

# Adil Gokturk\_HW1R

February 15, 2020

## 0.0.1 Adil Gokturk

## 0.1 HW1 Estimating Volatility from Historical Data

Set the working directory and load the libraries

```
[6]: setwd('C:/Users/hgokturk/Desktop/Spring2020/FIN659/Assignments/hw1')  
      getwd()
```

'C:/Users/hgokturk/Desktop/Spring2020/FIN659/Assignments/hw1'

```
[7]: # Load libraries  
      library(ggplot2)  
      library(IRdisplay)  
      library(psych)  
      library(quantmod)  
      library(tidyverse)
```

Registered S3 methods overwritten by 'ggplot2':

|                |       |
|----------------|-------|
| method         | from  |
| [.quosures     | rlang |
| c.quosures     | rlang |
| print.quosures | rlang |

Warning message:

"package 'psych' was built under R version 3.6.2"

Attaching package: 'psych'

The following objects are masked from 'package:ggplot2':

%+%, alpha

Warning message:

"package 'quantmod' was built under R version 3.6.2"Loading required package:

xts

Loading required package: zoo

Attaching package: 'zoo'

The following objects are masked from 'package:base':

```
as.Date, as.Date.numeric
```

Loading required package: TTR

Registered S3 method overwritten by 'quantmod':

```
method      from
as.zoo.data.frame zoo
```

Version 0.4-0 included new data defaults. See ?getSymbols.

```
-- Attaching packages ----- tidyverse 1.2.1 --
```

```
v tibble  2.1.1      v purrr   0.3.2
v tidyr   0.8.3      v dplyr   0.8.0.1
v readr   1.3.1      v stringr 1.4.0
v tibble  2.1.1      v forcats 0.4.0
```

Warning message:

```
"package 'stringr' was built under R version 3.6.2"-- Conflicts
```

```
----- tidyverse_conflicts() --
```

```
x psych::%+%( ) masks ggplot2::%+%( )
x psych::alpha( ) masks ggplot2::alpha( )
x dplyr::filter( ) masks stats::filter( )
x dplyr::first( ) masks xts::first( )
x dplyr::lag( ) masks stats::lag( )
x dplyr::last( ) masks xts::last( )
x purrr::reduce( ) masks rugarch::reduce( )
```

```
[8]: # Display HW1
display_png(file = "hw1.png")
```

### ESTIMATING VOLATILITY FROM HISTORICAL DATA

**Textbook Reference:** Section 15.4, pp. 323-327

**Points** **Steps to Follow:**

1. Go to the Yahoo! Finance website, search for **Apple Inc. (AAPL)**, and choose the link for "Historical Data"  
<https://finance.yahoo.com>
- 25.1 Set the **Time Period** to Dec 31, 2017 to Dec 31, 2018, set the **Frequency** to Daily, and click on the "Apply" button
- 25.1 Choose the link to "Download Data", open the spreadsheet, and copy the data into the space below
- 25.1 2. Calculate continuously compounded returns for each daily interval, using the function  $\text{LN}(\text{Today's Adj Close} / \text{Yesterday's Adj Close})$
- 15 3. Calculate the standard deviation of the returns, using the function  $\text{STDEV}$  across all returns
- 15 4. Estimate the annualized historical volatility, by multiplying the standard deviation of daily returns by the square root of the number of trading days in a year (252)
- 10 5. Estimate the annualized historical volatility for the last 3 months of the year only, by combining Steps 3 and 4 and applying them to the relevant returns

4.9 Which estimated annualized historical volatility is greater: that for the entire year, or that for the last quarter?  
Last quarter

5 What is the most likely explanation for your previous answer?  
A. Uncertainty related to Apple stock prices decreased during the last quarter of the year  
B. Uncertainty related to Apple stock prices increased during the last quarter of the year  
C. The Federal Reserve increased interest rates throughout the year  
D. Emerging market stock prices changed significantly during the last quarter of the year  
Choose the answer that you think is best.  
B

Step 1 (Data from Yahoo! Finance)

Step 2

Step 3

Step 4

Step 5

| Date | Open | High | Low | Close | Adj Close | Volume |
|------|------|------|-----|-------|-----------|--------|
|------|------|------|-----|-------|-----------|--------|

## 0.2 1. Go to the Yahoo! Finance website, search for Apple Inc. (AAPL), and download the "Historical Data"

Set the Time Period to \_\_Dec 31, 2017 to Dec 31, 2018,\_\_ set the Frequency to Daily, and click  
Choose the link to "Download Data", open the spreadsheet, and copy the data into the space be

