

Challenge 1: Comparing 3 and 4

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Dataset Creation

Your dataset should have in total 1000 randomly selected digits (feel free to use a `set.seed` command so that your results are reproducible). Your training dataset should have 800 observations and your testing should have 200 observations.

Our Approach

We have seen in class that the MNIST database (Modified National Institute of Standards and Technology database) is a large collection of handwritten digits used by the Machine learning community. The `dslabs` packages has a handy function called `read_mnist` that allows to load this dataset as follows:

```
mnist <- read_mnist("~/Mscs 341 S22/Class/Data")
str(mnist)

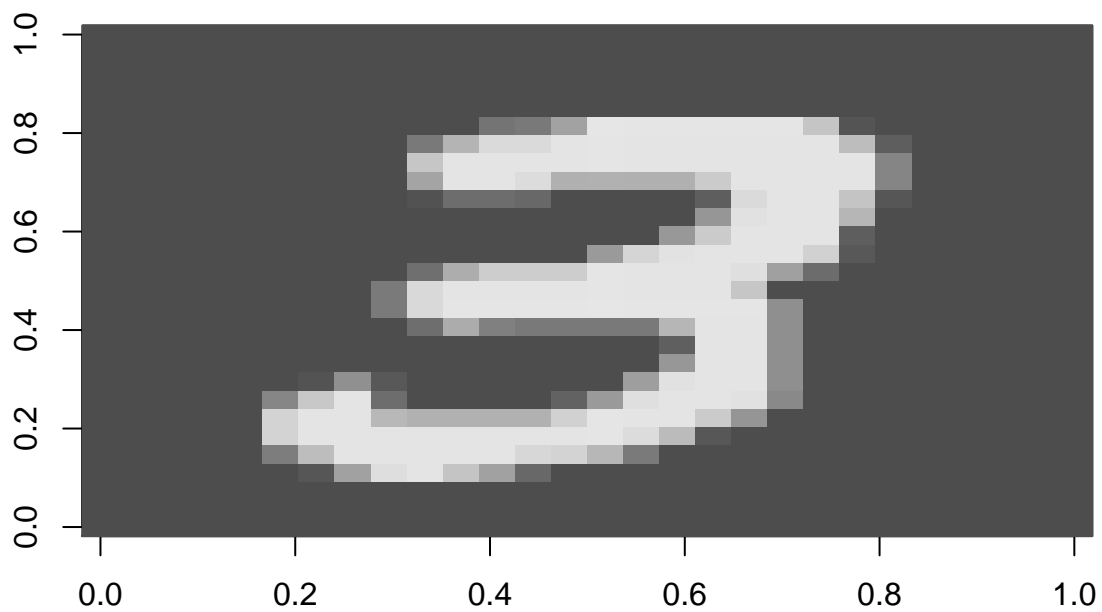
## List of 2
##  $ train:List of 2
##   ..$ images: int [1:60000, 1:784] 0 0 0 0 0 0 0 0 0 0 ...
##   ..$ labels: int [1:60000] 5 0 4 1 9 2 1 3 1 4 ...
##  $ test :List of 2
##   ..$ images: int [1:10000, 1:784] 0 0 0 0 0 0 0 0 0 0 ...
##   ..$ labels: int [1:10000] 7 2 1 0 4 1 4 9 5 9 ...
```

We can see that the Mnist has a training and testing set. The training dataset has 60,000 elements represented as a matrix of 6000×784 (every image is a vector of 784, representing a 28×28 image). It also has the labels corresponding to each of the images represented as integers. Finally the testing dataset has 10,000 elements represented in a similar way.

```
plotImage <- function(dat,size=28){
  imag <- matrix(dat,nrow=size)[,28:1]
  image(imag,col=grey.colors(256), xlab = "", ylab="")
}
```

Let's see an example of a 3 and 4 in our training dataset

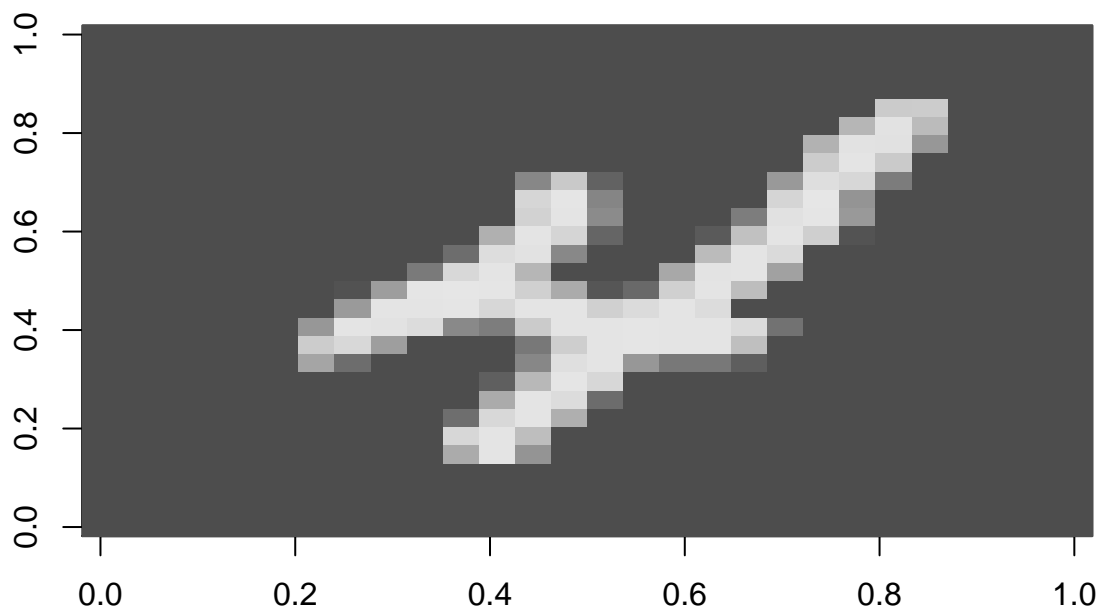
```
plotImage(mnist$train$images[8,])
```



```
mnist$train$labels[8]
```

```
## [1] 3
```

```
plotImage(mnist$train$images[10,])
```



```
mnist$train$labels[10]
```

```
## [1] 4
```

