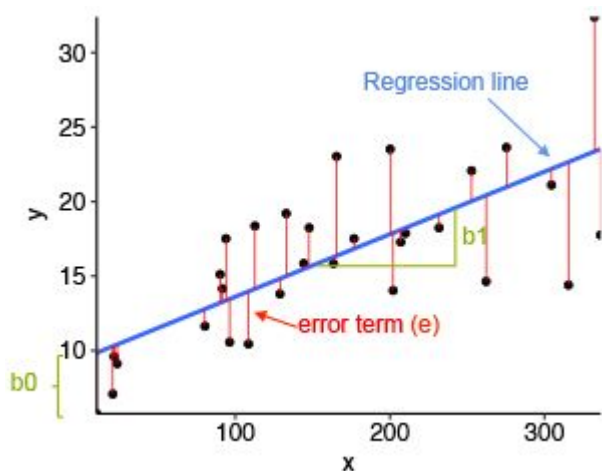

TUT206 OCT25

Announcement!

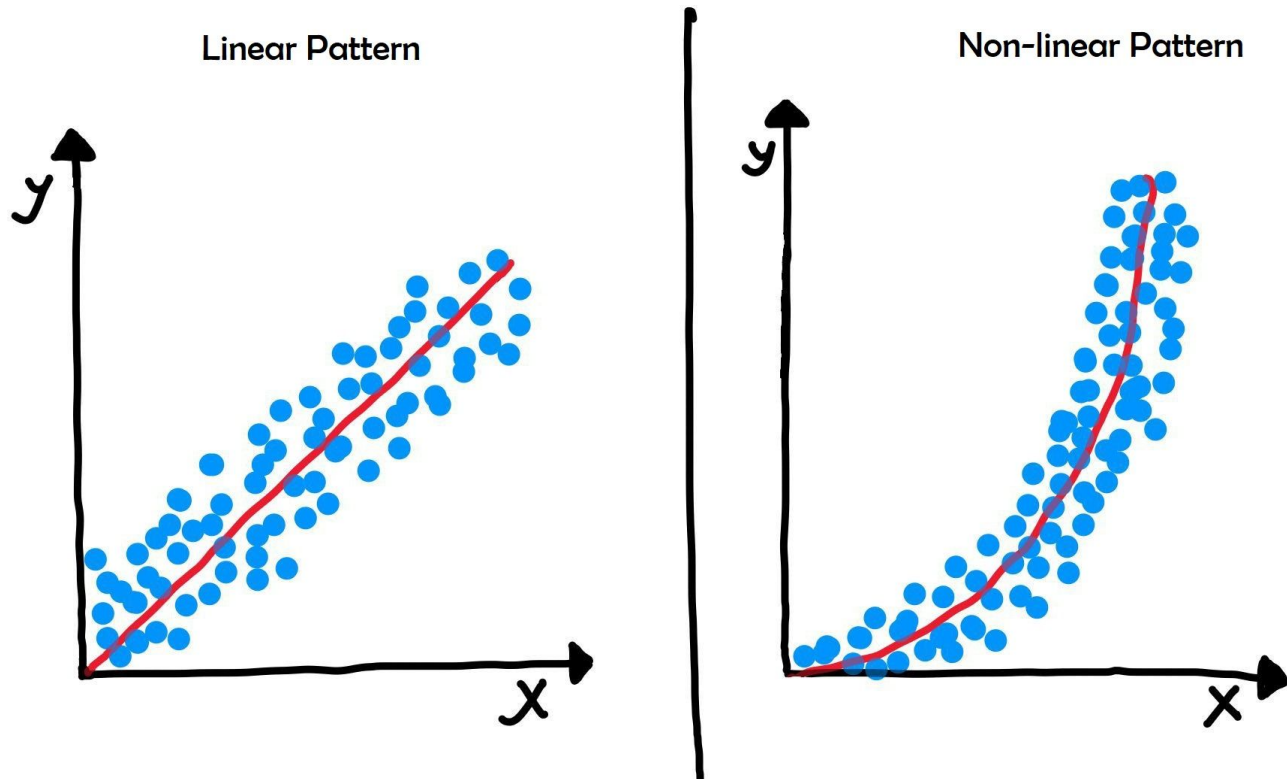
- The course project link
- **The MIDWAY ChatBot Experience**
FEEDBACK link
- Interaction? See github md

Recap: simple linear regression



$$Y_i = \beta_0 + \beta_1 x_i + \epsilon_i \quad \text{where} \quad \epsilon_i \sim \mathcal{N}(0, \sigma^2)$$