<https://finance.yahoo.com>

I used quantmod package to get data and set the date from="2018-1-1", to="2019-1-1" to get all the 2018 trading days

```
[9]: getSymbols(Symbols = "AAPL", from="2018-1-1", to="2019-1-1")
```

'getSymbols' currently uses auto.assign=TRUE by default, but will use auto.assign=FALSE in 0.5-0. You will still be able to use 'loadSymbols' to automatically load data. getOption("getSymbols.env") and getOption("getSymbols.auto.assign") will still be checked for alternate defaults.

This message is shown once per session and may be disabled by setting options("getSymbols.warning4.0"=FALSE). See ?getSymbols for details.

'AAPL'

```
[10]: length(AAPL$AAPL.Adjusted)
      head(AAPL)
```

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|            | AAPL.Open | AAPL.High | AAPL.Low | AAPL.Close | AAPL.Volume | AAPL.Adjusted |
|------------|-----------|-----------|----------|------------|-------------|---------------|
| 2018-01-02 | 170.16    | 172.30    | 169.26   | 172.26     | 25555900    | 166.8040      |
| 2018-01-03 | 172.53    | 174.55    | 171.96   | 172.23     | 29517900    | 166.7750      |
| 2018-01-04 | 172.54    | 173.47    | 172.08   | 173.03     | 22434600    | 167.5496      |
| 2018-01-05 | 173.44    | 175.37    | 173.05   | 175.00     | 23660000    | 169.4572      |
| 2018-01-08 | 174.35    | 175.61    | 173.93   | 174.35     | 20567800    | 168.8278      |
| 2018-01-09 | 174.55    | 175.06    | 173.41   | 174.33     | 21584000    | 168.8085      |

```
[11]: tail(AAPL)
```

|            | AAPL.Open | AAPL.High | AAPL.Low | AAPL.Close | AAPL.Volume | AAPL.Adjusted |
|------------|-----------|-----------|----------|------------|-------------|---------------|
| 2018-12-21 | 156.86    | 158.16    | 149.63   | 150.73     | 95744600    | 148.1472      |
| 2018-12-24 | 148.15    | 151.55    | 146.59   | 146.83     | 37169200    | 144.3140      |
| 2018-12-26 | 148.30    | 157.23    | 146.72   | 157.17     | 58582500    | 154.4769      |
| 2018-12-27 | 155.84    | 156.77    | 150.07   | 156.15     | 53117100    | 153.4743      |
| 2018-12-28 | 157.50    | 158.52    | 154.55   | 156.23     | 42291400    | 153.5530      |
| 2018-12-31 | 158.53    | 159.36    | 156.48   | 157.74     | 35003500    | 155.0371      |

**0.2.1 2. Calculate continuously compounded returns for each daily interval, using the function LN(Today's Adj Close / Yesterday's Adj Close)**

```
[12]: apple2018 <- dailyReturn(x = AAPL$AAPL.Adjusted) %>% round(4)
```

```
[13]: # let's take a look at the first 6 days' return
      (apple2018)
```

```
      daily.returns
2018-01-02      0.0000
2018-01-03     -0.0002
2018-01-04      0.0046
2018-01-05      0.0114
2018-01-08     -0.0037
2018-01-09     -0.0001
2018-01-10     -0.0002
2018-01-11      0.0057
2018-01-12      0.0103
2018-01-16     -0.0051
2018-01-17      0.0165
2018-01-18      0.0009
2018-01-19     -0.0045
2018-01-22     -0.0082
2018-01-23      0.0002
2018-01-24     -0.0159
2018-01-25     -0.0179
2018-01-26      0.0023
2018-01-29     -0.0207
2018-01-30     -0.0059
2018-01-31      0.0028
2018-02-01      0.0021
2018-02-02     -0.0434
2018-02-05     -0.0250
2018-02-06      0.0418
2018-02-07     -0.0214
2018-02-08     -0.0275
2018-02-09      0.0122
2018-02-12      0.0403
2018-02-13      0.0100
2018-02-14      0.0184
2018-02-15      0.0336
2018-02-16     -0.0032
2018-02-20     -0.0034
2018-02-21     -0.0045
2018-02-22      0.0084
2018-02-23      0.0174
2018-02-26      0.0198
2018-02-27     -0.0032
2018-02-28     -0.0015
2018-03-01     -0.0175
2018-03-02      0.0069
2018-03-05      0.0035
```