So the problem we are facing now is how do we sift through all of the labels to find numbers that belong to a certain set, the specific set we are looking for is numbers 3 and 4. After finding out how to access these sets we can then look into what exactly makes them different/easily classifiable.

```
#indices for 3
index_of3 <- c()
for (x in 1:length(mnist$train$labels)){
  if(mnist$train$labels[x] == '3'){
    index_of3 <- append(index_of3, x)
  }
}
index_of3 <- index_of3[1:500]

#indices for 4
index_of4 <- c()
for (x in 1:length(mnist$train$labels)){
  if(mnist$train$labels[x] == '4'){
    index_of4 <- append(index_of4, x)
  }
}
index_of4 <- index_of4[1:500]

index_of5 <- c()
```

```
for (x in 1:length(mnist$train$labels)){
  if(mnist$train$labels[x] == '5'){
    index_of5 <- append(index_of5, x)
  }
}
index_of5 <- index_of5[1:500]

indeces <- tibble(index_of3, index_of4, index_of5)
indeces
```

```
## # A tibble: 500 x 3
##   index_of3 index_of4 index_of5
##   <int>     <int>     <int>
## 1         8         3         1
## 2        11        10        12
## 3        13        21        36
## 4        28        27        48
## 5        31        54        66
## 6        45        59       101
## 7        50        61       133
## 8        51        62       139
## 9        75        65       146
## 10       87        90       174
## # ... with 490 more rows
```

```
#accessing matrix
accessMatrix <- function(dat,size=28){
  newmatrix <- matrix(dat,nrow=size)[,28:1]
}
```

```
#check for number 3
newmatrix3 <- accessMatrix(mnist$train$images[8,])
newmatrix3
```

```
##      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13]
## [1,]    0    0    0    0    0    0    0    0    0    0    0    0    0
## [2,]    0    0    0    0    0    0    0    0    0    0    0    0    0
## [3,]    0    0    0    0    0    0    0    0    0    0    0    0    0
## [4,]    0    0    0    0    0    0    0    0    0    0    0    0    0
## [5,]    0    0    0    0    0    0    0    0    0    0    0    0    0
## [6,]    0    0    0    0    49  208  208    61    0    0    0    0    0
## [7,]    0    0    0     7  157  252  252   183    5    0    0    0    0
## [8,]    0    0    0   103  252  252  252   252   75    0    0    0    0
## [9,]    0    0    0   235  252  252   147    29    9    0    0    0   45
## [10,]   0    0    0   252  252  252   134    0    0    0    0   31  223
## [11,]   0    0    0   172  252  252   134    0    0    0    0  123  253
## [12,]   0    0    0   103  252  252   134    0    0    0    0   52  253
## [13,]   0    0    0    24  217  252   134    0    0    0    0   44  253
## [14,]   0    0    0     0  207  252   203    18    0    0    0   44  253
## [15,]   0    0    0     0  146  253   253    92    0    0    0   44  255
## [16,]   0    0    0     0   45  230  252   239    98    0    0   44  253
## [17,]   0    0    0     0    0  153  252   252   242    86   15  143  253
## [18,]   0    0    0     0    0    8  188  252   252   252   252  252  253
## [19,]   0    0    0     0    0    0   83  243  252   252   252  252  253
## [20,]   0    0    0     0    0    0    0   65   74   74   74   74   74
```

```

## [21,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [22,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [23,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [24,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [25,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [26,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [27,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [28,] 0 0 0 0 0 0 0 0 0 0 0 0 0
##      [,14] [,15] [,16] [,17] [,18] [,19] [,20] [,21] [,22] [,23] [,24] [,25]
## [1,] 0 0 0 0 0 0 0 0 0 0 0 0
## [2,] 0 0 0 0 0 0 0 0 0 0 0 0
## [3,] 0 0 0 0 0 0 0 0 0 0 0 0
## [4,] 0 0 0 0 0 0 0 0 0 0 0 0
## [5,] 0 0 0 0 0 0 0 0 0 0 0 0
## [6,] 0 0 0 0 0 0 0 0 0 0 0 0
## [7,] 0 0 0 0 0 0 0 0 0 0 0 0
## [8,] 0 0 0 0 0 0 0 0 0 0 0 0
## [9,] 45 0 0 0 0 0 0 0 0 0 0 0
## [10,] 222 32 0 0 0 4 109 178 43 0 0 0
## [11,] 252 125 0 0 0 29 252 252 139 0 0 0
## [12,] 252 193 0 0 0 29 252 252 224 38 0 0
## [13,] 252 193 0 0 0 24 230 252 226 43 0 0
## [14,] 252 193 0 0 0 0 132 252 252 105 0 0
## [15,] 253 253 91 0 0 0 133 253 253 255 0 0
## [16,] 252 252 212 0 0 0 132 252 252 253 0 0
## [17,] 252 252 247 88 0 0 132 252 252 253 0 0
## [18,] 252 252 252 189 85 14 189 252 252 253 0 0
## [19,] 177 238 252 252 243 226 252 252 252 253 0 0
## [20,] 0 102 252 252 252 252 252 252 252 253 0 0
## [21,] 0 28 204 252 252 252 252 252 252 174 0 0
## [22,] 0 0 9 14 144 172 252 252 158 6 0 0
## [23,] 0 0 0 0 0 7 59 59 14 0 0 0
## [24,] 0 0 0 0 0 0 0 0 0 0 0 0
## [25,] 0 0 0 0 0 0 0 0 0 0 0 0
## [26,] 0 0 0 0 0 0 0 0 0 0 0 0
## [27,] 0 0 0 0 0 0 0 0 0 0 0 0
## [28,] 0 0 0 0 0 0 0 0 0 0 0 0
##      [,26] [,27] [,28]
## [1,] 0 0 0
## [2,] 0 0 0
## [3,] 0 0 0
## [4,] 0 0 0
## [5,] 0 0 0
## [6,] 0 0 0
## [7,] 0 0 0
## [8,] 0 0 0
## [9,] 0 0 0
## [10,] 0 0 0
## [11,] 0 0 0
## [12,] 0 0 0
## [13,] 0 0 0
## [14,] 0 0 0
## [15,] 0 0 0
## [16,] 0 0 0

```

```
## [17,] 0 0 0
## [18,] 0 0 0
## [19,] 0 0 0
## [20,] 0 0 0
## [21,] 0 0 0
## [22,] 0 0 0
## [23,] 0 0 0
## [24,] 0 0 0
## [25,] 0 0 0
## [26,] 0 0 0
## [27,] 0 0 0
## [28,] 0 0 0
```

#check for number 4

```
newmatrix4 <- accessMatrix(mnist$train$images[3,])
newmatrix4
```

```
##      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13]
## [1,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [2,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [3,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [4,] 0 0 0 0 0 0 0 0 0 0 0 0 150
## [5,] 0 0 0 0 0 0 0 0 0 0 0 119 253
## [6,] 0 0 0 0 0 0 0 0 0 0 0 177 237
## [7,] 0 0 0 0 0 0 0 0 0 0 0 177 207
## [8,] 0 0 0 0 0 0 0 0 0 0 0 177 207
## [9,] 0 0 0 0 0 0 0 0 0 0 0 177 207
## [10,] 0 0 0 0 0 0 0 0 0 0 0 177 253
## [11,] 0 0 0 0 0 0 0 0 0 0 0 98 254
## [12,] 0 0 0 0 0 0 0 0 0 0 0 56 250
## [13,] 0 0 0 0 0 0 0 0 0 0 0 0 240
## [14,] 0 0 0 0 0 0 0 0 0 0 0 0 198
## [15,] 0 0 0 0 0 0 0 0 0 0 0 0 143
## [16,] 0 0 0 0 0 0 0 0 0 0 0 0 91
## [17,] 0 0 0 0 0 0 0 0 0 0 0 0 28
## [18,] 0 0 0 96 169 169 169 169 169 169 169 102 5
## [19,] 0 0 0 254 255 254 254 255 254 254 254 254 233
## [20,] 0 0 0 153 153 153 96 94 57 57 137 220 250
## [21,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [22,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [23,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [24,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [25,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [26,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [27,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [28,] 0 0 0 0 0 0 0 0 0 0 0 0 0
##      [,14] [,15] [,16] [,17] [,18] [,19] [,20] [,21] [,22] [,23] [,24] [,25]
## [1,] 0 0 0 0 0 0 0 0 0 0 0 0
## [2,] 0 0 0 0 0 0 0 0 0 0 0 0
## [3,] 0 0 0 0 0 0 0 0 0 0 0 0
## [4,] 159 159 159 120 46 0 0 0 0 0 0 0
## [5,] 254 254 254 254 245 222 220 126 62 0 0 0
## [6,] 85 67 120 163 163 163 163 163 81 0 0 0
## [7,] 0 0 0 0 0 0 0 0 0 0 0 0
## [8,] 0 0 0 0 0 0 0 0 0 0 0 0
```

```

## [9,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [10,] 47 0 0 0 0 0 0 0 0 0 0 0 0
## [11,] 49 0 0 0 0 0 0 0 0 0 0 0 0
## [12,] 116 0 0 0 0 0 0 0 0 0 0 0 0
## [13,] 144 0 0 0 0 0 0 0 0 0 0 0 0
## [14,] 150 0 0 0 0 0 0 0 0 0 0 0 0
## [15,] 241 0 0 0 0 0 0 0 0 0 0 0 0
## [16,] 243 14 0 0 0 0 0 0 0 0 0 0 0
## [17,] 234 86 0 0 0 0 0 0 0 0 0 0 0
## [18,] 179 178 0 0 0 0 0 0 0 0 0 0 0
## [19,] 241 248 163 23 0 0 0 0 0 0 0 0 0
## [20,] 252 254 254 231 198 183 27 2 0 0 0 0 0
## [21,] 40 91 216 254 254 254 254 153 120 67 0 0 0
## [22,] 0 0 16 29 56 125 162 210 180 232 0 0 0
## [23,] 0 0 0 0 0 0 0 40 39 39 0 0 0
## [24,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [25,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [26,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [27,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [28,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [,26] [,27] [,28]
## [1,] 0 0 0
## [2,] 0 0 0
## [3,] 0 0 0
## [4,] 0 0 0
## [5,] 0 0 0
## [6,] 0 0 0
## [7,] 0 0 0
## [8,] 0 0 0
## [9,] 0 0 0
## [10,] 0 0 0
## [11,] 0 0 0
## [12,] 0 0 0
## [13,] 0 0 0
## [14,] 0 0 0
## [15,] 0 0 0
## [16,] 0 0 0
## [17,] 0 0 0
## [18,] 0 0 0
## [19,] 0 0 0
## [20,] 0 0 0
## [21,] 0 0 0
## [22,] 0 0 0
## [23,] 0 0 0
## [24,] 0 0 0
## [25,] 0 0 0
## [26,] 0 0 0
## [27,] 0 0 0
## [28,] 0 0 0

```

```

#check for number 5
newmatrix5 <- accessMatrix(mnist$train$images[1,])
newmatrix5

```

```

## [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13]