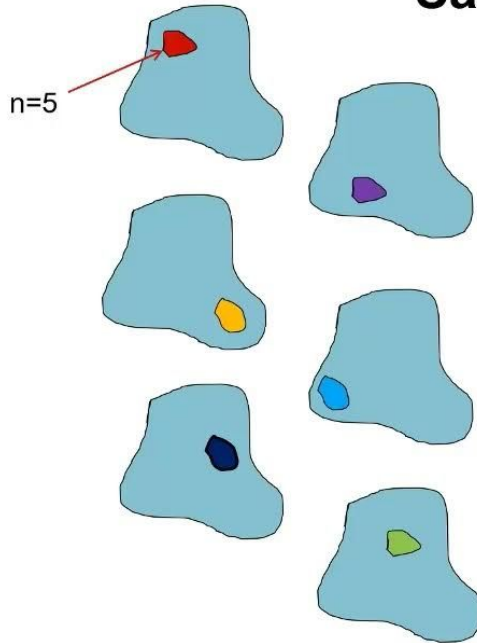
Recap: simple linear regression assumption



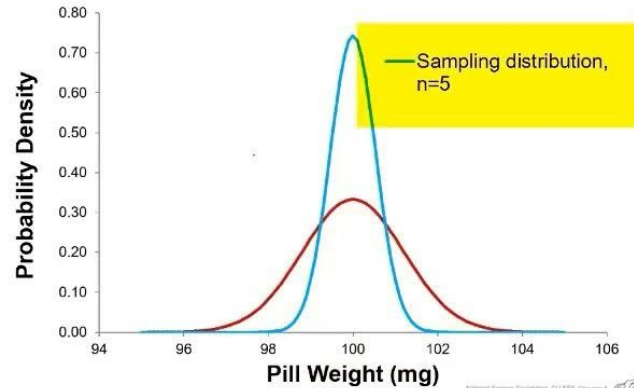
Recap: sample distribution! important

[Sampling Distribution vs Population Distribution \(youtube.com\)](#)

Sampling Distribution



1. Take sample of size n
2. Compute \bar{X} of those n items
3. Repeat many times to generate a distribution of \bar{X}



Recap: sample distribution! important

HW this time is Going To Be DIFFERENT: you MUST understand simulation to do it

AKA Hypothesis Testing, Sampling Distribution under the Null Hypothesis, and related topics regarding interpretation from Oct04 TUT and Oct11 TUT; **AND, Sampling Distribution, Bootstrapped Confidence Intervals**, and related topics regarding interpretation from Sep27 TUT and Sep30 LEC and Oct07 LEC

Show how
to using
notebooklm

Communication:

The Wheel of Destiny

Stella McStat had been running a small-time gambling operation on campus for several months during her first year at UofT...

- For each spin of the wheel, two gamblers take part. For a toonie each (\\$2 Canadian), Stella sells one a red ticket and one a black ticket (i.e., total \\$4). Then Stella spins the Wheel of Destiny. The person who holds the colour on which the spinner stops gets \\$3.50 (Stella keeps \\$0.50 per spin for running the game and providing snacks).

Communication



Communication

1. Null Hypothesis (H_0):

- In the context of “Stella McStat’s Wheel of Destiny,” the **Null Hypothesis** (H_0) could be that the **wheel is fair**. This means that the outcomes of the wheel occur at equal probability (e.g., no section of the wheel is favored over another).

2. Alternative Hypothesis (H_1):

- The **Alternative Hypothesis** (H_1) is that the **wheel is biased**. In this case, some outcomes may be more likely to occur than others, indicating that the wheel is not fair.

3. P-Value Definition:

- A **p-value** is the probability of obtaining a test statistic as extreme as (or more extreme than) the observed test statistic, assuming that the **null hypothesis** is true.

Communication:

Here's a possible example of x and y values:

- x : The size of each section on the wheel, measured in degrees or as a percentage of the wheel (e.g., 30%, 20%, 10%, etc.).
- y : The number of times the wheel lands on each section during a series of spins.

Communication:



Communication

In the context of **simple linear regression**, the **Null Hypothesis (H_0)** typically states that the **slope** $\beta_1 = 0$. This implies that there is no relationship between the predictor variable x and the response variable Y , meaning that changes in x do not affect Y .

The **Alternative Hypothesis (H_1)** is that $\beta_1 \neq 0$, which implies that there **is a relationship** between x and Y , meaning that changes in x are associated with changes in Y .

Mathematically, these hypotheses are:

- **Null Hypothesis (H_0):** $\beta_1 = 0$
- **Alternative Hypothesis (H_1):** $\beta_1 \neq 0$

Demo: concepts see zoom

Demo: Observed data setup



Show chatgpt canvas



Demo: Model fitting code demo

```
statsmodels.formula.api as smf
```

```
smf.ols(...).fit()
```