|            |         |
|------------|---------|
| 2018-03-06 | -0.0008 |
| 2018-03-07 | -0.0093 |
| 2018-03-08 | 0.0109  |
| 2018-03-09 | 0.0172  |
| 2018-03-12 | 0.0097  |
| 2018-03-13 | -0.0096 |
| 2018-03-14 | -0.0085 |
| 2018-03-15 | 0.0012  |
| 2018-03-16 | -0.0035 |
| 2018-03-19 | -0.0153 |
| 2018-03-20 | -0.0003 |
| 2018-03-21 | -0.0227 |
| 2018-03-22 | -0.0141 |
| 2018-03-23 | -0.0232 |
| 2018-03-26 | 0.0475  |
| 2018-03-27 | -0.0256 |
| 2018-03-28 | -0.0110 |
| 2018-03-29 | 0.0078  |
| 2018-04-02 | -0.0066 |
| 2018-04-03 | 0.0103  |
| 2018-04-04 | 0.0191  |
| 2018-04-05 | 0.0069  |
| 2018-04-06 | -0.0256 |
| 2018-04-09 | 0.0099  |
| 2018-04-10 | 0.0188  |
| 2018-04-11 | -0.0047 |
| 2018-04-12 | 0.0099  |
| 2018-04-13 | 0.0034  |
| 2018-04-16 | 0.0062  |
| 2018-04-17 | 0.0138  |
| 2018-04-18 | -0.0022 |
| 2018-04-19 | -0.0283 |
| 2018-04-20 | -0.0410 |
| 2018-04-23 | -0.0029 |
| 2018-04-24 | -0.0139 |
| 2018-04-25 | 0.0044  |
| 2018-04-26 | 0.0035  |
| 2018-04-27 | -0.0116 |
| 2018-04-30 | 0.0181  |
| 2018-05-01 | 0.0232  |
| 2018-05-02 | 0.0442  |
| 2018-05-03 | 0.0018  |
| 2018-05-04 | 0.0392  |
| 2018-05-07 | 0.0072  |
| 2018-05-08 | 0.0048  |
| 2018-05-09 | 0.0070  |
| 2018-05-10 | 0.0143  |
| 2018-05-11 | -0.0038 |

|            |         |
|------------|---------|
| 2018-05-14 | -0.0023 |
| 2018-05-15 | -0.0091 |
| 2018-05-16 | 0.0093  |
| 2018-05-17 | -0.0063 |
| 2018-05-18 | -0.0036 |
| 2018-05-21 | 0.0071  |
| 2018-05-22 | -0.0025 |
| 2018-05-23 | 0.0064  |
| 2018-05-24 | -0.0011 |
| 2018-05-25 | 0.0023  |
| 2018-05-29 | -0.0036 |
| 2018-05-30 | -0.0021 |
| 2018-05-31 | -0.0034 |
| 2018-06-01 | 0.0180  |
| 2018-06-04 | 0.0084  |
| 2018-06-05 | 0.0077  |
| 2018-06-06 | 0.0035  |
| 2018-06-07 | -0.0027 |
| 2018-06-08 | -0.0091 |
| 2018-06-11 | -0.0025 |
| 2018-06-12 | 0.0055  |
| 2018-06-13 | -0.0082 |
| 2018-06-14 | 0.0005  |
| 2018-06-15 | -0.0103 |
| 2018-06-18 | -0.0005 |
| 2018-06-19 | -0.0162 |
| 2018-06-20 | 0.0044  |
| 2018-06-21 | -0.0056 |
| 2018-06-22 | -0.0029 |
| 2018-06-25 | -0.0149 |
| 2018-06-26 | 0.0124  |
| 2018-06-27 | -0.0015 |
| 2018-06-28 | 0.0073  |
| 2018-06-29 | -0.0021 |
| 2018-07-02 | 0.0112  |
| 2018-07-03 | -0.0174 |
| 2018-07-05 | 0.0080  |
| 2018-07-06 | 0.0139  |
| 2018-07-09 | 0.0139  |
| 2018-07-10 | -0.0012 |
| 2018-07-11 | -0.0130 |
| 2018-07-12 | 0.0168  |
| 2018-07-13 | 0.0016  |
| 2018-07-16 | -0.0022 |
| 2018-07-17 | 0.0028  |
| 2018-07-18 | -0.0055 |
| 2018-07-19 | 0.0078  |
| 2018-07-20 | -0.0023 |