```

##	[1,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[2,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[3,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[4,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[5,]	0	0	0	136	55	0	0	0	0	0	0	0
##	[6,]	0	0	0	253	172	0	0	0	0	0	0	0
##	[7,]	0	0	0	253	226	18	0	0	0	0	0	0
##	[8,]	0	0	0	253	253	171	0	0	0	0	0	0
##	[9,]	0	0	0	212	253	219	23	0	0	0	0	0
##	[10,]	0	0	0	135	253	253	66	0	0	0	0	0
##	[11,]	0	0	0	132	253	253	213	24	0	0	0	0
##	[12,]	0	0	0	16	244	253	253	114	0	0	0	0
##	[13,]	0	0	0	0	133	253	253	221	39	0	0	0
##	[14,]	0	0	0	0	11	195	253	253	148	0	0	0
##	[15,]	0	0	0	0	0	80	253	253	229	46	0	45
##	[16,]	0	0	0	0	0	9	198	253	253	130	0	16
##	[17,]	0	0	0	0	0	0	81	253	253	183	0	93
##	[18,]	0	0	0	0	0	0	2	201	253	253	249	252
##	[19,]	0	0	0	0	0	0	0	78	250	253	253	253
##	[20,]	0	0	0	0	0	0	0	0	182	207	249	187
##	[21,]	0	0	0	0	0	0	0	0	0	2	64	0
##	[22,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[23,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[24,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[25,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[26,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[27,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[28,]	0	0	0	0	0	0	0	0	0	0	0	0
##		[,14]	[,15]	[,16]	[,17]	[,18]	[,19]	[,20]	[,21]	[,22]	[,23]	[,24]	[,25]
##	[1,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[2,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[3,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[4,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[5,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[6,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[7,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[8,]	0	0	0	0	0	0	18	49	0	0	0	0
##	[9,]	0	0	0	0	0	80	219	238	30	0	0	0
##	[10,]	0	0	0	0	14	156	253	253	36	0	0	0
##	[11,]	0	0	0	0	1	107	253	253	94	0	0	0
##	[12,]	0	0	11	139	154	253	253	253	154	0	0	0
##	[13,]	0	35	190	253	253	253	253	253	170	3	0	0
##	[14,]	81	241	253	190	90	205	253	253	253	18	0	0
##	[15,]	240	225	70	2	0	11	198	253	253	18	0	0
##	[16,]	253	160	0	0	0	0	182	253	253	18	0	0
##	[17,]	253	108	0	0	0	43	247	253	253	126	0	0
##	[18,]	119	1	0	0	0	154	241	251	253	136	0	0
##	[19,]	25	0	0	0	0	0	0	93	225	175	0	0
##	[20,]	0	0	0	0	0	0	0	82	172	26	0	0
##	[21,]	0	0	0	0	0	0	0	82	253	166	0	0
##	[22,]	0	0	0	0	0	0	0	56	242	255	0	0
##	[23,]	0	0	0	0	0	0	0	39	195	247	0	0
##	[24,]	0	0	0	0	0	0	0	0	64	127	0	0
##	[25,]	0	0	0	0	0	0	0	0	0	0	0	0


```
## [26,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [27,] 0 0 0 0 0 0 0 0 0 0 0 0 0
## [28,] 0 0 0 0 0 0 0 0 0 0 0 0 0
##      [,26] [,27] [,28]
## [1,] 0 0 0
## [2,] 0 0 0
## [3,] 0 0 0
## [4,] 0 0 0
## [5,] 0 0 0
## [6,] 0 0 0
## [7,] 0 0 0
## [8,] 0 0 0
## [9,] 0 0 0
## [10,] 0 0 0
## [11,] 0 0 0
## [12,] 0 0 0
## [13,] 0 0 0
## [14,] 0 0 0
## [15,] 0 0 0
## [16,] 0 0 0
## [17,] 0 0 0
## [18,] 0 0 0
## [19,] 0 0 0
## [20,] 0 0 0
## [21,] 0 0 0
## [22,] 0 0 0
## [23,] 0 0 0
## [24,] 0 0 0
## [25,] 0 0 0
## [26,] 0 0 0
## [27,] 0 0 0
## [28,] 0 0 0
```

Feature Definition

You are allowed to use only 2 features. Notice that you need to calculate those features directly from dataset. Make sure to describe what those features represent and why you chose them. Are those features capturing any intuition that you have about distinguishing those two digits?

For our focus features, we will look at symmetry over the top and bottom halves of the image, and the level of linearity that a 4 has vs a 3.

Symmetry

Starting with symmetry, we can see that a 3 is far more symmetrical between top and bottom halves than a 4 is. Thus, we will be looking at the number of pixels in the top half of the image divided by the number of pixels in the bottom half of the image, and the closer that value is to 1, the more symmetrical the image is, and the more likely the image is a 3.

```
#Calculating the symmetry of the upper quadrant
```

```
symmetry1 <- function(dat, newmatrix){
```

```

sum <- 0
for(x in 1:28){
  for(y in 1:14){
    sum = sum + newmatrix[x,y]
  }
}
sum
}
#Upper Quadrant symmetry for numbers 3(new matrix3) and number 4(newmatrix4)
symmetry1(mnist$train$images[8,], newmatrix3)

```

```
## [1] 18606
```

```
symmetry1(mnist$train$images[3,], newmatrix4)
```

```
## [1] 11587
```

```

#Calculating the symmetry of the lower quadrant
symmetry2 <- function(dat, newmatrix){
  sum <- 0
  for(x in 1:28){
    for(y in 15:28){
      sum = sum + newmatrix[x,y]
    }
  }
  sum
}
#Lower Quadrant symmetry for numbers 3(new matrix3) and number 4(newmatrix4)
symmetry2(mnist$train$images[8,], newmatrix3)

```

```
## [1] 17261
```

```
symmetry2(mnist$train$images[10,], newmatrix4)
```

```
## [1] 7856
```

Now that we have seen that it works for individual values, indices, and labels that represent 3 and 4, let's move on to see if it works generally. Here is the symmetry function we came up with:

```

ratio_calc <- function(index_of_minst){
  ratio <- c()
  y <- c()
  for (x in 1:500){
    matrix_group <- accessMatrix(mnist$train$images[index_of_minst[x],])
    upper_quadrant <- symmetry1(mnist$train$images[index_of_minst[x],], matrix_group)
    lower_quadrant <- symmetry2(mnist$train$images[index_of_minst[x],], matrix_group)
    ratio[x] = upper_quadrant/lower_quadrant
    y = 3
  }
  ratio
}

final_3 <- tibble(indeces = indeces$index_of3, ratio = ratio_calc(index_of3))
final_3 <- final_3%>%
  mutate(y = 3)
final_3

```

```
## # A tibble: 500 x 3
##   indeces ratio    y
##   <int> <dbl> <dbl>
## 1      8 1.08     3
## 2     11 0.882    3
## 3     13 1.22     3
## 4     28 0.967    3
## 5     31 1.02     3
## 6     45 1.07     3
## 7     50 0.822    3
## 8     51 0.856    3
## 9     75 0.951    3
## 10    87 0.784    3
## # ... with 490 more rows
```

```
final_4 <- tibble(indeces = indeces$index_of4, ratio = ratio_calc(index_of4))
final_4 <- final_4%>%
  mutate(y = 4)
final_4
```

```
## # A tibble: 500 x 3
##   indeces ratio    y
##   <int> <dbl> <dbl>
## 1      3 1.47     4
## 2     10 1.39     4
## 3     21 1.21     4
## 4     27 1.12     4
## 5     54 1.33     4
## 6     59 1.10     4
## 7     61 1.37     4
## 8     62 1.38     4
## 9     65 1.46     4
## 10    90 1.22     4
## # ... with 490 more rows
```

```
final_5 <- tibble(indeces = indeces$index_of5, ratio = ratio_calc(index_of5))
final_5 <- final_5%>%
  mutate(y = 5)
final_5
```

```
## # A tibble: 500 x 3
##   indeces ratio    y
##   <int> <dbl> <dbl>
## 1      1 1.09     5
## 2     12 1.10     5
## 3     36 0.986    5
## 4     48 1.32     5
## 5     66 0.897    5
## 6    101 1.03     5
## 7    133 1.11     5
## 8    139 1.38     5
## 9    146 1.19     5
## 10   174 1.06     5
## # ... with 490 more rows
```

```

symmetry_final <- final_3%>%
  full_join(final_4)
symmetry_final

```

```

## # A tibble: 1,000 x 3
##   indeces ratio      y
##   <int> <dbl> <dbl>
## 1      8 1.08      3
## 2     11 0.882     3
## 3     13 1.22      3
## 4     28 0.967     3
## 5     31 1.02      3
## 6     45 1.07      3
## 7     50 0.822     3
## 8     51 0.856     3
## 9     75 0.951     3
## 10    87 0.784     3
## # ... with 990 more rows

```

Linearity

Next we will look at Linearity, because a 4 typically has a clear vertical line. A 3 should have less obvious of any vertical line, which should help with identifying, while looking at a different feature than before.

```

Linear <- function(dat, newmatrix){
  min <- c()
  for(x in 1:28){
    sum <- 0
    for(y in 1:28){
      if(newmatrix[x,y] == 0){
        sum = sum + 1
      }
    }
    min[x] = sum
  }
  min(min)
}
Linear(mnist$train$images[8,], newmatrix3)

