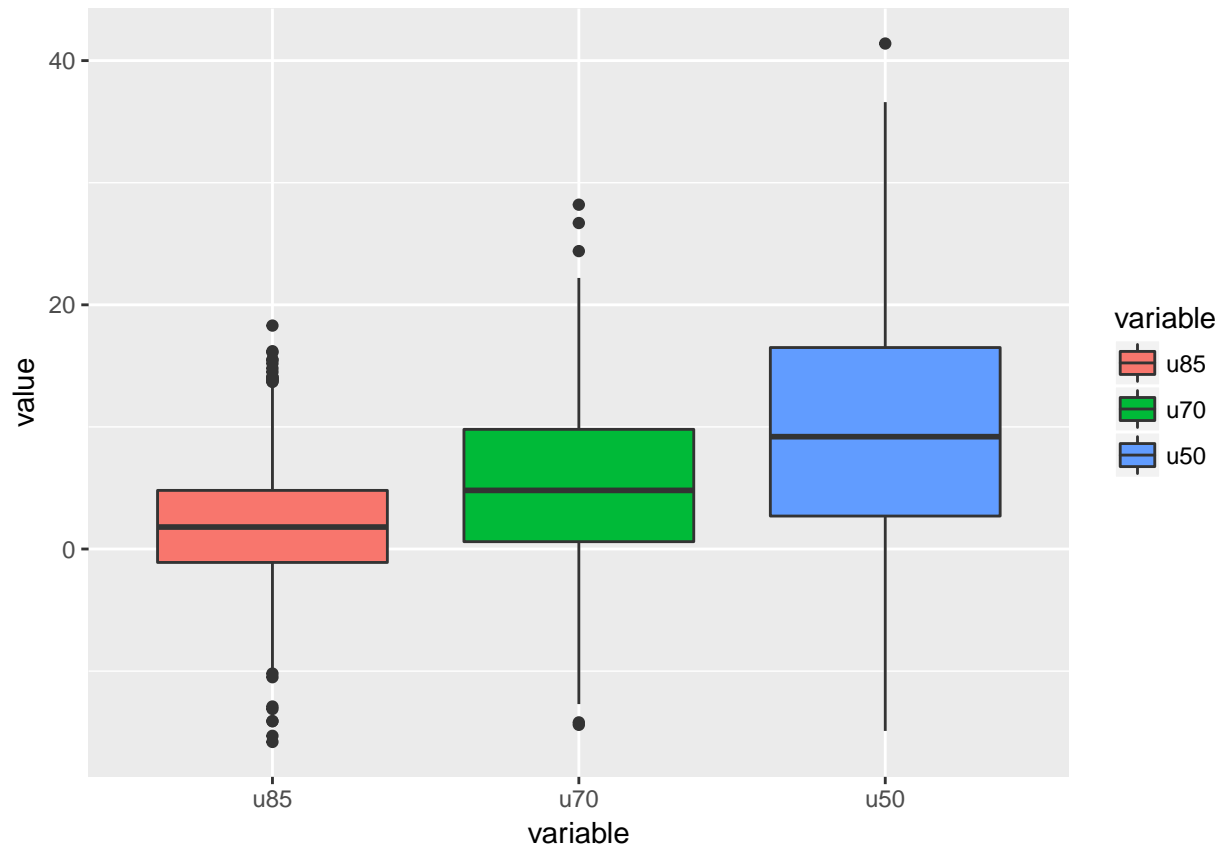
```
#Uwind
```

```
ns<-oneav[,c(7,12,17)]
```

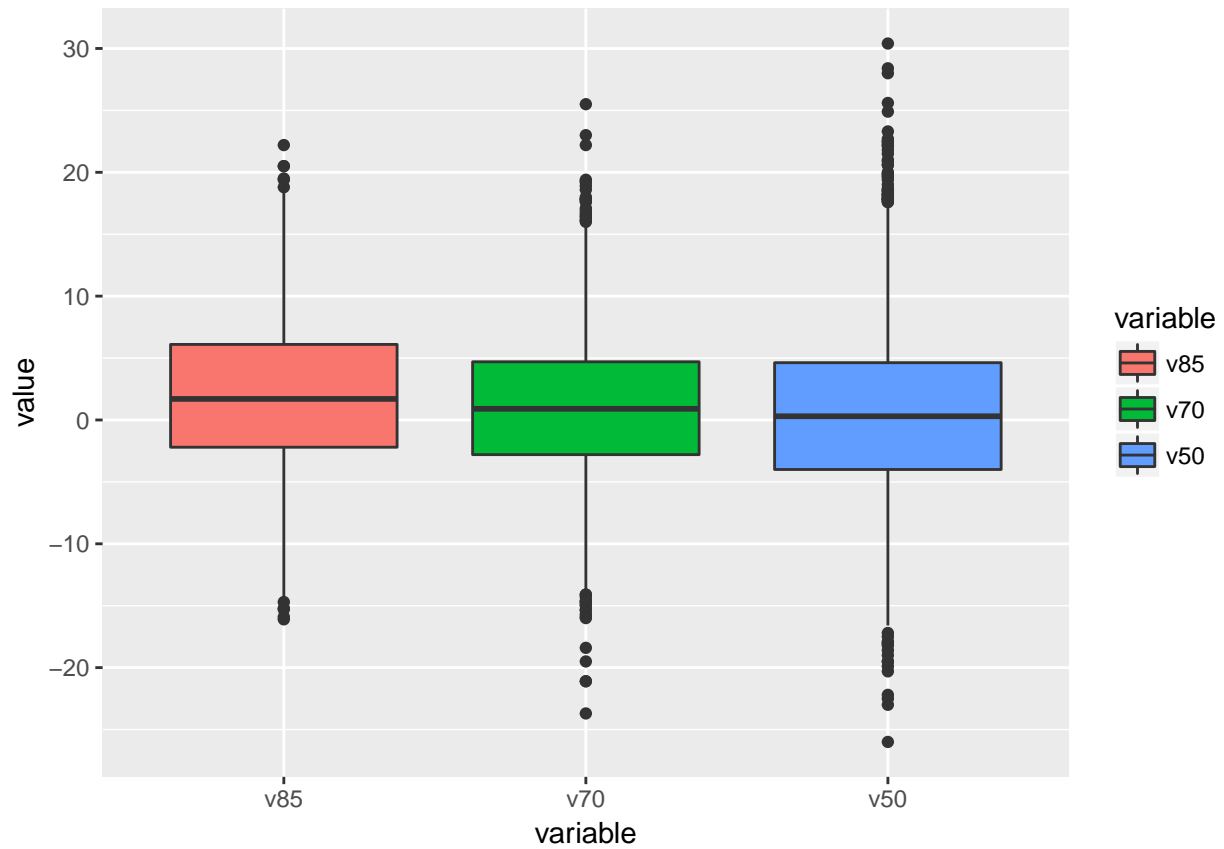
```
datans<- melt(ns)
```

```
## No id variables; using all as measure variables
```

```
ggplot(datans,aes(x=variable, y=value, fill=variable)) + geom_boxplot()
```



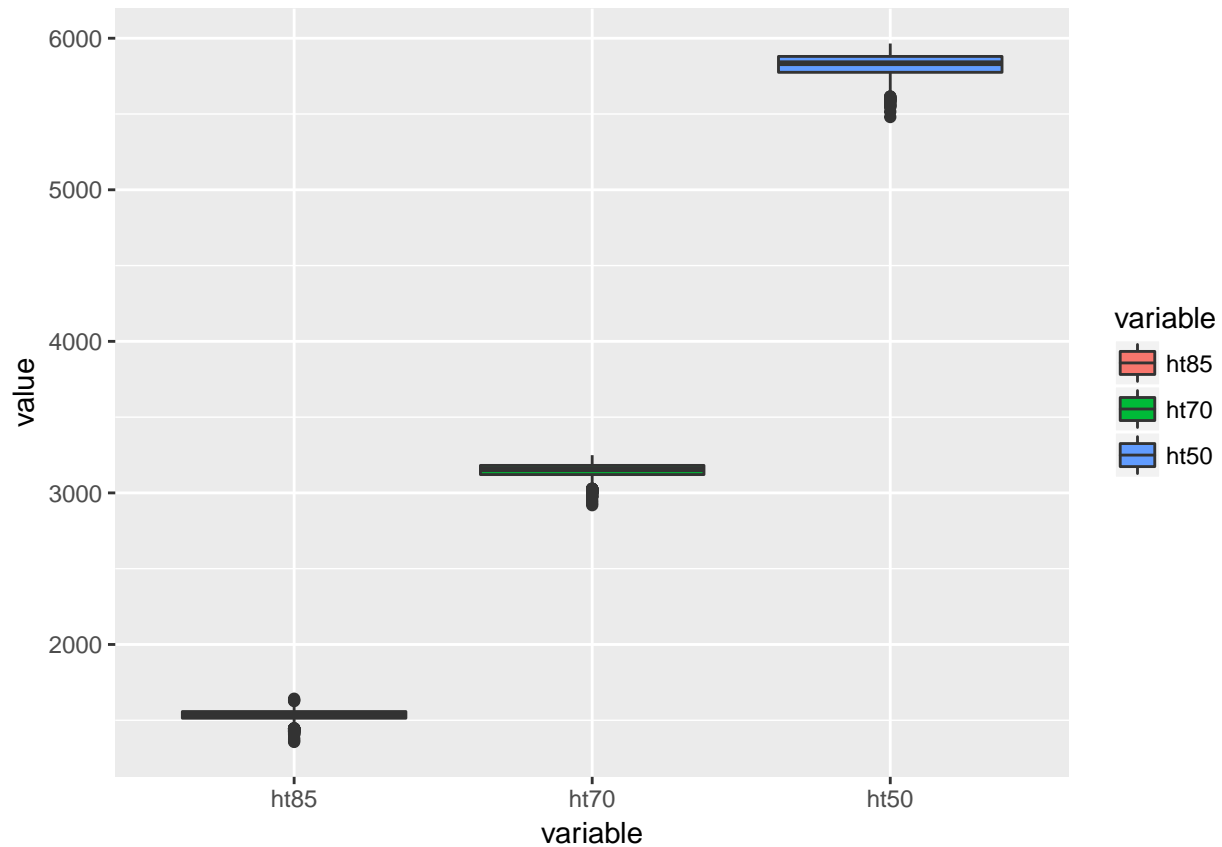
```
#Vwind  
ew<-oneav[,c(8,13,18)]  
dataew<-melt(ew)  
  
## No id variables; using all as measure variables  
ggplot(dataew,aes(x=variable, y=value, fill=variable)) + geom_boxplot()
```



```
#geopotential height
ht<-oneav[,c(9,14,19)]
dataht<-melt(ht)
```

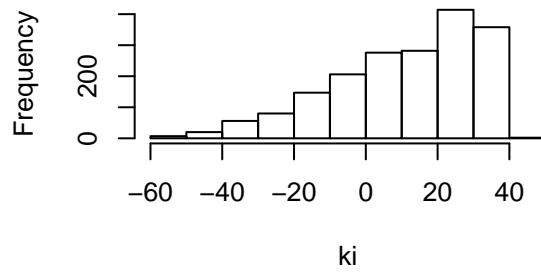
```
## No id variables; using all as measure variables
```

```
ggplot(dataht,aes(x=variable, y=value, fill=variable)) + geom_boxplot()
```

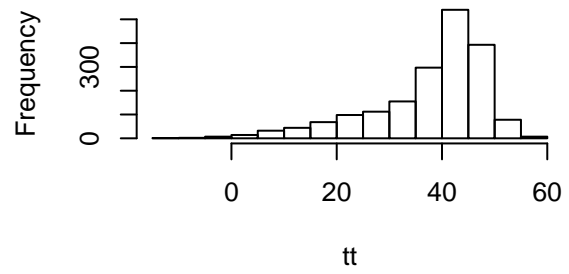


```
#combination of all plot
#install.packages("devtools")
library(devtools)
#install_github("easyGgplot2", "kassambara")
library(easyGgplot2)
plot1<-ggplot(datatemp,aes(x=variable, y=value, fill=variable)) + geom_boxplot()
plot2<-ggplot(datarhum,aes(x=variable, y=value, fill=variable)) + geom_boxplot()
plot3<-ggplot(datans,aes(x=variable, y=value, fill=variable)) + geom_boxplot()
plot4<-ggplot(dataew,aes(x=variable, y=value, fill=variable)) + geom_boxplot()
plot5<-ggplot(dataht,aes(x=variable, y=value, fill=variable)) + geom_boxplot()
ggplot2.multiplot(plot1,plot2,plot3,plot4,plot5, cols=1)
```

