

# Assignment 3 Theory

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## CFG rules

1 - Write a CFG for accepting strings with equal number of a's and b's.

$S \rightarrow aSb \mid bSa \mid ba \mid ab \mid \epsilon$

2- Write a CFG for accepting strings where the number of b's is twice the number of a's.

$S \rightarrow aSbSbS \mid bSbSaS \mid bSaSbS \mid \epsilon$

3- Write a CFG for accepting strings that is not a palindrome  $\Sigma = \{a,b\}$ .

$S \rightarrow aSa \mid bSb \mid aTb \mid bTa,$   
 $T \rightarrow aT \mid bT \mid \epsilon$

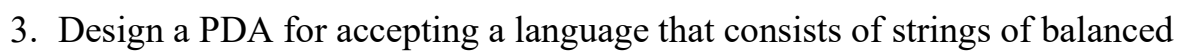
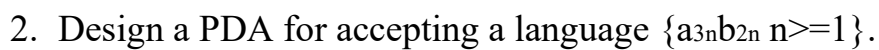
4- Write a CFG for accepting a language  $\{a^{2n+3}b^n \mid n \geq 0\}$ .

$S \rightarrow aaaT \mid \epsilon,$   
 $T \rightarrow aaTb \mid \epsilon$

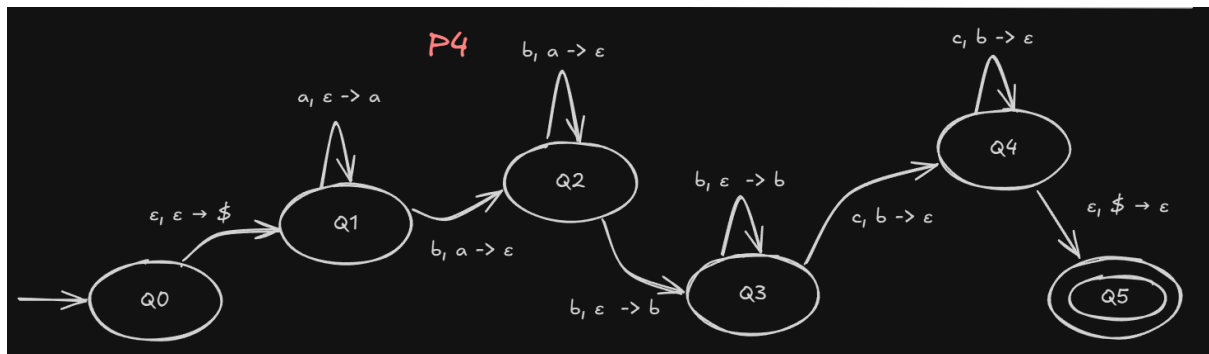
5- Write a CFG for accepting a language  $\{a^n b^m \mid n > m \text{ and } m \geq 0\}$ .

$S \rightarrow aS \mid aB,$   
 $B \rightarrow aBb \mid \epsilon$

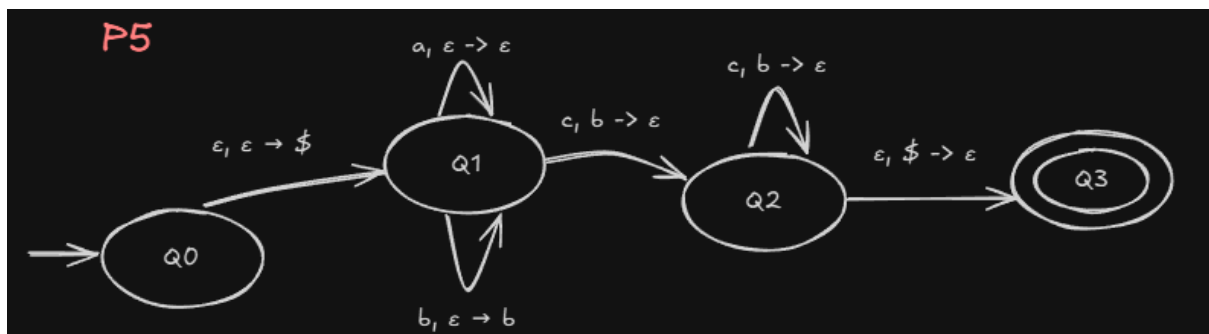
1. Design a PDA for accepting a language  $\{a^n b^m c^n | n, m \geq 0\}$ .



