Sunshine Math
Superstars III

Uranus
Grade 6

Neptune
Grade 7

Saturn
Grade 5

Pluto
Grade 8

Jupiter
Grade 4

Mercury
Kindergarten

Mars
Grade 3

Venus
Grade 1

Earth
Grade 2

Saturn
Grade 5

Acknowledgments

This project was conceived of and coordinated by the Florida Department of Education. In addition, it was supported financially through a grant to the School Board of Polk County. The rich history of these materials and the predecessor programs *Superstars* and *Superstars II*, goes back to the early 1980's. Dr. Andy Reeves initiated the program at the Department of Education, and many Florida teachers have been involved in developing and using these materials over the years.

The following Florida educators were primarily responsible for developing, field testing, and publishing *Sunshine Math*:

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Linda Ferriera	Carol Newman	Ken West
Mary Fletcher	Jill Nielson	Janet Williams
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Revisions were made to *Sunshine Math* by Sandy Berger, Frankie Mack and Linda Fisher with input from Andy Reeves and from volunteers and district staff in Broward, Duval, and Volusia school districts.

A copy of the complete set of revised materials, grades K-8, has been sent to the district office for use by all of the schools. School districts in Florida have permission to reproduce this document for use in their schools for non-profit educational purposes.

Under the provisions governing Eisenhower funds, it is the responsibility of the districts to furnish copies to public and private schools and to ensure that home schools have access to the materials. Questions regarding these responsibilities should be directed to the district contact persons for Eisenhower Funds and for Home Schools.

Additional copies of *Sunshine Math* may be purchased at cost from the Panhandle Area Educational Consortium (PAEC), 753 West Boulevard, Chipley, Florida 32428, or by calling the PAEC Clearinghouse, (850) 638-6131, Suncom 769-6131, FAX (850) 638-6336. Out-of-state schools that purchase copies have permission to reproduce the document for use with their students for non-profit educational purposes.

Preface

Sunshine Math and its predecessor programs, *Superstars* and *Superstars II*, dwell on the positive aspects of students, parents, teachers, and administrators working together. This program assumes that children, even young children, are capable of and interested in learning; that teachers want to help them learn to think for themselves; that administrators see their jobs as clearing the path so that quality education is delivered effectively in their schools; and that parents care about their child's learning and are willing to work with the school system toward that goal. Each of these four groups has a vital role to play in implementing *Sunshine Math*..

The program's initiators believed that elementary students are capable of much more than we normally ask of them, and the subsequent success of *Superstars* indicates that many children are on the path to becoming independent learners. A number of children in *any* classroom are bright, energetic, and willing to accept extra challenges.

The basic purpose of the *Superstars* program is to provide the extra challenge that self-motivated students need in mathematics, and to do so in a structured, long-term program that does not impinge on the normal classroom routine or the time of the teacher. The system is not meant to replace any aspect of the school curriculum -- it is offered as a peripheral opportunity to students who identify with challenges and who want to be rewarded for their extra effort. Participation in the program is always optional -- only those students who voluntarily choose to participate will, in the long run, benefit from this program. Any student, regardless of prior academic performance, should be encouraged to participate as long their interest is maintained.

The predecessor programs for *Sunshine Math* - the Florida Department of Education's *Superstars II* and *Superstars*-- have demonstrated that this concept can be extremely successful. What is required are several dedicated adults who devote a few hours each week to operate the system effectively in the school; an administrator who provides highly visible support; teachers who welcome a supplementary experience for their students to engage in higher-order thinking; and a typical classroom of students. If all of those ingredients are present, *Sunshine Math* will become an integral part of the school fabric.

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ORGANIZATION OF THESE MATERIALS

Section I   **Description of the *Sunshine Math* Program**

1. General Information
2. Information/ checklist for principals
3. Information/checklist for assisting adults
4. Information for teachers
5. Letter to participating students and their parents

Section II   **Student worksheets for *Sunshine Math***

Section III   **Commentary for student worksheets for *Sunshine Math***
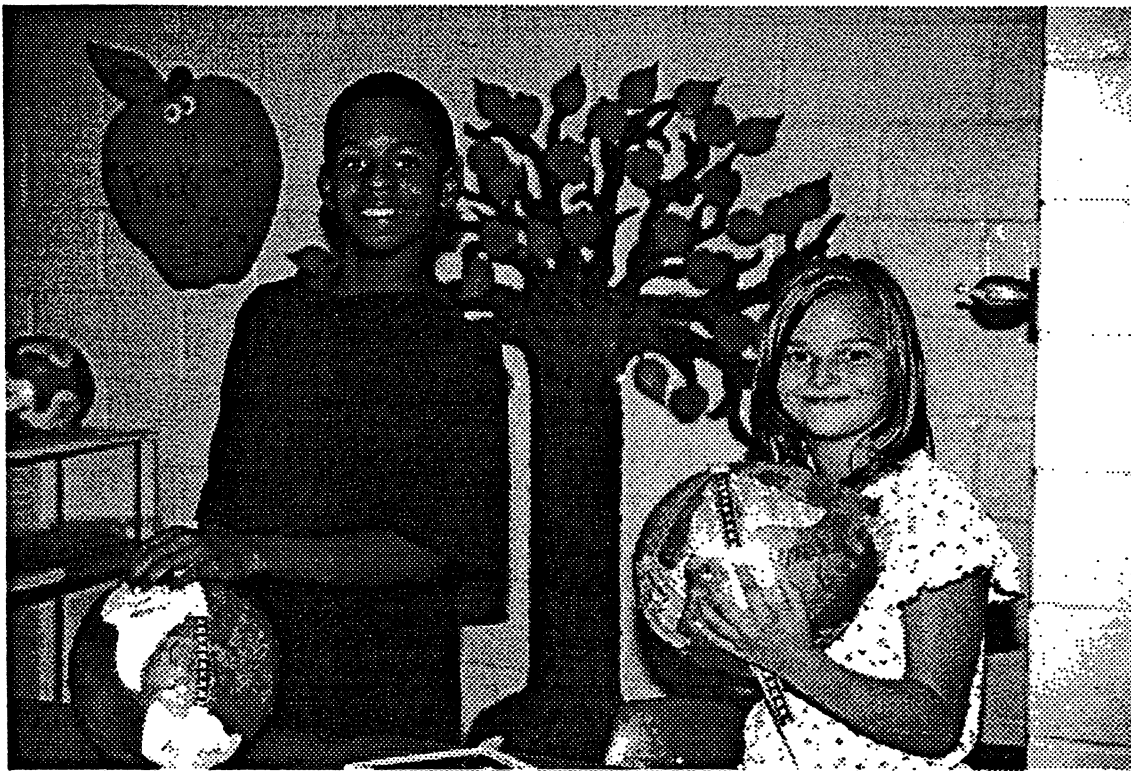
Sunshine Math General Information

Sunshine Math is a K-8 program designed as an enrichment opportunity for self-directed learners in mathematics. The levels of the program are named after the planets of our solar system:

Kindergarten	Mercury	Fifth Grade	Saturn
First Grade	Venus	Sixth Grade	Uranus
Second Grade	Earth	Seventh Grade	Neptune
Third Grade	Mars	Eighth Grade	Pluto
Fourth Grade	Jupiter		

Students of all ability levels choose on their own to participate in *Sunshine Math*. The visual reinforcement of seeing their names displayed in a prominent place in the school, with a string of stars indicating their success, is the reward a student receives for the extra work. In many cases, the school decides to enhance the basic reward system by awarding certificates or other forms of recognition for achieving certain levels of success in *Sunshine Math*.

Sunshine Math can function in a school in a number of different ways. The "tried and true" way is for assisting adults (volunteers, aides, etc.) to manage the program for the entire school, with support provided by school administrators and classroom teachers. This system has been modified at the school level, with varying degrees of success, over the years. The basic model for running *Sunshine Math* is discussed below, with variations described on the next page.

The Basic Model

The basic model for *Sunshine Math* is for a school to establish a weekly cycle early in the fall, according to these guidelines:

> On Monday of each week, student worksheets are distributed by the assisting adults to those in the program. Students have until Friday to complete the problems, working entirely on their own. On Friday, the classroom teacher hosts a brief problem-solving session for the students in the program. The more difficult problems on the worksheet for that week are discussed, with students describing their thinking about how to approach and solve the problems. They do not give their answers for the problems, only their strategies.

> Students get double-credit for problems they complete prior to the problem-solving session, and regular credit for those they complete successfully over the weekend. On Monday, all papers are handed in, checked by the assisting adult, and stars are posted for problems successfully worked. This completes the cycle for the preceding week, allows for the new worksheets to be passed out, and the cycle begins again.

Sunshine Math is not for every child -- it's only for those who are self-motivated and who are not easily frustrated by challenging situations. This does not diminish the value of the program, but rather makes us realize that there are children of all ability and socio-economic levels who are self-directed learners and who need challenges beyond those of the regular school day. These children will shine in *Sunshine Math*.

Variations of the Basic Model

The first variation that has been used successfully retains the weekly cycle and assisting adult role as in the basic model. However, the teacher involves the entire class in the problem-solving discussions. For example, the teacher might pick the four hardest problems on the worksheet for that week, and do a "parallel problem" with the entire class to open the mathematics class on Tuesday through Friday. Using this variation, all students are exposed to the problem-solving strategies, but only those who are in *Sunshine Math* exhibit that they have learned the material by completing the worksheet over the weekend.

A second variation is for the assisting adults to run the entire program, including the problem-solving session for students. This method has been used in situations in which some teachers in a school lacked commitment to the program, and thus it was being implemented inconsistently. In such cases, the assisting adults must have a progressive view of what constitutes problem solving in elementary mathematics. They must also be given extra assistance from the principal to ensure students are released from class and that the process works smoothly in general.

Yet another variation is for a parent to run *Sunshine Math* at home, for their own child. The basic rules are the same -- a child gets the worksheet once a week and time to work the problems alone. The parent has a pre-established night to listen to the way the child thought about each problem, interjecting her or his own methods only when the child seems stuck. The reward system is basically the same -- stars on a chart -- but is usually enhanced by doing something special for the child, such as a trip to the movies or to the skating rink, when the child reaches certain levels of success. If this method is adopted, the parent must be sure not to try to "teach the child." *Sunshine Math* is a program designed to stimulate discussion of problem-solving strategies; it is not a program designed for adults to "teach children how to think."

Other variations abound. The basic model on the previous page is the approach that reaches more children in a consistent fashion than any of the other methods. However, individual schools, teachers, or parents are encouraged to get some version started, even if it's not one of the above. Some sunshine is better than none at all!

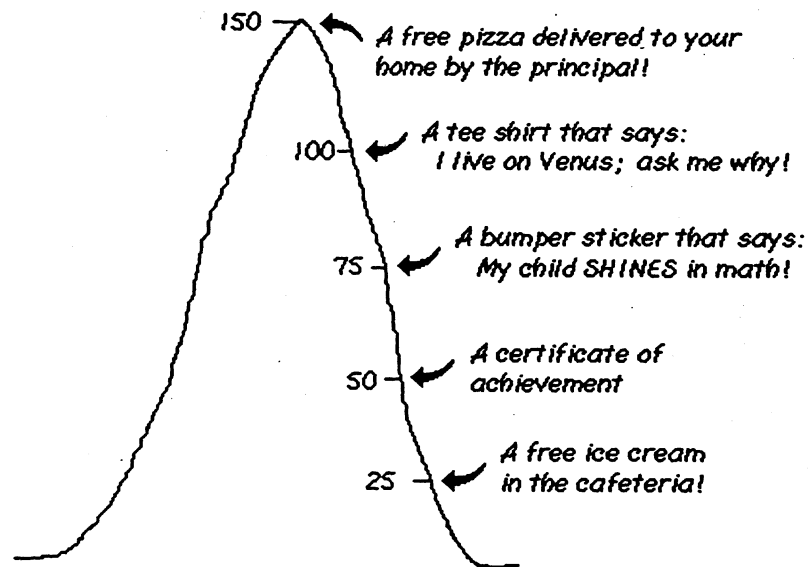## *Sunshine Math*: Information for Principals

       Sunshine Math is a K-8 enrichment package for mathematics, designed to be managed by volunteer assisting adults with coordinated support from the classroom teacher and school administrators. The purpose of the program is to give self-motivated students of all ability levels a chance to extend themselves beyond the normal mathematics curriculum. The complete set of materials comes in nine packages, one for each K-8 grade. The grade levels are named for the planets in the solar system, in order starting from the sun: Mercury, Venus, Earth, Mars, Jupiter, Saturn, Uranus, Neptune, and Pluto.

       Your support is vital if this program is to succeed. As the school administrator, you need to stay in close touch with *Sunshine Math*. A "checklist for success" follows:

❑ Become familiar with the philosophy and component parts of the program.

❑ Introduce *Sunshine Math* to the faculty early in the school year. Ensure that each teacher understands the philosophy of the program and has a copy of the student worksheets and commentary for that grade level.

❑ Speak to parents at your school's first "open house" of the year, explaining the purpose of *Sunshine Math* and the long-term value of children working independently on the worksheets.

❑ Recruit several assisting adults (PTA members, aides, senior citizens, business partners, churches, and so on) who are enthusiastic, dependable people to manage the program. Early in the year, meet with these assisting adults to plan such details as:

      ✔ A prominent place and format for the STAR CHART.

      ✔ A designated time each Monday and Friday for the assisting adult to be in the school to receive and distribute papers from students, and post stars.

      ✔ A system for the activity sheets to be duplicated each week.

      ✔ A plan for extra incentives for accumulating stars. ("World records" to be kept from year-to-year; a celebration day planned for the end of school; students earning prizes for attaining certain levels of success -- see the reverse side of this page for examples.)

      ✔ A schedule for when the program will begin, and whether or not there should be a "start over" point at some time in the school year. Review a school calendar, and use only weeks that have at least four school days in them. If there isn't time in the school year to cover all the activity sheets under these conditions, decide which sheets to eliminate or when to "double up."

      ✔ If possible provide volunteers with a *Sunshine Math* cap, name tag, tee-shirt, or other identifying feature.

❑ Monitor the program every two weeks to clear up any unforeseen problems. Administrators need to be highly visible for *Sunshine Math* to succeed.

Sunshine Math is an optional program for students. It should be available to any student who wants to participate, regardless of prior success in mathematics. A large number of students will usually begin the program, but a majority of them will lose interest. However, a significant number of students will continue their interest over the life of the program. This is normal and simply means that *Sunshine Math* is successfully addressing the needs of the self-directed learner.

Visual reminders help children see that mathematics is challenging and rewarding. Some ideas are presented below, merely to start your creative juices flowing:

150 ← A free pizza delivered to your home by the principal!

100 ← A tee shirt that says: I live on Venus; ask me why!

75 ← A bumper sticker that says: My child SHINES in math!

50 ← A certificate of achievement

25 ← A free ice cream in the cafeteria!

Climb the Mountain this Year!!!

Join the Sunshine Math Club

Tom Walker, Principal at Bashaw Elementary School in Bradenton, passes out awards for achievement levels in Superstars.

Sunshine Math: Information for Assisting Adults

Sunshine Math is designed to give assisting adults a well-defined role to play in the school's mathematics program. The success of *Sunshine Math* depends on a team effort among teachers, administrators, parents, and you. Reliability and punctuality are important -- students will rapidly come to depend upon you to be there as scheduled, to check their papers and post their stars, and to listen to alternate ways in which they may have interpreted a problem to arrive at a unique answer. If possible, wear an outfit that fits with the *Sunshine Math* logo; students will quickly begin to identify you as an important person in their school.

Participating students have from Monday until Friday to work the problems entirely on their own -- the only help they can receive during that time is for someone to read the problems to them. On Friday, the teacher hosts a problem-solving session in the classroom, having students describe their approaches to the more difficult problems. Students who have already worked the problems discussed, prior to the problem-solving session, can earn double stars -- you can identify these by looking for the teacher's initials beside certain problems. The students will have the weekend to complete any problems they want to -- for successfully completing these problems, they earn the indicated number of stars.

Be creative when designing a star chart. The basic method of posting stars individually is a good way to begin, but eventually you will want a color-coded system, or perhaps posting only one star each week, with a number in its center. Personalize the chart and the entire *Sunshine Math* center with pictures of students, "smiling faces," and so on. Occasionally bring in a reward for each child -- perhaps a cookie or a hand stamp in the shape of a star -- just for turning in their worksheet. Be creative and enjoy your role -- you are helping enthusiastic students develop higher-level thinking skills!

Checklist for assisting adults:

❑ Plan with the principal the following:

    ✔ A prominent place and format for the STAR CHART.

    ✔ The time and place for you to take up and check papers, and distribute new worksheets.

    ✔ The system for duplicating worksheets each week, ensuring legible copies.

    ✔ Any extra incentives ("world records," stickers, coupons, pencils, tee shirts, etc.) that will be part of the system for rewarding levels of achievement in *Sunshine Math.*

❑ Make the *Sunshine Math* center a happy place. Use bright colors, smiles, and cheerful words. Show confidence, friendliness, and encouragement to students.

❑ Collect the letters which are sent home prior to the first worksheet and signed by each student and parent . If in the future you have evidence that the work turned in does not represent the thinking of the student, discuss the situation with the classroom teacher. These situations are best handled individually in a firm, consistent manner.

❑ Check the worksheets from the previous week consistently. If you give partial credit for a problem with several parts, do so in a fair way that can be explained to students. Do not award partial credit for problems with only one answer.

❑ Have answer sheets available and encourage students to look at the answers when they hand in their worksheets. Allow them to explain their thinking if they arrived at a different answer. Award them full credit if they show a unique interpretation of the problem, and logical reasoning in obtaining an answer.

❑ Leave extra worksheets with the classroom teacher for participating students who were absent on Monday. Accept a late-arriving worksheet only if the student was absent on Monday. If a students' name is missing, or on the wrong place on a worksheet, check the paper but award the stars to "no name" on the STAR CHART. Adhering strictly to these rules will rapidly teach responsibility to the students, and keep your work load manageable.

❑ Keep all returned worksheets. As the same worksheets are used year-after-year, and many participating students have siblings who will later be in *Sunshine Math*, it is important that the students not be allowed to keep their worksheets.

❑ On weeks when *Sunshine Math* will not be available, post a sign such as "No star problems this week, but please come back after the vacation for more!"

Sunshine Math: Information for Teachers

Sunshine Math is a program designed to complement your regular classroom mathematics curriculum. It offers a peripheral opportunity for students to practice mathematics skills appropriate for their grade level and, at the same time, to participate in problem-solving experiences. It offers a challenge to those students who are self-directed learners by giving them something worthwhile to do outside of class.

Your involvement is strictly as a teacher. *Sunshine Math* will remain special to students if it's managed by someone outside the classroom, and if the teacher is viewed as a facilitator in the system, rather than as the authority figure. Your primary role is to monitor the system in your own classroom and host a brief problem-solving session for *Sunshine Math* students on Friday of each week. You will also need to release the participating students from your class at a set time on Monday to turn in their worksheet and obtain a new one. You might make yourself a special pin like that shown to the right, to wear on Monday and Friday to remind students that those days are special.
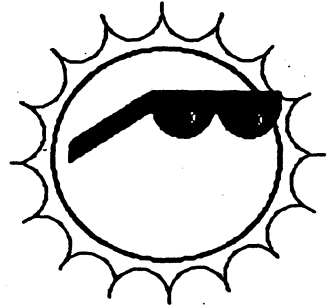
Each student worksheet has an accompanying commentary page. This sheet provides hints on parallel problems which you might use in the Friday problem-solving session. It is important that students participate actively in this session, and that you solicit from them their unique approaches to the problem discussed. Only after students present their ideas should you provide guidance on the problems, and then only when necessary. Even though there is a comment provided for each problem, you will have to decide which 3 or 4 problems you will cover during this brief session. Concentrate on those whose solution requires a strategy. The problem-solving session should last no more than 15 minutes.

Do not be disappointed if a large number of your students begin *Sunshine Math*, but many drop out after a few weeks. This is normal; problem solving requires a great deal of effort, and only certain students are ready for this challenge. On the other hand, you will also note that certain students *do* chose to stay in *Sunshine Math* week after week, even though they aren't as successful as other students at earning stars. Their participation should be encouraged, as they are certainly learning from the experience. Under no circumstances should *Sunshine Math* be reserved for only the advanced students in your class.

As a purely practical consideration, students are not allowed to discuss the problems with other students or their parents prior to the Friday "cooperative group" problem-solving session. This allows the "think time" necessary for students to develop into independent thinkers; it also prevents students from earning stars for work that is basically someone else's, which is the surest way to disrupt the entire *Sunshine Math* program. As the teacher, you must monitor this in your classroom and ensure that students abide by the established rule.

It is important that you understand and support the overall philosophy of *Sunshine Math*. Do not worry if students encounter problems for which they have not been prepared in class -- such is the nature of true problem solving. Do not provide remedial instruction to ensure that students master certain types of problems -- they will meet these same problem types repeatedly in the program, and likely will learn them on their own and from listening to other students at the problem-solving session. You should enjoy what the students *can* do, and not worry about what they can't do. You should also read over the general information about the program, to see how your role fits into the entire system.

Here are some hints that you might find useful in your support role for Sunshine Math:

✔ Allow your students to leave the classroom at the designated time on Monday to turn in their worksheets and pick up a new one.

✔ Read each week's worksheet yourself, and feel free to structure classroom activities that parallel those on the *Sunshine Math* worksheet.

✔ During the school week, students should be allowed to work on their *Sunshine Math* problems during their spare time, but the only help they can receive is for someone to read the problems to them. Give the students one warning if you observe them discussing the worksheets, and take away their papers for the next violation. If it happens another time, dismiss them from *Sunshine Math* for a month.

✔ At the problem-solving session on Friday, remember these points:

→ Students come to this session with their worksheets, but without pencils.

→ The session must be brief -- 15 minutes at most. Discuss only the 3 or 4 most difficult problems on the worksheet.

→ Help students summarize their own approaches to the problems, in a non-judgmental fashion. Offer your own approach last, and only when it's different from the student strategies. Do not allow answers to be given to the problems.

→ End the session by encouraging students to complete the problems over the weekend. Put your initials beside any problem discussed in class which a student has already completed successfully. The assisting adult will award double stars for these.

✔ Remember that part of the *Sunshine Math* philosophy is that students learn responsibility by following the rules of the system, if participation is important to them. *Sunshine Math* becomes very important to certain students, so they will adhere to rules about where their names goes on each paper, no credit if they forget their paper on Monday, no talking about the problems prior to the problem-solving session, etc., if *you* enforce the rules.

✔ Enjoy *Sunshine Math*. Students will impress you with their ability to think, and their creative ways to solve problems that appear to be above their level.

Here's a song for your students -- to the tune of "When you wish upon a star":

> # When you get your SUPERSTARS .....
> ## It won't matter who you are ....
> ## Try a few ....
> ## See what you can do ....
> ## .... and ....
> ## Success will come to you!!!

Sandy Parker, Lake Weir Middle School, Ocala, FL

★ ★ ★ ★ ★ ★ ★ ★ ★ ★ ★ ★ ★

WELCOME TO *SUNSHINE MATH !* We are happy that you want to try some new and different kinds of math problems! As you read the *SUNSHINE* problems, you may find yourself *?PUZZLED?*. Your teacher will be helping you each week with some of the hardest problems. Also, your parents may read the problems to you and offer hints for solving them.

If you would like to begin earning ★STARS★ for solving math problems, sign your name below.

