or simply  $-2.2634 < \mu_D < 0.5234$ , from which we can conclude that there is no significant difference between the mean TCDD level in plasma and the mean TCDD level in fat tissue.

## Exercises 9.3

- **9.35** A random sample of size  $n_1 = 25$ , taken from a normal population with a standard deviation  $\sigma_1 = 5$ , has a mean  $\bar{x}_1 = 80$ . A second random sample of size  $n_2 = 36$ , taken from a different normal population with a standard deviation  $\sigma_2 = 3$ , has a mean  $\bar{x}_2 = 75$ . Find a 94% confidence interval for  $\mu_1 \mu_2$ .
- **9.36** Two kinds of thread are being compared for strength. Fifty pieces of each type of thread are tested under similar conditions. Brand A has an average tensile strength of 78.3 kilograms with a standard deviation of 5.6 kilograms, while brand B has an average tensile strength of 87.2 kilograms with a standard deviation of 6.3 kilograms. Construct a 95% confidence interval for the difference of the population means.
- 9.37 A study was conducted to determine if a certain treatment has any effect on the amount of metal removed in a pickling operation. A random sample of 100 pieces was immersed in a bath for 24 hours without the treatment, yielding an average of 12.2 millimeters of metal removed and a sample standard deviation of 1.1 millimeters. A second sample of 200 pieces was exposed to the treatment, followed by the 24-hour immersion in the bath, resulting in an average removal of 9.1 millimeters of metal with a sample standard deviation of 0.9 millimeter. Compute a 98% confidence interval estimate for the difference between the population means. Does the treatment appear to reduce the mean amount of metal removed?
- 9.38 Two catalysts in a batch chemical process, are being compared for their effect on the output of the process reaction. A sample of 12 batches was prepared using catalyst 1, and a sample of 10 batches was prepared using catalyst 2. The 12 batches for which catalyst 1 was used in the reaction gave an average yield of 85 with a sample standard deviation of 4, and the 10 batches for which catalyst 2 was used gave an average yield of 81 and a sample standard deviation of 5. Find a 90% confidence interval for the difference between the population means, assuming that the populations are approximately normally distributed with equal variances.
- **9.39** Students may choose between a 3-semester-hour physics course without labs and a 4-semester-hour course with labs. The final written examination is the same for each section. If 12 students in the section with

labs made an average grade of 84 with a standard deviation of 4, and 18 students in the section without labs made an average grade of 77 with a standard deviation of 6, find a 99% confidence interval for the difference between the average grades for the two courses. Assume the populations to be approximately normally distributed with equal variances.

9.40 In a study conducted at Virginia Tech on the development of ectomycorrhizal, a symbiotic relationship between the roots of trees and a fungus, in which minerals are transferred from the fungus to the trees and sugars from the trees to the fungus, 20 northern red oak seedlings exposed to the fungus *Pisolithus tinctorus* were grown in a greenhouse. All seedlings were planted in the same type of soil and received the same amount of sunshine and water. Half received no nitrogen at planting time, to serve as a control, and the other half received 368 ppm of nitrogen in the form NaNO<sub>3</sub>. The stem weights, in grams, at the end of 140 days were recorded as follows:

No Nitrogen	Nitrogen
0.32	0.26
0.53	0.43
0.28	0.47
0.37	0.49
0.47	0.52
0.43	0.75
0.36	0.79
0.42	0.86
0.38	0.62
0.43	0.46

Construct a 95% confidence interval for the difference in the mean stem weight between seedlings that receive no nitrogen and those that receive 368 ppm of nitrogen. Assume the populations to be normally distributed with equal variances.

**9.41** The following data represent the length of time, in days, to recovery for patients randomly treated with one of two medications to clear up severe bladder infections:

Medication 1	Medication 2
$n_1 = 14$	$n_2 = 16$
$\bar{x}_1 = 17$	$\bar{x}_2 = 19$
$s_1^2 = 1.5$	$s_2^2 = 1.8$

Find a 99% confidence interval for the difference  $\mu_2 - \mu_1$ 

in the mean recovery times for the two medications, assuming normal populations with equal variances.