```

```
## [1] 10
```

```

linear_final <- function(index_of_minst){
  minimum_values <- c()
  y <- c()
  for (x in 1:500){
    matrix_group <- accessMatrix(mnist$train$images[index_of_minst[x],])
    minimum_values[x] = Linear(mnist$train$images[index_of_minst[x,]], matrix_group)
  }
  print(minimum_values)
}

```

```

final_3_linear <- tibble(indeces = indeces$index_of3, linearity = linear_final(index_of3))

```

```
## [1] 10 8 10 9 12 13 10 13 9 16 11 10 10 12 11 14 9 11 12 13 11 12 14 9 17
```

```
## [26] 11 9 16 13 11 13 11 11 11 11 11 10 11 9 12 11 11 15 12 15 10 10 12 11 13
## [51] 15 13 16 11 15 14 16 11 13 12 14 12 12 15 13 9 11 10 11 10 14 9 10 10 11
## [76] 9 14 9 12 8 11 9 13 13 12 11 10 11 15 11 10 13 11 10 12 9 11 10 13 9
## [101] 14 14 15 10 12 9 14 9 13 11 9 8 10 10 8 8 10 10 17 11 12 13 8 9 8
## [126] 14 10 13 10 9 11 10 15 10 11 10 14 12 9 14 13 13 14 12 11 11 9 11 12 12
## [151] 11 13 12 10 9 9 14 9 10 14 11 11 12 11 15 11 8 13 15 13 13 12 9 12 9
## [176] 10 10 9 10 15 11 14 12 10 11 14 11 8 10 12 14 12 9 9 10 10 16 12 9 13
## [201] 16 10 9 9 11 13 9 12 11 9 12 10 10 12 9 14 13 12 12 11 12 11 9 12 12
## [226] 9 14 13 15 13 14 10 16 13 12 11 14 13 12 12 14 15 12 13 12 13 11 13 14 13
## [251] 9 12 11 8 11 15 11 15 10 12 11 11 10 13 13 14 15 13 13 14 17 11 12 14 13
## [276] 9 10 11 11 9 11 10 12 13 12 11 12 10 14 11 11 8 11 11 11 11 11 8 13 11
## [301] 11 11 12 9 13 13 13 11 13 11 11 10 11 11 10 12 10 14 9 11 10 12 9 13 9
## [326] 14 12 11 10 8 14 10 12 11 13 11 9 10 10 10 11 11 13 9 13 11 13 10 13 11
## [351] 12 11 12 12 12 12 12 8 14 9 9 12 13 10 12 16 12 13 11 11 13 14 10 13 16
## [376] 14 12 11 9 13 10 8 10 10 8 9 15 12 12 9 10 9 11 10 9 9 9 8 11 9
## [401] 9 8 11 11 11 11 8 9 16 10 9 8 14 8 13 10 12 11 14 10 12 8 11 12 11
## [426] 10 11 14 11 12 16 13 12 13 8 8 13 12 13 11 14 11 12 8 13 9 14 12 12 15
## [451] 14 11 12 9 14 12 10 11 14 11 10 9 11 9 11 8 15 11 8 16 10 12 11 10 11
## [476] 10 15 14 8 10 12 13 11 13 11 14 12 11 11 9 8 10 10 11 9 12 11 11 12 9
```

```
final_3_linear <- final_3_linear%>%
  mutate(y = 3)
final_3_linear
```

```
## # A tibble: 500 x 3
##   indices linearity    y
##   <int>      <dbl> <dbl>
## 1      8         10    3
## 2     11          8    3
## 3     13         10    3
## 4     28          9    3
## 5     31         12    3
## 6     45         13    3
## 7     50         10    3
## 8     51         13    3
## 9     75          9    3
## 10    87         16    3
## # ... with 490 more rows
```

```
final_4_linear <- tibble(indices = indices$index_of4, linearity = linear_final(index_of4))
```

```
## [1] 10 12 8 15 14 8 10 14 16 13 8 15 14 12 13 17 10 13 8 15 9 10 10 11 17
## [26] 14 15 13 17 10 9 15 15 17 14 17 12 13 17 16 12 17 14 11 17 16 17 8 8 15
## [51] 17 16 16 14 14 12 10 16 11 16 11 9 17 14 18 14 14 11 12 9 11 12 8 12 13
## [76] 11 17 8 11 15 10 9 10 12 10 15 8 14 14 11 14 9 8 9 19 8 8 8 14 14
## [101] 14 14 14 9 12 8 8 14 9 13 13 13 16 8 11 14 10 15 10 16 16 14 14 9 14
## [126] 11 14 15 8 13 8 9 12 10 11 9 8 11 8 8 8 9 13 9 14 12 14 11 14 14
## [151] 18 10 8 13 10 15 15 15 14 12 9 15 13 17 15 10 8 16 11 9 8 8 14 8 14
## [176] 14 8 16 16 17 8 15 8 16 8 14 12 13 15 16 11 14 16 11 8 8 16 18 8 8
## [201] 13 11 8 15 14 10 8 8 12 16 9 16 8 10 12 8 14 9 9 11 8 9 8 9 12
## [226] 13 12 15 16 15 16 11 8 14 9 8 10 10 13 14 15 11 17 12 11 8 12 9 8 9
## [251] 10 13 15 12 13 13 8 8 11 14 10 8 17 9 13 14 8 10 10 10 13 13 10 13 8
## [276] 10 11 11 11 10 14 8 8 8 12 12 8 14 8 18 10 11 14 14 13 17 8 8 9 12
## [301] 8 12 19 15 15 8 16 15 15 11 9 13 11 10 16 14 9 13 10 12 14 8 13 12 9
## [326] 12 8 12 15 12 14 19 12 13 12 8 11 12 13 10 12 10 12 15 8 13 11 16 12 8
```

```
## [351] 14 10 9 8 11 13 14 8 10 8 10 8 8 13 8 14 15 9 12 9 9 9 14 14 14
## [376] 14 15 12 11 12 8 14 13 15 9 16 16 9 14 9 13 10 14 14 12 18 17 8 12 12
## [401] 8 10 13 8 15 8 18 13 12 12 14 17 16 11 11 14 15 16 8 17 14 14 11 13 8
## [426] 12 13 11 13 11 12 10 16 15 14 17 14 13 13 8 14 8 13 12 13 12 13 10 13 12
## [451] 14 12 16 11 8 8 8 15 9 14 11 14 14 8 8 15 12 15 9 13 15 8 15 12 15
## [476] 17 8 15 13 11 8 8 14 9 8 11 14 9 11 15 8 14 15 10 8 16 12 16 14 15
```

```
final_4_linear <- final_4_linear%>%
  mutate(y = 4)
final_4_linear
```

```
## # A tibble: 500 x 3
##   indeces linearity    y
##   <int>      <dbl> <dbl>
## 1      3         10     4
## 2     10         12     4
## 3     21          8     4
## 4     27         15     4
## 5     54         14     4
## 6     59          8     4
## 7     61         10     4
## 8     62         14     4
## 9     65         16     4
## 10    90         13     4
## # ... with 490 more rows
```

```
linear_final_tbl <- final_3_linear%>%
  full_join(final_4_linear)
linear_final_tbl
```

```
## # A tibble: 1,000 x 3
##   indeces linearity    y
##   <int>      <dbl> <dbl>
## 1      8         10     3
## 2     11          8     3
## 3     13         10     3
## 4     28          9     3
## 5     31         12     3
## 6     45         13     3
## 7     50         10     3
## 8     51         13     3
## 9     75          9     3
## 10    87         16     3
## # ... with 990 more rows
```

Will all this, now we put all the data into a combined table.

```
mnist_34 <- linear_final_tbl %>%
  bind_cols(symmetry_final)
mnist_34
```

```
## # A tibble: 1,000 x 6
##   indeces...1 linearity y...3 indeces...4 ratio y...6
##   <int>      <dbl> <dbl>      <int> <dbl> <dbl>
## 1      8         10     3         8 1.08     3
## 2     11          8     3        11 0.882    3
## 3     13         10     3        13 1.22     3
```

```
## 4      28      9      3      28 0.967      3
## 5      31     12      3      31 1.02      3
## 6      45     13      3      45 1.07      3
## 7      50     10      3      50 0.822     3
## 8      51     13      3      51 0.856     3
## 9      75      9      3      75 0.951     3
## 10     87     16      3      87 0.784     3
```

```
## # ... with 990 more rows
```

```
final.split <- initial_split(mnist_34, prop=0.8)
train.mnist_34 <- training(final.split)%>%
  mutate(y = as.factor(y...6))%>%
  mutate(x_1 = ratio)%>%
  mutate(x_2 = linearity)%>%
  select(x_1, x_2, y)
train.mnist_34
```

```
## # A tibble: 800 x 3
```

```
##       x_1    x_2 y
```

```
##    <dbl> <dbl> <fct>
```

```
## 1 1.07    11 3
```

```
## 2 0.909    11 3
```

```
## 3 1.17     14 3
```

```
## 4 0.975    12 3
```

```
## 5 1.38     14 4
```

```
## 6 1.04     11 3
```

```
## 7 0.965     9 4
```

```
## 8 1.07     13 3
```

```
## 9 1.11     14 4
```