★ ★ ★ ★ ★ ★ ★ ★ ★ ★ ★ ★ ★

(Your name)_____ I am

ready to begin the *SUNSHINE MATH* Program. I

promise to do my own thinking on each problem.

★ ★ ★ ★ ★ ★ ★ ★ ★ ★ ★ ★ ★

Dear Parents,

We welcome your child and you to *SUNSHINE MATH*, a program designed to enhance your child's journey through mathematics. By expressing an interest in more challenging problem solving, your child has taken the first step toward becoming an independent learner who is able to address many types of problems.

Your child will receive a worksheet each Monday which will be discussed on Friday and collected the following Monday. Each problem is ranked according to its level of difficulty. The more stars you see beside a problem, the higher the level of difficulty, and the more stars your child can earn for solving it.

Each Friday, your child will attend a "help session" to discuss the most challenging problems of the week. Any problem solved prior to the help session will be given double stars, or double credit. After the session, your child may rework problems before the sheets are collected on Monday.

Your role in *SUNSHINE MATH* is to encourage and facilitate problem solving. During the week, allow time for your child to think about each problem. You may need to read the problem to your child, explaining any new words encountered. Feel free to suggest a strategy for solving the problem, offer "counters" or manipulatives, or listen as your child shares her or his thinking, but please **DO NOT GIVE THE ANSWERS**. In order for this program to be effective, the thinking must be done by the students.

It is normal for a child NOT to be able to complete every problem on a worksheet. The process of reading, understanding and approaching the problems is a valuable step in solving many types of problems. Remind your child that she or he is not expected to know the answers to every problem.

Thank you for allowing your child the chance to embark on this mathematical adventure. Your signature gives permission for your child to begin.

_____

(parent's signature)

WORKSHEETS

SUNSHINE MATH - 5
Saturn, I

Name: _____

(This shows my own thinking.)

★★★★ 1. A worm is at the bottom of a 10 foot hill. He crawls up the hill $4\frac{1}{2}$ feet a day. At night when he rest he slides down $2\frac{1}{2}$ feet. How long does it take the worm to crawl up the hill? (Hint: Draw a picture.)

Answer: _____ days

★★★ 2. Jennifer was shopping, and using a calculator to find the price of a can of soda. She got the number shown on the display, but didn't know exactly how much money that was. How much money would the can of soda cost? Circle the best answer below.

(a) $6

(b) $.06

(c) $0.60

(d) 60¢

(e) 0.60¢

(f) both (c) and (d) above
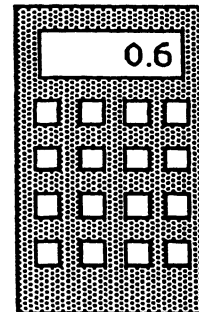
★ 3. If the 9th day of a month is on Tuesday, on what day is the 25th?

Answer: _____

★★★ 4. Put one digit from {1, 0, 3, 7} in each box to get the correct long division problem.

$$4 \quad 3$$

15

★ 5. Use this calculator in geometry. Circle two sides you could use to draw a set of *parallel* lines.
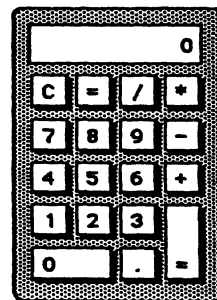
★★ 6. Use a ruler and measure the pencil below to the nearest millimeter.

Answer: _____mm

★★★★ 7. Mrs. Jones had some white paint and some green paint, and a bunch of wooden cubes. Her class decided to paint the cubes by making each face either solid white or green. Juan painted his cube with all 6 faces white--Julie painted her cube solid green. Hector painted 4 faces white and 2 faces green. How many cubes could be painted in the fashion, so that each cube is different from the others? Two cubes are alike if one can be turned so that it exactly matches, color for color on each side, the other cube.

Answer: _____ cubes can be painted so they are different

★ 8. Letia bought a milk shake at the ice cream shop, and gave the clerk a $10 bill. She got $9.61 in change. Is this reasonable? Why or why not?

Answer: _____

★★★ 9. The sum of my two digits is 13. I am not divisible by 2. List all possible numbers I could be.

Answer: _____

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Name: _____

(This shows my own thinking.)

★★★ 1. Use each of these digits one time in the number sentence below: 2, 4, 6, and 8. Fill in the blanks to produce the answer "14." Remember that you compute inside parentheses first.

$$(\underline{} \div \underline{}) + (\underline{} \times \underline{}) = 14$$

★★ 2. How many squares can be found in the figure to the right?

Answer: _____ squares
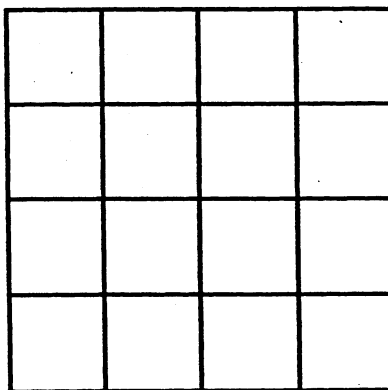
★ 3. Tamisha did a problem two different ways on her calculator. She got two different answers. Which of the two answers below represents the largest number? Circle it.

0.4		0.39
C = / *		C = / *
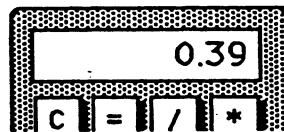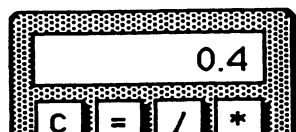
★★ 4. The girl scouts were going on a field trip to the zoo. There are 25 people going. They rented vans and each van has only 7 seat belts. How many vans do they need?

Answer: _____ vans

★ 5. Write the standard numeral: 9000 + 700 + 8 + 0.6 = _____

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★★★★ 6. What do you know about metrics? Circle the answers below that would make sense.

    a. The weight of a pineapple: 1 kg   1 g   1 mg

    b. The capacity of a can of soda: 35 mL   3.5 mL   350 mL

    c. The temperature on a summer day: 30° C   3° C   -3° C

    d. The distance from New York to Miami: 2200 cm 2200 km 2200 mm

★★★ 7. A class of 25 students has 10 boys. Three boys have braces and 4 girls have braces.

    a. What is the ratio of boys with braces to boys in class? _____

    b. What is the ratio of girls with braces to girls in class? _____

    c. Which of the two above ratios is larger? _____

★★★★ 8. The price and the sales tax are given. Compute the total cost. Tell how much change you would receive from $5.00.

                               Answer: _____ Total Cost

                               Answer: _____Change

Beach Ball

$2.59

6% sales tax
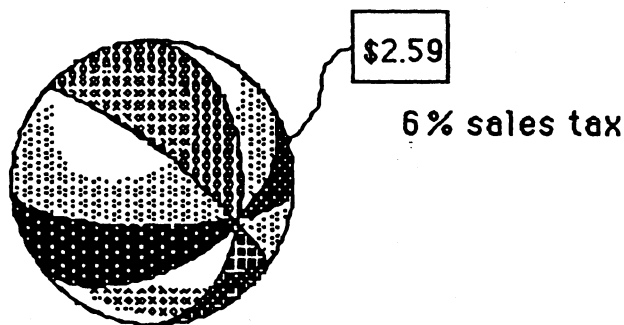
SUNSHINE MATH - 5
Saturn, III

Name: _____

(This shows my own thinking.)

★★ 1. Toni works in the school store. She sold 36 notebooks and 42 book covers. The notebooks cost $2.38 each, and the book covers cost $1.75 each. What is the total cost of Toni's sales?

Answer: _____

★ 2. A lot of students like to ride horses. Use the chart below to compare the primary grade riders (grades 1-3) with the intermediate grade riders. What is the difference in the number of riders between these two groups?

Horseback Riders

1st Grade	Ω Ω Ω Ω
2nd Grade	Ω Ω Ω Ω Ω
3rd Grade	Ω Ω
4th Grade	Ω
5th Grade	Ω Ω Ω Ω Ω Ω Ω Ω

Answer: _____

Key: Each Ω = 3 students

★★ 3. You have $100. You spend $\frac{1}{4}$ of your money to buy a new pair of jeans. You want to save $\frac{1}{5}$ of what you have left. How much will you save?

Answer: _____

★★★ 4. Use these digits only once: 1, 2, 4, and 8. Write a number sentence and use any of the operations (+, −, x, ÷) as many times as you like. You must get 0 as an answer. Use parentheses if you like.

Answer: My number sentence is: _____

19

★★ 5. Draw all the *lines of symmetry* of the figures below.
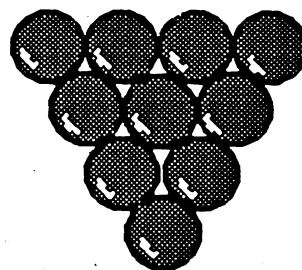
★ 6. Below is a *line of symmetry*. Draw a figure around it for which the line is a *line of symmetry*.
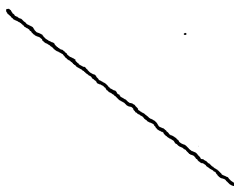
★★★ 7. Students arrived for school in groups. Bill was the first to arrive—consider him the "first group". Each group that arrived after Bill had two more people than the group that arrived before it. How many people were in school after 20 groups arrived?

Answer: _____

★ 8. How much does the can of paint weigh, by itself?   Answer: ____
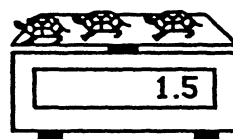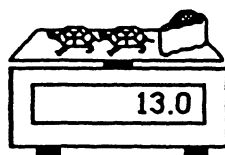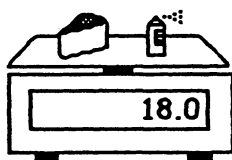
SUNSHINE MATH - 5
Saturn, IV

Name: _____

(This shows my own thinking.)

★★ 1. One, three, and six are triangular numbers. List all the other triangular numbers up to 36.

Answer: _____

★ 2. Jennifer earns $5.25 an hour. Starting Monday she will get a raise to $5.85 an hour. She works 40 hours each week. How much more will she make next week than she made last week?

Answer: _____

★★ 3. A diagonal joins two vertices of a polygon. Draw all the diagonals in the polygon to the right.
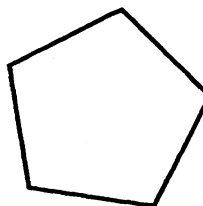
★★ 4. Marti plans to save 25% of the money she makes over the summer washing cars.

a. Shade in about 25% of the figure to the right to show how much she will save from every dollar she earns.
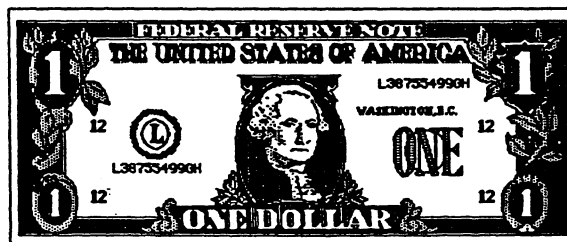
b. How much will Marti save for each car she washes for $5?

Answer: _____

★★ 5. The Phillips family wants to fence their backyard. They know the yard has a perimeter of 24 meters, and an area of 32 square meters. What is the yard's length and width?

Answers: The length is _____meters, and the width is _____ meters.

6. *Y* stands for the weight of 1 can of tuna fish on the scale. Find *Y*.

Answer: $Y =$ _____
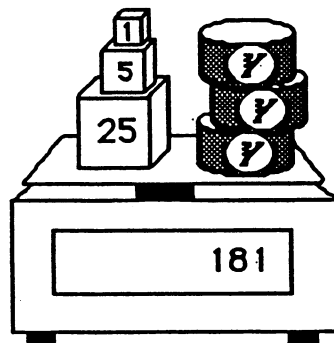
7. Write the problems and answers below each calculator:

_____ = ____   _____ = ____   _____ = ____
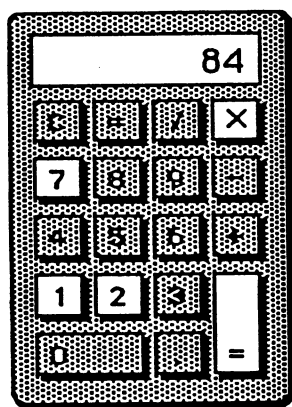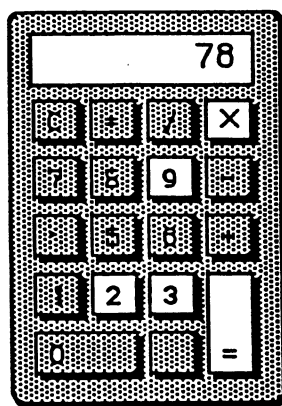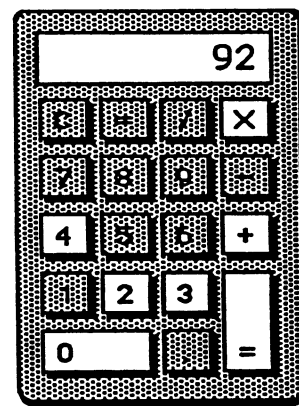
8. Look at the pattern below. How many squares would be in the 10th shape in the pattern?

Answer: _____ squares

22
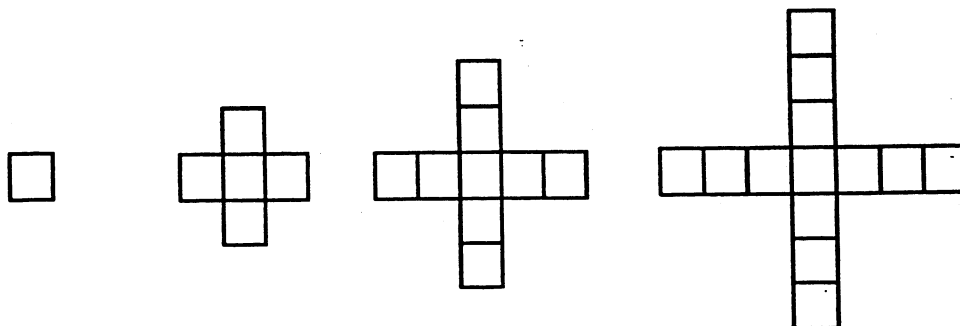
SUNSHINE MATH - 5
Saturn, V

(This shows my own thinking.)

★★ 1. Big Al has a set of non-metric wrenches that have these numbers on the end:

$$\frac{7}{16} \quad \frac{1}{4} \quad \frac{9}{16} \quad \frac{3}{8} \quad \frac{5}{16} \quad \frac{1}{2}$$

Which of his wrenches fits the largest nut?   Which fits the smallest nut?

Answer:s _____ fits the largest   _____ fits the smallest

★★★ 2. Jennifer bought a blender for her mother. The blender was on sale for $\frac{1}{3}$ off the marked price.
The regular price of the blender was $18.00. How much will she pay for the blender, including sales tax of 6% ?

Answer: _____

★ 3. Melissa and Sarah arranged the music hall for a concert. They made 42 rows with 35 chairs in each row, and 12 rows with 25 chairs per row. How many chairs did they use in all?

Answer: _____ chairs

★★ 4. The "square corners" on a sheet of writing paper are 90 degree angles. You can use these corners to estimate the measure of other angles.

About what is the angle of the piece of pizza being removed in the picture?

Answer: ____ degrees
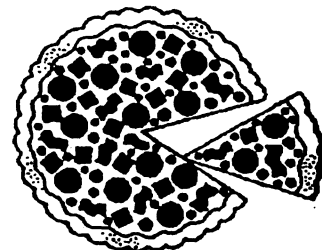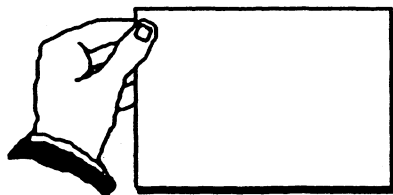
★★ 5. In the month of April, 9.45 inches of rain fell in Tallahassee. During the month of May, 9.6 inches of rainfall fell. Which month had the most rainfall, and what was the total for the two months?

Answer: _____ had the most; the total was _____ inches

★ 6. Complete the addition. Convert your answer to largest units. (i.e., change inches into feet and feet into yards, if possible)

$$2 \text{ yd.} \quad 2 \text{ ft.} \quad 3 \text{ in.}$$
$$+ 1 \text{ yd.} \quad 2 \text{ ft.} \quad 11 \text{ in.}$$

★★★ 7. Eli's Dad made him a birthday cake, but forgot to buy candles. He could only find a few. But Eli was smart in math, so his Dad said "The ratio of candles to years is 3 to 5." That gave him the right number.

How old was Eli? _____

★★★ 8. Kenya, Matt, Tia, and Justin live on the same street. Their houses are gray, green, blue, and white, but not necessarily in that order. Justin lives next door to the grey house. Matt and Justin live across the street from the green house. Tia's house is blue. Circle the one who lives in the white house.

a. Kenya   b. Matt   c. Tia   d. Justin

★★★ 9. Answer the questions after studying this pattern. Notice when the pattern starts repeating.
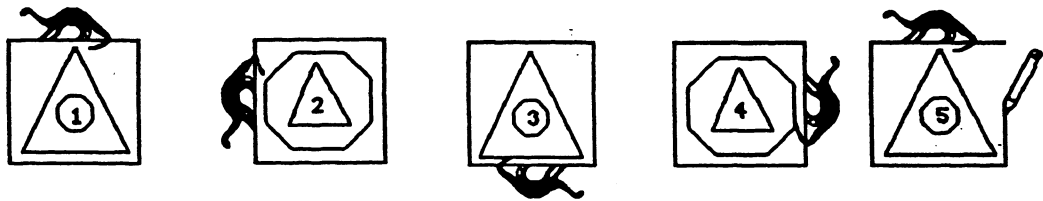
a. Circle the figure above that would be the same as figure 15 in the pattern.

b. List the numbers of 5 figures not shown that would be just like number 1: _____

c. What is the number of the figure above that is just like the 100th figure in line? _____

Name: _____

(This shows my own thinking.)

★★ 1. The Adams family uses a spinner each night to see who does the dishes. Carla is assigned number 4.

    a. What is Carla's chance of having to do the dishes on any given night? _____

    b. What is Carla's chance that she won't have to do the dishes on any given night? _____
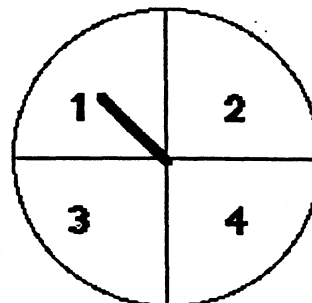
★★★★ 2. Bonita has 6 coins. All of them are pennies or dimes. What are the possible amounts of money she might have?

    Answer: She might have ___¢, ___¢, ___¢, ___¢, ___¢, ___¢, or ___¢

★★ 3. Compute this answer. $8 \times (7.5 + 2\frac{1}{2})$

                                                     Answer: _____

★★ 4. Solve this problem if you have enough information. If there is not enough information tell what you need to know in the space below.

> Kimberly orders a sweatshirt. The shirt costs $25.99 plus the cost for mailing. Kimberly paid with a $100 bill. How much change did she get back?

                  Answer: _____

★ 5. Use a ruler to draw a segment 52mm long, in the space below.

★★★ 6. Use the following graph to answer these questions.

    a. What is the total number of animals on the Williams' farm? _____

    b. What is the difference in the number of cattle and the number of pigs? _____

    c. How many more pigs do they need to equal the total number of cattle and sheep? _____

The William's Farm
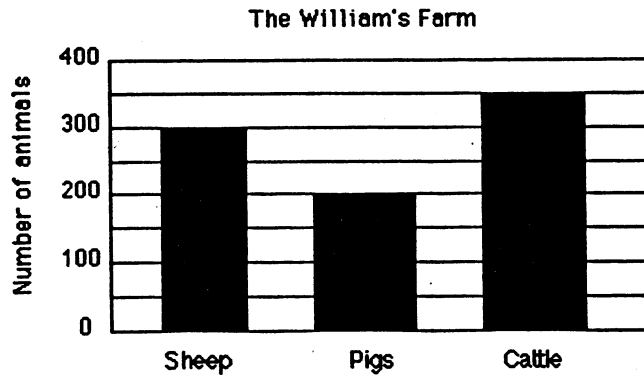
★★★ 7. Maria's bike odometer read 63 miles. She rode her bike to school and back 4 days last week. On Saturday she rode to the park and back, a total distance of 3 miles. At the end of those five trips, her odometer showed 74 miles. Find the distance d from her house to school and back. You can find d by using your number sense and the diagram below.
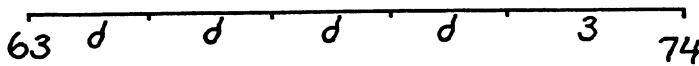
Answer: $d =$ _____ miles

★★ 8. Maria made a graph of the distance she travelled last week on her bike between school and home. Which day of the week did she not ride her bike to school?

    Answer: _____
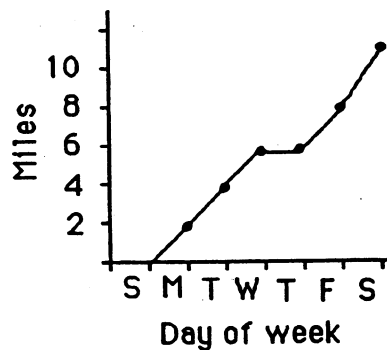
★★ 9. There are 34 classes in a school and each class could have between 23 and 30 children.

    a) What is the school's highest possible student population? _____

    b) What is the school's lowest possible student population? _____

Name: _____

(This shows my own thinking.)

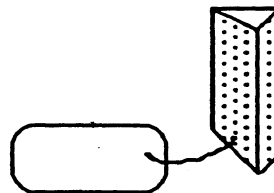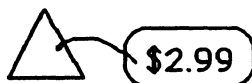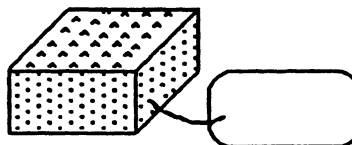★★ 1. What is the sum of these mixed numbers? $5\frac{2}{3}$, $3\frac{3}{4}$, $13\frac{1}{6}$, $8\frac{1}{2}$
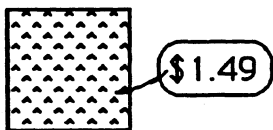
Answer: _____

★★★ 2. Artesia found a sale on skates. She got $\frac{1}{5}$ off the regular price of $34.50. What was the sale price of her skates?

Sale on skates!

Answer: $_____

★★★ 3. John needed two more shapes to complete his project. How much will each shape cost? Compute the cost of each shape using the key -- write the cost on each tag.

$1.49

$2.99

$1.59

★★★★ 4. Put >, <, or = between each pair of numbers.

a. 34.63 _____ $34\frac{1}{2}$

b. $3\frac{2}{5}$ _____ $1\frac{12}{5}$

c. 12.443 _____ 1.2443

d. 0.09 _____ 0.9

★★ 5. Mike and Sam are running a 26 mile marathon. They started out at 8:15 a.m.. They both crossed the finish line at 1:26 p.m.. How long did it take them to finish the race?

Answer: _____ hours and _____ minutes

★★★ 6. a. How many $1 bills are in $1,000,000? _____

b. How many $100 bills are in $1,000,000? _____

c. How many $1,000 bills are in $1,000,000? _____

★★★★ 7. Find the numbers that each letter stands for in the problem below.

$$\begin{array}{r} EFGH \\ \times\ \ \ \ 4 \\ \hline HGFE \end{array}$$

E = _____

F = _____

G = _____

H = _____

★ 8. Jim was putting carpet in his son's tree house. He needed to find the area of the floor. But he was having trouble with the multiplication. The measurements were 4.2 meters by 6.3 meters. Do the multiplication to help him find the area.