|            |         |
|------------|---------|
| 2018-07-23 | 0.0009  |
| 2018-07-24 | 0.0073  |
| 2018-07-25 | 0.0094  |
| 2018-07-26 | -0.0031 |
| 2018-07-27 | -0.0166 |
| 2018-07-30 | -0.0056 |
| 2018-07-31 | 0.0020  |
| 2018-08-01 | 0.0589  |
| 2018-08-02 | 0.0292  |
| 2018-08-03 | 0.0029  |
| 2018-08-06 | 0.0052  |
| 2018-08-07 | -0.0094 |
| 2018-08-08 | 0.0007  |
| 2018-08-09 | 0.0079  |
| 2018-08-10 | -0.0030 |
| 2018-08-13 | 0.0065  |
| 2018-08-14 | 0.0042  |
| 2018-08-15 | 0.0023  |
| 2018-08-16 | 0.0146  |
| 2018-08-17 | 0.0200  |
| 2018-08-20 | -0.0097 |
| 2018-08-21 | -0.0019 |
| 2018-08-22 | 0.0000  |
| 2018-08-23 | 0.0020  |
| 2018-08-24 | 0.0031  |
| 2018-08-27 | 0.0082  |
| 2018-08-28 | 0.0081  |
| 2018-08-29 | 0.0149  |
| 2018-08-30 | 0.0092  |
| 2018-08-31 | 0.0116  |
| 2018-09-04 | 0.0032  |
| 2018-09-05 | -0.0065 |
| 2018-09-06 | -0.0166 |
| 2018-09-07 | -0.0081 |
| 2018-09-10 | -0.0134 |
| 2018-09-11 | 0.0253  |
| 2018-09-12 | -0.0124 |
| 2018-09-13 | 0.0242  |
| 2018-09-14 | -0.0114 |
| 2018-09-17 | -0.0266 |
| 2018-09-18 | 0.0017  |
| 2018-09-19 | 0.0006  |
| 2018-09-20 | 0.0076  |
| 2018-09-21 | -0.0108 |
| 2018-09-24 | 0.0144  |
| 2018-09-25 | 0.0063  |
| 2018-09-26 | -0.0080 |
| 2018-09-27 | 0.0206  |

|            |         |
|------------|---------|
| 2018-09-28 | 0.0035  |
| 2018-10-01 | 0.0067  |
| 2018-10-02 | 0.0089  |
| 2018-10-03 | 0.0122  |
| 2018-10-04 | -0.0176 |
| 2018-10-05 | -0.0162 |
| 2018-10-08 | -0.0023 |
| 2018-10-09 | 0.0139  |
| 2018-10-10 | -0.0463 |
| 2018-10-11 | -0.0088 |
| 2018-10-12 | 0.0357  |
| 2018-10-15 | -0.0214 |
| 2018-10-16 | 0.0220  |
| 2018-10-17 | -0.0043 |
| 2018-10-18 | -0.0234 |
| 2018-10-19 | 0.0152  |
| 2018-10-22 | 0.0061  |
| 2018-10-23 | 0.0094  |
| 2018-10-24 | -0.0343 |
| 2018-10-25 | 0.0219  |
| 2018-10-26 | -0.0159 |
| 2018-10-29 | -0.0188 |
| 2018-10-30 | 0.0050  |
| 2018-10-31 | 0.0261  |
| 2018-11-01 | 0.0154  |
| 2018-11-02 | -0.0663 |
| 2018-11-05 | -0.0284 |
| 2018-11-06 | 0.0108  |
| 2018-11-07 | 0.0303  |
| 2018-11-08 | -0.0035 |
| 2018-11-09 | -0.0193 |
| 2018-11-12 | -0.0504 |
| 2018-11-13 | -0.0100 |
| 2018-11-14 | -0.0282 |
| 2018-11-15 | 0.0247  |
| 2018-11-16 | 0.0111  |
| 2018-11-19 | -0.0396 |
| 2018-11-20 | -0.0478 |
| 2018-11-21 | -0.0011 |
| 2018-11-23 | -0.0254 |
| 2018-11-26 | 0.0135  |
| 2018-11-27 | -0.0022 |
| 2018-11-28 | 0.0385  |
| 2018-11-29 | -0.0077 |
| 2018-11-30 | -0.0054 |
| 2018-12-03 | 0.0349  |
| 2018-12-04 | -0.0440 |
| 2018-12-06 | -0.0111 |



