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Hafsa Bajwa

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1 Question 1.2

3. Food is the range of :favouriteFood

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\begin{split} \Gamma &\models : \text{favouriteFood rdfs:subPropertyOf : eats} \\ \Gamma &\models : \text{eats rdfs:range : Food} \\ &\models \text{Food(eats, favouriteFood)} \\ \text{iff} \\ eats^I, favouriteFood^I &\in Food^I \end{split}
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Thus, We have favouriteFood in range of Food.

4. Bruce has some :favouriteFood.

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\begin{array}{l} \Gamma \models : & \text{Bruce rdf:type :} Fish \\ \Gamma \models : & \text{Fish rdfs:subClassOf :} Animal \\ \Gamma \models : & \text{favouriteFood rdfs:subPropertyOf :} eats \\ \Gamma \models : & \text{eats rdfs:domain :} Animal \\ \models & \text{Animal}(eats^I, favouriteFood^I) \\ & \text{iff} \\ & (eats^I, favouriteFood^I) \in \text{Animal} \\ & favouriteFood^I \in \text{Animal} \models \text{Animal}(fish^I, Bruce^I) \\ & \text{And} \\ & (fish^I, Bruce^I) \in \text{Animal} \\ & \text{Bruce} \in \text{Animal} \\ & \vdash \text{Animal}(favouriteFood^I, Bruce^I) \\ & \text{:} & \text{favouriteFood} \subseteq : \text{Animal} \\ & \text{and} \\ & \text{:} & \text{Bruce} \subseteq : \text{Animal} \\ & \text{:} & \text{:} & \text{Bruce} \subseteq : \text{Animal} \\ & \text{:} & \text{Bruce} \subseteq : \text{Animal} \\ & \text{:} & \text{:} & \text{Bruce} \subseteq : \text{Animal} \\ & \text{:} & \text{:} & \text{:} & \text{:} & \text{:} \\ & \text{:} & \text{:} & \text{:} & \text{:} \\ & \text{:} & \text{:} & \text{:} & \text{:} \\ & \text{:} & \text{:} & \text{:} \\ & \text{:} & \text{:} & \text{:} & \text{:} \\ & \text{:} & \text{:} & \text{:} \\ & \text{:} & \text{:} & \text{:} \\ & \text{:} & \text{:} & \text{:} & \text{:} \\ & \text{:} & \text{:} \\ & \text{:} & \text{:} & \text{:} \\ & \text{:} & \text{:} \\ & \text{:} & \text{:} \\ & \text{:} & \text{:}
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Thus, $:Bruce \subseteq :Fish \subseteq :Animal \subseteq :eats \subseteq :favouriteFood$

5. :Bruce is a vegetable,

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\begin{split} \Gamma &\models : \text{Bruce} \subseteq : \text{Fish} \\ \Gamma &\models : \text{Fish} \subseteq : \text{Animal, :} \text{Food} \\ \Gamma &\models : \text{Vegetable} \subseteq : \text{Food} \\ \text{Thus,} &\models : \text{Bruce} \subseteq : \text{Fish} \subseteq : \text{Food} \\ \text{and} &\models : \text{Vegetable} \subseteq : \text{Food} \\ \text{iff} &: Bruce^I \subseteq : Fish^I \subseteq : Food^I \\ \text{Also} &: Vegetables^I \subseteq : Food^I \\ \end{split}
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Since, Both belongs to Food, We can say both interconnect each other. Hence, it is proved.

6. Bruce ia a horse.

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\begin{array}{l} \Gamma \models : & \text{Bruce} \subseteq : & \text{Fish} \\ \Gamma \models : & \text{Fish} \subseteq : & \text{Animal}, : & \text{Food} \\ \Gamma \models : & \text{Horse} \subseteq : & \text{Animal} \\ & \text{Thus}, \models : & \text{Bruce} \subseteq : & \text{Fish} \subseteq : & \text{Animal} \\ & \text{and} : & \text{Horse} \subseteq : & \text{Animal} & \text{iff} \\ : & & Bruce^I \subseteq : & Fish^I \subseteq & Animal^I \\ & \text{Also}, \\ : & & Horse^I \subseteq & Animal^I \\ & \text{Hence}, & \text{statement is proved}. \end{array}
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7. Bruce is a Fish.

 $\begin{array}{l} \Gamma \models : \text{Bruce} \subseteq : \text{Fish} \\ \text{iff} : Bruce^I \subseteq : Fish^I \\ \text{Hence, it it proved that Bruce is a Fish.} \end{array}$