Answer: _____meters^2

★★ 9. Rewrite this riddle so it's easily understood.

The middle 3/5 of SHOWS.   The middle 1/5 of TRAPS.
The first 1/3 of DOODLE.   The first 6/6 of TURKEY.
The first 3/5 of YOURS.   The middle 1/2 of PINS.
The first 1/2 of KEEPSAKE.   The first 8/11 of SUSPENSEFUL.

Answer: The riddle is: _____

A good answer to the riddle might be: _____

SUNSHINE MATH - 5
Saturn, VIII

★★★   1.   Write true, sometimes, or false.

     a.   Perpendicular lines intersect. _____

     b.   Two sides of a triangle are parallel. _____

     c.   Two lines that are parallel to the same line are parallel to each other. _____
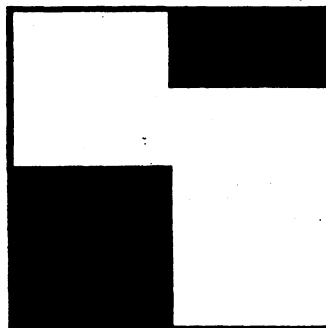
★★   2.   Solve:

$$9 \div (1 + 2) + 9 \div 3 = \; ?$$

                              Answer: _____

★   3.   Lisa and Sandy were comparing sticks. Lisa's stick was $\frac{2}{3}$ of a yard long. Sandy's stick was $1\frac{10}{12}$ of a foot long. Who's stick was the longest, and by how much?

                Answer: _____ was longer, by _____.

★★★★   4.   What fraction of the large square is shaded?

         Answer: ____ is shaded

★★   5.   Adrienne left home at 8 a.m.. She arrived in Los Angeles at 1:28 p.m.. Her friend Erica left home at 10 a.m.. She arrived in Los Angeles at 2:45 p.m.. Assume they are in the same time zone the whole trip and both trips take place during the same day. Altogether, how many hours did Adrienne and Erica spend traveling?

                Answer: _____ hours, _____ minutes

★★ 6. Mike had eighteen jellybeans in a bag. 12 of them were green, 1 was blue, 1 was black, 1 was white, 1 was pink, and 2 were orange. If he stuck his hand into the bag without looking, what is the probability of his pulling out an orange jellybean? Write your answer as a fraction.
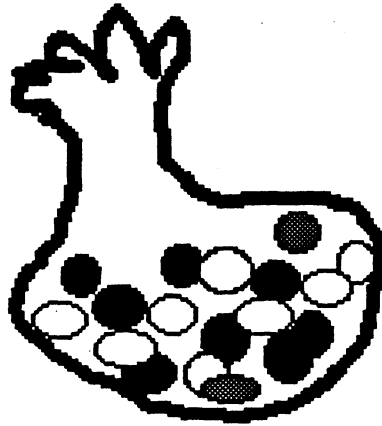
Answer: _____

★★★★ 7. Write a number sentence. Use every digit in the circle only once. Insert math symbols (+, −, x, ÷) and end with the number three. Use parentheses if necessary.
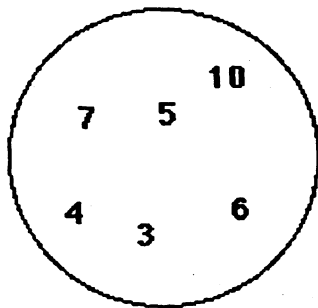
Answer: _____ = 3

★★ 8. Joe and Christine each bought a six pack of colas. Joe gave $\frac{2}{3}$ of his away to friends, and Christine gave away $\frac{1}{2}$ as many as Joe. How many more colas did Christine have, than Joe?

Answer: She had ____ more.

★ 9. Lo Ann's softball team had 16 players. One day it started raining at practice, and all but 5 players squeezed into the refreshment stand, out of the rain. How many were left to get wet?

Answer: _____ were left outside and got wet.
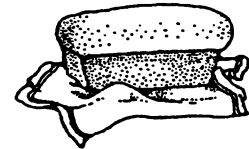
Name: _____

(This shows my own thinking.)

★★ 1. Sandra has eight coins which total $0.87. What coins does she have? (Hint: make a chart or a list.)

Answer : _____

★★ 2. Practice doing some problems like this. You will be given one when you turn in your paper, and you can only write the answer down. You'll have to use mental math.

Answer later: _____

Lonny has $15 to buy some groceries for his mom. Milk costs $2.39, bread costs $1.29, eggs cost $0.79, and mayonnaise costs $2.49. If he buys one of each item, can he expect to get $10 in change? _____ (yes or no)

★★ 3. Jack wants to buy an equal number of green, blue and white ornaments for his holiday tree. Green ornaments come in packages of 3; blue ornaments come in packages of 6; the white ones come in packages of 4. What is the least number of packages of each color he must he buy?
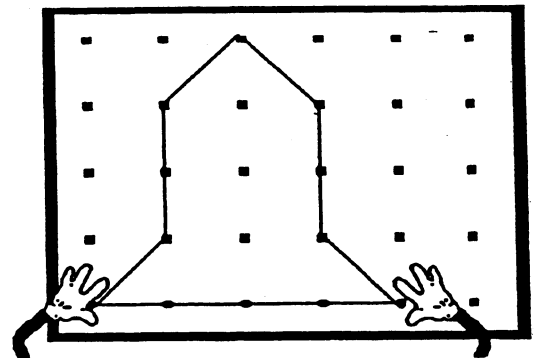
Answers: ____ packages of green
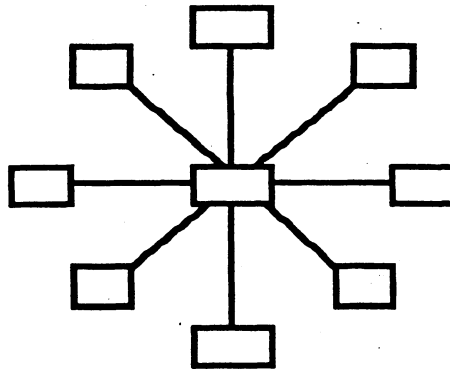
____ packages of blue

____ packages of white

★★ 4. Mickey made a space ship on his geoboard.

a. Draw any lines of symmetry on the space ship.

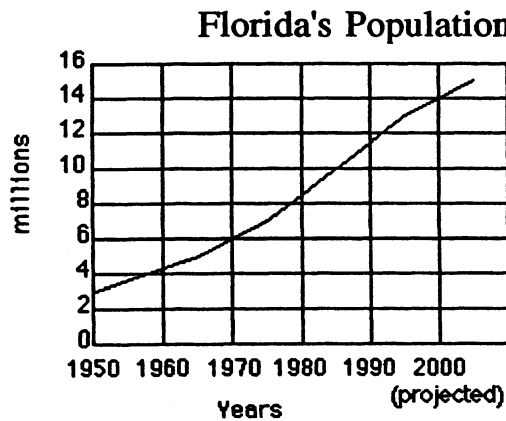b. Find the area of the space ship by counting whole and partial square units.

Answer: The area is _____ square units

31

★★★ 5. Use each digit from 1 to 9 to make each line sum to 15. Use each digit only once.

★★★ 6. Use the graph to answer the questions about Florida's growing population.

Florida's Population

a. What is the increase in population from 1950 to 2000?_____

b. What was the approximate population in 1980? _____

c. At the current rate of increase, what would the population be in 2010? _____

★★★ 7. Think about these spinners to answer the questions below.

a. Put a ✓ on the spinner that gives the white team the best chance to win.

b. What is the white team's chance of winning on the spinner with ✓? _____

c. What is the chance the white team would not win, on the spinner with ✓? _____
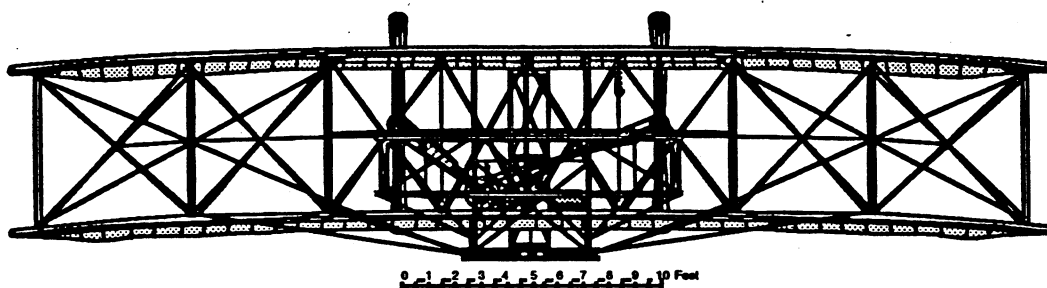

32
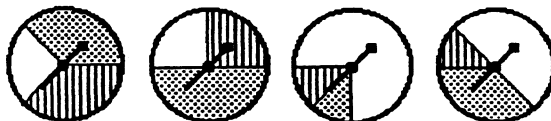
SUNSHINE MATH - 5
Saturn, X

★★ 1. The Wright Brothers each had two flights on that famous day at Kitty Hawk. Orville flew 120 ft. and 585 ft. Wilbur flew 340 ft. and 852 ft. What was the average distance flown that day? At that rate, how many flights would it have taken them to fly a mile? (rounded to the nearest whole number)

Average distance: _____

Flights to travel a mile: _____

★ 2. Use the scale underneath the plane above to find its wingspan, tip to tip. Answer: _____ ft.

★★ 3. The regular season for professional baseball is 162 games. A player was at bat 3 times in each game, and he played in $\frac{2}{3}$ of the games.

a. How many times was the player at bat during the season?   Answer : _____

b. The player hit 0.250, which means he got a hit 25% of the time, or once in every four at bats. How many hits did he get during the year?

Answer: _____

★★ 4. John needs to build a fence around his yard, which is 96 ft. wide and 120 ft. deep.

a. How much fence must he buy to enclose all four sides? Answer : _____

b. If the fence costs $12.87 for an 8 ft. length, how much will the entire fence cost before the tax is added?

Answer:_____

★ 5. A bag has 6 marbles in it. Each marble is either red, blue, or green. What is the least number of marbles that you must pull out of the bag to be sure you have two marbles the same color?

Answer:_____

★ 6. You will be given a problem like the one below when you turn in your paper. To earn your star, you'll have to estimate the answer in your head. Make up and practice some problems like this one.

Answer later: _____

> The store where Janice and Kanisha shop is having a sale on summer clothes. Each of the girls wants to buy 2 pairs of shorts and three tops. If shorts and tops are on sale for $11.50 each, what is the best estimate of how much each girl will spend? Circle your answer.
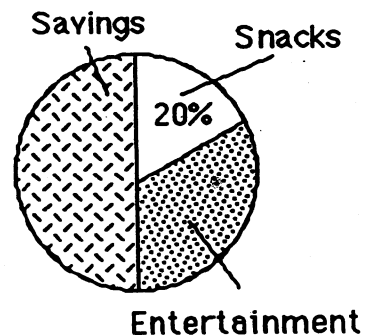>
> a. $40   b. $50   c. $60   d. $120

★★ 7. What whole number does N stand for if the number sentence below is true?

$(N + 5) + (3 \times 2) = 18$

Answer : _____

★★★ 8. Danny earns $5 a week. Use the graph to answer the questions below.

a. How much money does Danny spend on snacks? _____

b. How much money does Danny save? _____

c. How much money does Danny spend on entertainment? _____

Savings   Snacks
20%
Entertainment

★★★ 9. Franklin School has 3 boys for every 4 girls in the fifth grade. There are 140 students in the fifth grade.

a. How many are boys? _____   b. How many are girls? _____

SUNSHINE MATH - 5
Saturn, XI

Name: _____

(This shows my own thinking.)

★★ 1. Jacqueline, Kanisha, Howard, and Billy have jobs in their group. The jobs are Recorder, Materials Manager, Time Keeper, and Reporter. Kanisha sits across from the Recorder and next to the Materials Manager. Billy hurt his hand and cannot record the work done. Jacqueline is best friends with the Reporter, and lives down the street from the Recorder. Billy rides the bus with both the Materials Manager and the Reporter. What is the task of each student?

_____ Recorder   _____ Materials Manager

_____ Time Keeper   _____ Reporter

★★ 2. A sheet of plywood measures 4 feet by 8 feet. Armand wants to build a dog house using one whole sheet of plywood for the floor.

   a. Armand needs to put a "2 by 4" under the outer edge all the way around the floor, and another "2 by 4" that runs down the middle lengthwise, to give support to the plywood. If "2 by 4's" are sold in 8-foot lengths, how many should he buy? ____

   b. If he carpets the floor also, how many square feet of carpet should he buy? _____

★★★ 3. Pine Elementary School Chorus needs tapes to record their musical for the members. Tapes cost $7.95 for a package of 2 tapes and $11.75 for a package of 3 tapes. If 23 members want copies of the tape, what is the least amount they will have to spend?

Answer: _____

★★★ 4. If each sphere has a mass of 120 gms, what is the mass of a pyramid? _____ gms
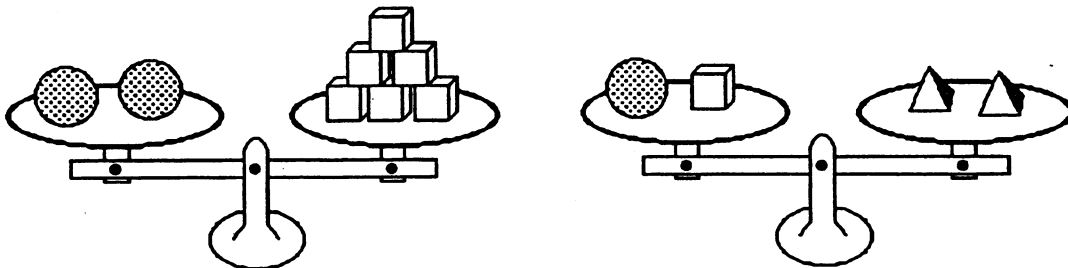
★★ 5. Sunny Ridge Elementary School was collecting cans for a food drive. The first two days of the drive, they collected 103 cans. They collected 5 cans more on the first day than on the second day. How many cans did they collect each day?

Answer : _____ 1st day   _____ 2nd day

★ 6. Josie found a pair of shoes she wanted priced at $55, but she did not want to pay that much. A few weeks later, the same shoes were marked down 20%. Including the 6% sales tax, how much will she pay if she buys the shoes on sale?

Answer: _____

20 % off

★★★★ 7. People who learn to multiply mentally usually do the opposite of what they do with paper-and-pencil. They start multiplying the "big numbers" first, and then add on the product of the smaller numbers. Watch James below:

To multiply 63 X 45, first multiply 60 X 40 to get 2400. Then add on 60 X 5 or 300, and you have 2700. Then add on 3 X 40 or 120, and you're up to 2820. Next add 3 X 5 or 15, and you have 2835. So 63 X 45 is 2835.

Practice multiplying this way with 2-digit by 2-digit multiplication problems that you make up. When you turn in your paper, you can earn 4 stars by doing a problem like this.

Answer later: _____

★★★ 8. Circle the best answer for the length of each line segment.
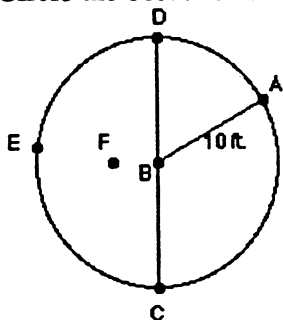
$\overline{FE}$ 12 ft.   10 ft.   8 ft.

$\overline{CD}$ 15 ft.   30 ft.   20 ft.

$\overline{BF}$ 5 ft.   4 ft.   1 ft.

36

★★★ 1. Bob's garden is a 20 ft. x 10 ft. rectangle. Bob plants tomatoes in half of his garden; then radishes in $\frac{1}{4}$ of the remainder; then cucumbers in $\frac{1}{2}$ of what is left. The last area is planted in peppers. What part of the garden is planted in peppers?

(Hint: draw a picture)

Answer : _____

★ 2. St. Augustine was founded in 1565 by Pedro Menendez de Aviles. The oldest house in that city still standing was built in 1703. How old is this house now?

Answer: _____

★★ 3. For your weekend at the beach, you have packed one pair each of red shorts, blue shorts, and tan shorts. You have also packed a white shirt, and a red shirt. How many outfits can you make with these clothes?

Answer: _____
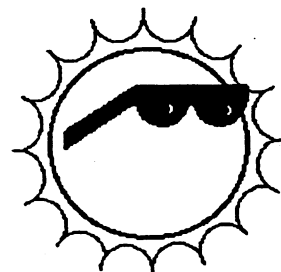
★★★ 4. A number n is divided by 3 and the result is multiplied by 7. Then 6 is subtracted from the result to give 36. What is the original number n ?

$$[(n \div 3) \times 7] - 6 \text{ gives } 36. \text{ What is } n ?$$

Answer : $n =$ _____

★★ 5. Which fraction is closest in value to 1? Circle the correct answer.

a. $\frac{3}{5}$ b. $\frac{2}{3}$ c. $\frac{1}{2}$ d. $\frac{7}{10}$

★★　6. There are 5,280 feet in a mile. If an airplane is flying at 35,000 feet above sea level, how high is it? Bubble in the correct choice.

    0   7 miles high
    0   a little less than 7 miles high
    0   a little more than 7 miles high

★★★　7. Juan entered a bike race in which he was to ride 45 miles, stopping at certain intervals during the race to check in with the scorers. He checked in 9 times before he crossed the finish line. If the intervals were equally spaced throughout the race, how far apart were they?
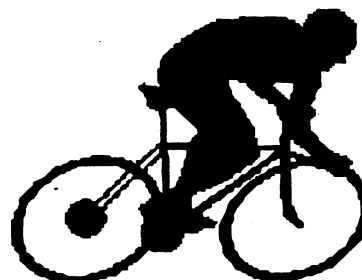
Answer: The intervals were spaced every _____ miles.

★★★★　8. The graph shows Juan's speed during the race, not counting when he stops at the checkpoints. Answer the questions below the graph.
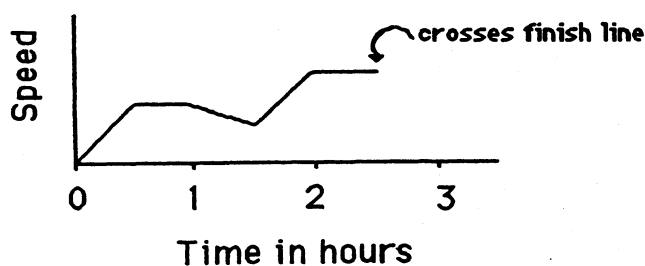
a. About how long did Juan take to finish the race?   Answer: _____

b. What can you say about Juan's speed during the first half hour of the race?

    Answer: _____

c. What can you say about Juan's speed during the second half hour of the race?

    Answer: _____

d. During what part of the race was Juan going the fastest?

    Answer: _____

38

SUNSHINE MATH - 5
Saturn, XIII

Name: _____

(This shows my own thinking.)

★   1. Mr. McMathy needs 129 seats for his 5th grade program. If the seats are arranged in rows of 10 seats, how many rows will he need?

Answer: _____ rows

★★★   2. In the United States, 154,000,000 tons of garbage are produced annually. On an average, about how many pounds is that each month for each person in the United States? The population of the United States is about 250 million.

Answer: _____ pounds

★★★★   3. The horizontal, vertical, and diagonal columns of a magic square all add to the same sum. Use the digits 1 - 9 one time each to make a magic square.
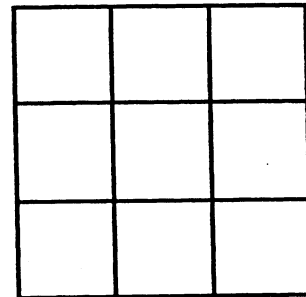
★★★   4. A *square number* is a number in which the dots can be arranged to form a square.

     1   4   9   16
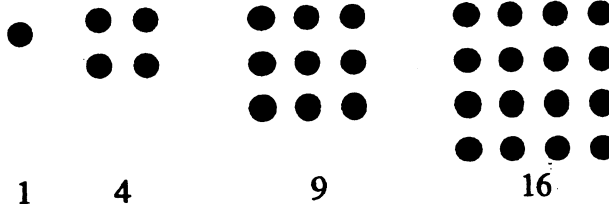
a. Find the next three square numbers. _____

b. Is 100 a *square number*? _____

c. Is 200 a *square number*? _____

★★   5. How many different rectangles exist which have whole numbers as the length and width, and also have an area of 36 sq. cm?

Answer: _____ rectangles

★★★ 6. You offer to do the dishes for your family for the next month. You suggest that they can pay you in one of three ways:

    a. $0.50 each day.

    b. $0.10 the first day, $0.20, $0.30 the 3rd day, and so on.

    c. $0.01 the first day, $0.02 the second day, $0.04 the third day, and so on, doubling every day.

If the month has 31 days, which rate of pay would be best for you? Circle your choice.

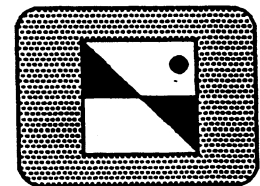★★ 7. You place these cards in a bag, and choose one without looking.
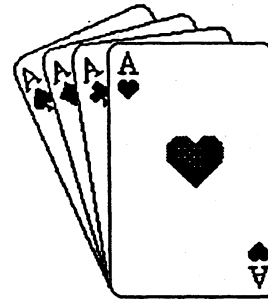
    a. What is the chance you will pull out a red card?
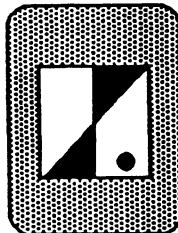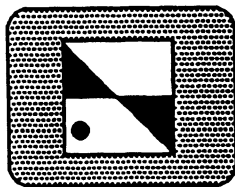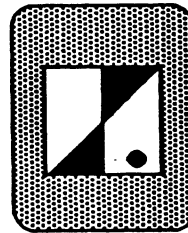
        Answer: ____

    b. What is the chance you will pull out a ♣?

        Answer: ____

★★ 8. Marcia drew the design to the right on a piece of clear plastic. She turned it 90° clockwise, then flipped it over horizontally and flipped it again vertically. Which is her card below? Circle it.
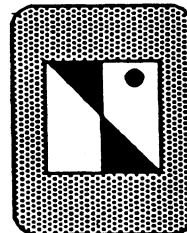
★ 9. Find the product: **5.7 x 17.3 x 651 x 387 x 0 x 82.1 = _____**

40

SUNSHINE MATH - 5
Saturn, XIV

Name: _____

(This shows my own thinking.)

★★★ 1. Complete each sentence by drawing a picture in the space beside it.

a. ☐ is to ■ as ◯ is to

b. ◯◯◯ is to ●● as ☐☐ is to

c. ☐ is to ☐ as ☐ is to

★ 2. Fill in the missing fractions. The same fraction is used in both spaces.

$$(\frac{4}{8} - \quad) + (\frac{5}{8} - \quad) = \frac{7}{8}$$

★ 3. Solve if there is enough information. If not, tell what is missing. Becky bought a pack of paper that cost $5.95. Tony bought a pack that cost $6.49. Who bought the most paper?

Answer: _____

★★★ 4. Maria works at the community relief center every summer. She is a really good worker. She earns $8.00 per hour for her regular 40-hours a week. Last week she worked 47 hours. How much did Maria earn if she gets "time and a half" for overtime?