|            |         |
|------------|---------|
| 2018-12-07 | -0.0357 |
| 2018-12-10 | 0.0066  |
| 2018-12-11 | -0.0057 |
| 2018-12-12 | 0.0028  |
| 2018-12-13 | 0.0109  |
| 2018-12-14 | -0.0320 |
| 2018-12-17 | -0.0093 |
| 2018-12-18 | 0.0130  |
| 2018-12-19 | -0.0312 |
| 2018-12-20 | -0.0252 |
| 2018-12-21 | -0.0389 |
| 2018-12-24 | -0.0259 |
| 2018-12-26 | 0.0704  |
| 2018-12-27 | -0.0065 |
| 2018-12-28 | 0.0005  |
| 2018-12-31 | 0.0097  |

```
[14]: # remove the ZERO valued First day form the data
apple2018 <- apple2018[-1,]
```

```
[15]: # let's check it
head(apple2018)
```

| daily.returns |         |
|---------------|---------|
| 2018-01-03    | -0.0002 |
| 2018-01-04    | 0.0046  |
| 2018-01-05    | 0.0114  |
| 2018-01-08    | -0.0037 |
| 2018-01-09    | -0.0001 |
| 2018-01-10    | -0.0002 |

```
[16]: tail(apple2018)
```

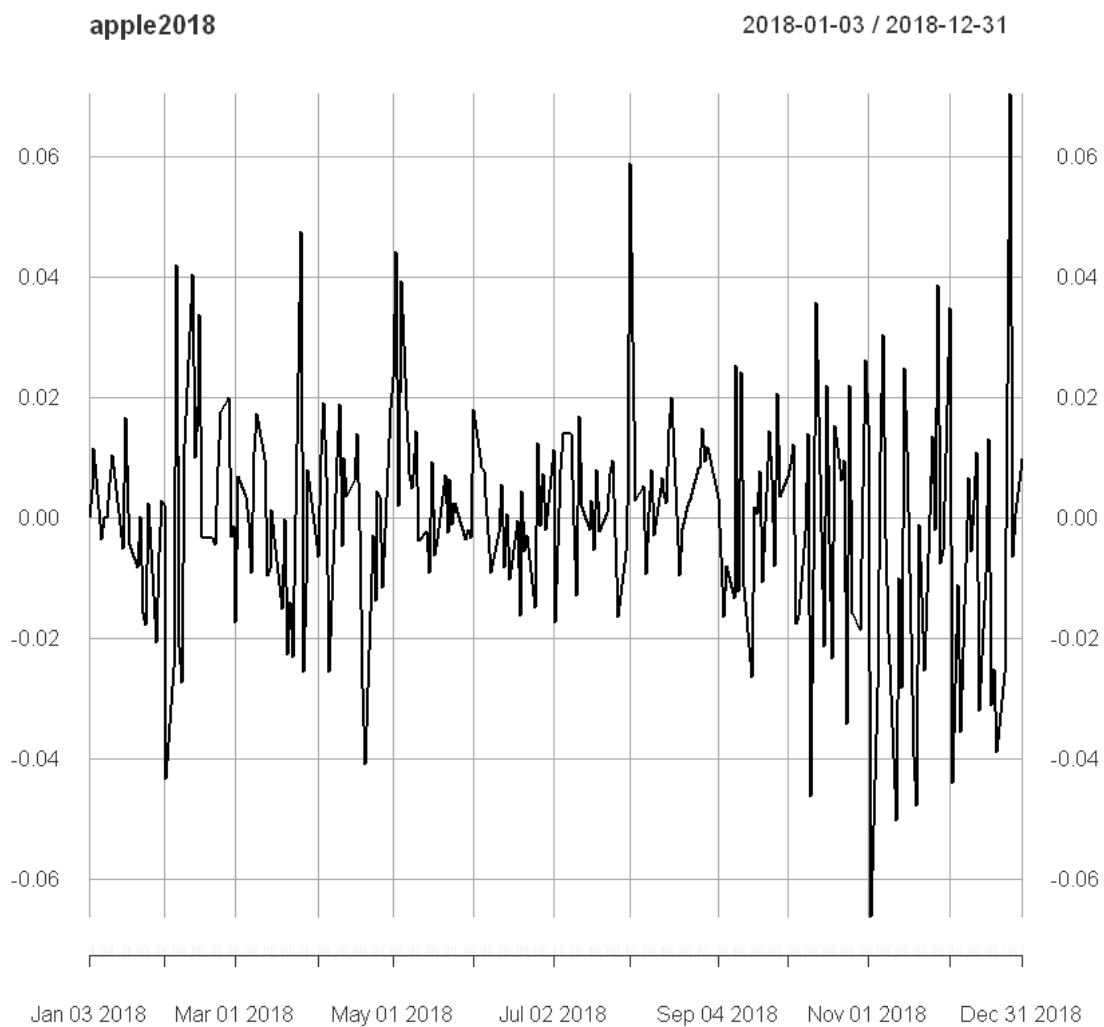
| daily.returns |         |
|---------------|---------|
| 2018-12-21    | -0.0389 |
| 2018-12-24    | -0.0259 |
| 2018-12-26    | 0.0704  |
| 2018-12-27    | -0.0065 |
| 2018-12-28    | 0.0005  |
| 2018-12-31    | 0.0097  |

```
[17]: # check the structure
str(apple2018)
```

```
An 'xts' object on 2018-01-03/2018-12-31 containing:
Data: num [1:250, 1] -0.0002 0.0046 0.0114 -0.0037 -0.0001 -0.0002 0.0057
```

```
0.0103 -0.0051 0.0165 ...  
- attr(*, "dimnames")=List of 2  
..$ : NULL  
..$ : chr "daily.returns"  
Indexed by objects of class: [Date] TZ: UTC  
xts Attributes:  
NULL
```

```
[18]: # Let's take a look at the daily volatility of the Apple stock price in 2018  
plot(apple2018)
```



