

## Summary of Time and Space Complexity for NP-Hard Problems

Problem	Worst-case Time Complexity	Best-case Time Complexity	Worst-case Space Complexity	Best-case Space Complexity
<b>Traveling Salesman</b>	$O(n!)$ or $O(2^n * n)$	Can be polynomial for small inputs or specific heuristics	$O(n * 2^n)$ (dynamic programming)	$O(n)$ (for greedy heuristics)
<b>Knapsack Problem</b>	$O(n * W)$ (dynamic programming)	$O(n)$ for greedy heuristic	$O(n * W)$ (dynamic programming)	$O(n)$ (for greedy approach)
<b>Vertex Cover</b>	$O(2^n)$ or $O(n!)$	Polynomial for small graphs	$O(n)$ for some special cases (like bounded treewidth)	$O(n)$ for bounded treewidth graphs
<b>Subset Sum Problem</b>	$O(2^n)$	$O(n)$ for small problems	$O(n * W)$ (if using dynamic programming)	$O(n)$ for specific instances
<b>Graph Coloring</b>	$O(2^n)$ or $O(n!)$	Polynomial for certain graph classes	$O(n^2)$ (if using DP for small graphs)	$O(n)$ for specific graph structures
<b>Independent Set</b>	$O(2^n)$	Polynomial for certain graph types	$O(2^n)$ or $O(n)$	$O(n)$ for specific instances
<b>Set Cover</b>	$O(2^m)$ or $O(m * 2^m)$	Polynomial for small $k$ or special cases	$O(2^m)$ or $O(m * n)$	$O(m + n)$
<b>Clique Decision</b>	$O(2^n)$	Polynomial for sparse graphs	$O(2^n)$ or $O(n * 2^n)$	$O(n)$ or better for sparse graphs
<b>3-Satisfiability (3-SAT)</b>	$O(2^n)$	Polynomial for specific instances	$O(2^n)$	$O(n)$