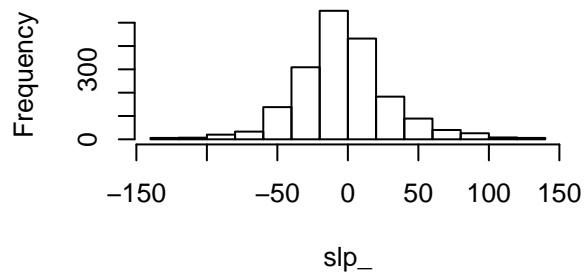

Histogram of ki



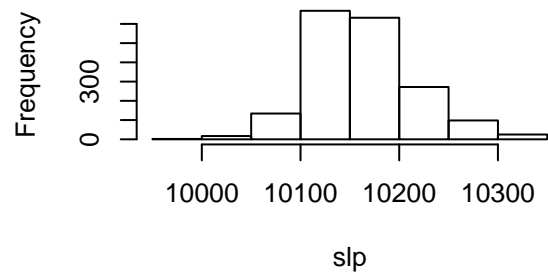
Histogram of tt



Histogram of slp_

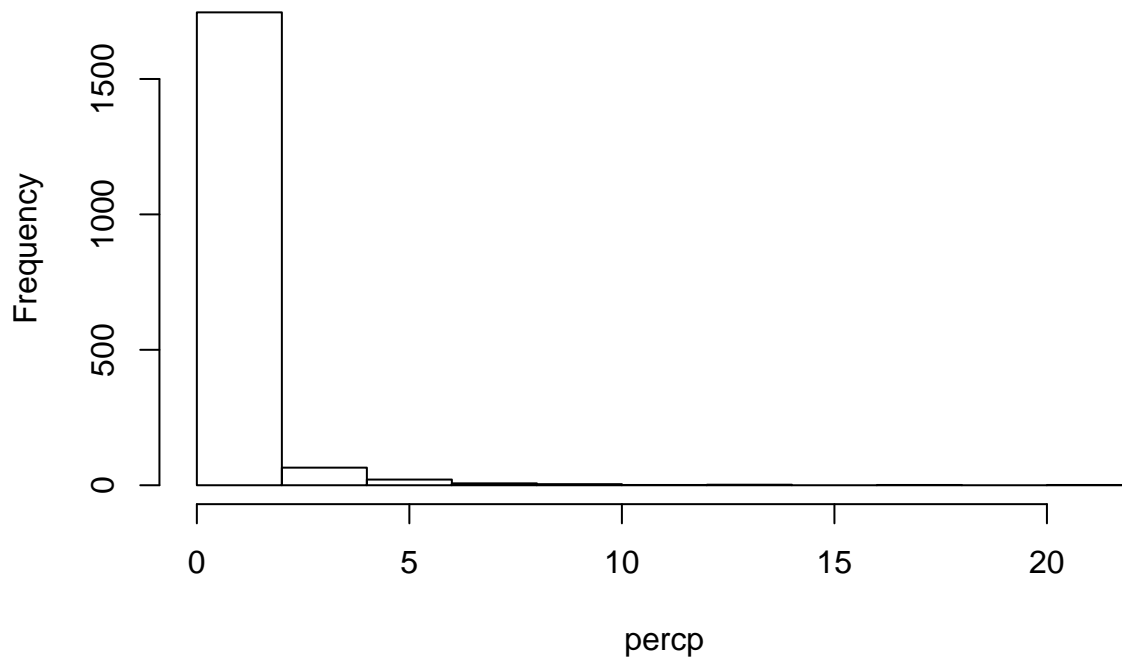


Histogram of slp



```
par(mfrow=c(1,1))  
hist(percp)
```

Histogram of percip



something to point out

```
summary(oneav)
```

```
##      wsr_pk      wsr_av      t_pk      t_av
## Min.   :1.200  Min.   :0.500  Min.   : 1.70  Min.   : 0.30
## 1st Qu.:3.400  1st Qu.:1.600  1st Qu.:21.70  1st Qu.:16.50
## Median :4.100  Median :2.200  Median :26.70  Median :22.50
## Mean   :4.177  Mean   :2.317  Mean   :25.89  Mean   :21.16
## 3rd Qu.:4.900  3rd Qu.:2.900  3rd Qu.:31.10  3rd Qu.:26.80
## Max.   :9.600  Max.   :6.400  Max.   :41.60  Max.   :33.60
##      t85      rh85      u85      v85
## Min.   : -4.50  Min.   :0.0000  Min.   : -15.800  Min.   : -16.100
## 1st Qu.:10.80  1st Qu.:0.4000  1st Qu.: -1.100  1st Qu.: -2.200
## Median :14.40  Median :0.6000  Median :  1.800  Median :  1.700
## Mean   :13.72  Mean   :0.5818  Mean   :  1.979  Mean   :  1.944
## 3rd Qu.:17.40  3rd Qu.:0.8000  3rd Qu.:  4.800  3rd Qu.:  6.100
## Max.   :24.50  Max.   :1.0000  Max.   : 18.300  Max.   : 22.200
##      ht85      t70      rh70      u70
## Min.   :1357  Min.   : -9.900  Min.   :0.000  Min.   : -14.400
## 1st Qu.:1514  1st Qu.:  3.700  1st Qu.:0.200  1st Qu.:  0.600
## Median :1537  Median :  6.800  Median :0.400  Median :  4.800
## Mean   :1534  Mean   :  6.077  Mean   :0.402  Mean   :  5.167
## 3rd Qu.:1558  3rd Qu.:  9.000  3rd Qu.:0.600  3rd Qu.:  9.800
```

```
## Max. :1642 Max. :16.200 Max. :1.000 Max. : 28.200
## v70 ht70 t50 rh50
## Min. :-23.700 Min. :2919 Min. :-24.8 Min. :0.000
## 1st Qu.: -2.800 1st Qu.:3121 1st Qu.: -13.2 1st Qu.:0.100
## Median : 0.900 Median :3156 Median : -10.1 Median :0.200
## Mean : 1.012 Mean :3148 Mean : -10.5 Mean :0.305
## 3rd Qu.: 4.700 3rd Qu.:3182 3rd Qu.: -7.4 3rd Qu.:0.500
## Max. : 25.500 Max. :3249 Max. : -1.7 Max. :1.000
## u50 v50 ht50 ki
## Min. :-14.90 Min. :-26.0000 Min. :5480 Min. : -56.700
## 1st Qu.: 2.70 1st Qu.: -4.0000 1st Qu.:5775 1st Qu.: -2.725
## Median : 9.20 Median : 0.3000 Median :5835 Median : 14.700
## Mean : 9.82 Mean : 0.6467 Mean :5822 Mean : 10.690
## 3rd Qu.: 16.50 3rd Qu.: 4.6250 3rd Qu.:5880 3rd Qu.: 27.825
## Max. : 41.40 Max. : 30.4000 Max. :5965 Max. : 42.100
## tt slp slp_ percp
## Min. :-10.1 Min. : 9995 Min. : -135.0000 Min. : 0.0000
## 1st Qu.: 33.0 1st Qu.:10130 1st Qu.: -20.0000 1st Qu.: 0.0000
## Median : 41.4 Median :10160 Median : 0.0000 Median : 0.0000
## Mean : 37.7 Mean :10165 Mean : -0.8496 Mean : 0.3597
## 3rd Qu.: 45.2 3rd Qu.:10195 3rd Qu.: 15.0000 3rd Qu.: 0.1000
## Max. : 59.2 Max. :10350 Max. : 140.0000 Max. :20.7000
## attribute
## Min. :0.00000
## 1st Qu.:0.00000
## Median :0.00000
## Mean :0.03084
## 3rd Qu.:0.00000
## Max. :1.00000
```

*#the one that is not negative is relative humidity, geometric height, and slp
#skew to the left, try trasnformation for squared and cube*

```
trrhum<-(rhum)^3
uniNorm(trrhum, type = "SW")
```

```
## $`Descriptive Statistics`
##      n Mean Std.Dev Median Min Max 25th 75th Skew Kurtosis
## rh85 1848 0.303 0.263 0.216 0 1 0.064 0.512 0.680 -0.410
## rh70 1848 0.155 0.215 0.064 0 1 0.008 0.216 1.834 3.202
## rh50 1848 0.097 0.177 0.008 0 1 0.001 0.125 2.558 6.678
##
## $`Shapiro-Wilk's Normality Test`
## Variable Statistic p-value Normality
## 1 rh85 0.8977 0 NO
## 2 rh70 0.7336 0 NO
## 3 rh50 0.6010 0 NO
```

```
summary(rhum)
```

```
##      rh85      rh70      rh50
## Min. :0.0000 Min. :0.000 Min. :0.000
## 1st Qu.:0.4000 1st Qu.:0.200 1st Qu.:0.100
## Median :0.6000 Median :0.400 Median :0.200
## Mean :0.5818 Mean :0.402 Mean :0.305
## 3rd Qu.:0.8000 3rd Qu.:0.600 3rd Qu.:0.500
```



```
## Max.      :1.0000   Max.      :1.000   Max.      :1.000
#skew to the left, try transformation for squared and cube
trht<-ht^3
uniNorm(trht, type = "SW")

## $`Descriptive Statistics`
##           n          Mean      Std.Dev        Median          Min          Max
## ht85 1848   3613282500  245682940   3630961153   2498846293   4427101288
## ht70 1848   31228028371 1370317276   31434820416  24871517559  34296447249
## ht50 1848   197487086783 7618916469 198665557875 164566592000 212242007125
##           25th          75th      Skew Kurtosis
## ht85   3466947585   3778193234 -0.484    0.859
## ht70   30400540561  32202959268 -0.748    0.783
## ht50  192599859375 203297472000 -0.760    0.327
##
## $`Shapiro-Wilk's Normality Test`
##      Variable Statistic    p-value Normality
## 1    ht85         0.9863         0      NO
## 2    ht70         0.9691         0      NO
## 3    ht50         0.9579         0      NO
#data contains negative
```