Answer: _____

41

★★★ 5. Complete the chart below. Each of the three students earns $5.75 per hour.

Employee work schedule and amount earned

Employee	I n	Out	Hours	Amt. Earned
Bachie	8:00 A.M.	6:00 P.M.		
Dustin	12:30 P.M.	5:00 P.M.		
Monica	9:00 A.M.	5:30 P.M.		

★★★★ 6. This pattern of buildings is made with blocks. Building 1 is made from 1 block, Building 2 from 4 blocks, and so on.
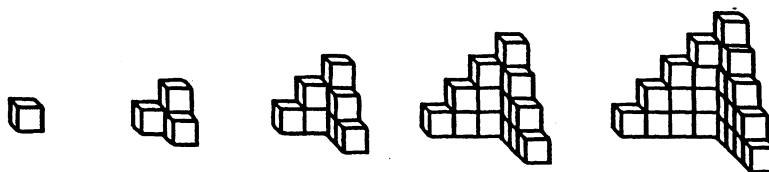
Bldg. 1   Bldg. 2   Bldg. 3   Bldg. 4   Bldg. 5   Bldg. 6 ....

a. How many blocks are needed for Building 3? ____

b. How many blocks are needed for Building 4? ____

c. How many blocks are needed for Building 10? ____

d. How many blocks for Building n, where n could stand for any number? ____

★ 7. Fold this sheet of paper so that you *bisect* the angle. *Bisect* means that you exactly cut it in half. With your pencil, darken-in the crease in the paper. The line you draw is the *bisector* of the angle.
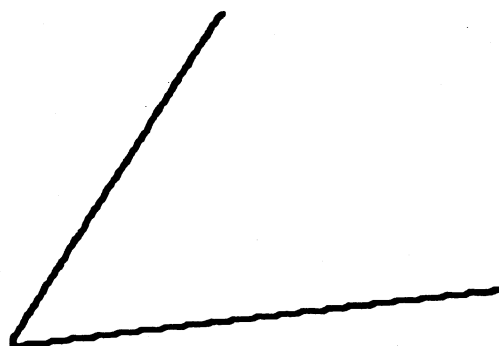
★★★ 8. Open a book and look at the two page numbers.

a. Is their sum an *even* number, or an *odd* number? _____

b. Is their product an *even* number, or an *odd* number? _____

c. If you opened the book to two different pages, would your answers to (a) and (b) be the same? _____

42

Name: _____

(This shows my own thinking.)

★★   1. Ms. Hill and Mr. Booth both had $500 to invest in
the stock market. Ms. Hill bought shares of
Sugarloaf at $10 per share while Mr. Booth bought
shares of Dandy's Butter at $20 per share. Ms.
Hill's shares went up in value $0.20 per share. Mr.
Booth's shares went up $0.50 per share. How
much did each earn on their shares?
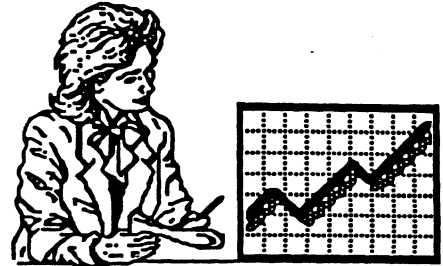
Answers: Ms. Hill $_____

            Mr. Booth $_____

★★★   2. Tiffany has $20 more that Ivan. Travis has $20. All three together have $41.

How much money does Tiffany have? _____ How much does Ivan have? _____

★   3. What number do you need to add to these numbers to get 1000? Try solving these in your
head. Then practice some more like these that you make up. Use your BRAIN POWER.
When you turn in your paper you will be asked to solve a problem like these in your head.

a. $300 + _____ = 1000$ b. $210 + _____ = 1000$

c. $450 + _____ = 1000$ d. $636 + _____ = 1000$

Answer for the problem given when you turn in your paper:_____

★★★★   4. You are having a pool party and invite 2 of
your best friends. These two friends each
invite 2 other people. These 2 people each
invite 2 people that have not been invited.
How many people will be invited if this
process continues for 4 rounds? (Hint:
Draw a diagram.)

Y'all come
my party

Answer: _____ people

★ 5. Which equation has the same solution as the first equation? Circle it.

$$n + 13 = 21$$

a. $t - 13 = 21$ b. $17 = 25 - p$ c. $9 + d = 16$

★★ 6. A box will hold 23 puzzles. How many boxes are needed to hold 238 puzzles?

Answer: _____ boxes

★ 7. A jacket Jason wants is priced at $18.99. The sales tax is 8%. What is the total cost of the jacket, including tax?

Answer: $_____

★ 8. Write the correct numbers in the boxes:

```
      4 □
  X 3 5
  ───────
    2 □ 5
  1 4 1 0
  ───────
  1 □ 4 □
```

★★★ 9. Connect the points with a heavy line as described below.

a. Connect (10, 1) to (10, 7)
b. Connect (2, 1) to (5, 1)
c. Connect (7, 4) to (10, 4)
d. Connect (7, 7) to (7, 1)
e. Connect (2, 7) to (5, 7)
f. Connect (3.5, 1) to (3.5, 7)
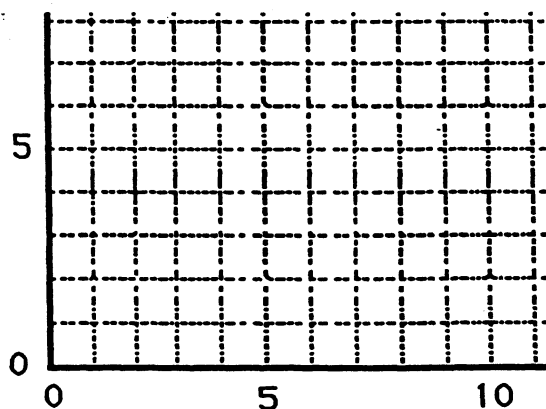
Name: _____

(This shows my own thinking.)

★★ 1. Find the missing measurement. The total perimeter of the polygon is 27 cm.

6 cm

?

4 cm

3.2 cm

5.3 cm

1.7 cm
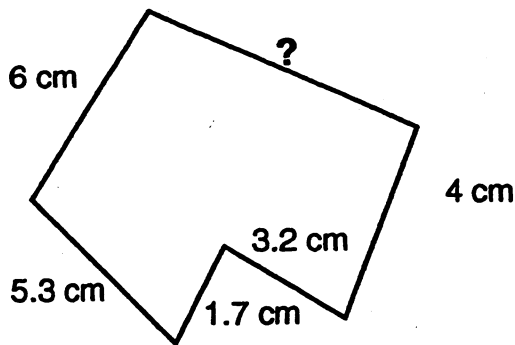
Answer:_____ cm

★★ 2. Fill the missing numbers in the division problem.

```
        □ □
  □ 3 √3 5 1
      □ □
      □ 1
      9 1
      ___
        0
```

★★★ 3. When you divide, you sometimes get a larger number than you started with. Show you understand this by placing the decimals in the answers below. The answers are correct, except for the decimal point not being there.

a. 1.25 ÷ 0.5 = 2 5 0   b. 0.84 ÷ 0.7 = 1 2 0   c. 13 ÷ 0.1 = 1 3 0 0

★★ 4. Report cards are coming out in three days. Your homework grades are 100, 90, 85, 78, 0, 80, and 92. The 0 occurred when you forgot to do your homework one night. What is the average of your homework grades?

Answer:_____

★★ 5. Using the grades from problem 4, what would your average be if you had done your homework that night, and made a 77 instead of a 0?

Answer:_____

★★★★ 6. Write an algebraic expression for each phrase below. Use the variable suggested.

    a. twice as old as Max's age a, less three years _____

    b. 10 times higher than the chair's height h, plus 3 inches_____

    c. $3 more than half of what Jason makes d _____

    d. five trips of x miles each, plus another 5.8 miles _____

★★ 7. Kalia skateboards 5 blocks west and 8 blocks north to get to her friend's house. Each block is $\frac{1}{8}$ mile in length.

    a. How far does she travel in a round trip? _____ miles

    b. Rounded to the nearest whole mile, how far is a round trip? _____ miles

★ 8. Bailey has physical education class $1\frac{1}{4}$ hours on Monday, Wednesday, and Friday. How many minutes does he get physically educated each week?

Answer: _____minutes

★★★ 9. Box A has 3 black marbles and 2 white marbles. Box B has 2 black marbles and 1 white marble.

If you have to close your eyes and pick a *black* marble to win a prize, which box gives you the best chance of winning? Bubble-in your answer.
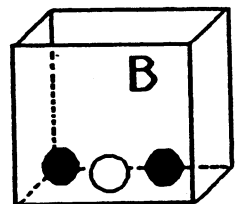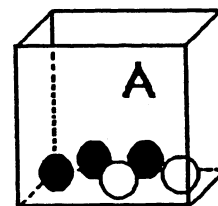
    0 Box A gives the best chance.

    0 Box B gives the best chance.

    0 The boxes give the same chance of winning.

SUNSHINE MATH - 5
Saturn, XVII

Name: _____

(This shows my own thinking.)

★★ 1. Learn to use mental math to do these problems with a 1-digit divisor. When you turn in your paper, you will have a chance to do one like these and write your answer below.

$2\overline{)10678}$ $3\overline{)2145}$ $5\overline{)2540}$ $6\overline{)12018}$ $4\overline{)2128}$ $7\overline{)4949}$

Answer later: _____

★★ 2. Marcus drives a delivery truck and spent $89 on gas his first week. If he drives for 8 months using about this much gas each week, how much would he spend on gas? Use estimation to find the answer to the nearest $1000.
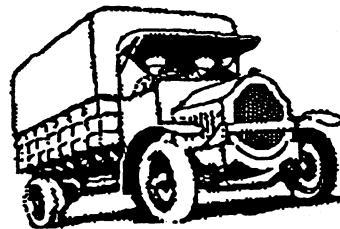
Answer: _____

★ 3. These numbers are examples of palindromic numbers.

232   11   505   325523

Find four other numbers that are palindromic.

Answer: _____, _____, _____, _____

★ 4. What do the numbers above have in common with this sentence?

A man, a plan, a canal, Panama!

Answer: _____

★★ 5. Someone your age has an average pulse rate of 70 beats per minute and is ten years old. This means that, for an average person your age, the heart has already beat about how many times? Round your answer to the nearest hundred million.

Answer: _____

47

★★★ 6. Marcus noticed that at 3:00 o'clock, the hour and minute hands on his watch made a *right angle*. He was curious about the angles formed inside the right angle, when the second hand was pointing at the 2:00 o'clock marker. What two angles would this make inside the right angle?

Answer: _____ degrees and _____ degrees
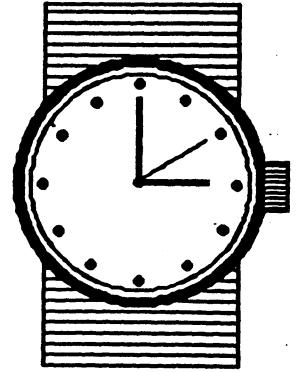
★★★ 7. On a 12-digit calculator, 3 ÷ 7 will give the answer shown. The calculator can't show the division process any farther. But the digits continue to repeat in this manner.

a. What will the 13th digit be? _____

b. What will the 14th digit be? _____

c. What will the 100th digit be? _____
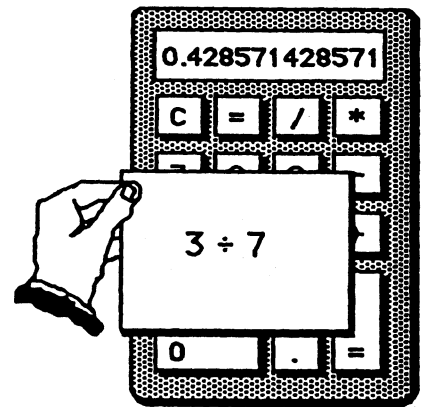
★★ 7. When Bonita makes a fruit salad, she always uses oranges and watermelons. This time she has 11 pieces of fruit. If she uses at least one of each and more oranges than watermelons, show all possible combinations by filling in the chart below.
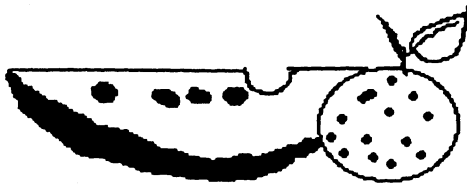
Oranges					
Watermelons					

★★★ 8. A bracelet cost $33.50. The earrings cost $12.65. How much does it cost to purchase the set if you get 10% off for buying both, and the sales tax is 6%?

Answer: $_____

48

Name: _____

(This shows my own thinking.)

★★ 1. In the third grade, some students have pets that are dogs, some have fish, and some have both. Use the Venn diagram to answer the questions.
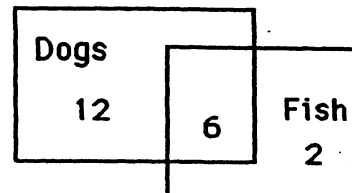
   a. How many students have fish? _____

   b. How many students have fish and a dog? _____

Dogs

12

6

Fish

2

★★ 2. You ran 1.5 miles before you decided you were running in the wrong direction. You turned around and ran back to where you started. Then you ran 2.75 miles in the other direction. How many miles did you run in all?

   Answer: _____ miles

★★ 3. It takes about 735 turns of an average 5th grader's bicycle tire to go 1 mile. To the nearest thousand, how many times would your tire turn around if you biked beside the runners in a 26-mile marathon?
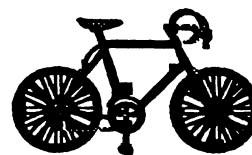
   Answer: _____ turns

★★★ 4. The graph below shows what a bicycle's speed might look like for a 26-mile marathon. The race started at 8:00 AM. Answer these questions about the graph.

   a. How long did the race last? _____ hours and _____ minutes

   b. At what time did the rider stop to get water? _____ A.M.

   c. What is happening to the rider's speed between 10:00 and 10:30? _____

Speed

8:00   9:00   10:00

49
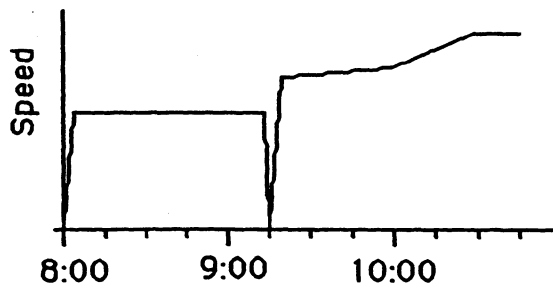
★★★ 5. Mrs. Jones' science class had to record the total amount of rain that fell the last week of school. It rained 1.66 inches on Monday, 0.23 inches on Tuesday, 0.76 inches on Wednesday, 1.2 inches on Thursday, and the skies were clear on Friday. What was the average amount of rain that fell daily from Monday to Friday? Round your answer to the nearest hundredth.

Answer: _____ inches

★ 6. Take a sheet of paper and fold it in half, fold it again, fold it again, fold it again, and then fold it again in half. If you opened the paper, how many sections would you have?

Answer: _____ sections

★★ 7. During the summer, Julio promised his Dad he would read 3 novels every 2 weeks. How many novels would that be during the 3 months of summer? (use 12 weeks for 3 months)

Answer: _____

★★ 8. Write two numbers in the spaces below to show what the two "tick marks" stand for on the number line, between 3 and 4.
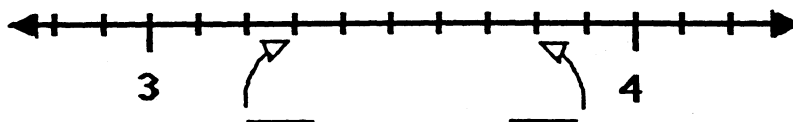
★★ 9. Mary had 10 yards 2 feet of ribbon. She needed to cut pieces for her 3 friends. If each friend got the same amount of ribbon, how much did each get? In your answer, there cannot be more than 12 inches

Answer: _____ yards, _____ foot, _____ inches

(Note: in your answer, inches must be converted to feet, if possible, and feet to yards.)

Name: _____

(This shows my own thinking.)

★★★★ 1. How many different squares are in each figure? Count the smallest squares first, then move up to the next size, and so on. Record the total number of squares below each figure and look for a pattern.

___   ___   ___   ___
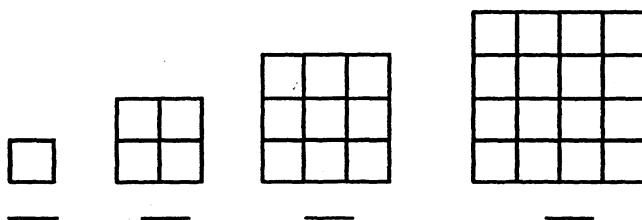
★★ 2. Herman thought he noticed a pattern to the problem above. The total number of squares is always the sum of the square numbers up to the figure number. For the 3rd figure, for example, the total number of squares is 14, which is also $1^2 + 2^2 + 3^2$.
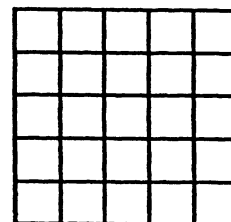
a. Does this pattern work for the next figure, the 5th? _____

b. What is the total number of squares in the 10th figure? _____

★ 3. Aki bought a new calculator for school. What is the cost of the calculator including sales tax of 6%? Round your answer up to the next cent, as a store would.

Answer: _____

14.99
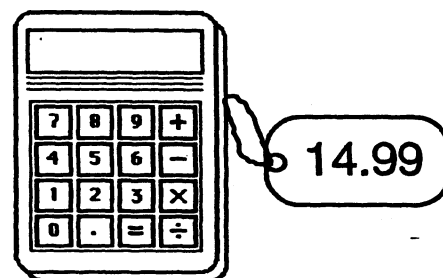
★★★ 4. Complete the chart below by putting a check in each column by which the number is divisible. You may have more than one number checked in each row or column. The first one is started for you.

		2	3	4	5
a.	6,945		✔		
b.	1,236,240				
c.	54,208				

51

★ 5. Draw the other half of the shape to make it symmetrical. If it helps you, fold the page along the vertical *line of symmetry*, hold it up to the light, and trace.

★★★★ 6. Complete the crossnumber puzzle.

DOWN
1. (28 X 126) - 21
3. ? + 716 = 4220
5. 6521 + 9963 - 12321 + 42896 + 30286
6. (364 X 265) - 41282
7. Average of 4728, 9630, 7465, and 725
11. $\sqrt{100489}$

ACROSS
2. 6000 - ? = 5486
4. 280644 ÷ (300 + 64)
6. $35^3 + 100^2 + 170$
8. $3 \times 10^3 + 3 \times 10^2 + 7 \times 10^1 + 6 \times 10^0$
9. Age the second year as a teenager
10. {[(238 ÷ 14) + 20] X 1560} + 18
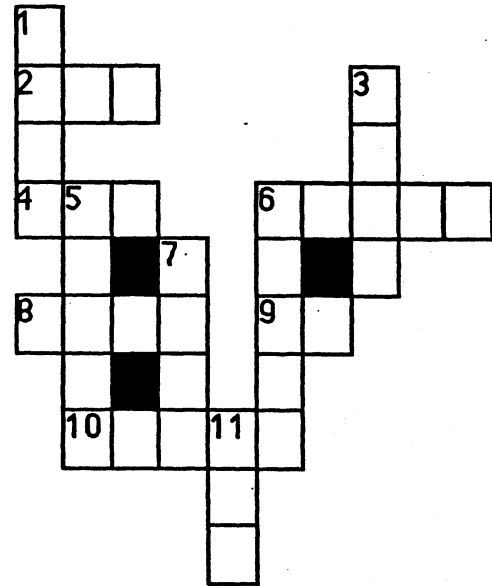
★★★★ 7. This weird kid from another planet multiplies differently from us! She gets the right answer, but her work doesn't look like anyone else's in class. Here's what she does:

Given:	Multiply 2 X 38:	Multiply 40 X 38:	Add:
42 X 38	42 X 38 76	42 X 38 76 1520	42 X 38 76 +1520 1596

Do these problems this way:	1 4 X 2 6	3 1 X 5 3	2 7 X 4 2	6 2 X 1 3 5

52

Name: _____

(This shows my own thinking.)

★★★ 1. A *perfect number* is one which is the sum of its proper divisors. Six is the smallest *perfect number*: 6 = 3 + 2 + 1. The next smallest *perfect number* is between 20 and 30. Find it!

Answer : _____

★★ 2. Find the missing digits in this problem.

```
              317 r 25
        _____
2 _ | __584
        __1
        ____
         48
         2__
        ____
        214
         18__
        ____
          25
```

★★★ 3. Carlos wants to learn to play golf, but he wants some information before he begins. He learned that the local 18 hole golf course is 6,550 yards long. It is a "par 72" course, which means that a good golfer should play the entire course with a total of 72 strokes.

   a. What is the average distance (rounded off) for each hole? _____

   b. What is the average number of strokes required per hole? _____

   c. For his first round, Carlos scored 108.
      How many strokes over par was he? ____

★ 4. A can of soda contains approximately? (circle the best answer)

   350 ℓ   350 mℓ   350 cℓ

★★★ 5. Shomika was helping her family pick oranges in their grove. She took some oranges home to share with three friends. She gave 3 more than half to Jennifer. Angela got half of the remainder and 3 more. She gave Josie half of the remainder plus 3. When she got home, she only had 10 oranges left. How many did she have when she left the grove?

Answer :_____

★ 6. Solve this problem:

$$3 \times (8 + 6) - 8 = Y$$ Answer: $Y = $ _____

★★ 7. Joann's class is planning a math celebration after half the class scores at least 100 stars in Sunshine Math Superstars. She surveyed the class to find out how many like chocolate cupcakes and how many like vanilla cupcakes. She organized the information to give to her mom, who is going to do the baking. Her results are shown to the right:
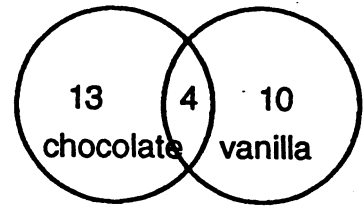
a. How many students were surveyed? ____

b. What percent (rounded to the nearest whole percent) like chocolate cupcakes? ____ %

★ 8. Fold your paper to show a line that is *perpendicular* to the one below .
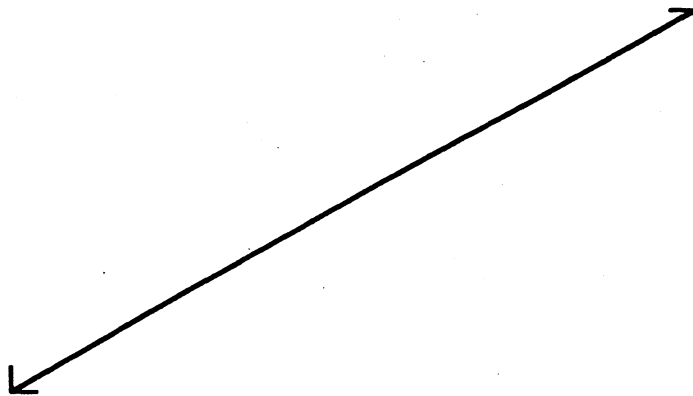
★ 9. Five fifth graders decided to clean up their community on Earth Day. Armed with dozens of garbage bags, they began work at 8:30 AM. They took two 15 minute breaks and a half-hour lunch break. When they had worked 5 hours, they knew it was time to go home. What time did they quit working?