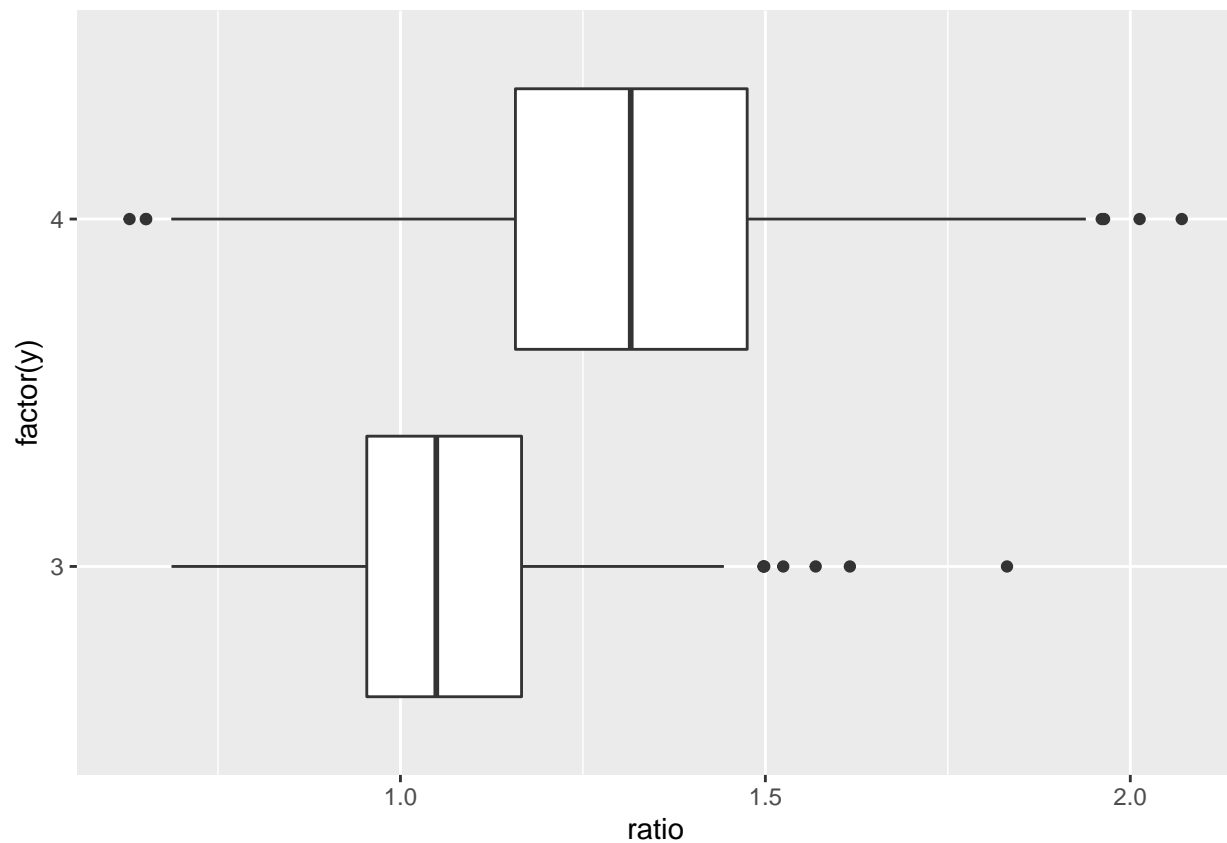
```
## 10 0.788   11 4
```

```
## # ... with 790 more rows
```

```
test.mnist_34 <- testing(final.split)%>%
  mutate(y = as.factor(y...6))%>%
  mutate(x_1 = ratio)%>%
  mutate(x_2 = linearity)%>%
  select(x_1, x_2, y)
```

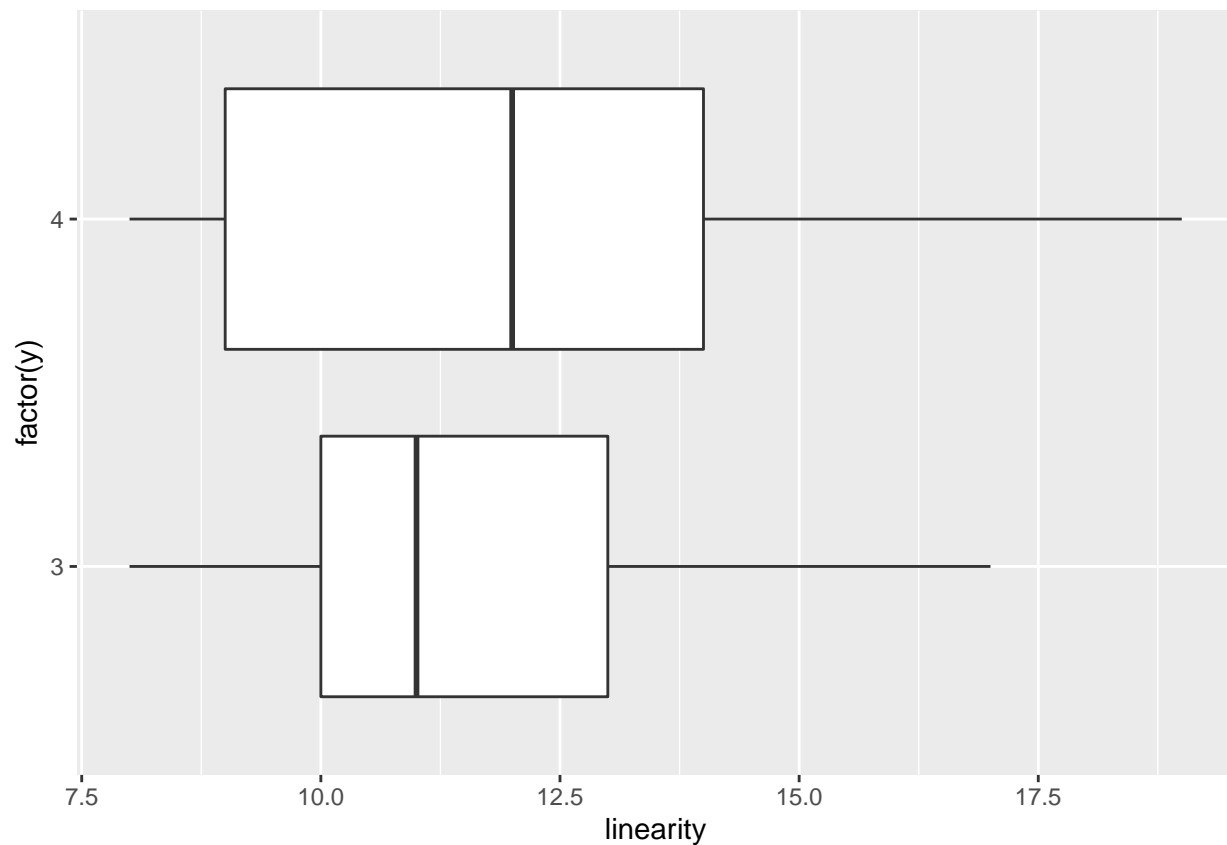
Here are some graphs that can help us better understand our distribution.

```
ggplot(symmetry_final, aes(x=ratio, y = factor(y)))+
  geom_boxplot()
```