correlation Matrix

```
#code taken from http://www.sthda.com/english/wiki/ggplot2-quick-correlation-matrix-heatmap-r-software-
#correlation matrix heatmap of the dataset
cormat<-round(cor(oneav),2)
cormat
```

```
##           wsr_pk wsr_av  t_pk  t_av  t85  rh85  u85  v85  ht85  t70
## wsr_pk      1.00   0.85 -0.17 -0.13 -0.09  0.03  0.18  0.39 -0.26 -0.09
## wsr_av      0.85   1.00 -0.23 -0.15 -0.08  0.06  0.18  0.48 -0.25 -0.04
## t_pk       -0.17 -0.23  1.00  0.97  0.83  0.17 -0.33  0.15  0.27  0.75
## t_av       -0.13 -0.15  0.97  1.00  0.86  0.27 -0.35  0.26  0.26  0.78
## t85        -0.09 -0.08  0.83  0.86  1.00  0.20 -0.27  0.32  0.19  0.87
## rh85        0.03  0.06  0.17  0.27  0.20  1.00 -0.04  0.32 -0.08  0.16
## u85         0.18  0.18 -0.33 -0.35 -0.27 -0.04  1.00  0.10 -0.42 -0.27
## v85         0.39  0.48  0.15  0.26  0.32  0.32  0.10  1.00 -0.12  0.33
## ht85       -0.26 -0.25  0.27  0.26  0.19 -0.08 -0.42 -0.12  1.00  0.19
## t70        -0.09 -0.04  0.75  0.78  0.87  0.16 -0.27  0.33  0.19  1.00
## rh70       -0.04 -0.02  0.07  0.15  0.22  0.52 -0.10  0.15 -0.02 -0.06
## u70         0.20  0.23 -0.61 -0.62 -0.54 -0.12  0.78 -0.01 -0.47 -0.50
## v70         0.34  0.41 -0.05  0.05  0.18  0.33  0.13  0.81 -0.21  0.19
## ht70       -0.25 -0.22  0.64  0.65  0.66  0.06 -0.46  0.09  0.85  0.65
## t50        -0.21 -0.18  0.72  0.76  0.81  0.24 -0.37  0.17  0.28  0.84
## rh50        0.03  0.05 -0.01  0.07  0.13  0.32 -0.02  0.22 -0.04  0.03
## u50         0.21  0.23 -0.68 -0.69 -0.62 -0.16  0.64 -0.04 -0.46 -0.56
## v50         0.26  0.29 -0.24 -0.15  0.01  0.28  0.18  0.54 -0.32  0.00
## ht50       -0.23 -0.20  0.75  0.78  0.81  0.14 -0.45  0.18  0.64  0.84
## ki         -0.01  0.01  0.41  0.50  0.54  0.75 -0.12  0.31 -0.01  0.28
## tt          0.07  0.09  0.39  0.47  0.47  0.81  0.00  0.38 -0.10  0.29
```

```

## slp      -0.13 -0.10 -0.47 -0.50 -0.58 -0.35 -0.09 -0.33  0.65 -0.48
## slp_     -0.23 -0.21 -0.14 -0.17 -0.13 -0.22 -0.09 -0.45  0.22 -0.10
## percp    0.12  0.07 -0.06 -0.01  0.05  0.17 -0.05  0.19 -0.05  0.00
## attribute -0.13 -0.16  0.17  0.14  0.12 -0.02 -0.11 -0.09  0.07  0.09
##          rh70  u70   v70  ht70   t50  rh50   u50   v50  ht50   ki
## wsr_pk   -0.04  0.20  0.34 -0.25 -0.21  0.03  0.21  0.26 -0.23 -0.01
## wsr_av   -0.02  0.23  0.41 -0.22 -0.18  0.05  0.23  0.29 -0.20  0.01
## t_pk      0.07 -0.61 -0.05  0.64  0.72 -0.01 -0.68 -0.24  0.75  0.41
## t_av      0.15 -0.62  0.05  0.65  0.76  0.07 -0.69 -0.15  0.78  0.50
## t85       0.22 -0.54  0.18  0.66  0.81  0.13 -0.62  0.01  0.81  0.54
## rh85      0.52 -0.12  0.33  0.06  0.24  0.32 -0.16  0.28  0.14  0.75
## u85      -0.10  0.78  0.13 -0.46 -0.37 -0.02  0.64  0.18 -0.45 -0.12
## v85       0.15 -0.01  0.81  0.09  0.17  0.22 -0.04  0.54  0.18  0.31
## ht85     -0.02 -0.47 -0.21  0.85  0.28 -0.04 -0.46 -0.32  0.64 -0.01
## t70      -0.06 -0.50  0.19  0.65  0.84  0.03 -0.56  0.00  0.84  0.28
## rh70      1.00 -0.10  0.23  0.07  0.19  0.51 -0.16  0.25  0.09  0.80
## u70      -0.10  1.00  0.12 -0.65 -0.59  0.00  0.88  0.24 -0.67 -0.24
## v70       0.23  0.12  1.00 -0.05  0.10  0.28  0.09  0.79  0.04  0.29
## ht70      0.07 -0.65 -0.05  1.00  0.67  0.04 -0.67 -0.23  0.94  0.25
## t50       0.19 -0.59  0.10  0.67  1.00  0.02 -0.62 -0.02  0.86  0.39
## rh50      0.51  0.00  0.28  0.04  0.02  1.00 -0.01  0.30  0.04  0.45
## u50      -0.16  0.88  0.09 -0.67 -0.62 -0.01  1.00  0.25 -0.70 -0.32
## v50       0.25  0.24  0.79 -0.23 -0.02  0.30  0.25  1.00 -0.15  0.23
## ht50      0.09 -0.67  0.04  0.94  0.86  0.04 -0.70 -0.15  1.00  0.33
## ki        0.80 -0.24  0.29  0.25  0.39  0.45 -0.32  0.23  0.33  1.00
## tt        0.47 -0.16  0.32  0.15  0.21  0.34 -0.24  0.22  0.22  0.85
## slp      -0.21  0.08 -0.29  0.19 -0.38 -0.14  0.15 -0.25 -0.09 -0.48
## slp_     -0.13  0.05 -0.32  0.10 -0.04 -0.11  0.08 -0.19  0.03 -0.20
## percp    0.25 -0.01  0.24 -0.02  0.03  0.23  0.00  0.21  0.00  0.20
## attribute -0.01 -0.15 -0.09  0.11  0.11 -0.07 -0.14 -0.09  0.12  0.03
##          tt   slp  slp_ percp attribute
## wsr_pk    0.07 -0.13 -0.23  0.12      -0.13
## wsr_av    0.09 -0.10 -0.21  0.07      -0.16
## t_pk      0.39 -0.47 -0.14 -0.06      0.17
## t_av      0.47 -0.50 -0.17 -0.01      0.14
## t85       0.47 -0.58 -0.13  0.05      0.12
## rh85      0.81 -0.35 -0.22  0.17      -0.02
## u85       0.00 -0.09 -0.09 -0.05      -0.11
## v85       0.38 -0.33 -0.45  0.19      -0.09
## ht85     -0.10  0.65  0.22 -0.05      0.07
## t70       0.29 -0.48 -0.10  0.00      0.09
## rh70      0.47 -0.21 -0.13  0.25      -0.01
## u70      -0.16  0.08  0.05 -0.01      -0.15
## v70       0.32 -0.29 -0.32  0.24      -0.09
## ht70      0.15  0.19  0.10 -0.02      0.11
## t50       0.21 -0.38 -0.04  0.03      0.11
## rh50      0.34 -0.14 -0.11  0.23      -0.07
## u50      -0.24  0.15  0.08  0.00      -0.14
## v50       0.22 -0.25 -0.19  0.21      -0.09
## ht50      0.22 -0.09  0.03  0.00      0.12
## ki        0.85 -0.48 -0.20  0.20      0.03
## tt        1.00 -0.53 -0.24  0.14      0.02
## slp      -0.53  1.00  0.32 -0.09      -0.05
## slp_     -0.24  0.32  1.00 -0.08      -0.01

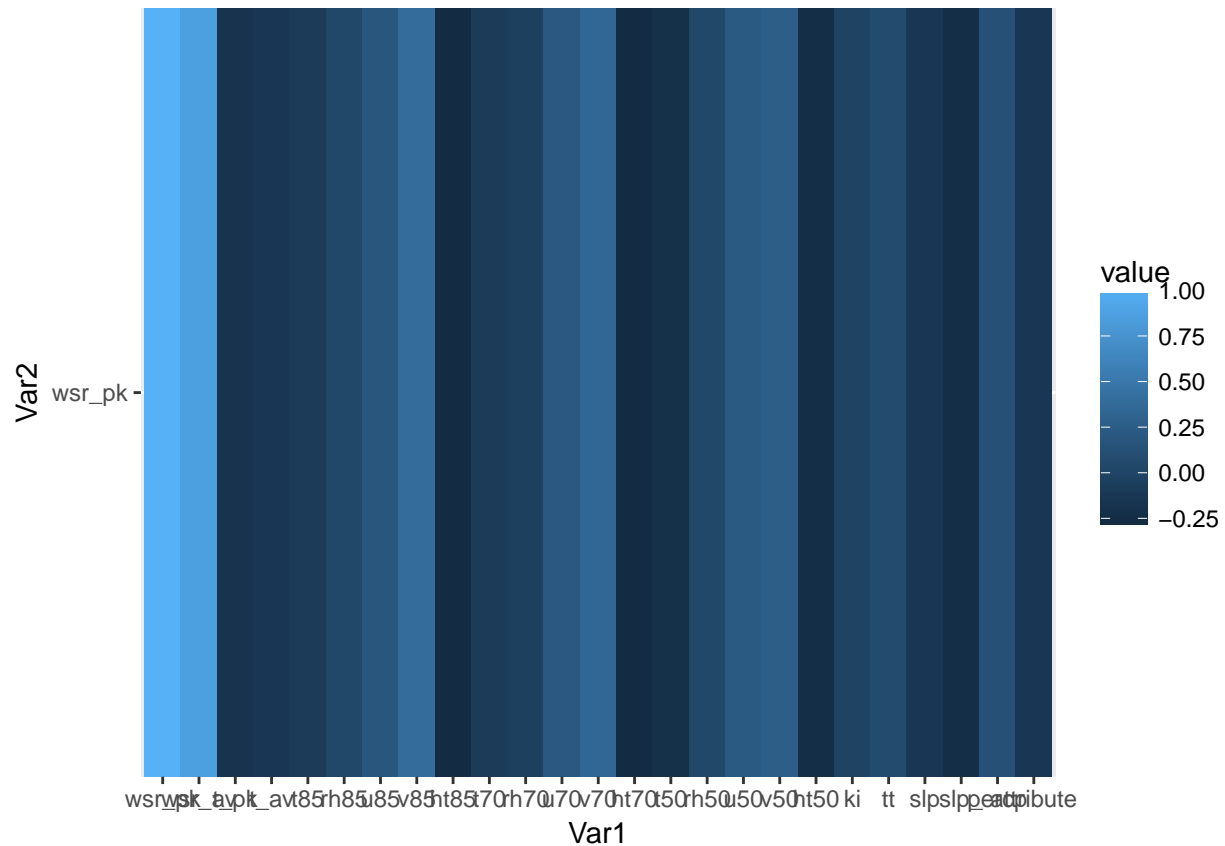
```

```
## percp      0.14 -0.09 -0.08  1.00      -0.04
## attribute  0.02 -0.05 -0.01 -0.04      1.00
```

```
#reshape
library(reshape2)
melted_cormat<-melt(cormat)
head(melted_cormat)
```

```
##      Var1  Var2 value
## 1 wsr_pk wsr_pk  1.00
## 2 wsr_av wsr_pk  0.85
## 3  t_pk wsr_pk -0.17
## 4  t_av wsr_pk -0.13
## 5   t85 wsr_pk -0.09
## 6  rh85 wsr_pk  0.03
```

```
attach(melted_cormat)
melted_cormat<-melted_cormat[Var1,]
library(ggplot2)
ggplot(data=melted_cormat, aes(x=Var1, y=Var2, fill=value))+geom_tile()
```



```
get_lower_tri<-function(cormat){
  cormat[upper.tri(cormat)] <- NA
  return(cormat)
}
# Get upper triangle of the correlation matrix
get_upper_tri <- function(cormat){
  cormat[lower.tri(cormat)]<- NA
```

```

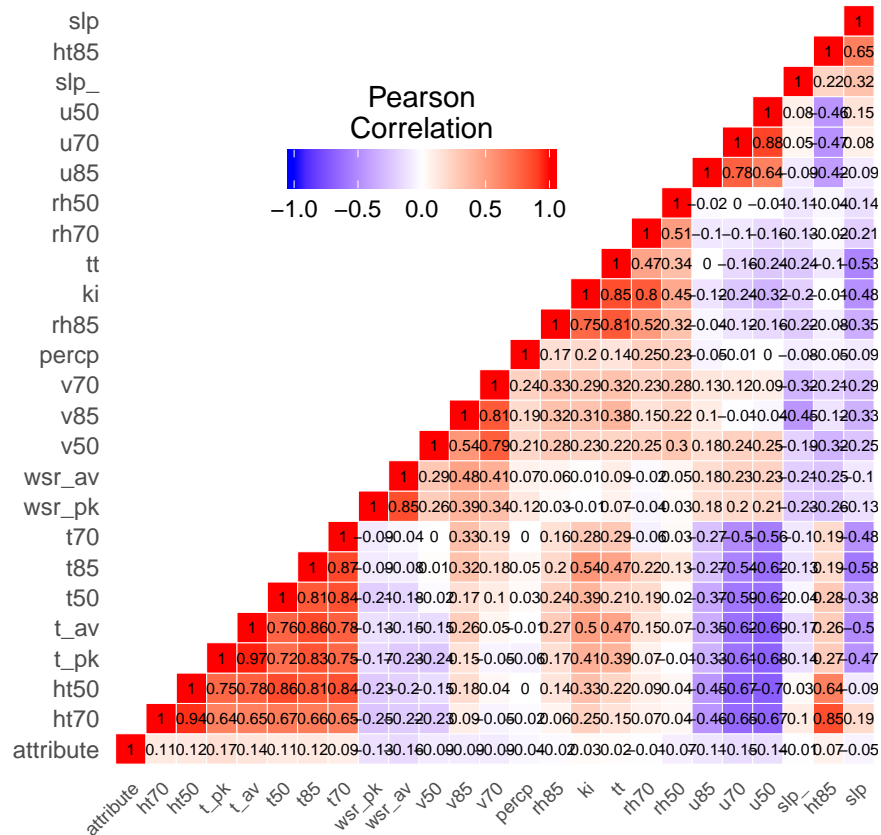
    return(cormat)
}

reorder_cormat <- function(cormat){
  # Use correlation between variables as distance
  dd <- as.dist((1-cormat)/2)
  hc <- hclust(dd)
  cormat <- cormat[hc$order, hc$order]
}

cormat <- reorder_cormat(cormat)
upper_tri <- get_upper_tri(cormat)
# Melt the correlation matrix
melted_cormat <- melt(upper_tri, na.rm = TRUE)
# Create a ggheatmap
ggheatmap <- ggplot(melted_cormat, aes(Var2, Var1, fill = value))+
  geom_tile(color = "white")+
  scale_fill_gradient2(low = "blue", high = "red", mid = "white",
    midpoint = 0, limit = c(-1,1), space = "Lab",
    name="Pearson\nCorrelation") +
  theme_minimal()+ # minimal theme
  theme(axis.text.x = element_text(angle = 45, vjust = 1,
    size = 7, hjust = 1))+
  coord_fixed()

ggheatmap +
  geom_text(aes(Var2, Var1, label = value), color = "black", size = 2) +
  theme(
    axis.title.x = element_blank(),
    axis.title.y = element_blank(),
    panel.grid.major = element_blank(),
    panel.border = element_blank(),
    panel.background = element_blank(),
    axis.ticks = element_blank(),
    legend.justification = c(1, 0),
    legend.position = c(0.6, 0.7),
    legend.direction = "horizontal")+
  guides(fill = guide_colorbar(barwidth = 7, barheight = 1,
    title.position = "top", title.hjust = 0.5))