4. Design a PDA for accepting a language  $\{a^n b^{n+m} c^m \mid n, m \geq 1\}$ .



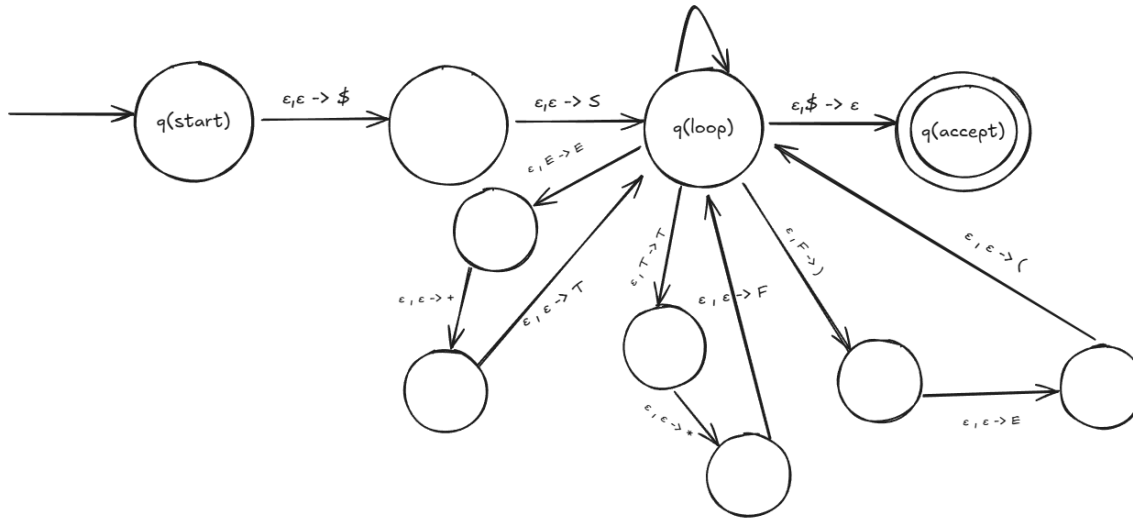
5. Design a PDA for language  $\{Wc^k \mid W \in \{a,b\}^* \text{ and } n \geq 0 \text{ and } k = |W|_b\}$  ( $k$ =the number of  $b$  in  $W$ ).



## BONUS - Convert the following CFG to PDA:

P1

$\epsilon, S \rightarrow E$	$0, 0 \rightarrow \epsilon$
$\epsilon, E \rightarrow T$	$1, 1 \rightarrow \epsilon$
$\epsilon, T \rightarrow F$	$2, 2 \rightarrow \epsilon$
$\epsilon, F \rightarrow N$	$3, 3 \rightarrow \epsilon$
$\epsilon, N \rightarrow 0$	$4, 4 \rightarrow \epsilon$
$\epsilon, N \rightarrow 1$	$5, 5 \rightarrow \epsilon$
$\epsilon, N \rightarrow 2$	$6, 6 \rightarrow \epsilon$
$\epsilon, N \rightarrow 3$	$7, 7 \rightarrow \epsilon$
$\epsilon, N \rightarrow 4$	$8, 8 \rightarrow \epsilon$
$\epsilon, N \rightarrow 5$	$9, 9 \rightarrow \epsilon$
$\epsilon, N \rightarrow 6$	$+, + \rightarrow \epsilon$
$\epsilon, N \rightarrow 7$	$(, ( \rightarrow \epsilon$
$\epsilon, N \rightarrow 8$	$), ) \rightarrow \epsilon$
$\epsilon, N \rightarrow 9$	$*, * \rightarrow \epsilon$



P2

$a, a \rightarrow \epsilon$
$b, b \rightarrow \epsilon$
$\epsilon, X \rightarrow \epsilon$