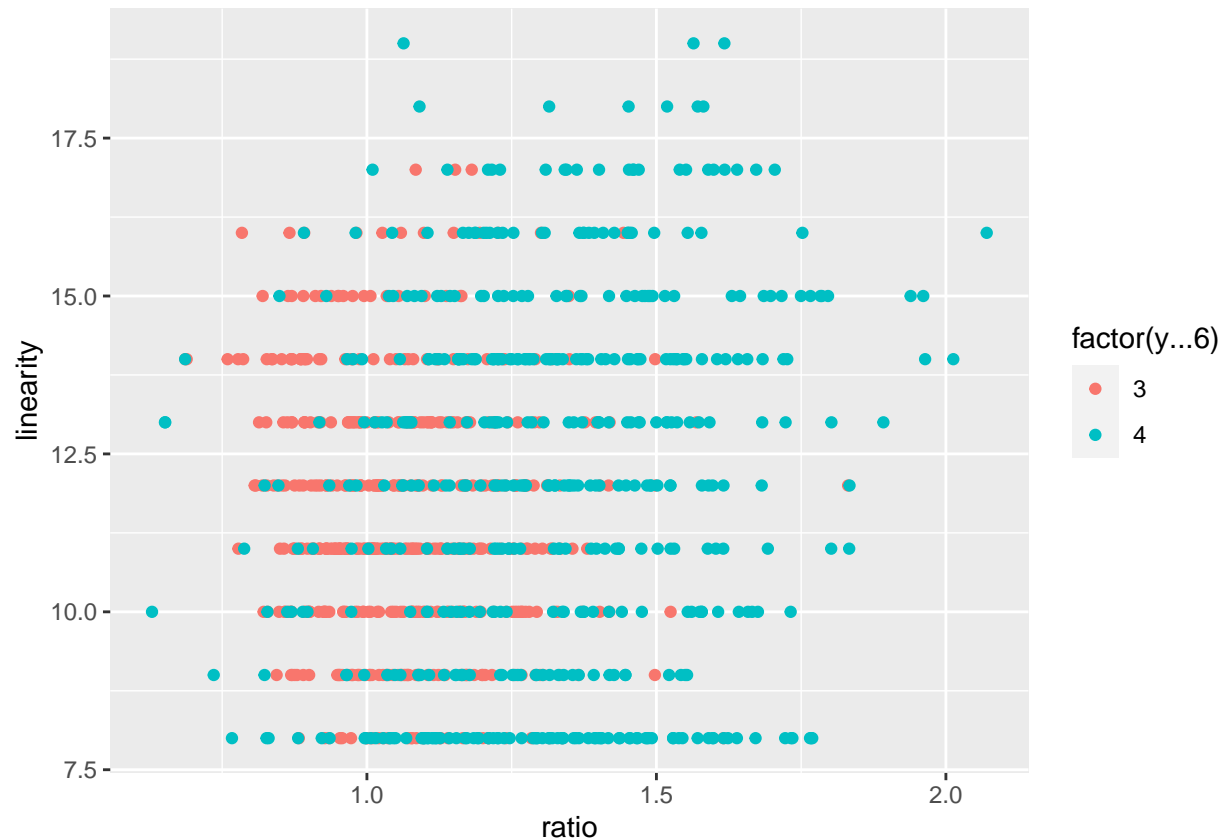
This box plot shows us how accurate the symmetry feature was, looking at the ratio of pixels from the top half to the bottom half. We can see that there's very little overlap between the numbers, and when identifying, a 3 will stick around a 1:1 ratio, showing symmetry, while the ratio for a 4 is either decently above or below 1.0 - typically above, as there should be more pixels in the top half than the bottom half, but sometimes below.

```
ggplot(linear_final_tbl, aes(x=linearity, y = factor(y)))+  
  geom_boxplot()
```

Now, when looking at the linearity box plot, we can see that this is far less accurate of a feature for us to be looking at, as there's a lot of overlap between the numbers. The values along the x axis show us the minimum number of zeros in a row in the image, trying to find the most linear line. The 4s actually shows more linearity than a 3 generally, at least in these images, we believe because a lot of the images in this dataset have the vertical line in a 4 somewhat diagonal.

```
ggplot(mnist_34, aes(x=ratio, y = linearity, color = factor(y...6)))+  
  geom_point()
```



This scatter plot is going more in depth with both features, seeing how well symmetry (on the x axis) and linearity (on the y axis) work together to identify the numbers. There's a significant amount of overlap, but we can see that the symmetry feature really helps identify a 3 from a 4, and the linearity helps somewhat, but mainly with outliers.

Model Creation, Optimization and Selection

- a) Create at least two different models for this classification and make sure to optimize the parameters those models have.

KNN Model

```
library(tidymodels)
library(kknn)
## devtools::install_github("KlausVigo/kknn")
tidymodels_prefer()

build_knn <- function (train.table, kVal) {
  knn.model <- nearest_neighbor(neighbors = kVal) %>%
    set_engine("kknn") %>%
    set_mode("classification")

  recipe <- recipe(y ~ x_1 + x_2, data=train.table)
```

```

knn.wflow <- workflow() %>%
  add_recipe(recipe) %>%
  add_model(knn.model)

knn.fit <- fit(knn.wflow, train.table)
}

knn.model <- build_knn(train.mnist_34, 5)

```

Cross Validation

```

knn.model.cv <- nearest_neighbor(neighbors = tune()) %>%
  set_engine("kkn") %>%
  set_mode("classification")

recipe <- recipe(y ~ x_1 + x_2, data=train.mnist_34)

knn.wf <- workflow() %>%
  add_recipe(recipe) %>%
  add_model(knn.model.cv)
knn.wf

## == Workflow =====
## Preprocessor: Recipe
## Model: nearest_neighbor()
##
## -- Preprocessor -----
## 0 Recipe Steps
##
## -- Model -----
## K-Nearest Neighbor Model Specification (classification)
##
## Main Arguments:
##   neighbors = tune()
##
## Computational engine: kkn

```

b) Calculate the missclassification rates for both models and select the model with the lowest error rate.

```

knn.final.fit <- predict(knn.model, test.mnist_34, type="prob")

pred34.test.tbl <- knn.model %>%
  augment(new_data = test.mnist_34)
pred34.test.tbl

## # A tibble: 200 x 6
##       x_1    x_2 y     .pred_class .pred_3 .pred_4
##   <dbl> <dbl> <fct> <fct>      <dbl>  <dbl>
## 1 1.22    10 3      4          0.12   0.88
## 2 0.967    9 3      3          0.64   0.36
## 3 1.02    10 3      3           1     0
## 4 0.989   12 3      3           1     0
## 5 0.977   13 3      3           1     0

```

```
## 6 0.930    12 3      3          0.72    0.28
## 7 1.30     16 3      4          0.2     0.8
## 8 1.04     11 3      3          0.72    0.28
## 9 1.09     10 3      3          1       0
## 10 1.32    11 3      4          0.48    0.52
## # ... with 190 more rows
```

```
accuracy(pred34.test.tbl, y, .pred_class)
```

```
## # A tibble: 1 x 3
##   .metric .estimator .estimate
##   <chr>   <chr>      <dbl>
## 1 accuracy binary      0.695
```

```
conf_mat(pred34.test.tbl, truth = y, estimate = .pred_class)
```

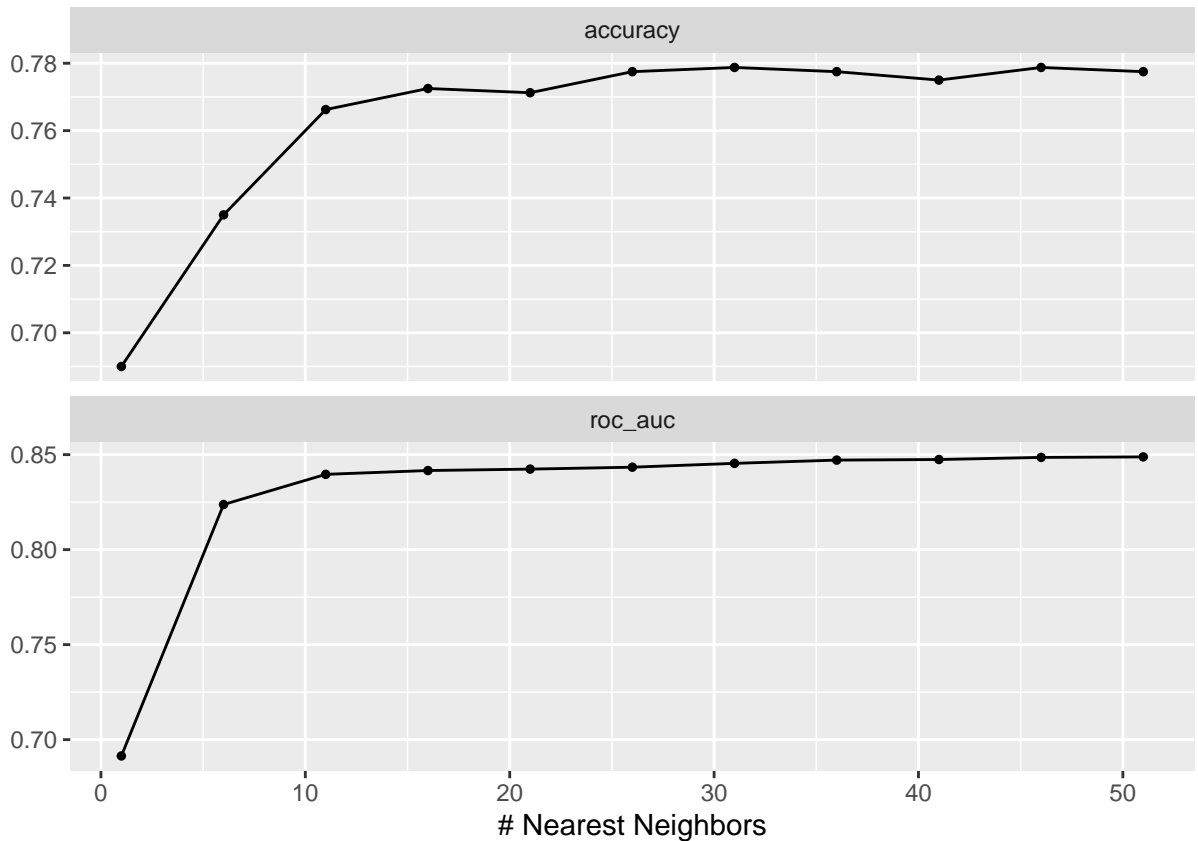
```
##           Truth
## Prediction 3  4
##           3 63 38
##           4 23 76
```