- 9.42 An experiment reported in *Popular Science* compared fuel economies for two types of similarly equipped diesel mini-trucks. Let us suppose that 12 Volkswagen and 10 Toyota trucks were tested in 90-kilometer-per-hour steady-paced trials. If the 12 Volkswagen trucks averaged 16 kilometers per liter with a standard deviation of 1.0 kilometer per liter and the 10 Toyota trucks averaged 11 kilometers per liter with a standard deviation of 0.8 kilometer per liter, construct a 90% confidence interval for the difference between the average kilometers per liter for these two mini-trucks. Assume that the distances per liter for the truck models are approximately normally distributed with equal variances.
- **9.43** A taxi company is trying to decide whether to purchase brand A or brand B tires for its fleet of taxis. To estimate the difference in the two brands, an experiment is conducted using 12 of each brand. The tires are run until they wear out. The results are

Brand A:  $\bar{x}_1 = 36,300$  kilometers,

 $s_1 = 5000$  kilometers.

Brand B:  $\bar{x}_2 = 38,100$  kilometers,

 $s_2 = 6100$  kilometers.

Compute a 95% confidence interval for  $\mu_A - \mu_B$  assuming the populations to be approximately normally distributed. You may not assume that the variances are equal.

**9.44** Referring to Exercise 9.43, find a 99% confidence interval for  $\mu_1 - \mu_2$  if tires of the two brands are assigned at random to the left and right rear wheels of 8 taxis and the following distances, in kilometers, are recorded:

Taxi	Brand $A$	Brand $B$
1	34,400	36,700
2	45,500	46,800
3	36,700	37,700
4	32,000	31,100
5	48,400	47,800
6	32,800	36,400
7	38,100	38,900
8	30,100	31,500

Assume that the differences of the distances are approximately normally distributed.

**9.45** The federal government awarded grants to the agricultural departments of 9 universities to test the yield capabilities of two new varieties of wheat. Each variety was planted on a plot of equal area at each university, and the yields, in kilograms per plot, were recorded as follows:

		University								
Variety	1	2	3	4	5	6	7	8	9	
1	38	23	35	41	44	29	37	31	38	•
2	45	25	31	38	50	33	36	40	43	

Find a 95% confidence interval for the mean difference between the yields of the two varieties, assuming the differences of yields to be approximately normally distributed. Explain why pairing is necessary in this problem.

**9.46** The following data represent the running times of films produced by two motion-picture companies.

Company	Time (minutes)							
I	103	94	110	87	98			_
II	97	82	123	92	175	88	118	

Compute a 90% confidence interval for the difference between the average running times of films produced by the two companies. Assume that the running-time differences are approximately normally distributed with unequal variances.

9.47 Fortune magazine (March 1997) reported the total returns to investors for the 10 years prior to 1996 and also for 1996 for 431 companies. The total returns for 10 of the companies are listed below. Find a 95% confidence interval for the mean change in percent return to investors.

	Total Return				
	to Investors				
Company	1986-96	1996			
Coca-Cola	29.8%	43.3%			
Mirage Resorts	27.9%	25.4%			
Merck	22.1%	24.0%			
Microsoft	44.5%	88.3%			
Johnson & Johnson	22.2%	18.1%			
Intel	43.8%	131.2%			
Pfizer	21.7%	34.0%			
Procter & Gamble	21.9%	32.1%			
Berkshire Hathaway	28.3%	6.2%			
S&P 500	11.8%	20.3%			

- **9.48** An automotive company is considering two types of batteries for its automobile. Sample information on battery life is collected for 20 batteries of type A and 20 batteries of type B. The summary statistics are  $\bar{x}_A = 32.91$ ,  $\bar{x}_B = 30.47$ ,  $s_A = 1.57$ , and  $s_B = 1.74$ . Assume the data on each battery are normally distributed and assume  $\sigma_A = \sigma_B$ .
- (a) Find a 95% confidence interval on  $\mu_A \mu_B$ .
- (b) Draw a conclusion from (a) that provides insight into whether A or B should be adopted.
- **9.49** Two different brands of latex paint are being considered for use. Fifteen specimens of each type of