```



Eigen values and variances explained

```
fitpca <- princomp(oneav, cor=TRUE)
summary(fitpca) # print variance accounted for
```

```
## Importance of components:
##               Comp.1   Comp.2   Comp.3   Comp.4   Comp.5
## Standard deviation  2.8475059 2.2186642 1.49690912 1.38280567 1.1165494
## Proportion of Variance 0.3243316 0.1968988 0.08962948 0.07648606 0.0498673
## Cumulative Proportion 0.3243316 0.5212304 0.61085990 0.68734596 0.7372133
##               Comp.6   Comp.7   Comp.8   Comp.9
## Standard deviation  1.04173087 0.98076082 0.93256131 0.89296877
## Proportion of Variance 0.04340813 0.03847567 0.03478682 0.03189573
## Cumulative Proportion 0.78062139 0.81909706 0.85388388 0.88577961
##               Comp.10  Comp.11  Comp.12  Comp.13
## Standard deviation  0.85342516 0.7249121 0.63323021 0.52187084
## Proportion of Variance 0.02913338 0.0210199 0.01603922 0.01089397
## Cumulative Proportion 0.91491299 0.9359329 0.95197211 0.96286608
##               Comp.14  Comp.15  Comp.16  Comp.17
## Standard deviation  0.49703295 0.471209589 0.347798097 0.320645664
## Proportion of Variance 0.00988167 0.008881539 0.004838541 0.004112546
## Cumulative Proportion 0.97274775 0.981629290 0.986467830 0.990580376
##               Comp.18  Comp.19  Comp.20  Comp.21
## Standard deviation  0.298215297 0.244025829 0.188064097 0.1311093615
```

```
## Proportion of Variance 0.003557295 0.002381944 0.001414724 0.0006875866
## Cumulative Proportion 0.994137671 0.996519615 0.997934339 0.9986219256
##                               Comp.22      Comp.23      Comp.24      Comp.25
## Standard deviation      0.1278202305 0.1061695382 0.0665481177 4.912459e-02
## Proportion of Variance 0.0006535205 0.0004508788 0.0001771461 9.652901e-05
## Cumulative Proportion 0.9992754461 0.9997263249 0.9999034710 1.000000e+00
```

```
loadings(fitpca) # pc loadings
```

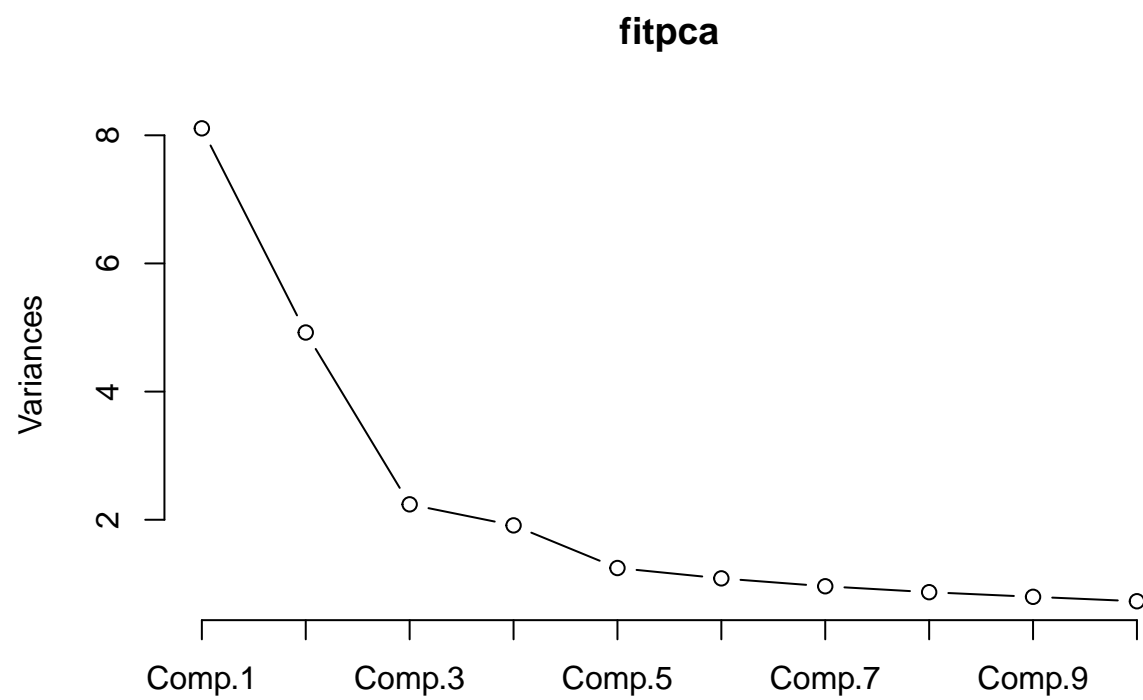
```
##
## Loadings:
##      Comp.1 Comp.2 Comp.3 Comp.4 Comp.5 Comp.6 Comp.7 Comp.8 Comp.9
## wsr_pk      -0.221 -0.329 0.177 -0.411 -0.198      -0.287
## wsr_av      -0.234 -0.335 0.220 -0.335 -0.246      -0.241 -0.124
## t_pk        -0.307      -0.208      0.115
## t_av        -0.321      -0.153
## t85         -0.317      -0.119 -0.123 0.114      -0.116
## rh85        -0.128 -0.261 0.298      -0.184 -0.155
## u85         0.177 -0.153      -0.214 0.350 -0.365 -0.151      0.329
## v85         -0.309 -0.265 0.213      -0.164 0.161
## ht85        -0.145 0.256      0.439      -0.215 -0.204      0.141
## t70         -0.290      -0.258      0.195
## rh70        -0.101 -0.208 0.428 0.112
## u70         0.265 -0.140      -0.117 0.316 -0.252      -0.150 0.143
## v70         -0.337 -0.171 0.248 0.250 0.195 -0.113 0.123 -0.142
## ht70        -0.279 0.167      0.273 0.133 -0.180 -0.100
## t50         -0.301      0.181      0.128
## rh50         -0.197 0.280 0.179      0.146
## u50         0.282 -0.114      0.266 -0.156      -0.139
## v50         -0.315      0.189 0.324 0.269      -0.318
## ht50        -0.317 0.105      0.137 0.173
## ki          -0.206 -0.252 0.331      -0.169
## tt          -0.174 -0.274 0.224      -0.116 -0.260 -0.149
## slp         0.137 0.262      0.467      -0.133 -0.189
## slp_         0.205 0.132      0.255 -0.193 0.310 -0.466 -0.532
## percp       -0.138 0.107 0.197      0.373 0.382 -0.396 0.599
## attribute   -0.141      0.367 -0.697 -0.575
##      Comp.10 Comp.11 Comp.12 Comp.13 Comp.14 Comp.15 Comp.16 Comp.17
## wsr_pk      0.319      0.180 0.568 -0.177
## wsr_av      -0.135 -0.147      -0.128 -0.623 0.237
## t_pk        0.300 0.192 0.209 0.388 -0.113 0.115
## t_av        0.102 0.236      0.205 0.348 -0.225 0.128
## t85        -0.115      0.131      -0.411
## rh85        0.411 0.134 -0.467      0.329
## u85         -0.106      0.146 -0.595 0.146      -0.128
## v85         0.113 0.263 -0.543      0.139      -0.477
## ht85        0.139
## t70         0.101 -0.321 -0.100      -0.227
## rh70        -0.246 -0.582 0.170 -0.154
## u70         0.253      0.108 0.415
## v70         0.179 -0.115      0.300 0.563
## ht70        -0.155
## t50         -0.347 -0.414      0.272
## rh50        -0.694 0.505 -0.213      0.114
## u50         -0.104      0.674      -0.280
```

```

## v50                                0.623                    -0.294 -0.200
## ht50                                -0.177
## ki                                -0.189  0.132                    -0.167
## tt                                0.252  0.321  0.106  0.103                    -0.353
## slp
## slp_                                0.220  0.208  0.259 -0.160 -0.142  0.161
## percp                                0.345
## attribute
##      Comp.18 Comp.19 Comp.20 Comp.21 Comp.22 Comp.23 Comp.24 Comp.25
## wsr_pk
## wsr_av
## t_pk                                0.115                    -0.424 -0.516 -0.117
## t_av                                0.412  0.518  0.316
## t85                                -0.130 -0.159  0.510                    -0.222  0.463 -0.107  0.176
## rh85                                0.126  0.356  0.175 -0.216
## u85                                -0.206  0.107
## v85                                0.271
## ht85                                -0.103  0.125                    0.105 -0.361 -0.418  0.470
## t70                                0.258  0.551 -0.330                    -0.326  0.119
## rh70                                0.410  0.173 -0.190  0.175
## u70                                0.578 -0.286  0.110
## v70                                -0.414
## ht70                                0.143  0.154                    -0.173                    -0.796
## t50                                -0.151 -0.473 -0.143 -0.304  0.190                    -0.207 -0.113
## rh50
## u50                                -0.437  0.204
## v50                                0.211
## ht50                                -0.158  0.812  0.289
## ki                                -0.260 -0.561  0.389 -0.344
## tt                                -0.104 -0.499  0.385
## slp                                -0.264 -0.225 -0.117  0.685
## slp_
## percp
## attribute
##
##      Comp.1 Comp.2 Comp.3 Comp.4 Comp.5 Comp.6 Comp.7 Comp.8
## SS loadings      1.00  1.00  1.00  1.00  1.00  1.00  1.00  1.00
## Proportion Var   0.04  0.04  0.04  0.04  0.04  0.04  0.04  0.04
## Cumulative Var   0.04  0.08  0.12  0.16  0.20  0.24  0.28  0.32
##
##      Comp.9 Comp.10 Comp.11 Comp.12 Comp.13 Comp.14 Comp.15
## SS loadings      1.00  1.00  1.00  1.00  1.00  1.00  1.00
## Proportion Var   0.04  0.04  0.04  0.04  0.04  0.04  0.04
## Cumulative Var   0.36  0.40  0.44  0.48  0.52  0.56  0.60
##
##      Comp.16 Comp.17 Comp.18 Comp.19 Comp.20 Comp.21 Comp.22
## SS loadings      1.00  1.00  1.00  1.00  1.00  1.00  1.00
## Proportion Var   0.04  0.04  0.04  0.04  0.04  0.04  0.04
## Cumulative Var   0.64  0.68  0.72  0.76  0.80  0.84  0.88
##
##      Comp.23 Comp.24 Comp.25
## SS loadings      1.00  1.00  1.00
## Proportion Var   0.04  0.04  0.04
## Cumulative Var   0.92  0.96  1.00

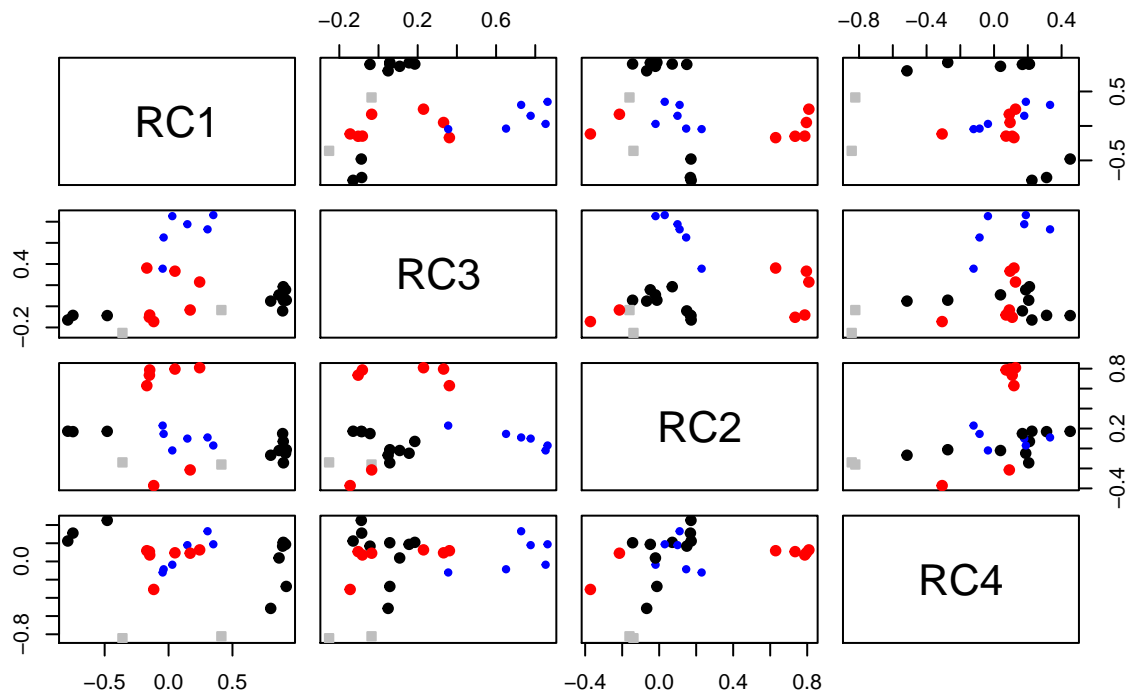
```

```
plot(fitpca,type="lines") # scree plot
```