Looking at our results from the KNN Model, the missclassification rate is 0.75, and in the confusion matrix we can see the results played out in more detail. These were really cool results to get, as it shows that this model is pretty accurate for identifying the numbers. Now we'll look at the rates with the cross validation, and see if it helps at all.

```
set.seed(12345)
digits.folds <- vfold_cv(train.mnist_34, v = 10)

neighbours <- seq(1, 51, by = 5)
neighbors.tbl <- tibble(neighbours)
neighbors2.tbl <- grid_regular(neighbors(range = c(1, 51)), levels = 11)

tune.results <- tune_grid(
  object = knn.wf,
  resamples = digits.folds,
  grid = neighbors2.tbl
)
autoplot(tune.results)
```



```
show_best(tune.results, metric = "accuracy")
```

```
## # A tibble: 5 x 7
##   neighbors .metric .estimator mean      n std_err .config
##   <int> <chr>      <chr>    <dbl> <int>  <dbl> <fct>
## 1      31 accuracy binary    0.779    10  0.0124 Preprocessor1_Model07
## 2      46 accuracy binary    0.779    10  0.0126 Preprocessor1_Model10
## 3      26 accuracy binary    0.778    10  0.0120 Preprocessor1_Model06
## 4      36 accuracy binary    0.778    10  0.0126 Preprocessor1_Model08
## 5      51 accuracy binary    0.778    10  0.0115 Preprocessor1_Model11
```

```
best.neighbor <- select_best(tune.results, metric = "accuracy")
knn.final.wf <- finalize_workflow(knn.wf, best.neighbor)
knn.final.fit_cv <- fit(knn.final.wf, train.mnist_34)
```

```
predict(knn.final.fit_cv, test.mnist_34, type="prob")
```

```
## # A tibble: 200 x 2
##   .pred_3 .pred_4
##   <dbl> <dbl>
## 1  0.580  0.420
## 2  0.854  0.146
## 3  0.954  0.0458
## 4  0.895  0.105
## 5  0.840  0.160
## 6  0.876  0.124
## 7  0.0926 0.907
```

```
## 8 0.849 0.151
## 9 0.795 0.205
## 10 0.575 0.425
## # ... with 190 more rows

pred34_cv.test.tbl <- knn.final.fit_cv %>%
  augment(new_data = test.mnist_34)
pred34_cv.test.tbl

## # A tibble: 200 x 6
##       x_1    x_2 y   .pred_class .pred_3 .pred_4
##   <dbl> <dbl> <fct> <fct>      <dbl> <dbl>
## 1 1.22    10 3     3           0.580 0.420
## 2 0.967    9 3     3           0.854 0.146
## 3 1.02    10 3     3           0.954 0.0458
## 4 0.989    12 3     3           0.895 0.105
## 5 0.977    13 3     3           0.840 0.160
## 6 0.930    12 3     3           0.876 0.124
## 7 1.30    16 3     4           0.0926 0.907
## 8 1.04    11 3     3           0.849 0.151
## 9 1.09    10 3     3           0.795 0.205
## 10 1.32    11 3     3           0.575 0.425
## # ... with 190 more rows
```

```
accuracy(pred34_cv.test.tbl, y, .pred_class)
```

```
## # A tibble: 1 x 3
##   .metric .estimator .estimate
##   <chr>    <chr>      <dbl>
## 1 accuracy binary      0.74
```

```
conf_mat(pred34_cv.test.tbl, truth = y, estimate = .pred_class)
```

```
##           Truth
## Prediction 3  4
##           3 72 38
##           4 14 76
```

Now with Cross Validation, the missclassification rate is 0.785, and the confusion matrix. This shows us that the Cross Validation model is more accurate than the KNN Model! It is only slightly better, but definitely worth it - this is our superior model, and now we'll plot these probabilities.

Visualization

Plot the probabilities across a grid and the decision boundary for your selected model.

We selected the Cross Validation model, as it had better results, and here is our plot.

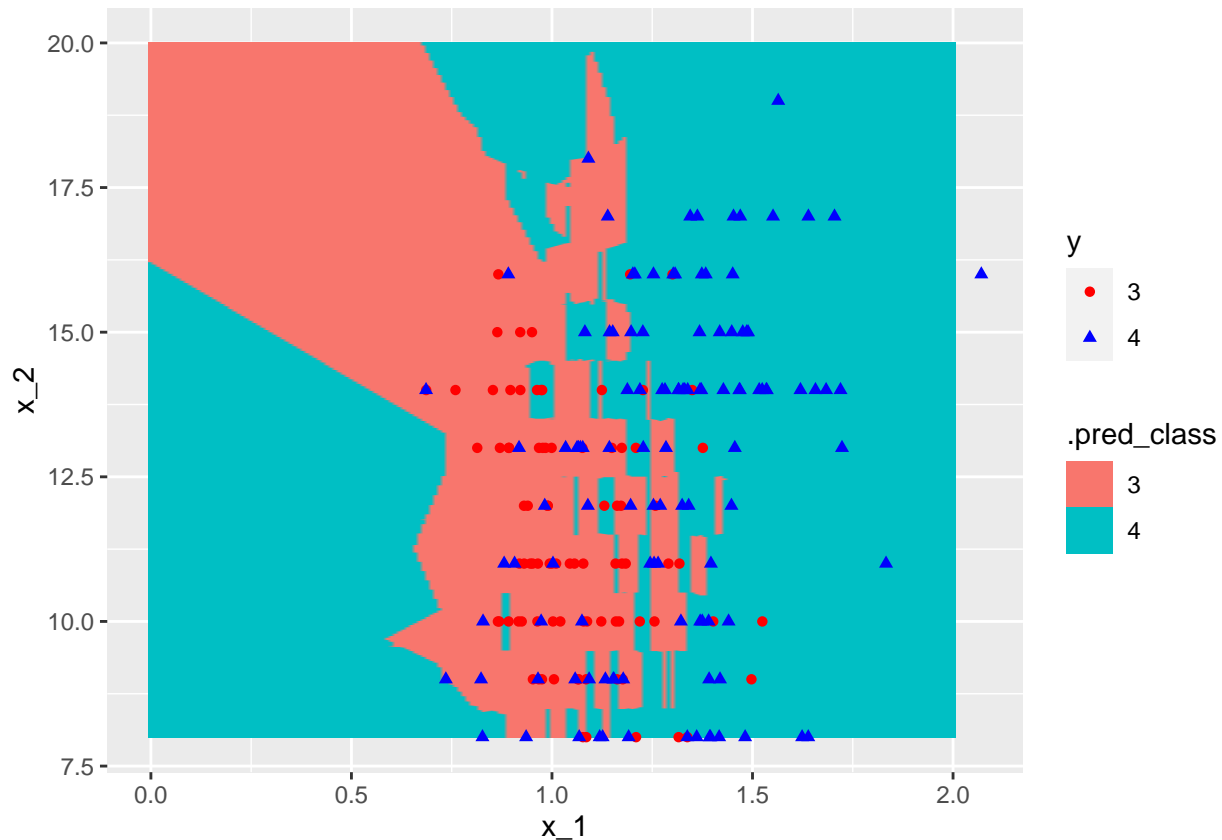
```
plot_boundary <- function(fit, test.tbl, delta){
  grid.tbl <- expand_grid(x_1=seq(0,2, by=delta),
                        x_2=seq(8,20, by=delta))

  augment(fit, grid.tbl)%>%
    ggplot() +
      geom_raster(aes(x_1, x_2, fill = .pred_class)) +
      geom_point(data=test.tbl, aes(x=x_1, y=x_2, color=y, shape=y))+
```

```

    scale_color_manual(values=c("red", "blue"))
  }
  plot_boundary(knn.model, test.mnist_34, 0.01)