Answer: _____

★★ 10.   3 weeks, 4 days, 13 hours, 21 minutes
       − 1 week, 5 days, 18 hours, 30 minutes
       ___ week, __days, __ hours, __ minutes

Name: _____

(This shows my own thinking.)

★★★   1. Use the numbers 1, 2, and 4 to make the numbers from 1 to 9. Use each of the three numbers only once and use only the four arithmetic operations. The first one is done for you.

Example: 4 - 2 - 1 = 1   _____ = 4   _____ = 7

         _____ = 2   _____ = 5   _____ = 8

         _____ = 3   _____ = 6   _____ = 9

★★   2. Race car driver Brad Heath was interviewed about his car's fuel use. He told the reporter that his car averages 3 miles per gallon. If his car holds 22 gallons of fuel, how far can he race on a tank of fuel?

Answer: _____ mi.

Racing fuel costs $3.40 per gallon.
How much does the tank of fuel cost?

Answer : _____
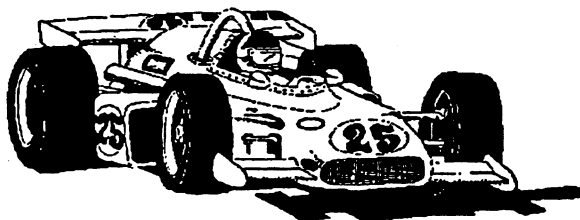
★★   3. Jan's class is entering a contest. The winner will receive tickets for the student and parents to visit the city of their choice. Jan lives in Buffalo, NY, so she would travel from New York. The distance in miles from New York to four European cities is given to the right.

Berlin	3,965
London	3,458
Paris	3,624
Moscow	4,665

a. What is the difference between the nearest and farthest European cities?

Answer: _____ miles

b. Jan's mother flies to Paris and back to New York once every month. How many miles does she fly each year? (Round to nearest 1000 miles.)

Answer: _____ miles

★   4. One acre of land will grow 11,000 heads of lettuce. If a farmer has 1,500 acres of land and he plants lettuce on half of his farm, how many heads of lettuce can he expect to grow?

Answer: _____ heads

★★★ 5. Harry and William bought a pizza for $8.99. Harry ate five pieces and William ate 3. Based on how much each one ate, how much should each pay?

Answer: Harry should pay _____ ; William should pay _____ .
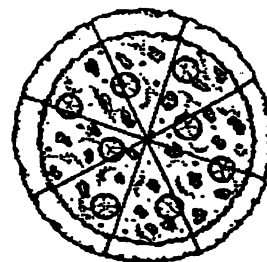
★★ 6. Use the clues to locate these points on Second Street.

W ─┼───┼───┼───┼───┼───┼───┼───┼───┼─ E

Second Street

The antique store, A, is at the *midpoint* (middle) of the street.
The museum, M, is 2 cm. west of the restaurant.
The restaurant, R, is 4 cm. east of the antique store.
The gift store, G, is 8 cm. west of the restaurant.
The theater, T, is halfway between the antique store and the museum.

★★★ 7. Draw arrows to show how to rearrange exactly 2 of these toothpicks so that you will have 4 squares instead of 5. Each square is to be the same size as the ones shown.
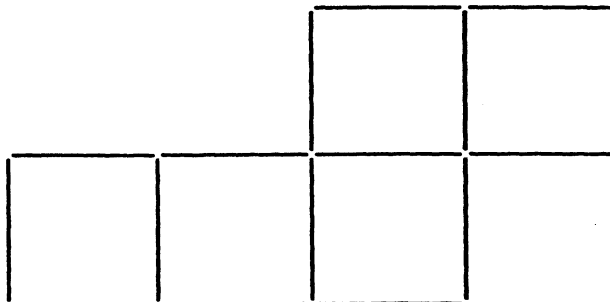
★★★ 8. How much change will I get back from a $5 bill if I buy three pairs of socks selling as advertised? Sales tax is 6%.

Answer: _____

SALE!!
Socks ....2 pairs for $1.98

★ 9. $\frac{3}{4} + \frac{1}{2} + \frac{5}{6} - \frac{1}{3} + \frac{7}{12} =$ ☐   (Be careful -- $\frac{1}{3}$ is being subtracted!)

Name: _____

(This shows my own thinking.)

★ 1. Let p stand for the weight of a whole pie. The equation $\frac{3}{4}p = 30$ shows the situation on the scale. How much did the whole pie weigh? Use your number sense.

Answer: $p =$ _____
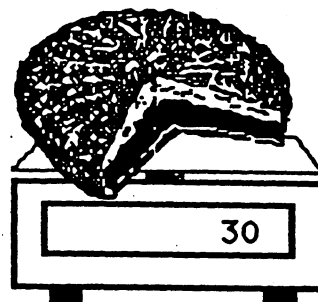
★★★ 2. A *square inch* is shown to the right.

Bubble-in the best estimate below of the area, in square inches, of this sheet of paper.

0   50 in²   0   90 in²

0   125 in²   0   150 in²
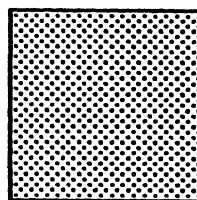
★★ 3. Make a *line graph* of the world population figures shown below. Use the graph paper to the right. Then answer this question: *If the population continues to increase as the graph shows, what will it be in 2000 AD?* _____

World Population

Year (AD):	Population (millions):
1	300
1000	350
1600	450
1700	700
1800	1,000
1900	1,700
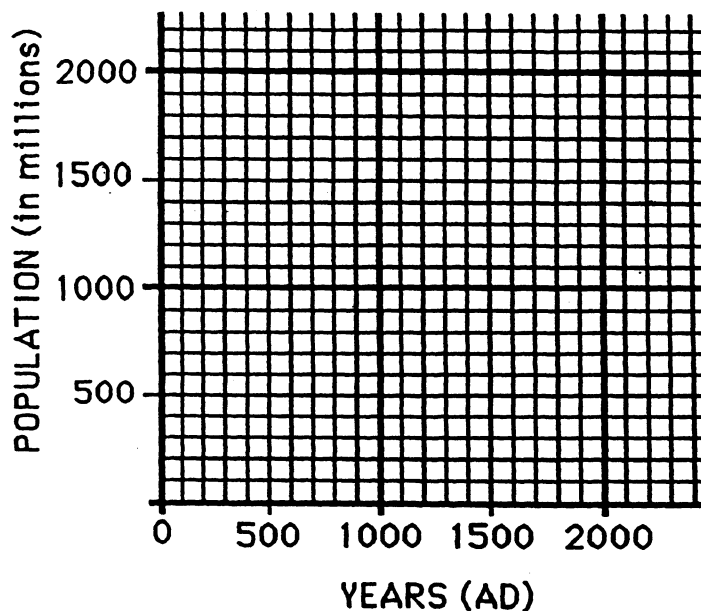
★★★★ 4. A machine changes the first number into the second number. Study the pattern and predict the rule the machine uses to change one number into another.

1	fl	7
2	fl	10
3	fl	13
.	.	.
10	fl	34
.	.	.
100	fl	304

a. What will the machine produce for 40? ____

b. What will the machine produce for 50? ____

c. The machine produced 904. What number did it start with?____

d. Describe the way the machine changes a number n:

_____

★★ 5. There are about 3,400 species of frogs and toads, and scientists tell us that they represent 90% of the amphibians in the world. Using this information, what is the total number of amphibian species scientists believe are in the world. (Round your answer to the nearest 100.)

Answer : _____

★ 6. Suzanne ordered a sandwich and a soda. The total, plus tax, came to $4.76. Suzanne gave the clerk $5.01. What is a good reason for Suzanne to give the clerk the extra penny?

Answer: _____

★★ 7. The missing digits for this problem are 0, 2, 4, 6, and 8. Put them in their correct boxes.

$$\square\ \square\ \square\ \square\ \times\ \square\ =\ 32,208$$

★★★ 8. Draw this pattern on scratch paper.

a. How many dots in the next 3 figures?

____, ____, and ____

b. How many dots for the 50th figure?____

c. How many dots for the 1000th figure? _____
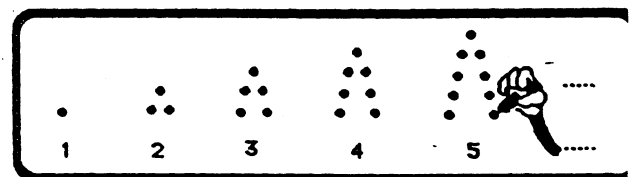
Name: _____

(This shows my own thinking.)

★   1. Laquinda and her 2 friends wanted a pizza after school. They
        did not have enough money, but Laquinda's mother promised to
        give them what they needed once they put their money together.
        Laquinda had $2.45; one friend had $3.72; the other friend had
        $0.87. How much did Laquinda's mother have to pay for the
        pizza if the total cost was $9.95?

        Answer: _____

★★★ 2. Use number sense to solve each equation. Find out what a single object weighs.
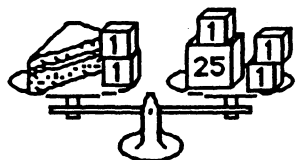
A piece of cake weighs:
$x + 2 = 28$
$x =$ ____
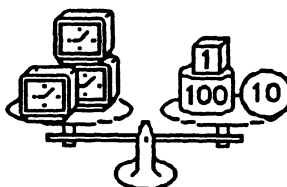
A clock weighs:
$3y = 111$
$y =$ ____
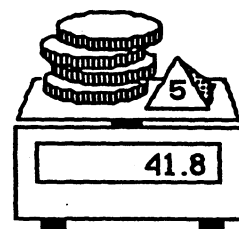
A coin weighs:
$4z + 5 = 41.8$
$z =$ ____

★   3. Circle the best estimate below for the sum of $13\frac{38}{39}$, $7\frac{16}{17}$, $4\frac{1}{9}$, and $4\frac{1}{42}$.

        a. 28   b. 30   c. $28\frac{23}{46}$ d. 20

★★ 4. Raoul's "school days" picture was
        accidentally made with a grid behind it.
        Estimate the area of the part of his body that
        is showing. Circle the best estimate below.

        a. 40 sq. units c. 60 sq. units

        b. 50 sq. units d. 80 sq. units

★★ 5. 100 adult customers were surveyed to determine which type of shop in the mall -- clothing store or shoe store -- they liked best. Forty-seven liked clothing stores best. Twenty-three preferred shoe stores. Fourteen liked both equally well. The rest did not like either type of store. Write 4 numbers in the appropriate section of the Venn diagram below to show these statistics.

neither

clothing shoe
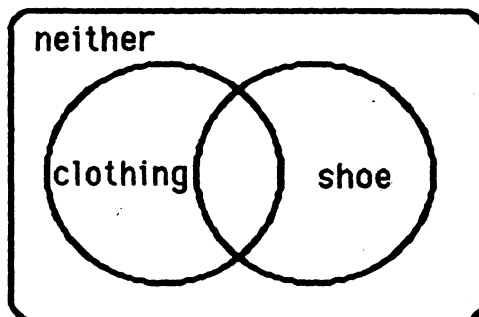
★ 6. Space shuttle Atlantis has traveled a distance of 2,000 miles one and a half minutes into its flight. If it continues to travel at this speed, how far will it have traveled in six minutes?

Answer: _____ miles
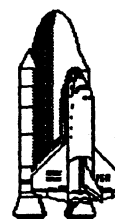
★★ 7. Joseph has a nickel and a penny in one pocket and two nickels and two pennies in the other pocket. Which pocket gives him the better chance of pulling out a penny?

Answer : _____

★ 8. Betty Jean has 18 coins. One sixth of the coins are quarters, one third of the coins are dimes, and one half of the coins are nickels. What is the value of Betty Jean's coins?

Answer: $_____

★★★ 9. Write the area of each geoboard figure on the line below the figure.

area = _____   area = _____   area = _____

60
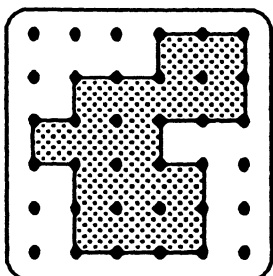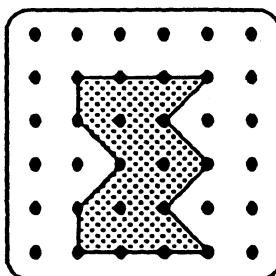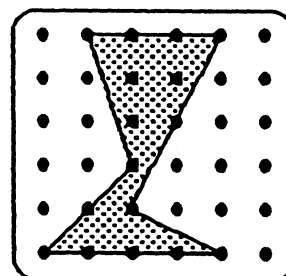
SUNSHINE MATH - 5
Saturn, XXIV

Name: _____

(This shows my own thinking.)

★★ 1. There were 22,600 tickets sold for the Magic's first game. 4,800 fewer people showed up for the second game. If tickets were $25 each, how much money was brought in by the two games?

Answer:_____

★★★★ 2. Marshall makes $20,000 a year. His budget is shown to the right.

    a. What is the sum of the percents on the graph? _____

    b. Does Marshall spend more money on education or on food? _____

    c. How much money does he spend on his car? $_____

    d. What is the total amount of money Marshall spends on clothing, entertainment, and savings? $_____
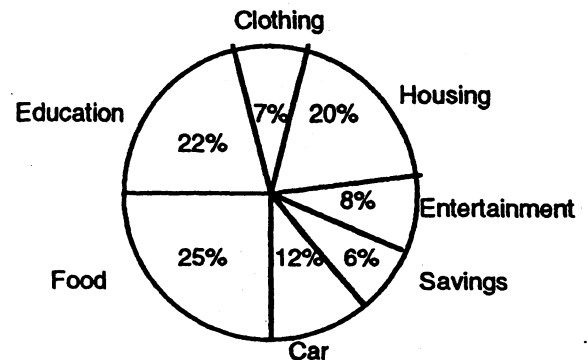
★★ 3. Juanita could not see the classroom clock hung on the back wall of the room without turning around in her seat. But one day she discovered that she could see it by using the mirror in her purse. If this is what she saw, what time was it?

Answer: _____

★ 4. Emily and Morris were discussing how fast a baseball travels. They asked Emily's Dad to hit a ball. The machine measured the ball's speed at 98.70465 miles per hour. Round this speed to the nearest hundredth mile per hour.

Answer: _____ mph

61
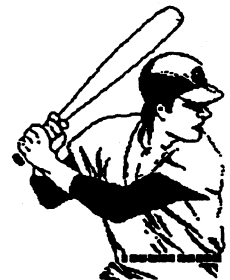
★★★ 5. Write an algebraic expression for each situation below, using the variable given.

   a. three times as high as the stack of books, x, plus 2 feet: _____

   b. $100, less twice Taria's money saved, s: _____

   c. one-half of Marcia's time, t, less 2 minutes: _____

★★ 6. Patti helped her Mom plan a patio. Estimate about how many bricks they should order. Circle the best estimate below, to have a few left over for breakage.

   a. 800   b. 600

   c. 1000   d. 700
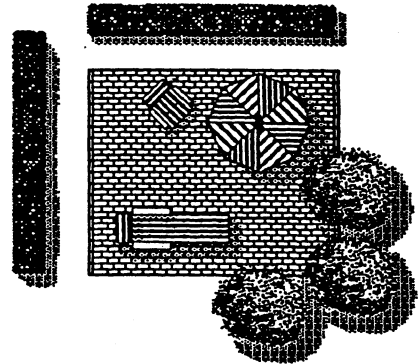
★★ 7. Spring is the time for snorkeling. Marcus enjoys snorkeling around the beach area at Panama City. Circle the temperature when he might enjoy this sport the most.

   a. 0°C   b. 25°C

   c. 50°F   d. 80°C

★★★★ 8. A man has a goose, a fox, and a bag of corn with him walking through the woods. He comes to a river, but there is only one boat available for crossing. The boat will only hold the man and one other thing each time across the river.

The man can't leave the fox and goose alone on the river bank, because the fox will eat the goose. He can't leave the goose and corn alone, because the goose will eat the corn.

What's the fewest number of crossings he can make in the boat, to get everything on the other side? (A *crossing* means going from one side of the river to the other.)

(Hint: draw a diagram.)   Answer: _____ crossings

62

Name: _____

(This shows my own thinking.)

★★ 1. The Drew Elementary School softball team needs bats and
mitts for their team. If bats cost $12 and mitts cost $15,
what is the greatest number of items they can buy for $200 if
they buy at least one of each?

Answer: _____

```
SALE!
Bats ..... $12
Mitts .... $15
```

★★★ 2. The numerator and denominator of a fraction are single digits which total 13. When you divide the numerator by the denominator, the answer is 0.86 rounded to the nearest hundredth. What is the fraction?

Answer: _____

★★★ 3. Use the menu to answer the questions.

Hamburger	$1.49	Hot Dog	$1.25
	Small	Large	
Fries	$.75	$.95	
Cola	.79	.99	
Shake	1.25	1.75	

a. If you buy a hamburger, small fries, and small cola, what will your bill be after adding the 7% sales tax? (Remember, stores will round any part of a cent *up!*)

Answer : _____

b. If you give your server $5.00, how much change will you receive?

Answer : _____

c. If you had $2, what combinations of food would you be able to buy with no items the same, if your friend agrees to pay the tax for you?

Answer : _____

_____

★ 4. Elvira was solving a complicated math problem. In her last step she divided by 5 and got the answer 13. Then she realized she should have multiplied by 5 instead of dividing by 5. What should her answer really have been? _____

★★★ 5. Mason was told by the vet to keep up with the weight of his 6 pups, which all looked alike. He weighed them by putting them all in a wooden box and weighing them together -- the scale showed 50 pounds. Then he weighed the box by itself -- it weighed 8 pounds. Answer the questions about Mason's equation for finding out how much each pup weighed.
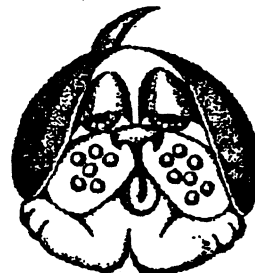
Equation: 6 x W + 8 = 50

a. What does W stand for in the problem? _____

b. Why is W multiplied by 6 in the equation? _____

c. What value for W solves the equation? _____

★★★ 6. Maxine's family wanted to build a pool in their backyard. The pool itself was to be 20 feet by 30 feet, and they wanted a 5-foot wide concrete border around it.

a. What are the dimensions of the whole area, pool plus concrete walk? _____ by _____

b. Before buying water sealer for the concrete walk, they need to know how many square feet of concrete they'll have to seal. How many square feet of concrete will there be? _____
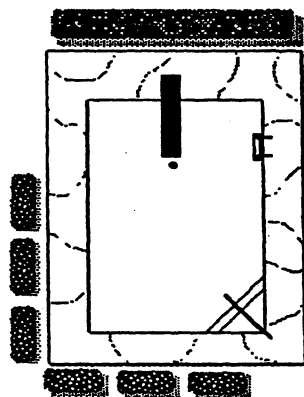
★★ 7. Label the sections of the spinner R for red, B for blue, and G for green so that you will land on red one-fourth of the time, on blue half the time, and on green one-fourth the time.
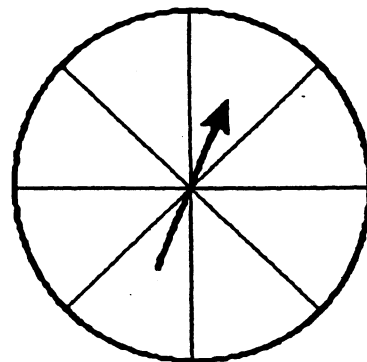
SUNSHINE MATH - 5
Saturn, XXVI

Name: _____

(This shows my own thinking.)

★★ 1. Saturn's diameter is about 71,000 miles. Its rings extend from the surface another 35,000 miles into space. What is the distance from the center of Saturn to the outer edge of its rings?

Answer: _____ miles

★★★★ 2. The circle shown here has four congruent angles drawn at the center. The angles are congruent to the 90° angle off to the side.

90°
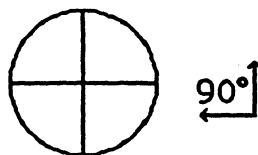
Draw as many angles as possible at the center of these circles which are congruent to the angles shown. All angles within each circle must share sides.

30°

120°

180°

45°
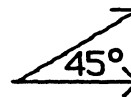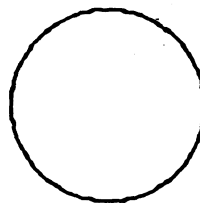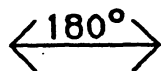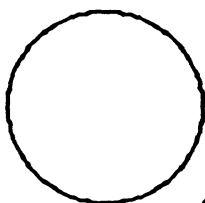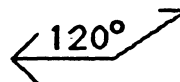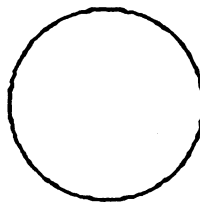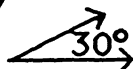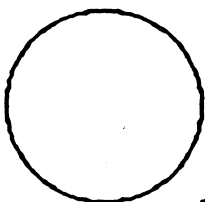
★★ 3. Find the pattern and write the next three numbers. Then answer this question: What number comes three numbers before the 2 if the pattern were extended to the left? _____

$$2, \ 1, \ \frac{1}{2}, \ \frac{1}{4}, \ \underline{\hspace{1cm}}, \ \underline{\hspace{1cm}}, \ \underline{\hspace{1cm}}, \ ....$$

★★ 4. Anne has duplicates of 125 stamps in her collection. She gives 50 to Sam, then she divides the remainder evenly among five friends. If two of her friends put their stamps together, how many will they have?

Answer : _____ stamps

★★★ 5. Henri spun a 3-color spinner 45 times. He filled in this tally chart and needs to complete it. Fill in the information he forgot.

Red	‖‖ ‖‖ ‖‖	$\frac{13}{45}$
Blue	‖‖ ‖‖ ‖‖	
Green		

★★ 6. Complete the problem.

$$
\begin{array}{r}
9\,2\,\square \\
\times\ \square\,8 \\
\hline
\square\,\square\,7\,6 \\
\square\,2\,\square \\
\hline
1\,6,5\,9\,\square
\end{array}
$$

★★★ 7. Susan's age is 3 times Andrea's age. Barbara is twice as old as Andrea. The sum of their ages is 30. How old is each girl?

Susan is ____ years old; Andrea is ____ years old; Barbara is ____ years old.

★★★ 8. Andy wants to run a 3-mile race at the same pace all the way through the race. He knows he can do this in 24 minutes. He stations his Dad at the 2-mile mark to give him his time as he passes by. His Dad calls out 15:30 as he passes by. What else did his Dad say? Circle the best choice:

a. Great! You're right on time!

b. Slow down! You're ahead of your pace!

c. Speed up! You're lagging behind your pace!

SUNSHINE MATH - 5
Saturn, XXVII

Name: _____

(This shows my own thinking.)

★ 1. Brandon counted 13 kids ahead of him in line to buy concert tickets. He then counted 17 behind him in line. Five more kids got "heads" from someone ahead of him, but then 2 kids behind him dropped out. How many kids were in the line at that point?