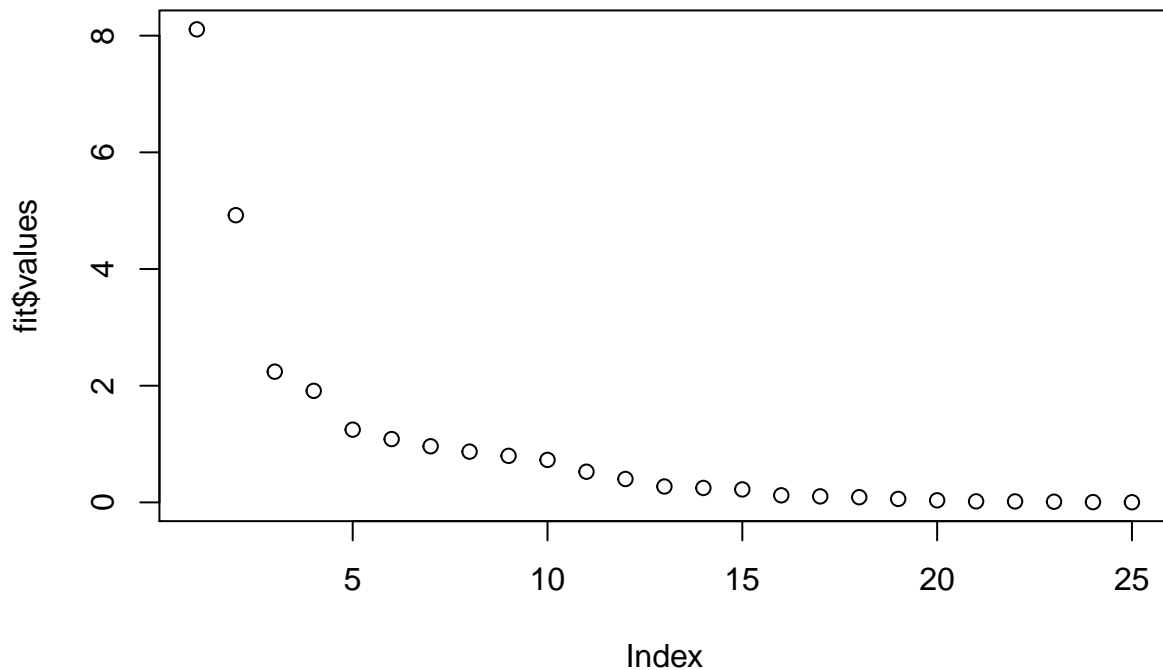


```
biplot(fitpca)
```


Principal Component Analysis



```
plot(fit$values)
```



```
fit$values
```

```
## [1] 8.108289780 4.922470805 2.240736904 1.912151516 1.246682488
## [6] 1.085203212 0.961891781 0.869670594 0.797393229 0.728334505
## [11] 0.525497529 0.400980496 0.272349172 0.247041758 0.222038477
## [16] 0.120963516 0.102813642 0.088932363 0.059548605 0.035368105
## [21] 0.017189665 0.016338011 0.011271971 0.004428652 0.002413225
```

```
#total variances
```

```
sum(fit$values[1:4])/sum(fit$values)
```

```
## [1] 0.687346
```

```
names(fit)
```

```
## [1] "values"      "rotation"    "n.obs"      "communality"
## [5] "loadings"    "fit"         "fit.off"    "fn"
## [9] "Call"        "uniquenesses" "complexity" "chi"
## [13] "EPVAL"       "R2"          "objective"  "residual"
## [17] "rms"         "factors"     "dof"        "null.dof"
## [21] "null.model"  "criteria"    "STATISTIC"  "PVAL"
## [25] "weights"     "r.scores"    "rot.mat"    "Vaccounted"
## [29] "Structure"   "scores"
```

```
name<-colnames(oneav)
```

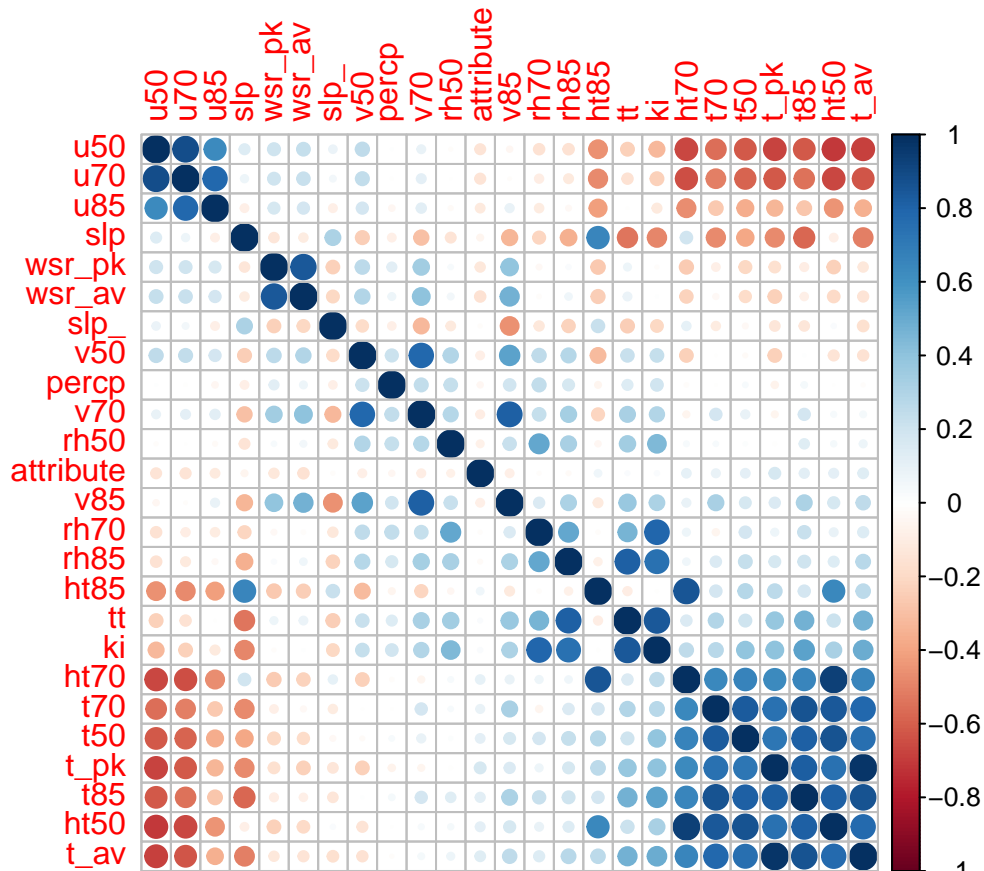
```
fitloading<-data.frame(fit$loadings[,1:4],name)
```

```
fitloading
```

```
##           RC1           RC3           RC2           RC4           name
```

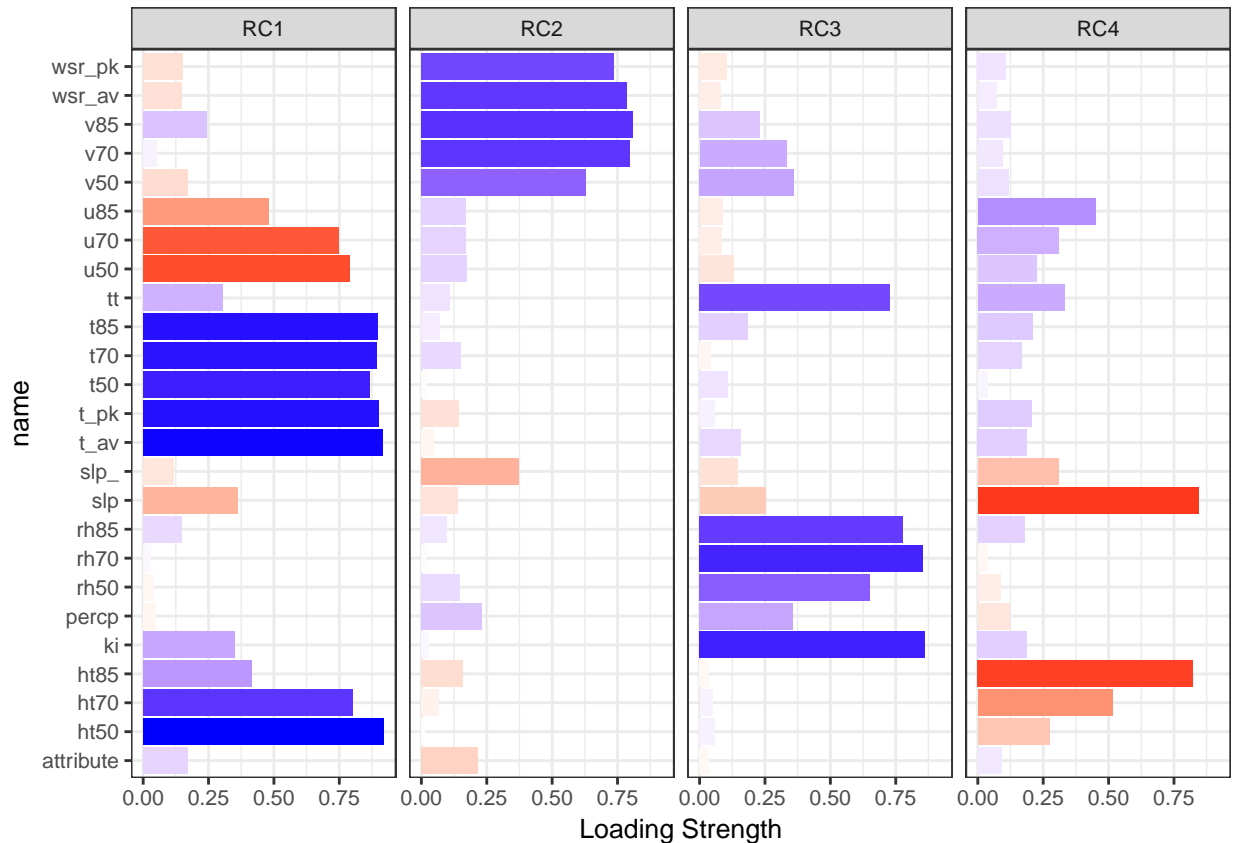
## wsr_pk	-0.14967717	-0.10387121	0.73465415	0.10758513	wsr_pk
## wsr_av	-0.14760352	-0.08235590	0.78690179	0.07099203	wsr_av
## t_pk	0.89873480	0.05749781	-0.14365053	0.20524199	t_pk
## t_av	0.91521395	0.15605111	-0.04778759	0.18760338	t_av
## t85	0.89748700	0.18522342	0.07068584	0.20957385	t85
## rh85	0.14727550	0.77654070	0.09927568	0.17897850	rh85
## u85	-0.47986472	-0.08777645	0.17183571	0.45106496	u85
## v85	0.24324192	0.22963282	0.80918884	0.12694184	v85
## ht85	0.41322167	-0.03563537	-0.16055255	-0.82226494	ht85
## t70	0.89263258	-0.04339647	0.14924922	0.16792791	t70
## rh70	0.02939269	0.85284641	-0.01944640	-0.03621383	rh70
## u70	-0.74825724	-0.08581162	0.16885749	0.31108401	u70
## v70	0.05014715	0.33210046	0.79574737	0.09486665	v70
## ht70	0.79926328	0.04918376	-0.06750865	-0.51573659	ht70
## t50	0.86470728	0.10811177	-0.02018109	0.03811741	t50
## rh50	-0.03840935	0.65087708	0.14602291	-0.08573260	rh50
## u50	-0.78853347	-0.12959144	0.17293447	0.22432528	u50
## v50	-0.17002674	0.36179751	0.62947079	0.11784381	v50
## ht50	0.92095887	0.05778277	-0.01225582	-0.27445050	ht50
## ki	0.35030815	0.86283258	0.03014040	0.18845557	ki
## tt	0.30519697	0.72792960	0.11065528	0.33171606	tt
## slp	-0.36097027	-0.25217505	-0.13912173	-0.84337065	slp
## slp_	-0.11624278	-0.14467341	-0.37167785	-0.30768551	slp_
## percp	-0.04604161	0.35575916	0.22953499	-0.12130184	percp
## attribute	0.16924212	-0.03497646	-0.21479997	0.09037418	attribute

```
library(corrplot)
C<-cor(oneav)
corrplot(C, method = "circle", order = "FPC")
```