```



Changing things up

- Create a new dataset that includes your two chosen digits and the digit 5. Create training and testing datasets that include 5 and your two given digits.
- Calculate the same 2 features for this new testing and training dataset.

```
final_5_linear <- tibble(indexes = indexes$index_of5, linearity = linear_final(index_of5))
```

```

##   [1] 13 18 16 18 16 15  8 13 17 17 15 13 17 14 11 14 10 14 14 12 14 16 16 18
##  [26] 11 16 16 14 16 15 15 17 14 16 17 16 10 12 14 12 14 17 15 15 17 14 16 14 10
##  [51] 18 13 16 12 12 12 14 10 13 13 12 13 12 13 12 12 13 16 12 15 18 12 11 11 13
##  [76] 14 13 11 18 14 17 15 15  9 17 15 17 13 14 13 13 17 16 10 15 13 14 14 16 12
## [101] 13 15 17 16 11 12 16 12  8  8 17 11 14 12 16 13 12 11 11 16 15 15  8 11 14
## [126] 13 16 12 14 19 12 17 12 17 13 17 12 14 13 11 13 14 13 17 17 17 12 13 17 18
## [151] 10 16 15 14 11 16 12 14 14 16 17 14 16 14 13 11 12 12 12 15 12 11 11 12 17
## [176] 14 13 10 15 11 13 15 10 14 13 16 11 13 13 14 13 12 14 11 14 16 12 10 13  9
## [201] 12 10 13  9 12 13 12 16 13 16 14 13 15 14 14 16 15 11 12 14 17 12 14 14 13
## [226] 17 12 15 14 15 13 18 17  8 10 12  9 13 16 13 18 12 15 16 14 17 13 19 15 13
## [251] 13 13 14 14 16 15 13 16 16 13 16 13 10 13 15 14 16 15 16 18 10 11 14 16 17
## [276] 17 14 14 18 13 15 15 15 16 14 13 14 12 13 10 17 11 14 11 12 11 10 12 15 14

```

```
## [301] 13 15 13 14 9 12 12 15 13 11 13 16 16 17 17 13 17 16 16 14 17 14 13 15 12
## [326] 13 16 15 12 15 16 13 11 13 15 13 11 14 13 13 17 11 15 15 16 15 17 11 13 13
## [351] 11 14 14 15 13 12 15 17 13 15 16 17 14 14 16 16 13 12 13 16 11 14 11 14 10
## [376] 14 12 14 14 14 13 16 16 14 17 15 14 13 16 11 12 11 13 12 14 13 16 13 18 16
## [401] 10 11 13 14 11 12 13 11 11 11 15 13 15 12 14 12 16 16 12 11 11 14 11 11 12
## [426] 8 14 14 15 15 16 13 15 13 13 11 12 12 17 13 13 15 14 19 14 15 17 15 13 14
## [451] 12 14 18 12 18 18 13 14 14 11 13 18 14 11 14 16 12 13 14 13 11 11 15 14 13
## [476] 15 14 9 17 15 13 16 16 14 14 14 11 11 18 16 12 14 11 16 13 14 16 20 13 15
```

```
final_5_linear <- final_5_linear%>%
  mutate(y = 5)
final_5_linear
```

```
## # A tibble: 500 x 3
##   indeces linearity    y
##   <int>      <dbl> <dbl>
## 1      1         13     5
## 2     12         18     5
## 3     36         16     5
## 4     48         18     5
## 5     66         16     5
## 6    101         15     5
## 7    133          8     5
## 8    139         13     5
## 9    146         17     5
## 10   174         17     5
## # ... with 490 more rows
```

```
linear_final_tbl_3_4_5 <- linear_final_tbl%>%
  full_join(final_5_linear)
linear_final_tbl_3_4_5
```

```
## # A tibble: 1,500 x 3
##   indeces linearity    y
##   <int>      <dbl> <dbl>
## 1      8         10     3
## 2     11          8     3
## 3     13         10     3
## 4     28          9     3
## 5     31         12     3
## 6     45         13     3
## 7     50         10     3
## 8     51         13     3
## 9     75          9     3
## 10    87         16     3
## # ... with 1,490 more rows
```

```
symmetry_final_3_4_5 <- symmetry_final%>%
  full_join(final_5)
symmetry_final_3_4_5
```

```
## # A tibble: 1,500 x 3
##   indeces ratio    y
##   <int> <dbl> <dbl>
## 1      8 1.08     3
## 2     11 0.882     3
```



```

## 3      13 1.22      3
## 4      28 0.967     3
## 5      31 1.02      3
## 6      45 1.07      3
## 7      50 0.822     3
## 8      51 0.856     3
## 9      75 0.951     3
## 10     87 0.784     3
## # ... with 1,490 more rows

mnist_345 <- linear_final_tbl_3_4_5%>%
  bind_cols(symmetry_final_3_4_5)
mnist_345

## # A tibble: 1,500 x 6
##   indeces...1 linearity y...3 indeces...4 ratio y...6
##   <int>      <dbl> <dbl>      <int> <dbl> <dbl>
## 1         8        10  3          8 1.08    3
## 2        11         8  3         11 0.882   3
## 3        13        10  3         13 1.22    3
## 4        28         9  3         28 0.967   3
## 5        31        12  3         31 1.02    3
## 6        45        13  3         45 1.07    3
## 7        50        10  3         50 0.822   3
## 8        51        13  3         51 0.856   3
## 9        75         9  3         75 0.951   3
## 10       87        16  3         87 0.784   3
## # ... with 1,490 more rows

final.split_345 <- initial_split(mnist_345, prop=0.8)
train.mnist_345 <- training(final.split_345)%>%
  mutate(y = as.factor(y...6))%>%
  mutate(x_1 = ratio)%>%
  mutate(x_2 = linearity)%>%
  select(x_1, x_2, y)
train.mnist_345

## # A tibble: 1,200 x 3
##   x_1    x_2 y
##   <dbl> <dbl> <fct>
## 1 1.02    12 3
## 2 1.32    11 3
## 3 0.804   14 5
## 4 0.965    9 4
## 5 0.969   16 5
## 6 0.864   15 3
## 7 1.20    15 4
## 8 1.12    10 5
## 9 1.08    11 3
## 10 0.966   11 3
## # ... with 1,190 more rows

test.mnist_345 <- testing(final.split_345)%>%
  mutate(y = as.factor(y...6))%>%
  mutate(x_1 = ratio)%>%
  mutate(x_2 = linearity)%>%

```

```
select(x_1, x_2, y)
```

- c) Calculate the missclassification rate on this new dataset. Create also the confusion matrix and comment on what digits seem to get confused more and why.

```
build_knn_345 <- function (train.table, kVal) {
  knn.model <- nearest_neighbor(neighbors = kVal) %>%
    set_engine("kknn") %>%
    set_mode("classification")

  recipe <- recipe(y ~ x_1 + x_2, data=train.table)

  knn.wflow <- workflow() %>%
    add_recipe(recipe) %>%
    add_model(knn.model)

  knn.fit <- fit(knn.wflow, train.table)
}

knn.model_345 <- build_knn(train.mnist_345, 5)

knn.final.fit_345 <- predict(knn.model_345, test.mnist_345, type="prob")

pred345.test.tbl <- knn.model_345 %>%
  augment(new_data = test.mnist_345)
pred345.test.tbl
```

```
## # A tibble: 300 x 7
##   x_1    x_2 y .pred_class .pred_3 .pred_4 .pred_5
##   <dbl> <dbl> <fct> <fct>      <dbl> <dbl> <dbl>
## 1 0.945   11 3      3          0.72  0      0.28
## 2 0.996   11 3      3          0.72  0.28   0
## 3 0.958    9 3      3          0.76  0.24   0
## 4 1.30    16 3      5          0      0.04  0.96
## 5 1.05    13 3      5          0.12  0      0.88
## 6 1.11    11 3      3          0.52  0.36  0.12
## 7 0.844    9 3      3          1      0      0
## 8 0.995   15 3      5          0.24  0      0.76
## 9 1.17    10 3      3          0.68  0.32   0
## 10 0.836   14 3      3          0.6   0      0.4
## # ... with 290 more rows
```

```
accuracy(pred345.test.tbl, y, .pred_class)
```

```
## # A tibble: 1 x 3
##   .metric .estimator .estimate
##   <chr>    <chr>      <dbl>
## 1 accuracy multiclass  0.517
```

```
conf_mat(pred345.test.tbl, truth = y, estimate = .pred_class)
```

```
##           Truth
## Prediction  3  4  5
##           3 53 30 27
##           4 18 46 14
##           5 33 23 56
```

Once we add in the 5, our accuracy with the KNN Model drops significantly with a missclassification rate of 0.517. As we can see from the confusion matrix, the 3s and 5s are most often confused, which makes sense because with the way we calculated symmetry, a 5 would also be seen as quite symmetrical. 4s were the least confused, but still easily confused. As we can see, the numbers are still more accurate than not, but only slightly. Now we'll see the plot that should help us visualize.

d) Plot the probabilities across a grid and the decision boundary for your model.

```
plot_boundary3 <- function(fit, test.tbl, delta){
  grid.tbl <- expand_grid(x_1=seq(0,2, by=delta),
                        x_2=seq(8,20, by=delta))

  augment(fit, grid.tbl)%>%
    ggplot() +
      geom_raster(aes(x_1, x_2, fill = .pred_class)) +
      geom_point(data=test.tbl, aes(x=x_1, y=x_2, color=y, shape=y))+
      scale_color_manual(values=c("red", "green", "blue"))
}
plot_boundary3(knn.model_345, test.mnist_345, 0.01)
```