Answer : _____

★★ 2. Juan had 7 pennies, 4 dimes, and 3 nickels in his pocket. If he reached into his pocket 10 times, putting the previous coin back each time, which number best indicates how many times you would expect him to pull out a penny? Circle your answer.

a. 7   b. 10   c. 1   d. 5

★★★★ 3. Place each number from 1 through 10 in a box. Each box must contain a number that is the *difference* of two boxes above it, if there are two above it.
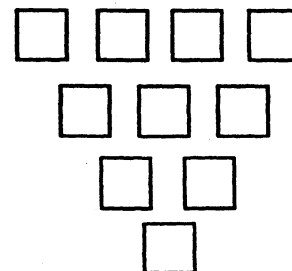
★★ 4. What are the whole numbers that Y might represent on the scale, and the right side would still be heavier? Or, find the whole numbers Y which will make this number sentence true:

$$Y + 3 < 8$$

Answer: _____

67
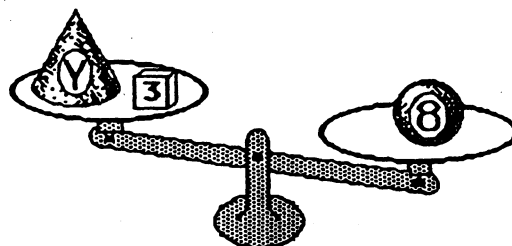
★★★★ 5. The first 500 people to visit the baseball game were given their choice of an autographed ball, a cap, a pennant, or a cup with the team logo. $\frac{1}{4}$ chose the ball, $\frac{1}{2}$ chose a cap, $\frac{1}{10}$ chose a pennant. How many of each gift were given away?

Answer: _____ balls, _____ caps, _____ pennants, and _____ cups

★★ 6. Circle the sensible measurement for each item.

thickness of a book	28 mm	28 cm	28 m
height of a flagpole	10 cm	10 m	10 km
distance walked in $\frac{1}{2}$ hour	3 mm	3 kg	3 km
length of a field	30 dm	30 m	30 mm

★ 7. Jay earns $10 each week during the summer mowing lawns in his neighborhood. His parents require him to save 25% of his earnings. If he works 9 weeks during the summer, how much can he expect to save by the end of the summer?

Answer: _____

★★★★ 8. The fifth grade was surveyed to find which pets they liked. The diagram shows the results:

a. How many like dogs and birds but not cats? _____

b. How many like only cats? _____
c. How many like dogs, cats, and birds? _____

d. What is the ratio of students who like all pets to those who answered the survey? _____
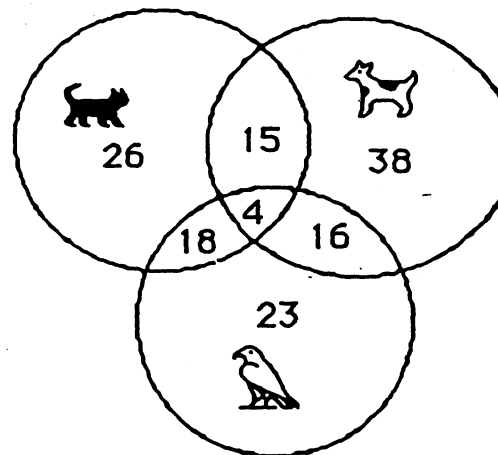
ANSWERS

Commentary
Saturn, I

1. **(4 days)** Students can draw a diagram for the worm's trip. The first day, he reaches 4.5 feet but then slips back to 2 feet level at night. The next day he reaches 6.5 feet, but then slips back to 4 feet at night. The 3rd day he reaches 8.5 feet but then slips back to 6 feet. On the fourth day, he reaches 10 feet and is on top of the hill, so doesn't slip back.

2. **(f)** Problems such as this one should help students realize that their answer should make sense in terms of the real world. Knowing that a soda costs around 60¢, the challenge for the student is to decide which of these answers is the correct way to interpret the calculator display. This problem might lead to a class discussion about common misuse of the decimal point in advertising, such as writing ".60¢" for "60¢" and "$199" for "$1.99."

3. **(Thursday)** Students might list the days of the week, and count from the 9th starting on a Tuesday.

4. $(7\overline{\smash{)}301})$ This problem can be approached through *guess-check-revise*.

5. **(Either the top and bottom can be circled, or the two sides)** A set of parallel lines are lines that never cross. These can be demonstrated by having students use pieces of spaghetti to represent lines. They might be encouraged to look for parallel lines immediately around them--notebook paper, the top and bottom of classroom walls, etc.

6. **(96 mm, may want to accept anything from 94 to 97 mm)** Students should use a metric ruler rather than one marked in inches. They might count each centimeter mark as 10 millimeters, and then the extra millimeters, from the eraser to the tip of the pencil.

7. **(10 ways)** Sugar, unifix or wooden cubes can be used for students to go through the experiment in a concrete way. The faces can be colored with a crayon or magic marker, or simply labelled "G" and "W." At home, students can use any box they can find although using only 1 box over-and-over means they must be careful in keeping track of the different cubes already made.

Combinations:	*1 cube each*--6 W; 6 G; 1 G and 5 W; 5G and 1W
	2 ways each--2 G and 4 W; 2 W and 4 G; 3 G and 3 W

8. **(NO)** Students should realize a milk shake costs more than $0.39, unless there's a special. If a student mentions this, they should receive credit also.

9. **(85, 67, 49)** Students might list all the pairs of single digits with a sum of 13. Each such pair of digits make up 2 two-digit numbers. Only the resulting numbers with the odd digit in the units place is not divisible by 2.

   $8 + 5 = 13$, giving 85 as a solution (but not 58)
   $6 + 7 = 13$, giving 67 as a solution (but not 76)
   $4 + 9 = 13$, giving 49 as a solution (but not 94)

Commentary
Saturn, II

1. **[(8 + 4) + (6 x 2) = 14]** Students can use *trial and error* to find the correct order.

2. **(30 squares)** There are 16 small squares, 9 of the next largest in which 4 of the smallest are put together, 4 of the next largest of 9 small ones together, and the one large square itself.

3. **(left-hand calculator)** Students who have trouble with this problem might be encouraged to think of money. The 0.4 might be $\frac{4}{10}$ of a dollar or 40¢, whereas 0.39 might be 39¢. Another way would be for a student to subtract each number from the other on a calculator. The way which gives a positive number on the display means the largest number was entered first.

4. **(4)** Students might divide the total number of people going by the number of people that can fit in one van, with one person per seat belt. If so, they should realize that 21 people can go in 3 vans, but an extra van is needed for the remaining 4 people. This is a case in which the answer to a division problem requires rounding the decimal remainder up, rather than to the nearest whole number.

5. **(9708.6)** This is a simple recognition of place value task.

6. **(1 kg; 350 mL; 30° C; 2200 km)** Students should be encouraged to use "bench mark" metric measurements to estimate reasonable answers. For example, their math book weighs about a kilogram, a mL is about one drop from an eyedropper, a comfortable room temperature is about 30° C, and the distance across the United States is about 5000 km.

7. **(3 to 10, 3:10, or $\frac{3}{10}$; 4 to 15, 4:15, or $\frac{4}{15}$; boys)** Any of these answer forms are acceptable. To find which ratio is larger, 3:10 or 4:15, students can be encouraged to transform the ratios by doubling, tripling, etc., until they get two ratios with the same size comparison group. By doubling, 3 boys out of 10 is the same as 6 boys out of 20. By tripling, you get the ratio 9 boys out of 30. By doubling, 4 girls out of 15 is the same as 8 out of 30. Since 9 out of 30 is more than 8 out of 30, the boys with braces represents a larger ratio.

8. **($2.75 total cost and $2.25 change)** Sales tax of 6% can be interpreted by students as paying $.06 on each dollar spent. On $2 spent, the tax would be $0.12 and on 59¢, the tax would be another 4¢. Sales tax is a real-life example in which partial amounts of money are *rounded up*, rather than to the *nearest*, penny. The total cost would then be $2.59 + 12¢ + 4¢ or $2.75; the change from $5 would then be $2.25.

Commentary
Saturn, III

1. **($159.18)** Multiply 36 times $2.38 and 42 times $1.75. Add the two totals together.

2. **(6 students)** Students can count the number of students for each grade, adding grades 1-3 together and grades 4-5 together, and subtract to find the difference. Or they might count the total number of stars in each group, subtract and find a difference of 2 stars, then multiply by 3.

3. **($15)** Students might find $\frac{1}{4}$ of $100, getting $25. They have $75 left. They can find $\frac{1}{5}$ of $75 by dividing 75 into five equal shares, getting $15 per share. That's the amount saved.

4. **[(8÷4) − (2÷1) is one possibility.]** This is a *guess-check-revise* problem. They must substitute until they come up with the correct order.

5. **Answers shown below.**
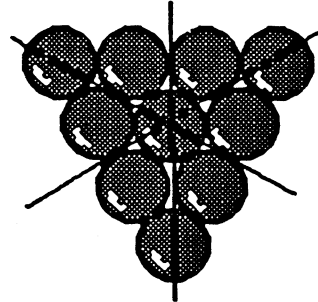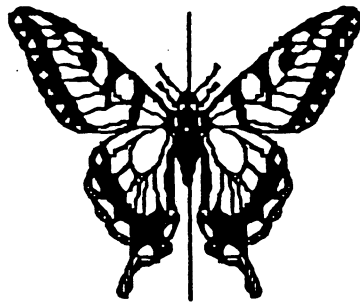
6. **Answers will vary.** To decide if the figure is symmetric about the line, fold it and see if the sides match up.

7. **(400)** Students might make a list to organize the approach to this problem. Such a list as the one below helps to observe a pattern:

Group number	People in group	Total
1	1	1
2	3	4
3	5	9
4	7	16
.	.	.
.	.	.
20	39	

If students don't notice the pattern that the total after n groups is n^2, they can still solve the problem by adding the "people in each group" column. Notice that $1+39 = 40$, $3+37=40$, $5+35=40$, etc. There are ten such subtotals of 40, giving 400.

8. **(6)** Students might find this in a variety of ways. One way is to look at the third scale and conclude that 1 turtle weighs 0.5, and then from the second scale the 2 turtles would weigh 1 leaving the cake to weigh 12. Then from the first scale, you know that the can must weigh 6 since the cake weighs 12.

1. **(10, 15, 21, 28, 36)** Triangular numbers can be found by arranging a number of dots in a pattern, and the pattern forms an equilateral triangle.

2. **($24.00 more)** $5.25 x 40 = $210, $5.85 x 40 = $234, and $234.00 − 210.00 = $24.00. Another approach would be to notice that there's a difference of 60¢ in the hourly rate, and 40 x $0.60 = $24.

3. **(5 diagonals)**
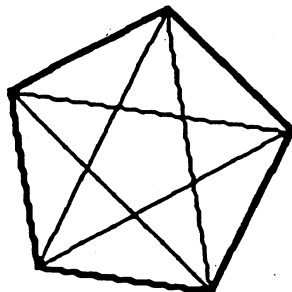
4. **(One fourth of the dollar bill should be shaded. $1.25)** Students can shade in 1/4 of the dollar bill in several different ways. The only criteria is that the dollar bill be divided into 4 equal pieces, and 1 is shaded. Hopefully students will realize that 1/4 of the dollar bill is equivalent, money-wise, to a quarter. This will enable them to find the answer to the second part.

5. **(8 meters and 4 meters)** The students will guess all the pairs of numbers that can be multiplied together to give 32. Then they have to see if the pairs can be added to get a perimeter of 24. Drawing a picture helps.

6. **(50)** This problem is a precursor to solving an equation of the form $3Y + 31 = 181$. Students intuitively know that they can remove the 31 from the scale, and have 3 cans that weigh 150. Dividing 150 by 3 gives that each can weighs 50. So $Y = 50$ solves the equation.

7. **(7 x 12 = 84 or 12 x 7 = 84; 39 x 2 = 78 or 2 x 39 = 78; (20 + 3) x 4 = 92 or (3 + 20) x 4 = 92 or 4 x 23 + 0 = 92)** The problems can be found by using number sense, and estimating mentally. Some students might not use parentheses in writing the last problem. In fact, on most calculators it's not necessary to use parentheses for this problem. However, writing the problem out to be done by hand requires parentheses for without it, *order of operations* would require multiplying 3 x 4 first, and adding that to 20, resulting in 32.

8. **(37)** The numerical pattern for the number of squares is: 1, 5, 9, 13, 17, ... Adding 4 more squares to each figure produces the next figure. Algebraically, if the figure number is n, the number of squares could be written as $4n - 3$.

Commentary
Saturn, V

1. ($\frac{9}{16}$; $\frac{1}{4}$) This is a real world example where students need to find a common denominator to be able to do the problem mathematically. It might be nice to bring such a set of wrenches so that when students turn in their paper, they can actually compare their results with what the wrenches tell them. Some students might solve this problem using real wrenches at home, avoiding the mathematics altogether.

2. ($12.72) Find a third of $18, and then subtract that amount to leave $12. Six percent of $12 is $0.72, which is added. Another way to approach the problem is to multiply $12 by 1.06, which gives the total cost, including sales tax.

3. (1770) Students can compute 42 x 35 and add that to 12 x 25.

4. (45) A corner of a sheet of paper can be placed over the hole where the piece of pizza is being removed. It's easy to see that this hole is about half of the square corner.

5. (May; 19.05) For students to be successful, they need to understand that zeros can be added to the right end of a decimal without changing its value. Therefore 9.6 can be thought of as 9.60, and 9.60 is easy to compare with 9.45. It's also easy to add the two, once they have the same number of decimal places.

6. (4 yd. 2 ft. 2 in.) Add and get a total of inches, feet and yards. Then convert each measurement to the next highest measurement.

7. (15) Candles can be counted in groups of 3. Each group of three candles represents 5 years. The nine candles on the cake give three groups of 3, which corresponds to 15 years.

8. (d. Justin) Make a chart. The chart could have four columns across and four down. The top could be labeled gray, green, blue, and white. The side could then be labeled Tia, Matt, Kenya, and Justin. Eliminate things that can't be true, resulting in the final choice.

9. (3 is circled; 9, 13, 17, 21, 25 or any number 1 more than a multiple of 4; 4) Hopefully students will notice as they count to find the answers that there is a numerical pattern that underlies these figures. They repeat every four figures, so number 4 will always be like the other multiples of 4 in the pattern. Number 1 will be like the multiples of four plus 1, and so on.

Commentary
Saturn, VI

1. ($\frac{1}{4}$ or 25%, $\frac{3}{4}$ or 75%) There are four numbers on the spinner. Therefore, the chances of getting 4 is one out of four or 1/4. The chances of not getting a 4 is 3 out of 4, or 3/4. These could also be written as percentages.

2. (6¢, 15¢, 24¢, 33¢, 42¢, 51¢, and 60¢) Students can make a chart or list of the possible combinations of coins that would fit the criteria. A chart like the one below might be made:

pennies	6	5	4	3	2	1	0
dimes	0	1	2	3	4	5	6
money	6¢	15¢	24¢	33¢	42¢	51¢	60¢

3. (80) Computing inside the parentheses is important. The problem is written so that students can use number sense to compute inside the parentheses easily -- 7.5 is $7\frac{1}{2}$, and $7\frac{1}{2} + 2\frac{1}{2}$ gives 10. Then 8 x 10 is 80.

4. (Not enough information -- you need to know the cost to mail the sweatshirt.)

5. (Measure the student's line. It should be 52 mm.)

6. (850; 150; 450) For (a), find 350 + 300 + 200 or 850. For (b), compute 350 - 200 to get 150. To find (c), add 350 and 300 to get 650, then subtract 200 to get 450.

7. (2) This problem can lead to algebraic thinking. A variable d is introduced, along with a diagram that students can use to find the value of the variable. They can *guess-check-revise* to find d, or solve the situation logically as they would the equation $4d + 3 = 11$, by subtracting 3 from 11 and then dividing what's left by 4. The problem is intended to help students see a real-life situation that would later lead to an equation, and know that in such cases their solution to the equation should make sense in the real world.

8. (Thursday) Students can tell from the graph that the total distance did not change on Thursday, because the line was horizontal at that point. Therefore that's the day when she did not ride her bike to school.

9. (a. 1,020; b. 782) For (a), multiply the highest number of students per class by 34. For (b), multiply the lowest number of students per class by 34.

Commentary
Saturn, VII

1. $(31 \frac{1}{12})$ Students will need to find a common denominator for the fractions. 12 is the smallest such, although others (24, 36, etc.) would work also. If the fractions are converted into those with denominator 12, they will sum to 25/12 or $2\frac{1}{12}$. When added to the whole number parts, the answer is $31\frac{1}{12}$.

2. **($27.60)** Students can find one-fifth of $34.50 by dividing by 5. They then subtract this from $34.50. Another way would be to find four-fifths (or 80%) of $34.50.

3. **($9.34 and $10.75)** Students will have to use their visual acuity to see the sides of the figures that aren't shown. The top figure has two square faces at $1.49 each, and four rectangular faces at $1.59 each. It's price is given by: ($1.49 x 2) + ($1.59 x 4) = $9.34. The other figure has two triangular pieces at $2.99 each, and three rectangular pieces at $1.59 each. It's total price is given by ($2.99 x 2) + ($1.59 x 3) = $10.75.

4. **(a. > b. = c. > d. <)** In (a), the students can change 1/2 to 0.50 and compare 34.63 to 34.50. In (b), students can think of 1 as 5/5, so by taking 2 whole units from $3\frac{2}{5}$ and changing them into fifths, they would get 10/5. Or, $3\frac{2}{5} = 2\frac{7}{5} = 1\frac{12}{5}$. In (d), students have to realize that 9/100 is smaller than 9/10.

5. **(5 hours 11 minutes)** Count the hours from 8:15 to 1:15, then the minutes from 1:15 to 1:26.

6. **(a. 1,000,000; b. 10,000; c. 1,000)** This is a good problem to check on *number sense* for students. Students who have trouble with (b) and (c) might profit from starting with smaller numbers in similar problems.

7. **(E = 2; F = 1; G = 7; H = 8)** Students might start by noticing several critical features of this problem. E must be either 1 or 2, since the answer does not carry over into the ten thousands place. They might further guess that E ≠ 1 since this would result in H = 4, and the problem doesn't disallow this, but 4 is already in use so it's not likely. Choose E = 2 and assume H = 8, then, and proceed from there.

8. **(26.46)** Multiplication is called for to find the area of the carpet. 6.3 x 4.2 = 26.46

9. **(How do you keep a turkey in suspense?)** This riddle is a fun way for students to practice finding a fractional part of a set. Some possible answers are "I'll tell you tomorrow!" and "Delay Thanksgiving one day!"

Commentary
Saturn, VIII

1. **(a. true, b. false, c. true)** Perpendicular lines intersect and form right angles. Parallel lines do not cross or intersect. Students can draw diagrams or work with spaghetti to see if these statements seem true to them. For the last one, they might consider the lines on a sheet of notebook paper, for verification.

2. **(6)** This problem can verify if students can use *order of operations*. Work the parentheses first, divide, then add. Notice that if students do this problem left to right, as if entering it in a calculator, they would get the answer 20/3.

3. **(Lisa's stick, by 2 inches)** Lisa's stick is 2/3 of a yard, which is 2 feet. Sandy's is $1\frac{10}{12}$ feet, or 1 foot, 10 inches. 2 feet is longer than 1 foot, 10 inches by 2 inches.

4. **($\frac{3}{8}$)** The square can be divided into eight equal parts. If the square in the lower left corner were partitioned into two parts, three-eighths would be shaded.

5. **(10 hours, 13 minutes)** Adrienne traveled 5 hours, 28 minutes. Erica traveled 4 hours, 45 minutes. The only difficult part is to rename the total minutes, 73, as 1 hour, 13 minutes.

6. **($\frac{2}{18}$ or $\frac{1}{9}$)** There are 18 jellybeans in the bag. Two of them are orange. The chances of pulling out an orange marble would be 2 out of 18. In lowest terms, the answer would be 1 out of 9.

7. **(4 + 3 -7 + [6 ÷ (10 + 5)] is one possibility.)** There may be other solutions. Check each answer. Students may use parentheses.

8. **(2)** Joe gave away 2/3 of six colas, or 4 colas, leaving him 2. Christine gave away half as many as Joe, so she gave away 2 colas, leaving her with 4. So she had 2 more than Joe, in the end.

9. **(5)** The problem will show if some students mistakenly apply the traditional method of solving subtraction word problems -- "*how many left* means to subtract." In this case, the number left is the same as the number who couldn't squeeze into the refreshment stand.

Commentary
Saturn, IX

1. **(2 quarters, 3 dimes, 1 nickel, 2 pennies or 1 half dollar, 2 dimes, 3 nickels, 2 pennies)** Students can experiment with coin values to find the answer. It helps to write down some headings -- half dollars, quarters, dimes, nickels, pennies -- and begin listing coins under them that sum to 87¢, checking to see if you have eight coins. If not, modify the list. Notice that right away, you can tell that you have to have at least two pennies.

2. **(Yes, to the problem below.)** Write this problem on several 3 by 5 cards so students can read the problem privately, estimate, and write their answer down when they hand in their paper:

> Martin has $20. He wants to buy a magazine for $3.95, a baseball cap for 5.99, and a cola for 89¢. Will he have enough left to spend $6 on a movie ticket?

3. **(4 green, 2 blue, 3 white)** Finding the least common multiple will help students determine that Jack must buy 12 of each color ornament. An intuitive way for students to find the *least common multiple* is: Start with the largest number, 6, and look at its multiples, 6, 12, 18, and so on. When you find a number that's also a multiple of both other numbers, you've found the *least common multiple*.

4. **(vertical line down the middle, 8)** The "fold line" or *line of symmetry* splits the space ship in half, along the vertical. The area is found by counting 6 whole squares and 4 half squares, for a total are of 8.

5. **(The center number is 5. Numbers in "opposite boxes" total 10)** Students might solve this by guess and check, or they might think of what must be true for 3 numbers to sum to 15. Their average would have to be 5, so start by placing 5 in the center box. Then the other two numbers along each line have to total 10 for the whole line, including 5, to sum to 15. So just pick numbers for "opposite boxes" that sum to 10.

6. **(a. 11 million b. 8.5 million c. 16 million)** Answers may vary somewhat from these given, particularly (b), but they should be close to these numbers.

7. **(a. 3rd from left   b. $\frac{3}{4}$ or 75%   c. $\frac{1}{4}$ or 25%)** In this problem, the chances of winning are related to the area of the circular space. The white team's space is about $\frac{1}{4}$ of the area of the circle in the 1st and 2nd spinners, and about $\frac{1}{2}$ in the 4th spinner.

Commentary
Saturn, X

1. **(474.25 or 474 1/4 feet, Flights--about 11)** The first part of this problem is simply averaging the four distances given -- 120, 585, 340, and 852. Students might have to look up the number of feet in a mile -- 5,280. They can then divide that number by their average and round off the answer.

2. **(39 or 40 feet)** The scale shows 10 feet. Measuring accurately gives 39.5 feet, so accept an answer anywhere between 39 and 40 feet. It might be interesting to extend the thinking by asking questions such as -- would this plane fit in your classroom? In your garage?

3. **(a. 324 times b. 81)** Students might first find 1/3 of 162 games, then double that amount for 2/3. That answer of 108 is then multiplied by 3, obtaining 324. Very few students will notice that 3 x 2/3 x 162 can be found by simply multiplying 2 x 162. For part (b), students can either find 1/4 of 324 by dividing by 4, or find 25% of 324 by multiplying 324 by 0.25.

4. **(a. 432 ft. b.$694.98)** Students might profit from drawing a sketch of the yard, and labeling the four sides with their lengths. The first answer is obtained by simply adding 96, 120, 96, and 120. The second can be found by dividing 432 by 8 and then multiplying by $12.87.

5. **(4)** It is possible to pull out one of each color marble on the first three draws. Therefore, the fourth marble will match one of the first three.