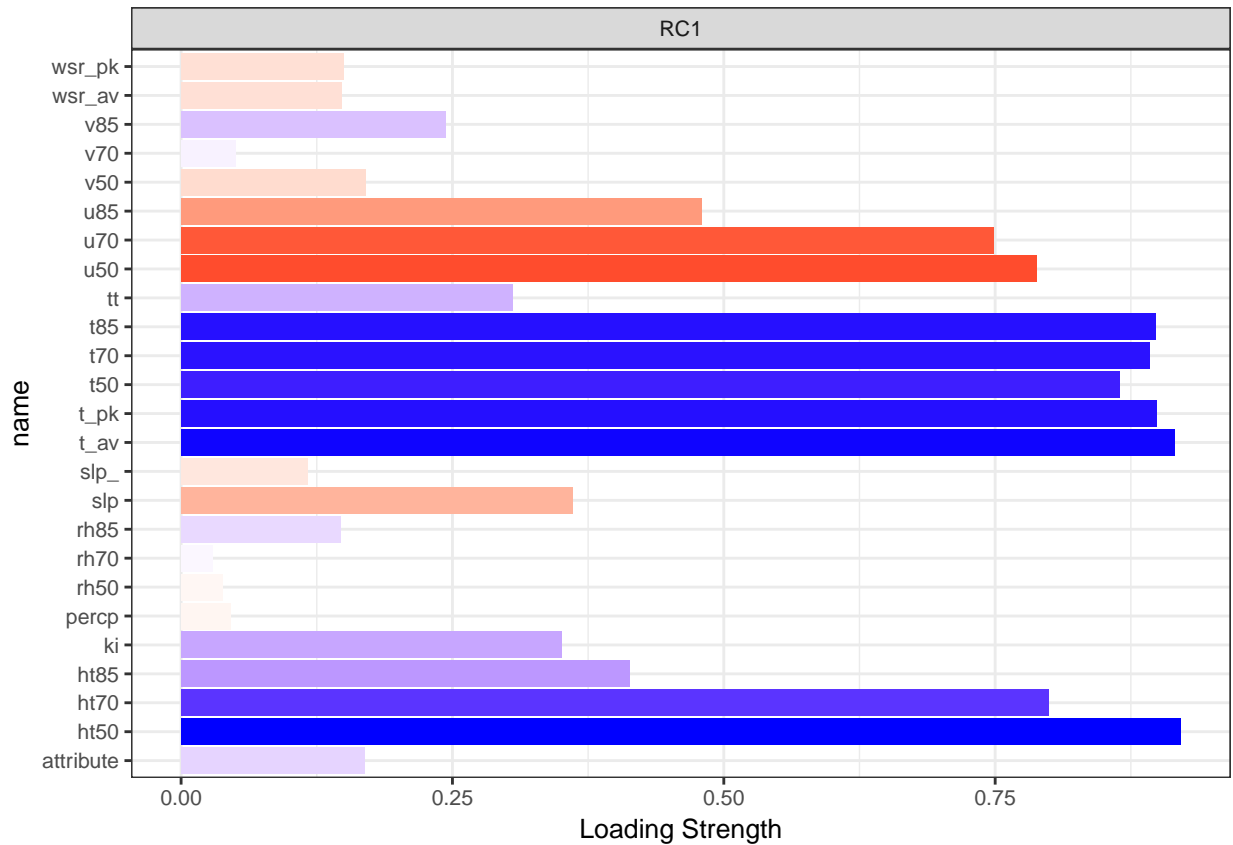
#Visualization of the LOADINGS

```
#visualization of all loadings
loadings.m <- melt(fitloading, id="name",
  measure=c("RC1", "RC2", "RC3", "RC4"),
  variable.name="Factor", value.name="Loading")
ggplot(loadings.m, aes(name, abs>Loading), fill=Loading)) +
  facet_wrap(~ Factor, nrow=1) + #place the factors in separate facets
  geom_bar(stat="identity") + #make the bars
  coord_flip() + #flip the axes so the test names can be horizontal
  #define the fill color gradient: blue=positive, red=negative
  scale_fill_gradient2(name = "Loading",
    high = "blue", mid = "white", low = "red",
    midpoint=0, guide=F) +
  ylab("Loading Strength") + #improve y-axis label
  theme_bw(base_size=10) #use a black-and-white theme with set font size
```



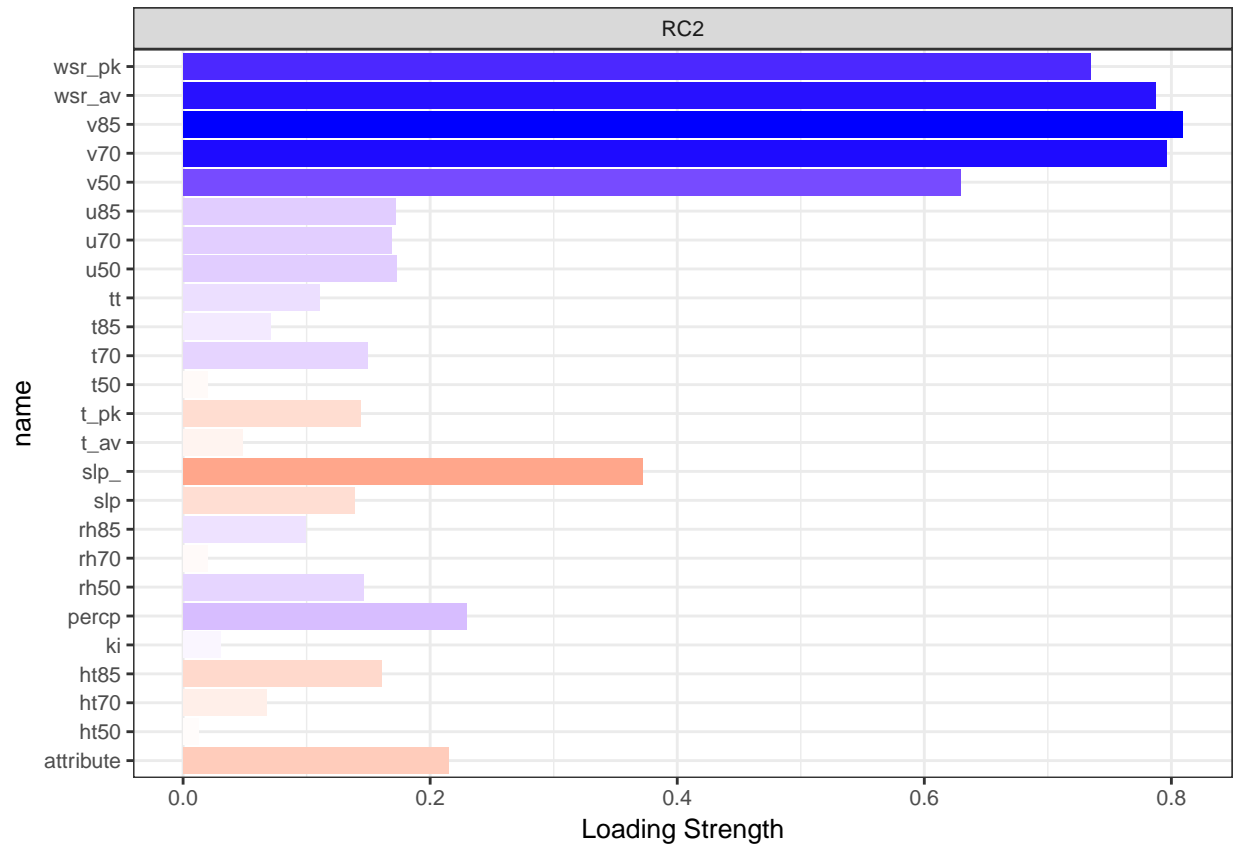
#####VISUALIZATION OF THE LOADINGS#####
#Visualization of loading 1

```
loadings.1 <- melt(fitloading, id="name",
                  measure=c("RC1"),
                  variable.name="Factor", value.name="Loading")
ggplot(loadings.1, aes(name, abs>Loading), fill=Loading)) +
  facet_wrap(~ Factor, nrow=1) + #place the factors in separate facets
  geom_bar(stat="identity") + #make the bars
  coord_flip() + #flip the axes so the test names can be horizontal
  #define the fill color gradient: blue=positive, red=negative
  scale_fill_gradient2(name = "Loading",
                      high = "blue", mid = "white", low = "red",
                      midpoint=0, guide=F) +
  ylab("Loading Strength") + #improve y-axis label
  theme_bw(base_size=10) #use a black-and-white theme with set font size
```