**0.2.2 3. Calculate the standard deviation of the returns, using the function STDEV across all returns**

```
[19]: # standard deviation of the returns
apple2018.sd <- sd(apple2018)
apple2018.sd
(apple2018.sd *100) %>% round(2) # Percentage %
```

0.0181071952637973

1.81

**0.2.3 Calculated standard deviation of the returns= 0.0181071952637973 or 1.81 %**

**0.2.4 4. Estimate the annualized historical volatility, by multiplying the standard deviation of daily returns by the square root of the number of trading days in a year (252)**

```
[20]: apple2018.hist.volatility <- apple2018.sd*sqrt(252)
apple2018.hist.volatility
(apple2018.hist.volatility*100) %>% round(2) # Percentage %
```

0.287442813653366

28.74

**0.2.5 Annualized historical volatility = 28.74 %**

It is slightly different than the solution of 28.78%! I assume R still use more than 4 decimal to calculate.

**0.2.6 5. Estimate the annualized historical volatility for the last 3 months of the year only, by combining Steps 3 and 4 and applying them to the relevant returns**

```
[21]: # Let's get the last 3 months return data
length(apple2018) # 2018 data
length(apple2018[188:250,]) # last 3 months
head(apple2018[188:250,]) # Let's check it
tail(apple2018[188:250,])
```

250

63

|            | daily.returns |
|------------|---------------|
| 2018-10-01 | 0.0067        |
| 2018-10-02 | 0.0089        |
| 2018-10-03 | 0.0122        |
| 2018-10-04 | -0.0176       |
| 2018-10-05 | -0.0162       |
| 2018-10-08 | -0.0023       |

|            | daily.returns |
|------------|---------------|
| 2018-12-21 | -0.0389       |
| 2018-12-24 | -0.0259       |
| 2018-12-26 | 0.0704        |
| 2018-12-27 | -0.0065       |
| 2018-12-28 | 0.0005        |
| 2018-12-31 | 0.0097        |

```
[22]: # Calculate the annualized historical volatility for the last 3 months of the
      ↪ year
      (apple2018.quarter4.volatility <- sd(apple2018[188:250,])*sqrt(252))
      (apple2018.quarter4.volatility *100) %>% round(2)
```

0.402237257862699

40.22

**0.2.7 The annualized historical volatility for the last 3 months of the year = 40.22%**

It is slightly different than the solution of 40.42! I assume R still use more than 4 decimal to calculate.

**0.2.8 Which estimated annualized historical volatility is greater: that for the entire year, or that for the last quarter?**

**0.3 Last Quarter**

**0.3.1 What is the most likely explanation for your previous answer?**

**0.4 B. Uncertainty related to Apple stock prices increased during the last quarter of the year!**

I found another R package—PerformanceAnalytics, I think it minimizes algebra usage in Financial analytics.