6. **($95)**   Have the problem below written on several 3 by 5 cards for students to read prior to handing in their paper. They must do the problem in their heads, and simply write the answer in the space provided. Number sense will play a role here, as $18.95 is about $1 less than $20. So 5 times $18.95 should be close to 5 x $20, less $5.

> Chris needs to buy five new shirts for a vacation trip coming up over Thanksgiving. The shirts are on sale for $18.95 each. What is the best estimate of what the five shirts might cost?
>
> a. $75   b. $85   c. $95   d. $105

7. **(7)** Students should be encouraged to *guess-check-revise* to find the value of X. They might try $X = 1$ to start, and see that this results in less than 18 when used in the left side of the number sentence. So they would adjust their guess up, and continue until they found that $X = 7$ produces 18, when the left side is computed.

8. **(a. $1 b. $2.50 c. $1.50)** Snacks consume 20% of Danny's money, and 20% of $5 is 1/5 of $5, or $1. The graph is divided so that his savings are half of his money, and half of $5 is $2.50. The percent spent on entertainment can be found by adding 50% and 20% to get 70%, and realizing that the rest of the chart must then be 30%. The entertainment money is then 30% of $5, or $1.50.

9. **(a. 60 b. 80)** Drawing a picture might help students interpret what "3 boys for every 4 girls" means. They can put together two such groups and know that "6 boys for every 8 girls" is the same ratio, but with larger numbers. Continuing in this fashion, by using ten such groups, they would have the proper number overall -- 140 students, consisting of 60 boys and 80 girls.

Commentary
Saturn, XI

1. **(Howard--Recorder, Jacqueline--Materials Manager, Billy--Time Keeper, Kanisha--Reporter)** Students might make a chart crossing out the jobs that each student does not have. From "Kanisha sits across from the Recorder and next to the Materials Manager," for example, we can mark off that Kanisha has neither of those jobs. A chart and *process of elimination* can therefore be used to match each job with the child.

2. **(a. 4; b. 32)** It would help for students to draw and label a diagram of the floor. For (a), they need a separate 2 by 4 for each 8-ft. side of the plywood sheet, and another to go down the middle. They can buy one more 8-ft. 2 by 4 and cut it in half to get two 4-ft lengths for the short sides of the plywood. This is a total of four 2 by 4's. For (b), the area of the plywood sheet is the amount of carpet to purchase--4 x 8 or 32 square feet.

3. **($90.20)** First, students need to be sure that tapes are cheaper if bought in packages of 3 than in packages of 2. Then the strategy of "buy all the packages of 3 you can first, and finish out with packages of 2" can be used. Seven packages of 3 tapes per package can be purchased for $82.25. Two more tapes are needed to total 23, and one package of 2 will add $7.95 for a total of $90.20.

4. **(80 gms.)** 2 spheres (240 gms) equal 6 boxes, so a box must equal 40 gms. If one sphere and one box (120 + 40) equal 2 pyramids, then each pyramid is half of that sum, or 80.

   Students might be encouraged to begin writing an explanation of how they solve these types of problems using a variable as shorthand notation. For example, they might show the steps above as:
   $2s = 240 = 6b$, so $1b = 40$ from the left scale.
   $1s + 1b = 120 + 40 = 160 = 2p$, so $1p = 80$ from the right scale.

5. **(1st day--54 cans, 2nd day--49 cans)** Students might estimate half of the cans collected as 50, and adjust that number up or down for the two days using *guess and test* to meet the conditions of the problem.

6. **($46.64)** Students with good number sense might think of 20% as $\frac{1}{5}$, and one-fifth of $55 is $11 off, so the sale price of the shoes is $44. Tax is $2.64. Another way to approach the problem, particularly if a calculator is handy, is to realize that she will pay 80% of the regular price and compute $55 x 80%. This amount is then multiplied by 1.06 to "add on" the sales tax in one step.

7. **(735)** It's interesting for students to realize that people who work mentally in arithmetic sometimes follow the "reverse procedure" from what they are taught to do with paper-and-pencil. In this case, James works with the larger numbers first, and works his way down to the smaller numbers. Notice that if he makes a mistake somewhere down the line, he'll probably be close to the right answer because he dealt with the larger number first.

   Have this problem on 3 x 5 index cards for students to see when they hand in their paper. They are allowed to write only their answer down: 21 x 35.

8. **($\overline{FE}$ = 8 ft.; $\overline{CD}$ = 20 ft.; $\overline{BF}$ = 4 ft.)** Students can find $\overline{FE}$ by noticing that it's visually a little shorter than $\overline{AB}$. $\overline{CD}$ is exactly twice $\overline{AB}$. $\overline{BF}$ is less than half of $\overline{AB}$ visually, but not enough less to be 1.

Commentary
Saturn, XII

1. ($\frac{3}{16}$) Students are encouraged to make a diagram. If they do so, they can find the area of the peppers in several ways. The tomatoes take up $\frac{1}{2}$, and the radishes $\frac{1}{4}$ of what is left, or $\frac{1}{8}$ of the total garden. This leaves $\frac{3}{8}$ of the garden for the cucumbers and peppers, to be split evenly. Thinking of $\frac{3}{8}$ as $\frac{6}{16}$, it's easy to see that half of that is $\frac{3}{16}$.
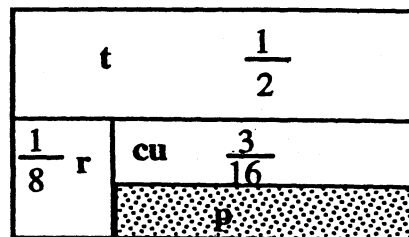
2. **(In 1996, 293 years; in 1997, 294 years; etc.)** This subtraction problem can be enhanced with a little Florida history about St. Augustine being the oldest city in the United States.

3. **(6 outfits)** One strategy is to make a chart, as below. Another is to make a diagram.

	red shorts	white shorts	blue shorts
red shirt	4	4	4
white shirt	4	4	4

4. **(18)** One strategy is to work backwards, asking students what they would have if they had not subtracted 6. They should see that they would have 42. Therefore, something times 7 equals 42. Knowing that the something must be 6, they will recognize that 18 divided by 3 equals 6. Another approach is to *guess-check-revise*. They could start by guessing a number like 30 for n, and check to see that 30 is too high because [(30÷3) x 7 – 6] gives 64, not 36. So they would adjust the guess down, and try again.

5. **(D, or 7/10)** Students could place these numbers on a number line or divide a piece of paper into pieces for comparison. Another method would be to change them all so they have a common denominator (30 is the least such) and compare the resulting numerators.

6. **(a little less than 7 miles high)** 5,280 is a little more than 5,000. 5,000 goes into 35,000 exactly 7 times. So 5,280 would go into 35,000 a little less than 7 times.

7. **(4.5 mi.)** The 45-mile race would have no checkpoints at the start and finish lines. A picture will show that there are 9 checkpoints resulting in 10 spaces between "start" and "finish."

8. **($2\frac{1}{2}$ hours; increasing; constant; last half hour)** This problem has students look at a line graph and interpret it visually. The graph stops at about $2\frac{1}{2}$ hours along the time axis, meaning it took him about $2\frac{1}{2}$ hours to finish. The line is going up at a constant rate during the first half hour, so his speed is increasing.) During the second half hour, the line is horizontal (meaning his speed was constant. The line is at its highest point during the last half hour, meaning that during this time period he was traveling at his greatest speed. An extension activity would be for students to make their own graph of his trip, to match a story they make up about his speed, and to included his check-point stops.

Commentary
Saturn, XIII

1. **(13)** Students might forget that the 9 remaining when 129 is divided by 10 represents seats which are needed for the class. Twelve rows would not be sufficient.

2. **(about 100 pounds per month)** Students will need to read carefully--the amount produced annually is given in tons, but the answer is asked for in pounds. Students can multiply tons of garbage per year by 2,000 to get pounds per year, then divide by 12 to get pounds per month. This result is then divided by 250 million to get each person's share per month. The actual answer is about 103 pounds per month, but any reasonable answer should be accepted.

3. **(1st row: 8, 1, 6; 2nd row: 3, 5, 7; 3rd row: 4, 9, 2)** There are several possible solutions to this magic square. One possibility is given. Students may be encouraged to use number tiles to help solve the problem. One strategy that would help is to assume the center number might be 5, which is the middle number of 1-9. Then you know that "opposite diagonal numbers" must sum to 10, so place 8, 6, 4, and 2 in the diagonals in this fashion. Continue making good guesses, checking, and making adjustments as called for.

4. **(25, 36, 49; yes; no)** Students can continue making figures by hand, if necessary, but hopefully they will notice a relationship between the number of the figure (1st, 2nd, 3rd, ...) and the total number of dots in the figure (1, 4, 9, ...). The next figure in the pattern would have 5 dots on each side, and so 25 in all, and so on. 100 is a square number because a 10-by-10 square can be formed from 100 dots. 200 is not a square number -- a 14-by-14 square would have 196 dots, and a 15-by-15 would have 225.

5. **(5)** The rectangles are: 1 x 36; 2 x 18, 3 x 12; 4 x 9; 6 x 6

6. **(c)** Students would enjoy experimenting with these three ways of earning money, using a calculator. (a) would give you only $0.50 x 31 or $15.50 for the month. (b) would give you the sum of the numbers from 1 to 31, multiplied by $0.10, or $49.60. (c) shows the power of doubling -- by the 15th day, for example, you would make $163.84 on that day alone. Using the calculator, your group will notice the rapidity with which the product increases when the number doubles daily.

7. **($\frac{2}{4}$ or $\frac{1}{2}$; $\frac{1}{4}$)** Since the four aces have two red ones (hearts and diamonds), the chances of pulling a red card at random are 2 in 4 (written either $\frac{2}{4}$, $\frac{1}{2}$, or 50%). There is one club out of the four cards, so the chances of pulling a club at random from the bag is 1 in 4, written as $\frac{1}{4}$ or 25%.

8. **(far right card)** Students with good spatial visualization skills will find this card quite readily. Other students may profit from actually drawing the design on a thin sheet of paper, and follow the steps in order holding the paper up to the light to see what happens.

9. **(0)** Students with good operation sense will realize, if they "look ahead" in the problem, that the answer is zero. Any number multiplied by zero results in zero, so if zero is one of the factors shown in a multiplication problem such as this, the answer is automatically zero.

Commentary
Saturn, *XIV*

1. **(answer shown below)** These visual puzzles become increasingly difficult, but notice that some students will see the analogies immediately. In (a), the figure goes simply from unshaded to shaded. In (b), only two-thirds of the figure is considered, and it also goes from unshaded to shaded. In (c), the figure turns 180°.

    a. ●   b. ◼   c. ▢

2. **($\frac{1}{8}$)** Students might guess-check-revise to find the fraction, or they might notice that $\frac{4}{8} + \frac{5}{8}$ will give $\frac{9}{8}$, so $\frac{2}{8}$ must be removed to produce $\frac{7}{8}$. Since there are two fractions to be subtracted, $\frac{2}{8}$ can be written as $\frac{1}{8}$ twice in the spaces, fulfilling the conditions.

3. **(Missing information -- How much paper is in each pack?)** There is not enough information given to solve the problem.

4. **($404)** There are a number of ways that students might approach this problem. Akeem makes $8 x 40 = $320 for his regular work week. The remaining 7 hours is overtime, at "time and a half." Time and a half means $8 + $4 for each hour, instead of $8. So the overtime pay is $12 per hour. $12 x 7 = $84. $320 + $84 = $404.

5. **(Bachie -- 10 hrs, $57.50; Dustin -- 4.5 hrs, $25.88; Monica -- 8.5 hrs, $48.88)** Students can count from the In time to the Out time to find the hours worked. These hours might be written as a fraction also. Multiplying the hours worked by $5.75 gives the resulting amount earned. This is easy to do using a calculator if the hours are written as a decimal instead of as a fraction. Dustin's and Monica's "amounts earned" have been rounded up to the nearest cent.

6. **(9, 16, 100, nxn or n^2)** Students might be encouraged to build these figures out of cubes, and look at the pattern that occurs.

7. This problem encourages students to internalize what it means to *bisect an angle* before they meet the term later and are expected to use a compass to perform the task. They can hold the sheet of paper up to a light source, and fold the paper so that the two sides of the angle match up. Paper folding can also be used to teach terms such as *perpendicular bisector of a line segment*.

8. **(odd, even, yes)** Opening an actual book and looking at the page numbers will enable students to internalize what this problem means. Books universally start with page 1 on the right-hand side. The right-hand page numbers from there on, therefore, are always *odd*. The left-hand page numbers are always *even* numbers. An *odd* added to an *even* always gives an *odd* number. An *odd* times an *even* always produces an *even* number.

Commentary
Saturn, XV

1. **(Ms. Hill - $10, Mr. Booth - $12.50)** Ms. Hill buys 50 shares for $500, and makes $0.20 on each for a total of $10. Mr. Booth buys 25 shares for $500, and makes $0.50 on each for a total of $12.50.

2. **(Tiffany has $20.50, Ivan has $0.50)** Subtracting $20 from $41 leaves $21 for Tiffany and Ivan together. Therefore, Ivan must have $0.50. Any other amount would mean Tiffany has more or less than $20 more than Ivan.

3. **(265)** When the students turn in their paper, have this problem on 3x5 cards for them to solve: $735 + \underline{\hspace{1cm}} = 1000$ Students MAY NOT use pencil, paper, or a calculator.

4. **(30 people)** A diagram such as the one to the right will help students realize that 30 have been invited altogether.
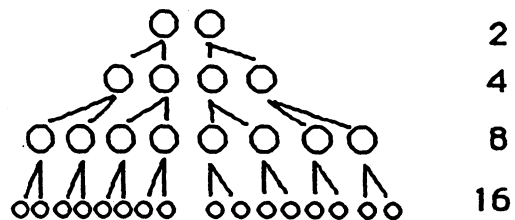
5. **(B)** $17 = 25 - p$ has the solution 8, which is the same solution as for $n + 13 = 21$. Students might be encouraged to think of the variable as representing a number they are searching for, to make the given statement a valid one. They can solve these by *guess-check-revise*.

6. **(11)** Students might divide 238 by 23 and get 10 r 8, or add 23 until they get close to 238, counting the number of times they add. In any approach, 10 boxes hold 230 puzzles, with 8 puzzles left for the 11th box.

7. **($20.51)** One approach is to multiply $18.99 times 8%, rounding up to get the tax on the jacket. Add this tax to the price.. A one-step approach is to multiply $18.99 by 1.08.

8. **(The answer is shown to the right.)**
Students can use number clues to narrow down the choices for the box on the top row. Once that box is determined, the rest can be obtained by computation.

9. **("HI" is spelled out, backwards)**
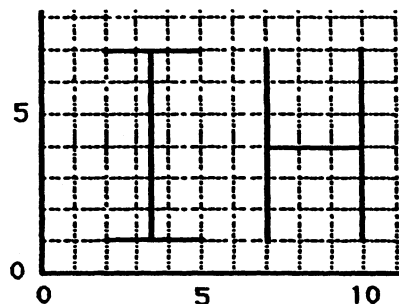
Commentary
Saturn, *XVI*

1. **(6.8 cm)** One approach is to add sides given and subtract the sum from the total perimeter. Another is to subtract each known side individually from the total.

2. **(See the worked-out problem to the right.)** Students who are new to this type of problem might begin at the end, and "work backward." (i.e., the box above 9 must have a 9 in it, which means that the box above it must be a 6 since that's what subtracts from 5 to get 9.) A few clever guesses and checks from this point will result in the solution.

   $$\begin{array}{r} 27 \\ 13\overline{)351} \\ \underline{26} \\ 91 \\ \underline{91} \\ 0 \end{array}$$

3. **(2.50; 1.20; 130.0)** If students have not been taught to move the decimal point in divisor and dividend, they can think of these problems as explained below.

   a. $1.25 \div 0.5$ means how many 1/2s are in 1 1/4. They can draw a diagram to find the answer is 2 1/2.

   b. There would have to be about one 7/10 in 8/10 because they're about the same size. So the only reasonable choice, of those given, is 1.20.

   c. They can think of (c) along these lines: there are 10 one-tenths in 1 whole, so there would be 13 x 10 one-tenths in 13. Therefore the answer is 130.

4. **(75)** The average would be found by adding 100, 90, 85, 78, 0, 80, and 92, and dividing by 7. Some students may mistakenly think that 0 doesn't count, and divide by 6 instead.

5. **(86)** You would follow the same steps as in number 4, but replace 0 with 70. Hopefully students will realize how important it is, if they are graded by an average, to not have a 0.

6. **(a. $2a - 3$; b. $10h + 3$; c. $3 + \frac{1}{2}d$; d. $5x + 5.8$)** Note that alternatives to the answers given should be accepted. For example, other common ways of writing (a) include $a + a - 3$ and $2 \times a - 3$. Students need much practice with expressing these types of verbal situations mathematically, using variables.

7. **((a.) $\frac{26}{8}$ or $3\frac{2}{8}$ or $3\frac{1}{4}$ (b) 3)** Drawing a picture will help students count the 26 total blocks, and see that the total length is $26 \times \frac{1}{8}$ or $\frac{26}{8}$ miles. Their only task, then, is to express this amount as a fraction, mixed number, or possibly a decimal.

8. **(225)** Three $1\frac{1}{4}$'s is $3\frac{3}{4}$ total hours, which is 3 x 60 + 45 minutes.

9. **(B)** The chance of drawing a black marble is 3:5 for A, and 2:3 for B. Doubling and tripling, etc., these ratios until you find a "common unit" for the comparison is a good strategy. 3:5 is the same as 6:10, 9:15, etc. 2:3 is the same as 4:6, 6:9, 8:12, and 10:15. Notice we finally have a common unit -- 15 -- for comparison purposes. Since 10:15 is a higher ratio than 9:15, box B gives the best chance.

Commentary
Saturn, *XVII*

1. **(604)** Have this problem -- $4\overline{)2416}$ -- prepared on 3x5 cards to give to students when they are about to hand in their paper. They can only write the answer, doing the division mentally.

2. **($3000)** $89 is about $90, and $90 x 4 weeks per month x 8 months = $2880, or $3000 to the nearest thousand.

3. **(131, 767, 505, 8998 are examples of correct answers)** Check to see if the numbers written are the same when the numbers are reversed, left to right.

4. **(This sentence is a palindrome made from letters instead of numbers.)** Some students who might not have seen the visual pattern in problem 3 will see the pattern here, and then can return to problem 3. Single words can be palindromes -- MOM, POP, BOB-- for example.

5. **(400,000,000)** Students can multiply 70 x 60 x 24 x 365 on a calculator, but the display will then be filled on an 8-digit model by 36,792,000. Multiplying this by 10 can be done mentally, giving 367,920,000. Rounded, the answer is 400,000,000.

6. **(60 and 30)** Students will need to realize that a right angle has 90°, and that the 2 equally spaced marks for 1:00 and 2:00 divide the 90° angle into three equal parts. The second hand pointing at 2:00 divides the 90° angle into 2/3 of 90° and 1/3 of 90°.

7. **(4, 2, 5)** The 13th digit will be the next one in line, and the pattern is ready to repeat again. Therefore the 13th and 14th digits will be 4 and 2. To find the 100th digit, notice the pattern repeats every 6 digits. 6 x 16 = 96, so the pattern will be ready to start repeating again with the 97th digit. The 97th digit is 4, the 98th is 2, the 99th is 8, and the 100th is 5.

8. **(One arrangement of the chart is shown below.)** The entries could be rearranged, but the sum of the numbers in each column must be 11, and the larger number must be on top.

Oranges	10	9	8	7	6
Watermelons	1	2	3	4	5

8. **($44.03)** Students may go through steps of finding the per cent and sales tax as separate processes, adding or subtracting them to the base figure they're working from. Or they might take a shortcut of taking 90% of the total cost of $46.15, and then multiplying by 1.06. On a calculator, this can become an easily done 2-step problem.

Commentary
Saturn, *XVIII*

1. **(a. 8; b. 6)** There is only a 2 in the circle for fish, meaning that there are 2 children with only fish for pets. There are 6 kids in the overlap area of dogs and fish, which means that 6 have both dogs and fish. So there are 8 altogether that have fish.

2. **(5.75)** The distance you ran before turning around, and the distance back to the starting point, was 3 miles. Then 2.75 is added to the first 3 miles.

3. **(19,000)** Multiplying 735 times 26 gives 19,110. Since this is only an approximation situation, rounding to the nearest thousand turns makes sense. 19,110 is closer to 19,000 than to 20,000, so it is rounded to 19,000.

4. **(2 hours, 45 minutes; 9:15; increasing)** The problem involves looking at a graph over time, and making judgements about the real-world situation from the shape of the curve. The curve stops at the 3rd "tick mark" after 10:00, and each tick mark stands for 15 minutes. So the race must end at 10:45, and lasted 2 hours 45 minutes. The rider stopped when the speed drops to zero, which is at 9:15. The line is steadily on the rise between 10:00 and 10:30, so his speed is increasing.

5. **(0.77)** There are 3 typical ways that students might make mistakes here. First, they might not "line up the decimal points" when adding the numbers -- if using a calculator, this won't be a problem. Second, they might divide by 4 instead of dividing by 5, forgetting to count Friday as the fifth day, with 0.00 inches. And last, they might try to "round off the answer", although it's unnecessary since it's already only to the hundredths place. The computation *(1.66 + 0.23 + 0.75 + 1.2) ÷ 5 = 0.77* shows how to successfully solve the problem.

6. **(32)** Students can actually fold a sheet of paper to find the answer, if they don't have good visual skills.

7. **(18)** This can be thought of as a ratio problem. Three books every two weeks means 6 books every 4 weeks (or 1 month). Six books each month means 18 books for three months (or the summer).

8. **(3.3 and 3.8)** The line is divided into 10 parts. The arrows point to the 3rd and 8th *tick marks*. The answers can either be written as decimals (3.3 and 3.8) or mixed numbers ($3\frac{3}{10}$ and $3\frac{8}{10}$).

9. **(3 yards, 1 foot, 8 inches)** There are several ways to approach this problem. One way is to convert 10 yards, 2 feet into 384 inches, divide that by 3 to get 128 inches for each girl, then convert 128 inches into feet and yards by dividing first by 12, then by 3. Another, more challenging way is to solve the long-division problem below:

$$3 \overline{)\ 10 \text{ yards } 2 \text{ feet } 0 \text{ inches}}$$

The challenge above is in renaming the number obtained after the subtraction step of the process, and joining it with the next digit.

Commentary
Saturn, XIX

1. **(1, 5, 14, 30)** Stuents can find these answer by actually counting squares. They are encouraged to do so in an organized fashion, starting with the smallest individual squares, then moving up to count larger squares.

2. **(yes, 385)** The pattern does work for the next figure in line -- students can verify this by actually counting individual squares again. Assuming the pattern holds, the 10th figure would have $1^2 + 2^2 + 3^2 + 4^2 + 5^2 + 6^2 + 7^2 + 8^2 + 9^2 + 10^2 = 385$ squares.

3. **($15.89)** Multiply the price of the calculator times 6% and add that amount to the cost of the calculator. Or, you could do this all in one step on a calculator, by multiplying $14.99 x 1.06, rounding up the answer.