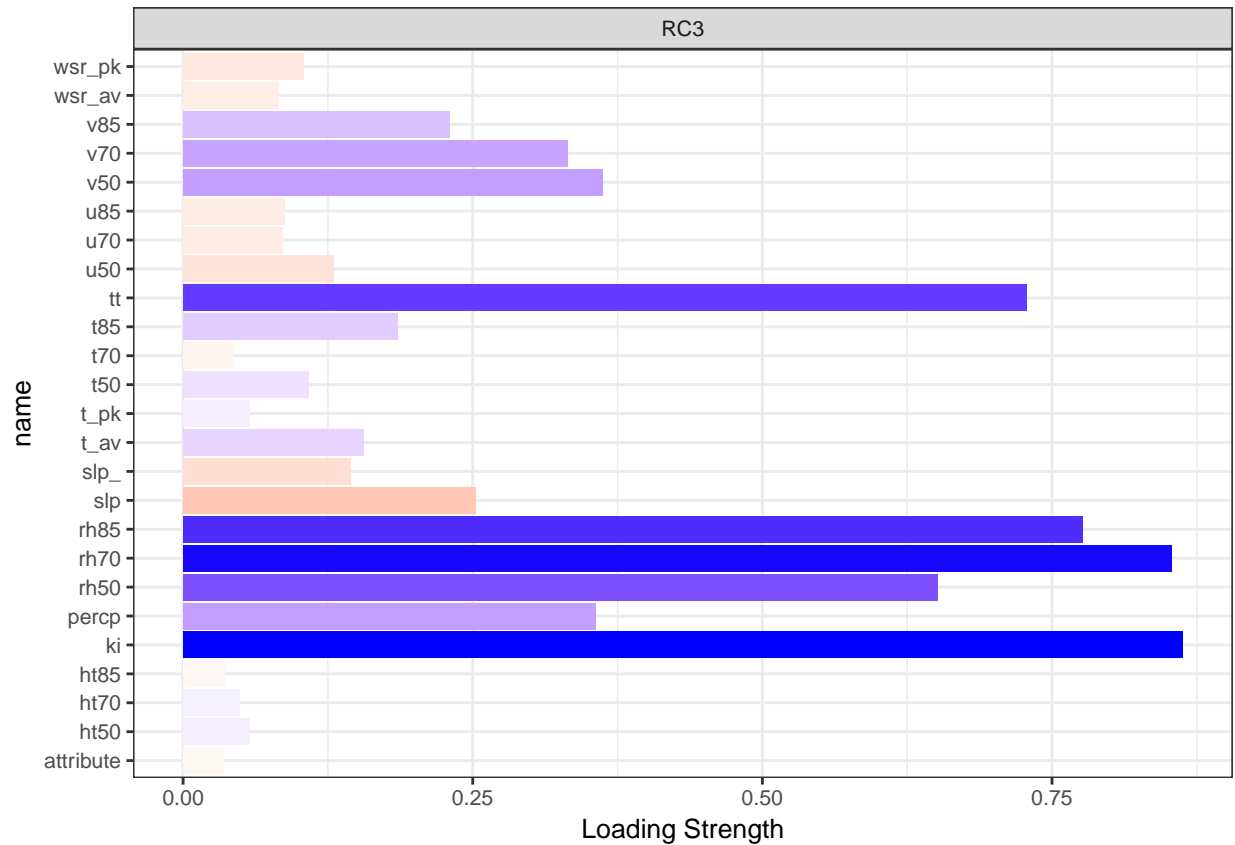


#Visualization of loading 2

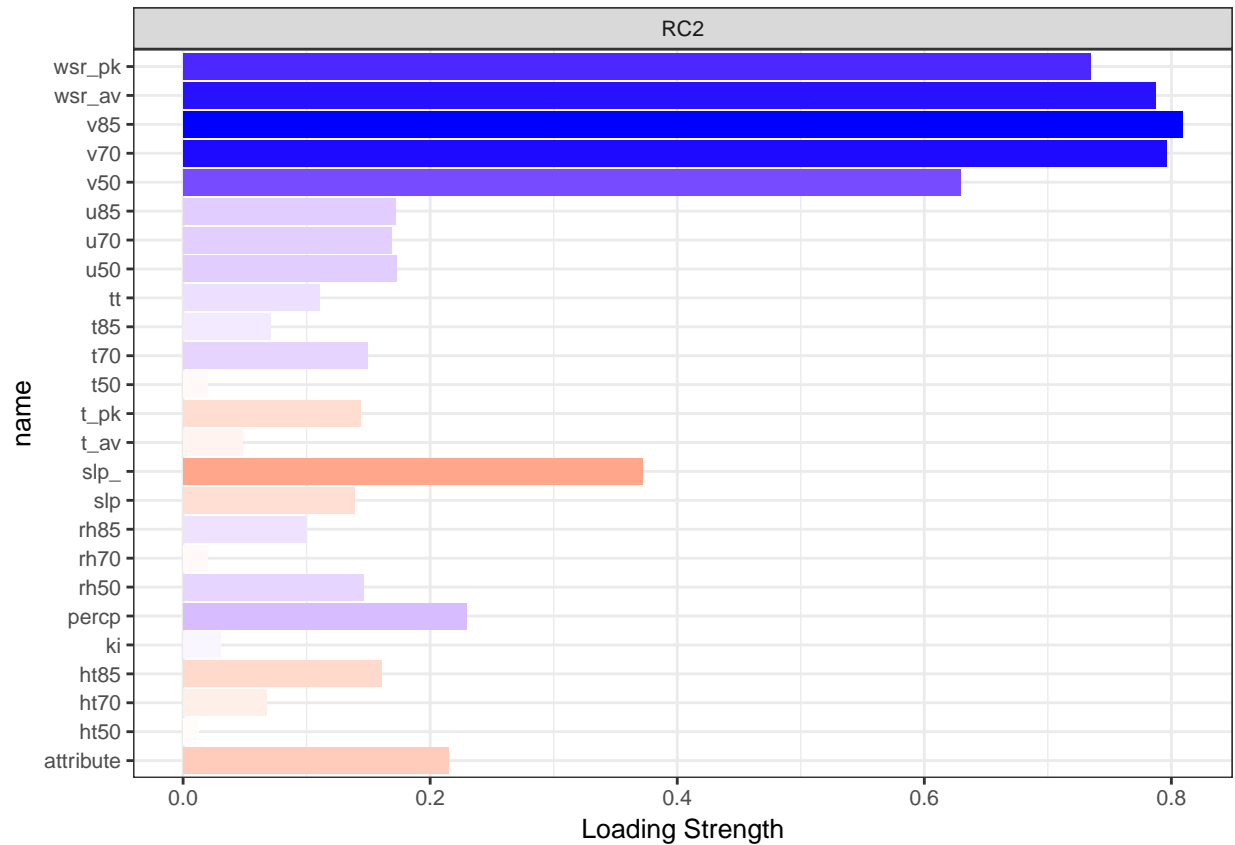
```
loadings.2 <- melt(fitloading, id="name",
                  measure=c("RC2"),
                  variable.name="Factor", value.name="Loading")
ggplot(loadings.2, aes(name, abs>Loading), fill=Loading)) +
  facet_wrap(~ Factor, nrow=1) + #place the factors in separate facets
  geom_bar(stat="identity") + #make the bars
  coord_flip() + #flip the axes so the test names can be horizontal
  #define the fill color gradient: blue=positive, red=negative
  scale_fill_gradient2(name = "Loading",
                      high = "blue", mid = "white", low = "red",
                      midpoint=0, guide=F) +
  ylab("Loading Strength") + #improve y-axis label
  theme_bw(base_size=10) #use a black-and-white theme with set font size
```



```
#Visualization of Loading 3
loadings.3 <- melt(fitloading, id="name",
                  measure=c("RC3"),
                  variable.name="Factor", value.name="Loading")
ggplot(loadings.3, aes(name, abs>Loading), fill=Loading)) +
  facet_wrap(~ Factor, nrow=1) + #place the factors in separate facets
  geom_bar(stat="identity") + #make the bars
  coord_flip() + #flip the axes so the test names can be horizontal
  #define the fill color gradient: blue=positive, red=negative
  scale_fill_gradient2(name = "Loading",
                      high = "blue", mid = "white", low = "red",
                      midpoint=0, guide=F) +
  ylab("Loading Strength") + #improve y-axis label
  theme_bw(base_size=10) #use a black-and-white theme with set font size
```

```
#Visualization of Loading 4
loadings.4 <- melt(fitloading, id="name",
                  measure=c("RC4"),
                  variable.name="Factor", value.name="Loading")
ggplot(loadings.2, aes(name, abs>Loading), fill=Loading)) +
  facet_wrap(~ Factor, nrow=1) + #place the factors in separate facets
  geom_bar(stat="identity") + #make the bars
  coord_flip() + #flip the axes so the test names can be horizontal
  #define the fill color gradient: blue=positive, red=negative
  scale_fill_gradient2(name = "Loading",
                      high = "blue", mid = "white", low = "red",
                      midpoint=0, guide=F) +
  ylab("Loading Strength") + #improve y-axis label
  theme_bw(base_size=10) #use a black-and-white theme with set font size
```



```
names(fit)
```

```
## [1] "values"      "rotation"    "n.obs"      "communality"
## [5] "loadings"    "fit"         "fit.off"    "fn"
## [9] "Call"        "uniquenesses" "complexity" "chi"
## [13] "EPVAL"       "R2"          "objective"  "residual"
## [17] "rms"         "factors"     "dof"        "null.dof"
## [21] "null.model"  "criteria"    "STATISTIC"  "PVAL"
## [25] "weights"    "r.scores"    "rot.mat"    "Vaccounted"
## [29] "Structure"   "scores"
```

```
fit$loadings
```

```
##
## Loadings:
##      RC1    RC3    RC2    RC4
## wsr_pk -0.150 -0.104  0.735  0.108
## wsr_av -0.148         0.787
## t_pk   0.899         -0.144  0.205
## t_av   0.915  0.156         0.188
## t85    0.897  0.185         0.210
## rh85   0.147  0.777         0.179
## u85    -0.480         0.172  0.451
## v85    0.243  0.230  0.809  0.127
## ht85   0.413         -0.161 -0.822
## t70    0.893         0.149  0.168
## rh70           0.853
```

```
## u70      -0.748      0.169  0.311
## v70      0.332  0.796
## ht70     0.799      -0.516
## t50      0.865  0.108
## rh50      0.651  0.146
## u50     -0.789 -0.130  0.173  0.224
## v50     -0.170  0.362  0.629  0.118
## ht50     0.921      -0.274
## ki       0.350  0.863      0.188
## tt       0.305  0.728  0.111  0.332
## slp      -0.361 -0.252 -0.139 -0.843
## slp_     -0.116 -0.145 -0.372 -0.308
## percp      0.356  0.230 -0.121
## attribute 0.169      -0.215
##
##              RC1   RC3   RC2   RC4
## SS loadings  7.614 3.667 3.313 2.590
## Proportion Var 0.305 0.147 0.133 0.104
## Cumulative Var 0.305 0.451 0.584 0.687
```

#code taken from http://www.chrisbilder.com/multivariate/Section2/goblet_CA.r

```
PCA.CA.plot<-function(data.set, cluster.results, numb.clust, plot.title, cor.use = TRUE, inches = 0.5) {
```

```
  clusters<-cutree(tree = cluster.results, k = numb.clust)
```

#PC scores

```
pca.cor<-princomp(x = data.set, cor = cor.use, scores = FALSE)
```

```
pca.cor$scale<-apply(X = data.set, MARGIN = 2, FUN = sd)
```

```
score.cor<-predict(pca.cor, newdata = data.set)
```

#Scatter plot of first two PCs

```
par(pty = "s")
```

```
common.limits<-c(min(score.cor[,1:2]), max(score.cor[,1:2]))
```

```
plot(x = score.cor[,1], y = score.cor[,2], xlab = "PC #1", ylab = "PC #2",
     main = paste("PCs with", plot.title, "and", numb.clust, "clusters"),
     xlim = common.limits, ylim = common.limits, panel.first = grid(col = "lightgray", lty = "dotted"),
     col = clusters, pch = clusters)
```

```
abline(h = 0)
```

```
abline(v = 0)
```

```
text(x = score.cor[,1], y = score.cor[,2]+0.2)
```