4. **(See the chart to the right.)**

		2	3	4	5
a.	6,945		✔		✔
b.	1,236,240	✔	✔	✔	✔
c.	54,208	✔		✔	

5. **(See drawing to the right.)**
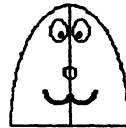
6. **(The completed puzzle is shown to the right.)**
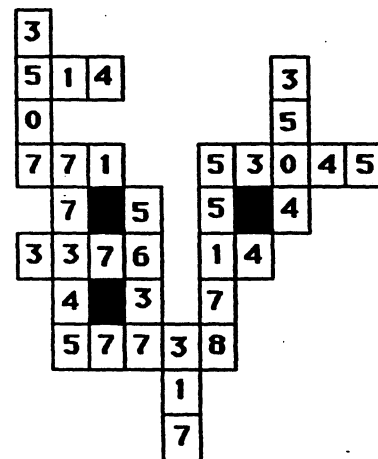
7. **(The completed problems are shown below.)** Look carefully at the partial products, as well as the answer. The partial products are where the differences show up.

$$
\begin{array}{r} 14 \\ \times 26 \\ \hline 104 \\ 260 \\ \hline 364 \end{array}
\qquad
\begin{array}{r} 31 \\ \times 53 \\ \hline 53 \\ 1590 \\ \hline 1643 \end{array}
\qquad
\begin{array}{r} 27 \\ \times 42 \\ \hline 294 \\ 840 \\ \hline 1134 \end{array}
\qquad
\begin{array}{r} 62 \\ \times 135 \\ \hline 270 \\ 8100 \\ \hline 8370 \end{array}
$$

Commentary
Saturn, XX

1. **(28)** Encourage students to experiment with several other numbers less than 10, to check and see if they are *perfect numbers.* This will give them a feel for what they are searching for. The proper factors of 28 are 1, 2, 4, 7, and 14, and their sum is 28.

2. **(See problem to the right.)** Working backwards will help the students find the missing digits quickly.

$$
\begin{array}{r}
317 \text{ r } 25 \\
27\overline{)8584} \\
\underline{81} \\
48 \\
\underline{27} \\
214 \\
\underline{189} \\
25
\end{array}
$$

3. **(a. 364 yards b. 4 strokes c. 36 strokes)** Students unfamiliar with golf might profit from looking at a golf score card from a local course. Usually those cards have a picture of the course, with the yardage for each hole and the par for the hole. Looking at such a card and discussing the game in general -- how long a good drive might be, etc. --will help them understand the terms. The average distance per hole is found by computing 6550 ÷ 18; the average number of strokes per hole is given by 72 ÷ 18; Carlos was 108 - 72 or 36 strokes over par.

4. **(350 ml)** Students can simply look at a can of soda. They might also be encouraged to visualize a can of soda as about 1/3 liter.

5. **(122 oranges)** *Working backwards* is one strategy. Shomika had 26 oranges so that she could give Josie 1/2 of that, plus 3, leaving 10. Shomika had 58 oranges so she could give Angela half, plus 3, leaving 26. Shomika started with 122 oranges so she could give half, plus 3, to Jennifer, leaving 58. A different way to begin the problem is to *guess-check-revise.* You might begin by guessing 100, checking to see if Shomika winds up with 10 in the end. If not, revise the guess either higher or lower, depending on the result.

6. **(34)** Students should compute inside the parentheses first, then multiply before subtracting, following the *order of operations* rules.

7. **(a. 27 b. 63%)** There are 13 + 4 + 10 or 27 students. The diagram shows that 17 students like chocolate cupcakes. 17 out of 27 is the same as 17/27 or 17 ÷ 27, which is 63% when rounded to the nearest whole percent.

8. **(The fold line should show a line that forms 90° angles with the one given).** Students can find such a fold line by holding the paper up to a light source, and folding it so that the lines seen through the paper fall on top of each other. This problem can be expanded into finding the *perpendicular bisector* of a line segment. In this case, the endpoints of the segment would also have to line up, to be sure the fold cut the segment exactly in half.

9. **(2:30)** The boys worked five hours, and had a total of another hour of breaks. They were therefore at the clean-up site for 6 hours, starting at 8:30.

10. **(1 week, 5 days, 18 hours, 51 minutes)** This problem asks students to rename given units of time before subtracting. The value is that students will see that regrouping for subtraction requires them to think about the units involved.

Commentary
Saturn, XXI

1. Mental math should help students solve this problem. Below is one possible set of answers. Accept other correct solutions.

 | | |
   |---|---|
   | 4 - 2 X 1 = 2 | 4 + 2 + 1 = 6 |
   | 4 - 2 + 1 = 3 | 2 + 1 + 4 = 7 |
   | 4 + (2 - 1) = 4 | 4 X 2 + 1 = 8 |
   | 4 + 2 - 1 = 5 | 4 X 2 + 1 = 9 |

2. **(66 mi., $74.80)** If Brad can go 3 miles on each gallon, he can go 3 x 22 miles on 22 gallons. If each gallon costs $3.40, then 22 gallons cost $3.40 x 22.

3. **(a. 1,207 miles, b. 87,000 miles)** The nearest city is London, at 3,458 miles. The farthest is Moscow at 4665 miles. The difference is 4,665 – 3,458, or 1,207 miles. Round trip to Paris is 3,624 x 2; that distance 12 times is 86,976 miles, or about 87,000 miles.

4. **(about 8,250,000 heads of lettuce)** Multiply 11,000 x 1,500 x 1/2. Drawing a picture of the acreage might benefit some students.

5. **(Harry: $5.62 and William: $3.37)** There are a number of ways to approach this problem. One is to divide $8.99 by 8, getting $1.12 per slice. Then multiplying by the number of slices will produce the answers. Another way is to realize that Harry ate $\frac{5}{8}$ and William $\frac{3}{8}$, convert each of those into a decimal or a percent, and multiplying each by $8.99 to get the answers.

6. **(See picture below.)** Students will use clues and measuring skills. Measure to be sure that the distances are correct. Answer below gives correct relational locations, but distances are approximations.
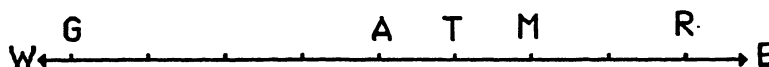
7. **(See picture below.)**
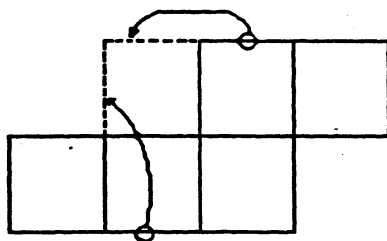
8. **($1.85)** Two pair for $1.98 means another pair can be purchased for half that, or $0.99. The total is then $2.97. Adding tax can be done by multiplying by 1.06 on a calculator, giving a total cost of $3.15. The change can be "counted up" from $3.15 to $5, getting $1.85.

9. **($\frac{28}{12}$ or $2\frac{4}{12}$ or $2\frac{1}{3}$)** Students can use the common denominator 12, convert each fraction to that denominator, and add or subtract the numerators. An interesting real-life problem for these numbers would be to use several 12-packs of colas to show the fractions.

Commentary
Saturn, XXII

1. **(40)** Rather than trying to solve this equation through computation, students might think of solving it by asking "What number could p be so that so 3/4 of its weight is 30?" Intuition will lead most students to think of trying 40 for p, and asking "Is 3/4 of 40 equal to 30?" Yes, so their intuition is correct.

2. **(90 in^2)** Students might cut out a sheet of paper this size, and line it up repeatedly to approximate the area. Some students might think of marking off inches along the length and width, and computing with those numbers. A few might know that a sheet of paper like this is 8.5 by 11 inches, giving an actual area of 93.5 in^2.

3. **(Line graph shown to the right. Accept any answer over 2 billion for population in 2000 AD)** This problem might draw students into a discussion about the world's population and what will happen if it continues to grow unchecked.
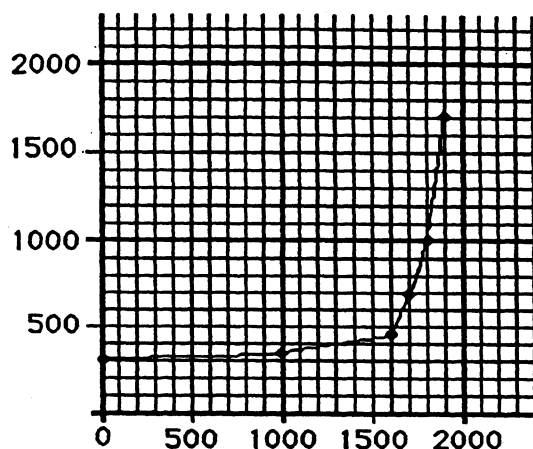

4. **(124, 154, 300, 3 x n + 4)** It's difficult to tell what the machine is doing by looking at what happens to the first few numbers. A hint as to what the machine is doing (multiplying by 3, then adding 4) can be gained by looking at what happens to 10 and 100.

5. **(3,800)** If 3,400 is 90% of the number sought, then 3,400 can be divided by 0.90 and rounded to the nearest 100. Students may discover other ways to find this number, such as guessing what number from {3500; 3600; 3700; 3800; 3900; ...} might work, and checking to see if 90% of each gives 3400. Allow them to feel comfortable with their methods.

6. **(... so she would get back only one coin in change)** This is a common practice among people who have good number sense, and should be encouraged for students as it provides continuous practice with mental mathematics in a real-world setting.

7. **(4026 x 8)** One way to approach such a problem is to begin by seeking digits that would produce 32 in the thousands place of the answer, 4 and 8. From that point, *guessing and checking* will lead to the answer.

8. **(a. 11, 13, and 15; b. 99; c. 1999)** It's easy for students to go from one figure to the next, in progression. They will notice that these are the odd numbers in sequence. To find the number of dots in the 50th figure, some will actually count the odd numbers that far, while others will begin to approach it analytically -- the 50th odd number is one less than twice the number. This type of generalization is almost a necessity for obtaining the number of dots in the 1000 figure. An extension is to ask students, given the figure number n, what algebraic expression tells the number of dots needed?

91

Commentary
Saturn, XXIII

1. **($2.91)** The three girls' combined money is $7.04. Subtract this from the $9.95.

2. **($x = 26$; $y = 37$; $z = 9.2$)** These problems present solving simple equations in a way in which students can follow the logic of the steps typically involved. In the first, removing 2 from each side of the scale leaves the scale still balanced, and the cake weighing 26. This is called *isolating the variable*. In the second picture, intuitively you divide both sides of the scale by 3 to find what one clock weighs. In the last picture, if you remove 5 from the scale, 4 coins remain and weigh $41.8 - 5 = 36.8$. Then dividing by 4 means that each coin would weigh 9.2.

3. **(b. 30)** $13\frac{38}{39}$ and $7\frac{16}{17}$ both have fractions that are very close to 1, so these mixed numbers can be rounded to 14 and 8. $4\frac{1}{9}$ and $4\frac{1}{42}$ have fractions close to zero, and so each can be rounded down to 4. The estimated sum is then $14 + 8 + 4 + 4$ or 30. This is a good measure of *number sense.*

4. **(a. 40 sq. units)** In this problem, students can estimate the area of a figure visually. There are a number of ways to do this. One is to count whole and then partial squares, putting together partial ones to get whole ones. Another way is to count all the whole ones, and then just count the partial squares and divide it by two, which assumes that the partial squares will average about 1/2 sq unit each. There are many other ways to get the estimate.

5. **(See the diagram to the right.)** The difficult part for some students will be to remember to put in the diagram the number of people who liked neither store.
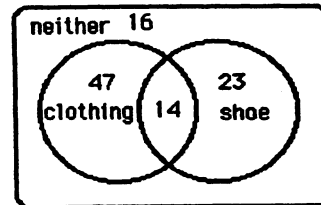
6. **(8,000 mi.)** This can be thought of in several ways. One approach is to reason as a ratio — 2,000 miles in 1.5 minutes is 4,000 in 3 minutes, 6,000 in 4.5 minutes, and 8,000 in 6 minutes. Another approach, if a calculator is handy, is to find out with $2000 \div 1.5$ that the shuttle is travelling 1333.33 miles per minute; this number times six minutes would be 8,000.

7. **(Neither)** The probability of pulling out a penny is 1 out of 2, in both cases.

8. **($1.80)** Students can find 1/6 of 18 coins and know that there are 3 quarters, 1/3 of 18 is 6 dimes, and 1/2 of 18 is 9 nickels. These coins add to $1.80.

9. **(15, 9, $8\frac{1}{2}$)** These 3 figures get progressively more difficult to find the area by counting unit squares. The first and second, when grid lines are drawn in, can be found by counting whole squares and half squares. The third figure can be partitioned so that rectangles are drawn around certain trianglular parts. Since the area of the triangles are half of the surrounding rectangles, the partial areas can be found this way and summed for the total. One way to do this is shown.
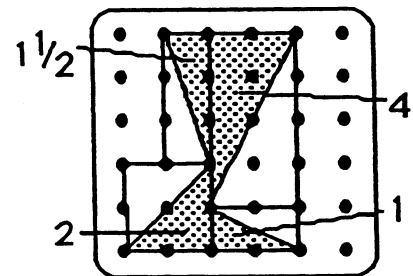
Commentary
Saturn, XXIV

1. **($1,010,000)** Students can perform arithmetic to find that 40,400 attended those two games. Students might enjoy investigating such large amounts of money for several sports events in large facilities in their state or across the country.

2. **(a. 100%, b. food, c. $2,400 d. $4,200)** (a) Students should recognize that the whole circle always represents 100% (b) Compare the percents for food and education. (c) Multiply 12% times $20,000. (d) Add 7%, 8%, and 6%, then find 21% of $20,000.

3. **(1:45)** Students with good spatial sense will likely get this answer immediately, if they realize that a mirror reverses images left-to-right. For students who have trouble visualizing the situation, they can actually hold the paper up to a mirror to see the time for themselves, or possibly hold the paper to a light source, turn it over, and look at the clock from the back side.

4. **(98.70 mph)** Round to the nearest hundredth.

5. **(a. 3 x x + 2, b. 100 -2 x s, c. $\frac{1}{2}$ x t -2)** The importance of students being able to rephrase real-world situations using a variable makes problems like this extremely valuable. It is unlikely at this stage that the students will have encountered the "shorthand notation" of writing 3 x x, 2 x s, and $\frac{1}{2}$ x t as 3x, 2s, and $\frac{1}{2}t$. It is unnecessary for them to use such conventions at this age.

6. **(a. 800)** Students can count the bricks along the length and width, and find that there are 36 rows with 21 in each row, for a total of 756 bricks. Notice that students can't count them all because of the lawn furniture and trees partially blocking the view. 800 would give some extras, but not so many as to cost a great deal more money. 700 is obviously too few.

7. **(b. 25°)** 25° C (or 77° F) is about room temperature. Most swimmers begin when the weather gets that warm. Students should develop benchmark temperatures in both Fahrenheit and Celsius -- such numbers as when water freezes and boils, their own body temperature, a cold drink, and so on.

8. **(7)** A drawing of the trips across, and what is left on the bank each time, is shown below:

93
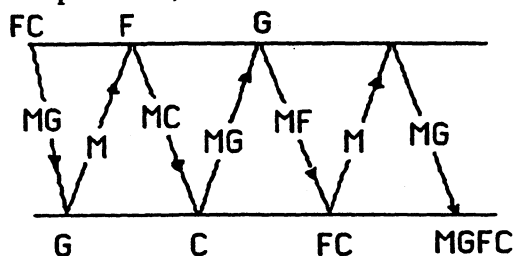
Commentary
Saturn, XXV

1. **(16 items -- 15 bats and 1 mitt or 14 bats and 2 mitts)** One approach is to make a chart of all of the combinations which could be purchased, and select the entry which gives the largest number of items. Another approach is to realize that the way to get the largest number of items is to purchase only one at the higher price, and spend the rest of the money on the lower priced items.

2. **(6/7)** Students can use *guess, check, revise* to find their answer. Number sense will tell them not to try fractions with the numerator bigger than the denominator, and that the numerator must be fairly close to the denominator in size.

3. **(a. $3.25   b.$1.75   c. see list below)**
   small fries, hot dog   *small fries, small shake*
   small fries, small cola   *large fries, small cola*
   small fries, large cola   *large fries, large cola*

4. **(325)** Elvira will have to multiply 13 by 5 to return to the previous stage in the problem, and multiply by 5 again to finish the problem correctly. The real answer, then, is 13 times 25 or 325.

5. **(a. the weight of one pup; b. the weight of all 6 pups is 6 X W ; c. 7 pounds)** This problem is designed for students to see a real-world use of algebraic equations, but one which they can solve by using *number sense.* At this point, they should attempt to find the value for W in any intuitive way that makes sense to them. Some will want to subtract 8 from 50, then divide by 6. This is the typical method that will be taught later and is fine if done intuitively. It's also acceptable for students at this point to simply search for a replacement value for W that makes sense. They can use *guess-check-revise* for this approach.

6. **(a. 30' by 40'; b. 600 ft^2)** Part (a) of the problem is easily solved by simply labelling the diagram of the pool, and adding on the extra 10 feet to each dimension. Students might approach part (b) in several ways. One is to calculate the area in square feet of the 30 by 40 pool and walk combined, and then subtract the area of the 20 by 30 pool itself. Another approach is to partition the concrete walk itself into smaller pieces, find the area of each, and add them together -- there are several ways to partition the walk in this fashion. Both approaches are shown below:
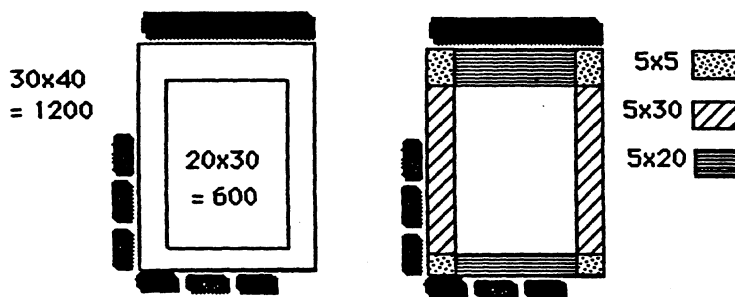

7. **(2 sections will be red, 4 will be blue, and 2 will be green.)** This problem should help students see a real-world example in which $\frac{1}{4} = \frac{2}{8}$ and $\frac{1}{2} = \frac{4}{8}$ is intuitively obvious. Visually they can see if they have $\frac{1}{4}$ or $\frac{1}{2}$ of the spinner shaded, so they can count the sections.

Commentary
Saturn, XXVI

1. **(70,500 miles)** Drawing a diagram will help students see that, to find the distance from the center to the outer edge of the rings, they need to find the radius of the planet, or 35,500 miles. This number is then added to the distance to the edge of the rings, 35,000.
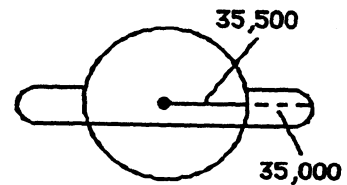
2. **(The circles will appear as shown below.)** Students might try tracing the angles given using a dark pencil or ink pen, so the angle will show through from the underside of the paper. They can then use this dark angle to trace the angles in their circle.
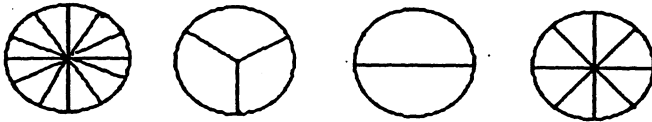
3. **($\frac{1}{8}$, $\frac{1}{16}$, $\frac{1}{32}$; 16 comes three numbers before 2)** Students should notice that each number of the pattern is one half the previous number. Making a rectangle and sketching in 1/4 will help them find 1/2 of 1/4, and then 1/2 of that, and so on. In this manner they will have a visual image to show that taking half of a fraction doubles the denominator. The pattern still holds, going to the left.

4. **(30 stamps)** Anne gave the first 50 stamps to Sam, leaving 75 stamps to divide. Each of the five friends would then receive 15 stamps.

5. **($\frac{12}{45}$, 20 tally marks, $\frac{20}{45}$)** The fraction $\frac{13}{45}$ combines the tally mark information with the number of spins, 45. In a similar fashion, the second fraction would then be $\frac{12}{45}$. The tally marks for green must then be 20 as they all sum to 45. The missing fraction is then $\frac{20}{45}$.

6. **(The completed problem is shown to the right.)** Students might find it easier to work backwards on this problem. If so, they can fill in the lower boxes first, simply by finding missing addends. Then number sense can take over and they can find the two missing numbers in the two numbers being multiplied.

$$\begin{array}{r} 922 \\ \underline{\times 18} \\ 7376 \\ \underline{9220} \\ 16596 \end{array}$$

7. **(Susan is 15, Andrea is 5, and Barbara is 10)** Using *guess, check, revise* as a strategy, students may try various ages. It's probably easier to always start guessing with the youngest person's age, compute the others from that, and check against the conditions.

8. **(b. Slow down! ...)** Students will use different approaches in this problem. One obvious one is to divide 24 minutes by 3 miles and get that Andy needs to run each mile in 8 minutes. Therefore he needs to run 2 miles in 16 minutes, and he is running faster than that. Some students might have a difficult time accepting the strategy of slowing down in a race, if they have never run a long distance.

Commentary
Saturn, XXVII

1. **(34)** The problem is not difficult to solve, except that some students will forget to count Brandon himself.

2. **(d)** There are 14 coins, 7 of which are pennies. Therefore a penny will be drawn about half the time. So out of 10 draws, you would expect to get 5 pennies. Students might enjoy testing this theory by actually drawing coins at random.

3. **(See one solution to the right.)** This computational puzzle is one which has a number of different solutions. Students will enjoy coming back to this puzzle throughout the year, and will usually get a different answer each time. One hint which might get students started is to realize that 10 must go in the top row, because it can't be the difference of two other numbers.

```
 6   10   1   8

   4   9   7

     5   2

       3
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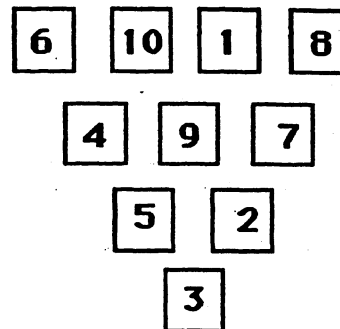
4. **(0, 1, 2, 3, 4)** Students can intuitively see that y must be a whole number less than 5. Some students might not include 0 in the solution because the physical situation -- an object on a scale -- would naturally have some weight. Give them credit if they do not include 0, but be sure they understand that some things (Styrofoam and plastic wrap used in grocery stores to wrap meat, for example) have such a miniscule weight, that they are counted as 0.

5. **(125; 250; 50; 75)** There are a number of ways students can use *number sense* to find 1/4 of 500, 1/2 of 500, and 1/10 of 500. One hint for a student having trouble is to think of the 500 as 500 pennies, or $5. Once they determine the first three fractional parts of 500, they can then find the remaining number -- the cups -- by subtraction.

6. **(28 mm; 10 m; 3 km; 30 m)** Students should be encouraged to remember benchmark measures for distances in the metric system, and use those for estimation purposes. They might remember something that is a millimeter long, a centimeter long, a decimeter long, a meter long, and a kilometer long.

7. **($22.50)** Students should use the form of a percent that makes sense for a given problem. In this case, knowing 25% is equivalent to 1/4 might enable them to easily find one week's savings, as they can divide $10 into 4 equal shares. $2.50 a week for 9 weeks is $22.50.

8. **(a. 16 b. 26 c. 4 d. 4 to 140)** For students who are new to Venn diagrams, it would be helpful for them to start with some simple ones -- limited to 2 circles -- to understand what the various numbers mean, in overlap areas. They can gradually increase the difficulty.

Florida Department of Education