#Bubble plot of first three PCs

```
par(pty = "s")
```

```
PC3.positive<-score.cor[,3] - min(score.cor[,3]) #Bubble needs to contain all values > 0
```

```
col.symbol<-ifelse(test = score.cor[,3]>0, yes = "red", no = "blue")
```

```
symbols(x = score.cor[,1], y = score.cor[,2], circles = PC3.positive,
       xlab = "PC #1", ylab = "PC #2", main = paste("PCs with", plot.title, "and", numb.clust, "clusters"),
       xlim = common.limits, ylim = common.limits, panel.first = grid(col = "lightgray", lty = "dotted"),
       fg = col.symbol)
```

```
text(x = score.cor[,1], y = score.cor[,2], col = clusters)
```

```
abline(h = 0)
```

```
abline(v = 0)
```

```

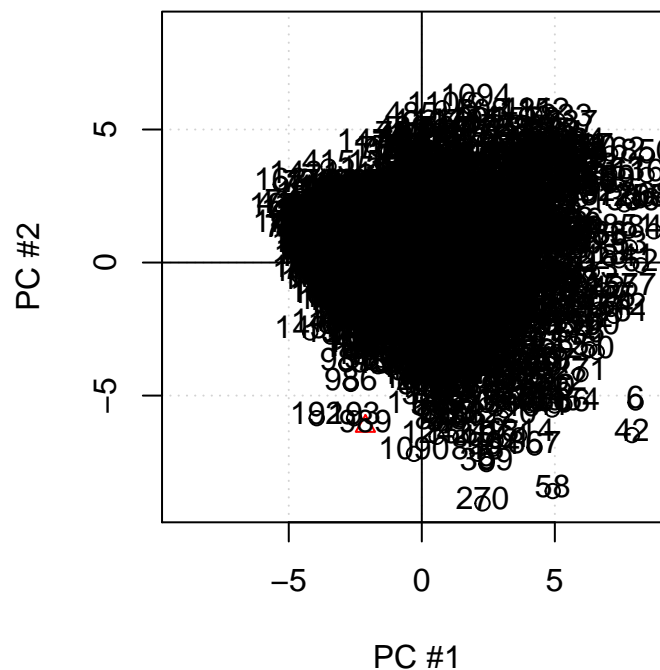
#3D plot - Note: I used common limits for all three dimensions here because the distance between poin
plot3d(x = score.cor[,1], y = score.cor[,2], z = score.cor[,3], xlab = "PC #1", ylab = "PC #2",
       zlab = "PC #3", type = "h", xlim = common.limits, ylim = common.limits, zlim = common.limits)
plot3d(x = score.cor[,1], y = score.cor[,2], z = score.cor[,3], add = TRUE, col = clusters, size = 6)
persp3d(x = common.limits, y = common.limits, z = matrix(data = c(0,0,0,0), nrow = 2, ncol = 2),
        add = TRUE, col = "green") #Put a plane on the plot
grid3d(side = c("x", "y", "z"), col = "lightgray")

invisible()
}

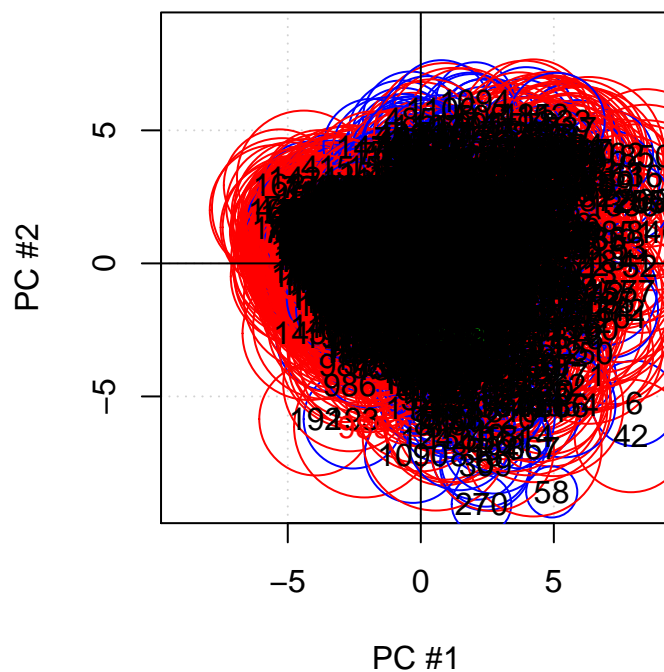
Z<-scale(oneav)
dist.mat<-dist(x = Z, method = "euclidean")
clust.nn<-hclust(d = dist.mat, method = "single")
PCA.CA.plot(data.set = oneav, cluster.results = clust.nn, numb.clust = 3,
            plot.title = "nearest neighbor CA method")

```

PCs with nearest neighbor CA method and 3 clusters

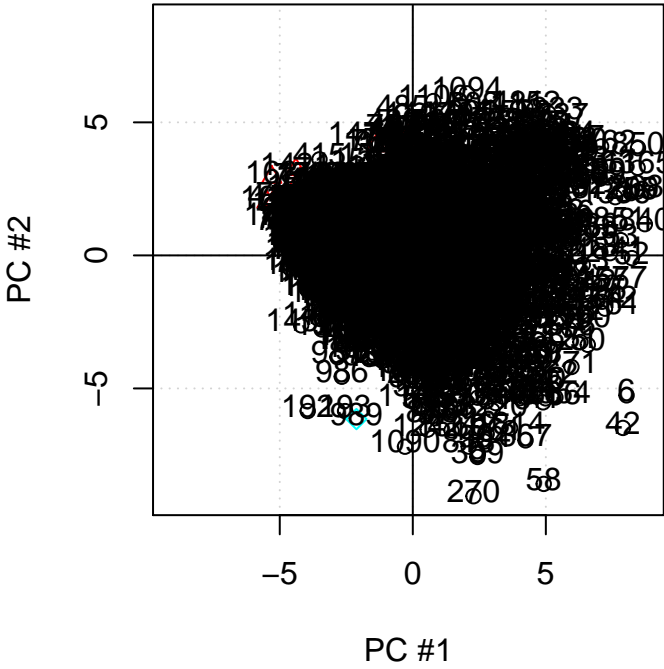


PCs with nearest neighbor CA method and 3 clusters

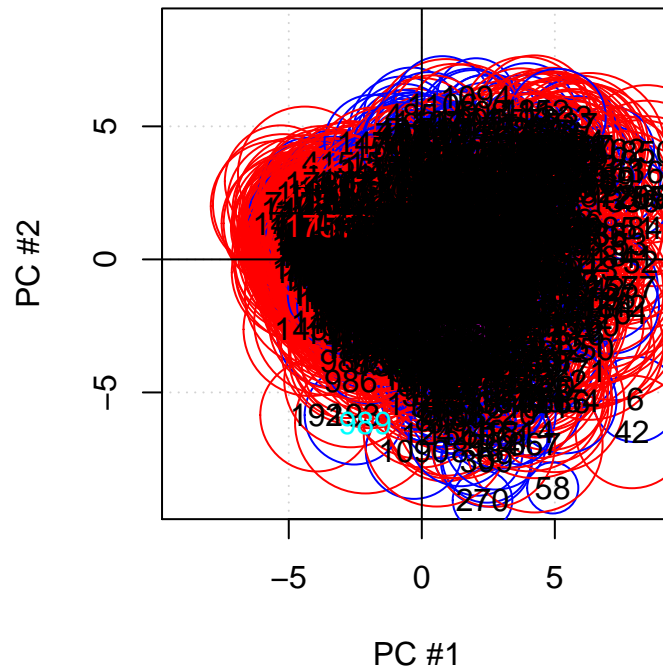


```
PCA.CA.plot(data.set = oneav, cluster.results = clust.nn, numb.clust = 6,  
            plot.title = "nearest neighbor CA method")
```

PCs with nearest neighbor CA method and 6 clusters



PCs with nearest neighbor CA method and 6 clusters



```
##### Principal Component K-Means Clustering#####
PCA.CA.plot2<-function(data.set, cluster.results, plot.title, cor.use = TRUE, inches = 0.5) {

  numb.clust<-length(cluster.results$size)

  #PC scores
  pca.cor<-princomp(x = data.set, cor = cor.use, scores = FALSE)
  pca.cor$scale<-apply(X = data.set, MARGIN = 2, FUN = sd)
  score.cor<-predict(pca.cor, newdata = data.set)

  #Scatter plot of first two PCs

  common.limits<-c(min(score.cor[,1:2]), max(score.cor[,1:2]))
  plot(x = score.cor[,1], y = score.cor[,2], xlab = "PC #1", ylab = "PC #2",
       main = paste("PCs with", plot.title, "and", numb.clust, "clusters"),
       xlim = common.limits, ylim = common.limits, panel.first = grid(col = "lightgray", lty = "dotted"),
       col = cluster.results$cluster, pch = cluster.results$cluster)
  abline(h = 0)
  abline(v = 0)
  text(x = score.cor[,1], y = score.cor[,2]+0.2)

  #Bubble plot of first three PCs

  PC3.positive<-score.cor[,3] - min(score.cor[,3]) #Bubble needs to contain all values > 0
```

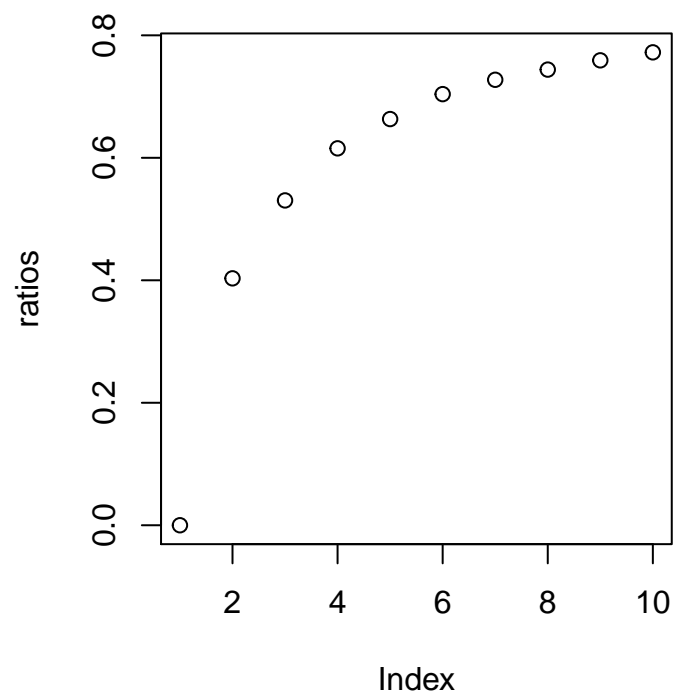
```

col.symbol<-ifelse(test = score.cor[,3]>0, yes = "red", no = "blue")
symbols(x = score.cor[,1], y = score.cor[,2], circles = PC3.positive,
        xlab = "PC #1", ylab = "PC #2", main = paste("PCs with", plot.title, "and", numb.clust, "clusters",
        xlim = common.limits, ylim = common.limits, panel.first = grid(col = "lightgray", lty = "dotted"),
        fg = col.symbol)
text(x = score.cor[,1], y = score.cor[,2], col = cluster.results$cluster)
abline(h = 0)
abline(v = 0)

#3D plot - Note: I used common limits for all three dimensions here because the distance between points is
plot3d(x = score.cor[,1], y = score.cor[,2], z = score.cor[,3], xlab = "PC #1", ylab = "PC #2",
       zlab = "PC #3", type = "h", xlim = common.limits, ylim = common.limits, zlim = common.limits)
plot3d(x = score.cor[,1], y = score.cor[,2], z = score.cor[,3], add = TRUE, col = cluster.results$cluster)
persp3d(x = common.limits, y = common.limits, z = matrix(data = c(0,0,0,0), nrow = 2, ncol = 2),
        add = TRUE, col = "green") #Put a plane on the plot
grid3d(side = c("x", "y", "z"), col = "lightgray")

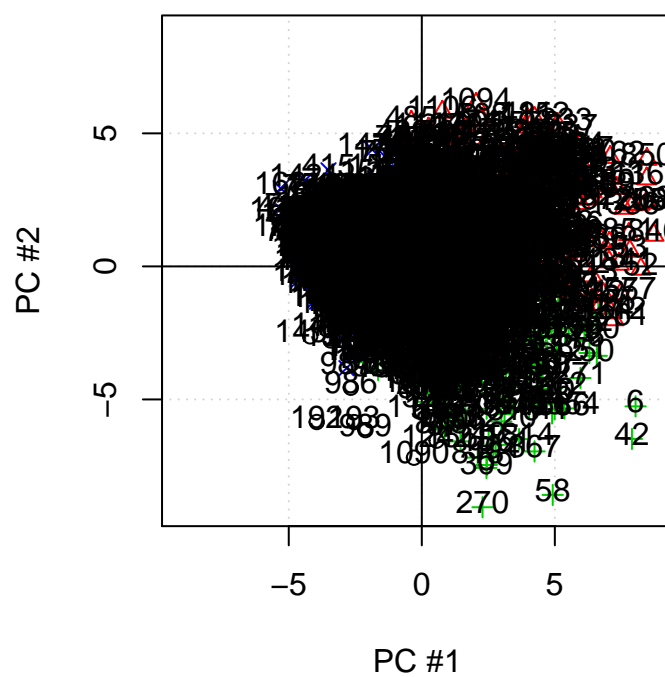
invisible()
}
# determine the number of clustering
oneav.c <- kmeans(oneav, 3, nstart=10)
ratios <- vector()
for (k in 1:10) {
  oneav.c <- kmeans(oneav, k, nstart=10)
  ratios[k] <- oneav.c$betweenss / oneav.c$totss
}
plot(ratios)

```

```
oneav.c<-kmeans(x = Z, centers = 4)
PCA.CA.plot2(data.set = oneav, cluster.results = oneav.c,
              plot.title = "K-means clustering")
```

PCs with K-means clustering and 4 clusters



PCs with K-means clustering and 4 clusters

